

SECANT METHOD

(PRACTICAL-3)

Que 1: Find the roots of the given function using secant method: $x^3 + 2x^2 - 3x + 1$

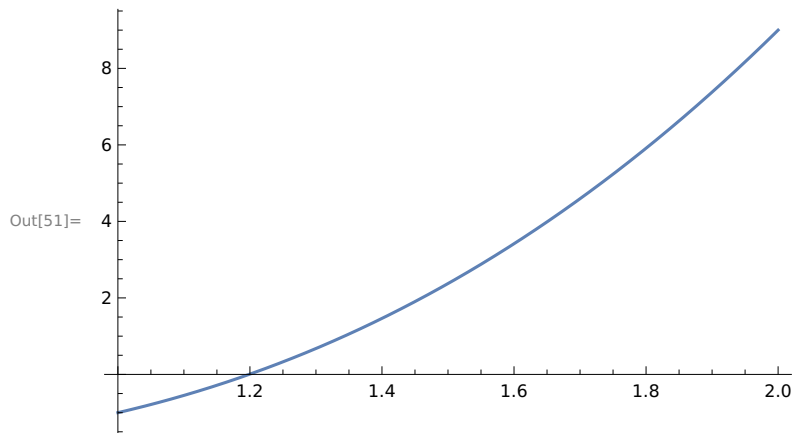
```
In[44]:= f[x_] := (x ^ 3) + 2 * (x ^ 2) - 3 * x - 1;
In[46]:= Subscript[p, 0] = 2;
In[47]:= Subscript[p, 1] = 1;
In[48]:= eps = 0.000005;
In[49]:= Nmax = 10;
In[50]:= For[n = 2, n ≤ Nmax, n++,
  Subscript[p, n] =
    N[Subscript[p, n - 1] - f[Subscript[p, n - 1]] * (Subscript[p, n - 1] - Subscript[p, n - 2]) /
      (f[Subscript[p, n - 1]] - f[Subscript[p, n - 2]])];
  If[Abs[Subscript[p, n] - Subscript[p, n - 1]] < ε, Return[Subscript[p, n]]];
  Print[n - 1, "th iteration value is : ", Subscript[p, n]];
  Print["Estimated Error is : ", Abs[Subscript[p, n] - Subscript[p, n - 1]]];
  Plot[f[x], {x, 1, 2}]
```

```

1th iteration value is : 1.1
Estimated Error is : 0.1
2th iteration value is : 1.22173
Estimated Error is : 0.121729
3th iteration value is : 1.19649
Estimated Error is : 0.0252442
4th iteration value is : 1.19865
Estimated Error is : 0.00216004
5th iteration value is : 1.19869
Estimated Error is : 0.000045968

```

Out[50]= 1.19869



Que 2: Find the roots of the given function using secant method: $\text{Exp}[-x] - x$

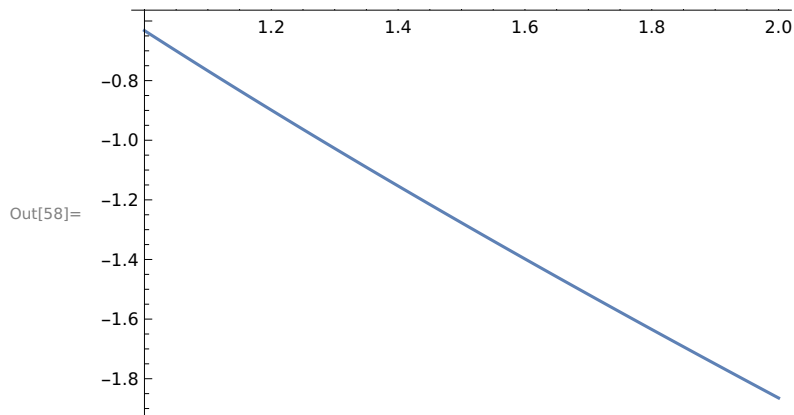
```

In[52]:= f[x_] := Exp[-x] - x
In[53]:= Subscript[p, 0] = 0;
In[54]:= Subscript[p, 1] = 1;
In[55]:= eps = 0.000005;
In[56]:= Nmax = 10;
In[57]:= For[n = 2, n ≤ Nmax, n++,
  Subscript[p, n] =
    N[Subscript[p, n - 1] - f[Subscript[p, n - 1]] * (Subscript[p, n - 1] - Subscript[p, n - 2]) /
      (f[Subscript[p, n - 1]] - f[Subscript[p, n - 2]])];
  If[Abs[Subscript[p, n] - Subscript[p, n - 1]] < ε, Return[Subscript[p, n]]];
  Print[n - 1, "th iteration value is : ", Subscript[p, n]];
  Print["Estimated Error is : ", Abs[Subscript[p, n] - Subscript[p, n - 1]]];
  Plot[f[x], {x, 1, 2}]

```

1th iteration value is : 0.6127
 Estimated Error is : 0.3873
 2th iteration value is : 0.563838
 Estimated Error is : 0.0488614
 3th iteration value is : 0.56717
 Estimated Error is : 0.00333197
 4th iteration value is : 0.567143
 Estimated Error is : 0.0000270518

Out[57]= 0.567143



Que 3 : Find the roots of the given function using secant method : $x^3 - 13$

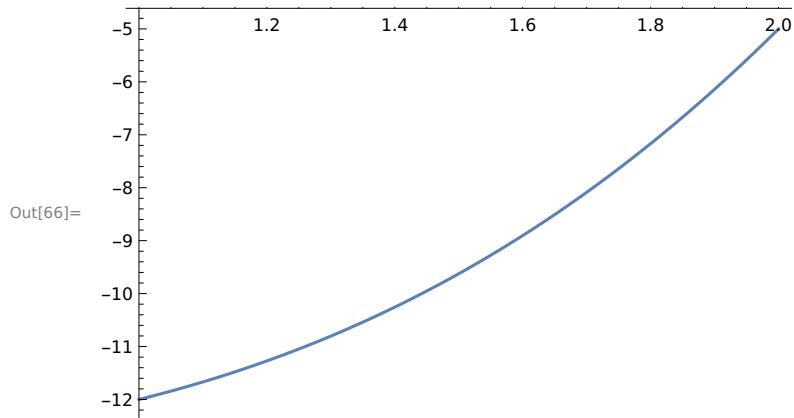
```
In[59]:= f[x_] := x^3 - 13
In[60]:= Subscript[p, 0] = 0;
In[62]:= Subscript[p, 1] = 3;
In[63]:= eps = 0.000005;
In[64]:= Nmax = 10;
In[65]:= For[n = 2, n ≤ Nmax, n++,
  Subscript[p, n] =
    N[Subscript[p, n - 1] - f[Subscript[p, n - 1]]*(Subscript[p, n - 1] - Subscript[p, n - 2])/
      (f[Subscript[p, n - 1]] - f[Subscript[p, n - 2]])];
  If[Abs[Subscript[p, n] - Subscript[p, n - 1]] < ε, Return[Subscript[p, n]]];
  Print[n - 1, "th iteration value is : ", Subscript[p, n]];
  Print["Estimated Error is : ", Abs[Subscript[p, n] - Subscript[p, n - 1]]];
  Plot[f[x], {x, 1, 2}]
```

```

1th iteration value is : 1.44444
Estimated Error is : 1.55556
2th iteration value is : 2.09207
Estimated Error is : 0.647629
3th iteration value is : 2.49729
Estimated Error is : 0.405212
4th iteration value is : 2.33475
Estimated Error is : 0.162534
5th iteration value is : 2.35034
Estimated Error is : 0.0155903
6th iteration value is : 2.35134
Estimated Error is : 0.000999479
7th iteration value is : 2.35133
Estimated Error is :  $7.03717 \times 10^{-6}$ 

```

Out[65]= 2.35133



Que 4 : Find the roots of the given function using secant method :

$$x^3 - 3x^2 + 2x + 5$$

In[67]:= `f[x_] := x^3 - 3*x^2 + 2*x + 5`

In[68]:= `Subscript[p, 0] = 0;`

In[69]:= `Subscript[p, 1] = -1;`

In[70]:= `eps = 0.000005;`

In[71]:= `Nmax = 10;`

```

In[72]:= For[n = 2, n ≤ Nmax, n++,
  Subscript[p, n] =
    N[Subscript[p, n - 1] - f[Subscript[p, n - 1]]*(Subscript[p, n - 1] - Subscript[p, n - 2])/
      (f[Subscript[p, n - 1]] - f[Subscript[p, n - 2]])];
  If[Abs[Subscript[p, n] - Subscript[p, n - 1]] < ε, Return[Subscript[p, n]]];
  Print[n - 1, "th iteration value is : ", Subscript[p, n]];
  Print["Estimated Error is : ", Abs[Subscript[p, n] - Subscript[p, n - 1]]];
  Plot[f[x], {x, 1, 2}]

1th iteration value is : -0.833333
Estimated Error is : 0.166667
2th iteration value is : -0.900277
Estimated Error is : 0.0669437
3th iteration value is : -0.904325
Estimated Error is : 0.00404786
4th iteration value is : -0.90416
Estimated Error is : 0.000164377

```

Out[72]= -0.904161

