

# MANY MACROS, TONS OF TYPES

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PLT Scheme is a programming language designed for conducting research and running educational programs that is *also* used for commercial purposes.

Don't run out and switch your heavy-duty commercial e-business site to the PLT Scheme web server without conducting a feasibility study.

Instead, this talk is about ideas that you can take away and apply to your Lisp.

PLT Scheme is really many  
different languages.

There is **PLT Scheme** proper.

There is **R6R Scheme**.

We have **Typed Scheme**.

For real programmers,  
there's **Lazy Scheme**.

And documentation is a  
program, too. For that we  
provide **Scribble**.

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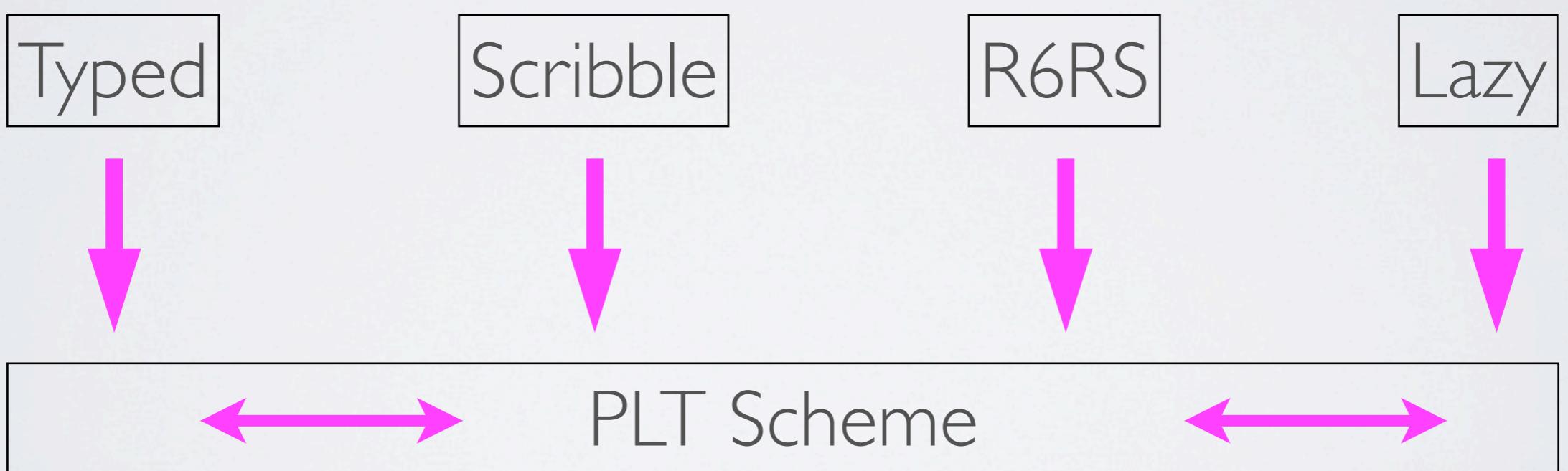
We have **Typed Scheme**.

For real programmers, there's **Lazy Scheme**.

And documentation is a program, too. For that we provide **Scribble**.

**Productivity:** Systems consist of many modules each written in one of these “dialects” and importing/exporting from each other.

And it all works via macro expansion and a high level of value communication.



#lang scribble/base

@title{The Fibonacci Sequence}

The Fibonacci sequence begins with two copies of the number 1 and continues @emph{forever} by adding the two most recent numbers together to get the next number. The first seven numbers of the sequence are 1, 1, 2, 3, 5, 9, 14, ... because 1 + 1 is 2, 2 + 3 is 5, and so on.

@section{Fibs in nature}

It is a well-known rumor that rabbits ...

## doc.scrbl

```
#lang scribble/base
```

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The Fibonacci sequence begins with two copies of the number 1 and continues @emph{forever} by adding the two most recent numbers together to get the next number. The first seven numbers of the sequence are 1, 1, 2, 3, 5, 9, 14, ... because 1 + 1 is 2, 2 + 3 is 5, and so on.

```
@section{Fibs in nature}
```

It is a well-known rumor that rabbits ...



```
(module doc scribble/base/lang
  (#%module-begin
    doc
    values
    ()
    "\n"
    "\n"
    (title "The Fibonacci Sequence")
    "\n"
    "\n"
    "The Fibonacci sequence begins with two copies of"
    "\n"
    "the number 1 and continues "
    (emph "forever")
    " by adding"
    "\n"
    "the two most recent numbers together to get the next"
    "\n"
    "number. The first seven numbers of the sequence are"
    "\n"
    "1, 1, 2, 3, 5, 9, 14, ... because 1 + 1 is 2,"
    "\n"
    "2 + 3 is 5, and so on."
    "\n"
    "\n"
    (section "Fibs in nature")
    "\n"
    "\n"
    "It is a well-known rumor that rabbits ..."))
```

doc.scrbl

```
#lang scribble/base
```

```
@title{The Fibonacci Sequence}
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The Fibonacci sequence begins with two copies of the number 1 and continues *forever* by adding the two most recent numbers together to get the next number. The first seven numbers of the sequence are 1, 1, 2, 3, 5, 9, 14, ... because  $1 + 1$  is 2,  $2 + 3$  is 5, and so on.

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## The Fibonacci Sequence

The Fibonacci sequence begins with two copies of the number 1 and continues *forever* by adding the two most recent numbers together to get the next number. The first seven numbers of the sequence are 1, 1, 2, 3, 5, 9, 14, ... because  $1 + 1$  is 2,  $2 + 3$  is 5, and so on.

### 1 Fibs in nature

It is a well-known rumor that rabbits ...

doc.scrbl

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```
@section{Fibs in nature}
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Ouch!

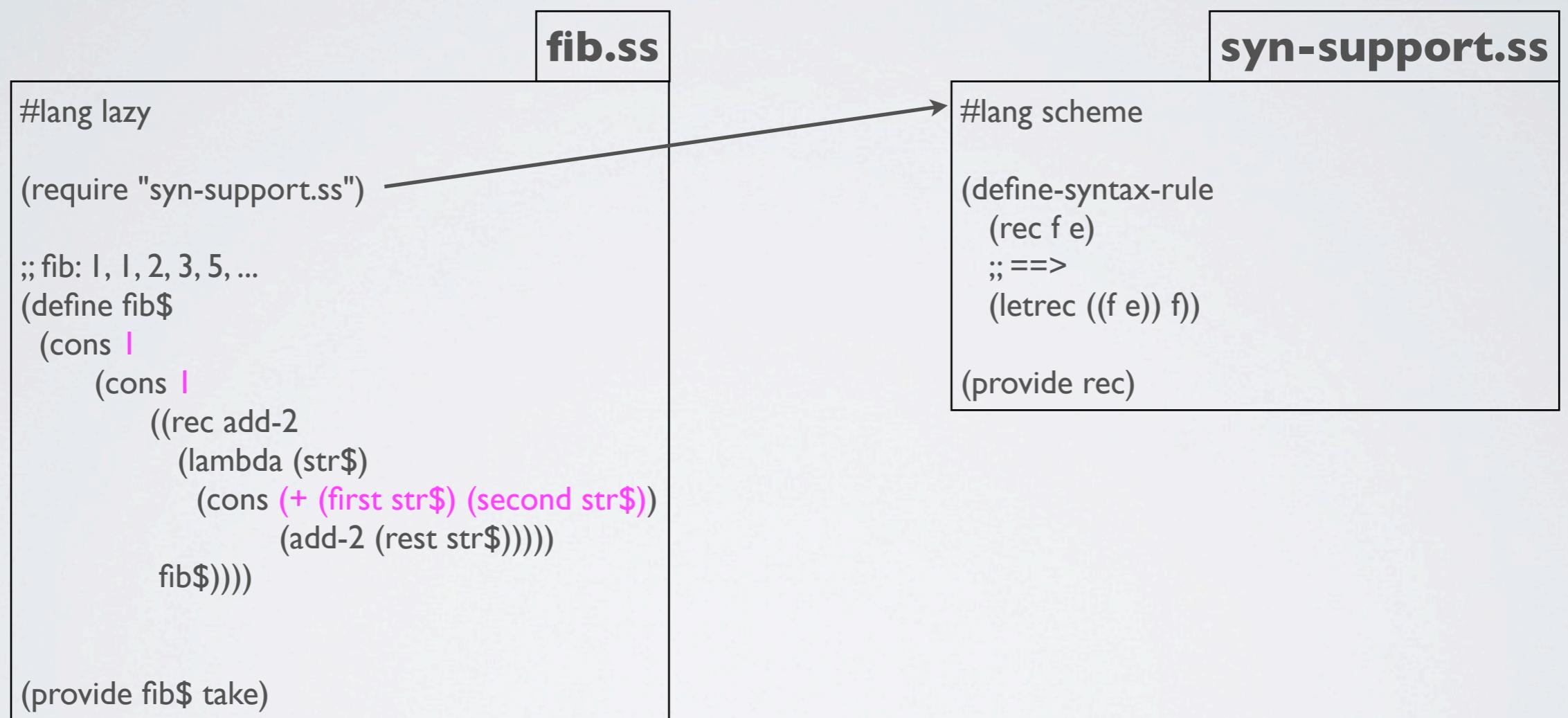
## **fib.ss**

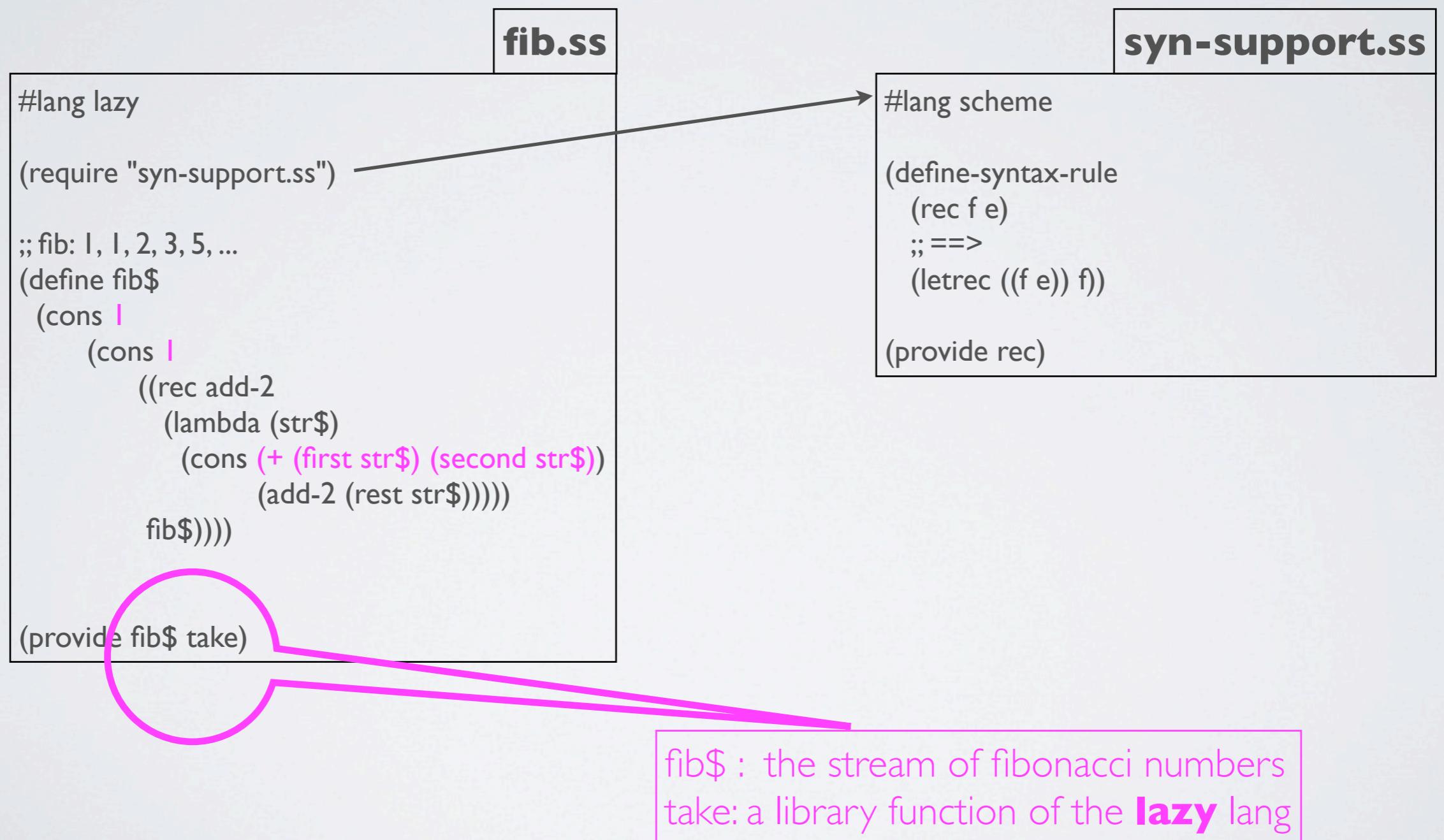
```
#lang lazy

(require "syn-support.ss")

;; fib: I, I, 2, 3, 5, ...
(define fib$
  (cons I
    (cons I
      ((rec add-2
        (lambda (str$)
          (cons (+ (first str$) (second str$))
            (add-2 (rest str$))))))
        fib$)))))

(provide fib$ take)
```





## doc-v2.scrbl

```
#lang scribble/base
```

```
@(require lazy/force "fib.ss")  
@title{The Fibonacci Sequence}  
@(define fib7 (! (take 7 fib$)))
```

The Fibonacci sequence begins with two copies of the number 1 and continues @emph{forever} by adding the two most recent numbers together to get the next number. The first seven numbers of the sequence are

```
@(foldr (lambda (f r)  
          (string-append (format "~a, " f) r))  
         "..."  
         fib7)
```

because  $1 + 1$  is 2,  $2 + 3$  is 5, and so on.

```
@section{Fibs in nature}
```

It is a well-known rumor that rabbits ..

## doc-v3.scrbl

```
#lang scribble/base

@(require lazy/force "fib.ss" "lib-support.rkt")

@title{The Fibonacci Sequence}

@(define fib7 (!! (take 7 fib$)))

The Fibonacci sequence begins with two copies of the number 1 and continues @emph{forever} by adding the two most recent numbers together to get the next number. The first seven numbers of the sequence are
@(foldr (lambda (f)
  (string-append (format "~a, " f) r))
  "..."
  fib7)

because 1 + 1 is 2, 2 + 3 is 5, and so on. Another way to illustrate this idea is with this kind of table:
@(fib-tab fib7)
...
```

## The Fibonacci Sequence

The Fibonacci sequence begins with two copies of the number 1 and continues *forever* by adding the two most recent numbers together to get the next number. The first seven numbers of the sequence are 1, 1, 2, 3, 5, 8, 13, ... because  $1 + 1$  is 2,  $2 + 3$  is 5, and so on. Another way to illustrate this idea is with this kind of table:

n	n+1	n+2
1	1	2
1	2	3
2	3	5
3	5	8
5	8	13
8	13	...

### 1 Fibs in nature

It is a well-known rumor that rabbits ...

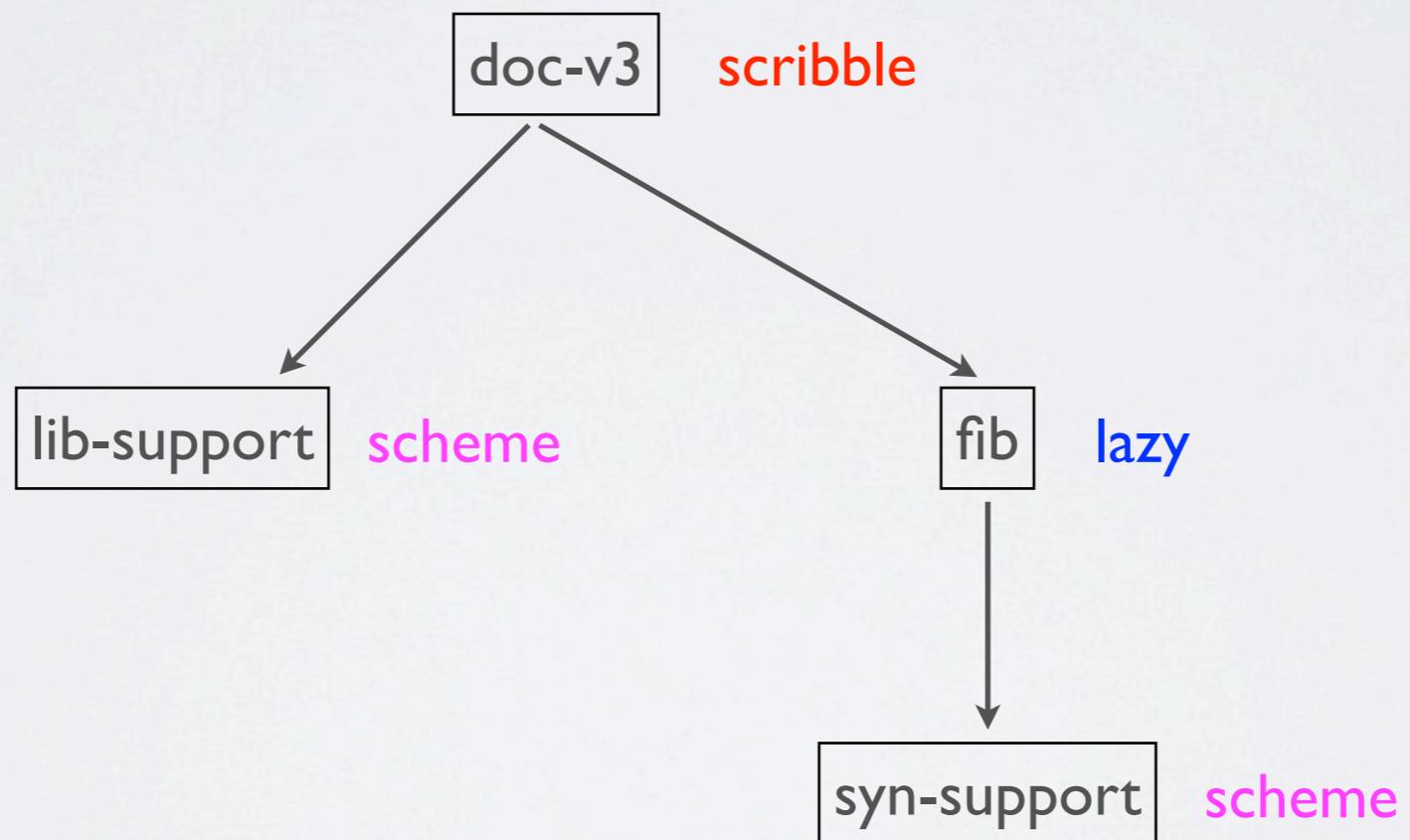


## lib-support.ss

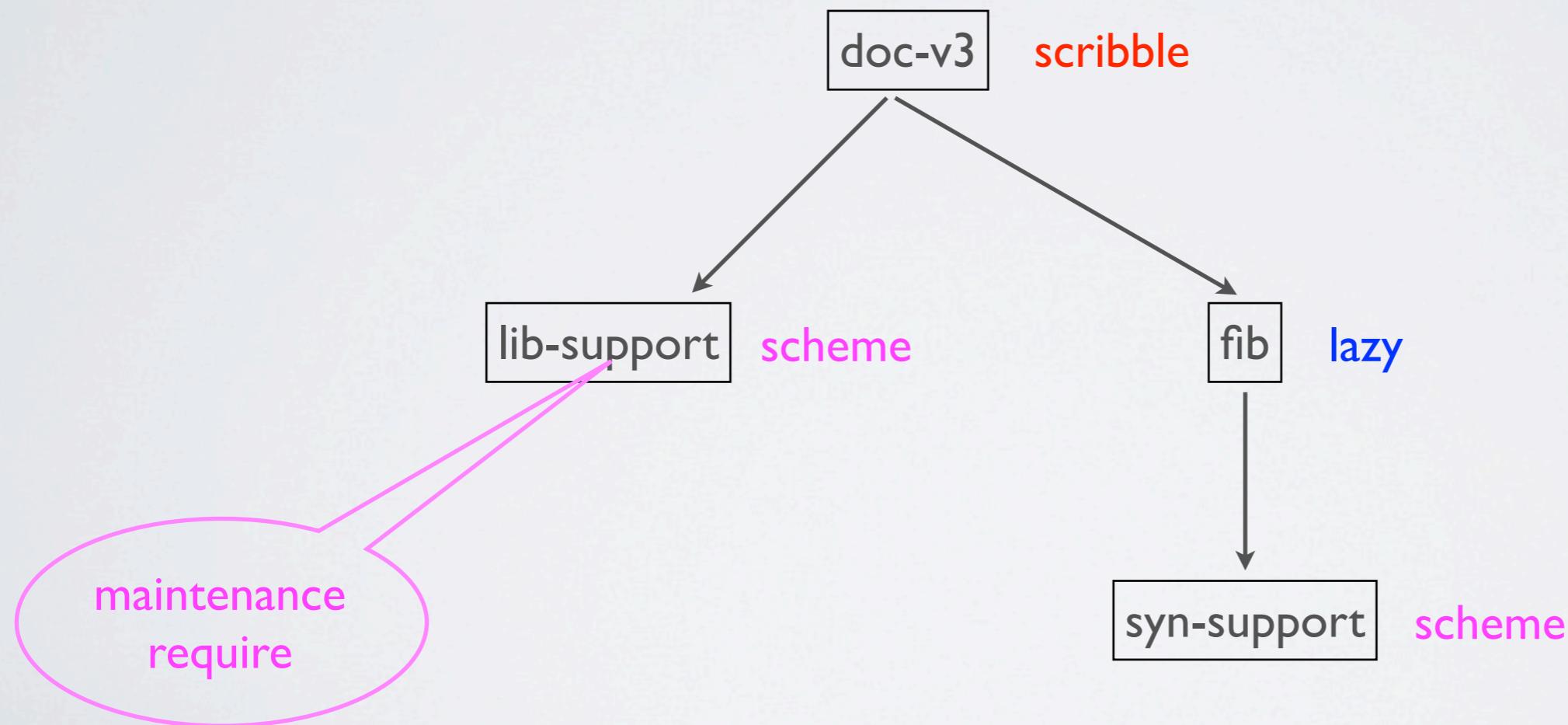
```
#lang scheme
```

```
;; (cons Natural (cons Natural [Listof Natural])) -> TABLE
;; convert a list of at least two Nats into a scribble table
(define (fib-tab l)
  ;; [Listof Natural] -> Any
  (define (result lst)
    (if (cons? (rest (rest lst))) (third lst) "..."))
  ;; Any -> PARAGRAPH
  (define (b x)
    (make-paragraph (make-style #f '[]) (format "~a" x)))
  ;; -- IN --
  (make-table (make-style 'boxed '())
    (cons (map b (list "n" "n+l" "n+2"))
      (let loop ([l l])
        (if (empty? (rest l))
            '()
            (cons (map b (list (first l) (second l) (result l)))
                  (loop (rest l))))))))
(require scribble/core)
(provide fib-tab)
```

## How the modules hang together



## How the modules hang together



You need to recall the “types”  
you had in mind originally.

## lib-support.ss

```
#lang scheme

;; (cons Natural (cons Natural [Listof Natural])) -> TABLE
;; convert a list of at least two Nats into a scribble table
(define (fib-tab l)
  ;; [Listof Natural] -> Any
  (define (result lst)
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  (define (b x)
    (make-paragraph (make-style #f '[]) (format "~a" x)))
  ;; -- IN --
  (make-table
    (make-style 'boxed '())
    (cons (map b (list "n" "n+1" "n+2"))
          (let loop ([l l])
            (if (empty? (rest l))
                '()
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                      (loop (rest l))))))))
  (require scribble/core)

(provide fib-tab)
```

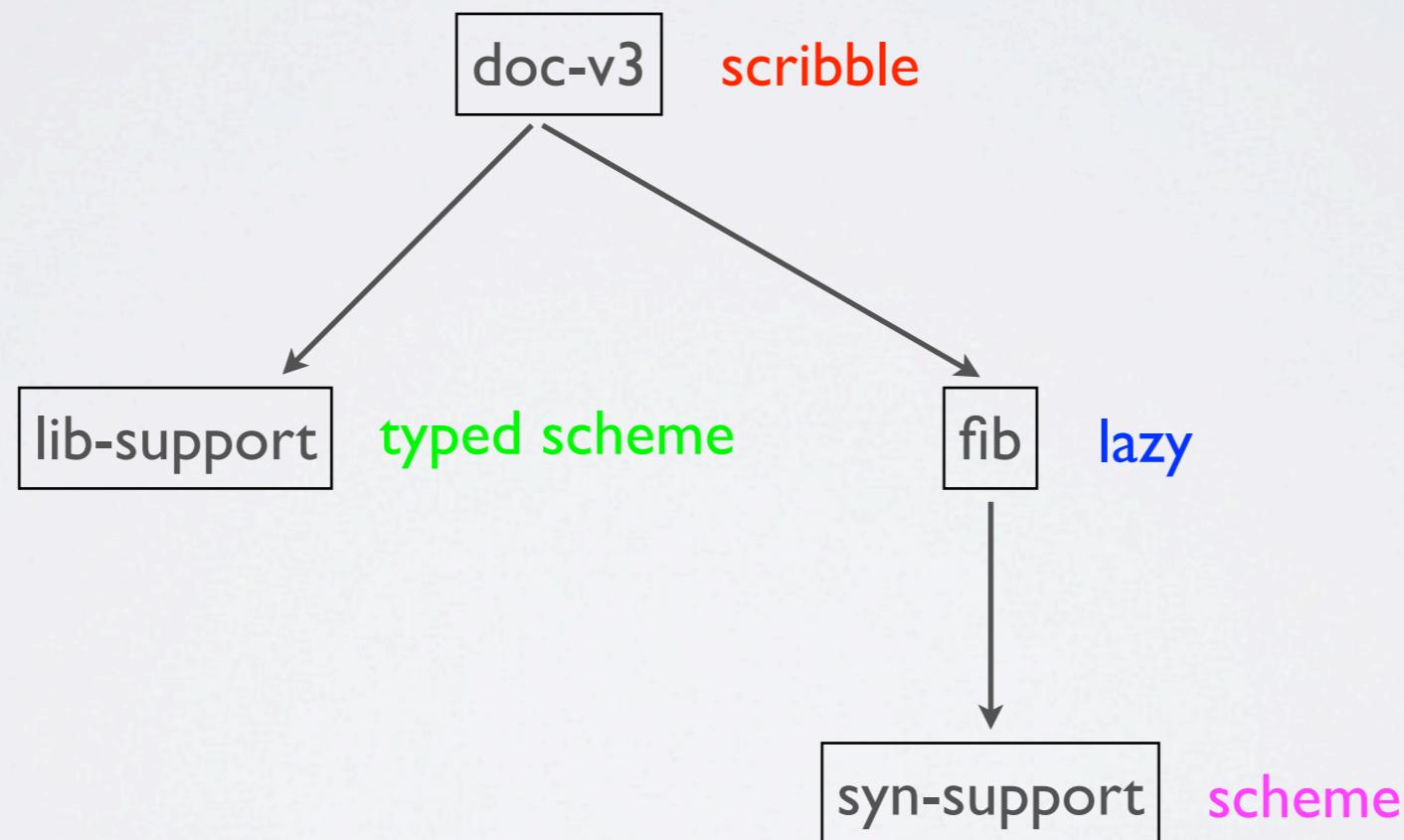
You might as well make them explicit and checkable.

## lib-support.ss

```
#lang typed/scheme

(: fib-tab ((cons Natural (cons Natural [Listof Natural])) -> table))
;; convert a list of at least two Nats into a scribble table
(define (fib-tab l)
  (: result ([Listof Natural] -> Any))
  (define (result lst)
    (if (cons? (rest (rest lst))) (third lst) "..."))
  (: b (Any -> paragraph))
  (define (b x)
    (make-paragraph (make-style #f '[]) (format "~a" x)))
  ;; -- IN --
  (make-table (make-style 'boxed '())
    (cons (map b (list "n" "n+1" "n+2"))
      (let: loop : [Listof [Listof paragraph]] ([l : [Listof Natural] l])
        (if (empty? (rest l))
          '()
          (cons (map b (list (first l) (second l) (result l)))
            (loop (rest l))))))))
  (require/typed
    scribble/core
    [struct style ([name : (U False Symbol)] [properties : [Listof Any]])]
    [struct paragraph ([style : style] [content : String])]
    [struct table ([style : style] [blockss : [Listof [Listof paragraph]]])])
  (provide fib-tab))
```

How the modules hang together,  
still, even with types added.



## Two ideas worth studying

- how to implement languages like this with macros (Lisp macros vs PLT Scheme macros)
- how to add types and protect the integrity of multi-lingual modules (typed vs untyped)

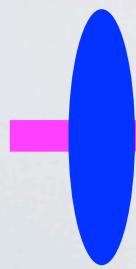
# MACROS MATTER

Macros are a compiler  
API. -- Matthew Flatt  
and many other Schemers

McIlroy, *Macro Extensions of Compiler Languages*



1960



Macros are a compiler  
API. -- Matthew Flatt  
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McIlroy, *Macro Extensions of Compiler Languages*

Hart, *Macro Definitions for LISP*

1960 1963



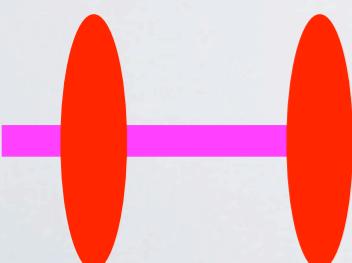
Macros ought to be abstractions,  
that is definition and use should  
be independent.

Kohlbecker, Friedman, Felleisen, Duba *Hygienic Macros*

Clinger & Rees *Macros that Work*

Dybvig, Bruggeman, Hieb *Syntactic Abstractions*

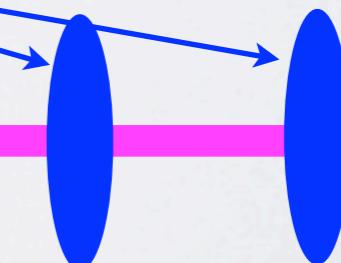
1960 1963



1985



1991 1993



Languages are modules and have two parts: syntax and run-time.

syntax

run-time library

### lib-support.ss

#lang scheme

```
(define-syntax (close-by stx)
  (syntax-case stx ()
    [(_ p q)
     #:==>
     #'(let ([delta (posn- p q)])
         (if (<= (posn-distance0 delta) EPSILON)
             p
             q))))
```

```
(define EPSILON 1)

(struct posn (x y) #:prefab)

(define (posn- p q)
  (posn (- (posn-x p) (posn-x q)) (- (posn-y p) (posn-y q)))))

(define (posn-distance0 p)
  (sqrt (+ (sqr (posn-x p)) (sqr (posn-y p))))))
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             q))]))
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syntax

run-time  
library

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```

Hygiene ensures that two different substitutions work.

## lib-support.ss

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#lang scheme
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            p
            q))))
```

```
(close-by (posn 0 0) (posn 3 4))
```

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(struct posn (x y) #:prefab)

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```



expand

```
(let ([delta (posn- (posn 0 0) (posn 3 4))])
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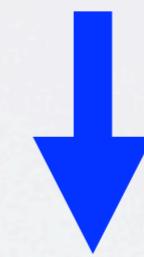
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```

```
(define (f x)
  (define (posn- p)
    (posn (- (posn-x p)) (- x (posn-y p)))))
  ;; -- IN --
  (close-by (posn 0 0) (posn 12 5)))
```

Hygiene ensures that two different substitutions work.

## lib-support.ss

```
#lang scheme
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(define-syntax (close-by stx)
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Macro bodies are substituted for macro calls. Which *posn-* is meant?

Hygiene ensures that two different substitutions work.

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  (sqrt (+ (sqr (posn-x p)) (sqr (posn-y p))))))
```

```
(define delta
  (posn- (posn 12 6) (posn 0 1)))

(close-by delta origin)
```

Hygiene ensures that two different substitutions work.

## lib-support.ss

```
#lang scheme
```

```
(define-syntax (close-by stx)
  (syntax-case stx ()
    [(_ p q)
     #: ==>
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```
(define delta
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Macros arguments are substituted into the macro body. Which *delta* is meant?

Hygiene ensures that two different substitutions work.

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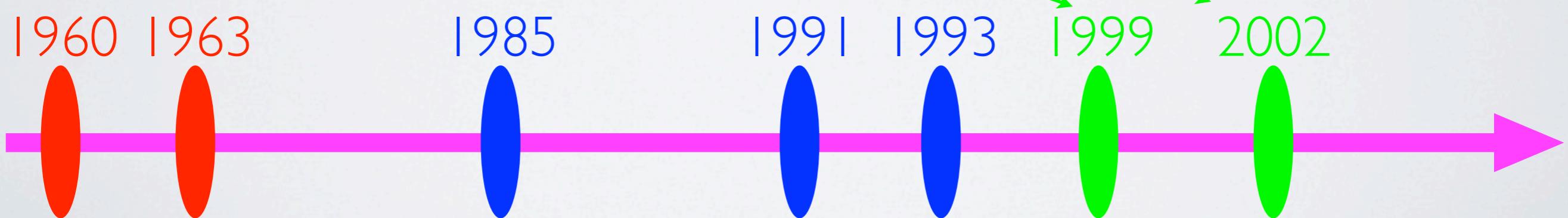
```
(define delta
  (posn- (posn 12 6) (posn 0 1)))
  (close-by delta origin))
```

Macros arguments are substituted into the macro body. Which *delta* is meant?

Modules and macros must interact properly.  
Macro expansion must live in its own separate  
phase and enable separate compilation.

Dybvig and Bruggeman *Extending the Scope of Macros*

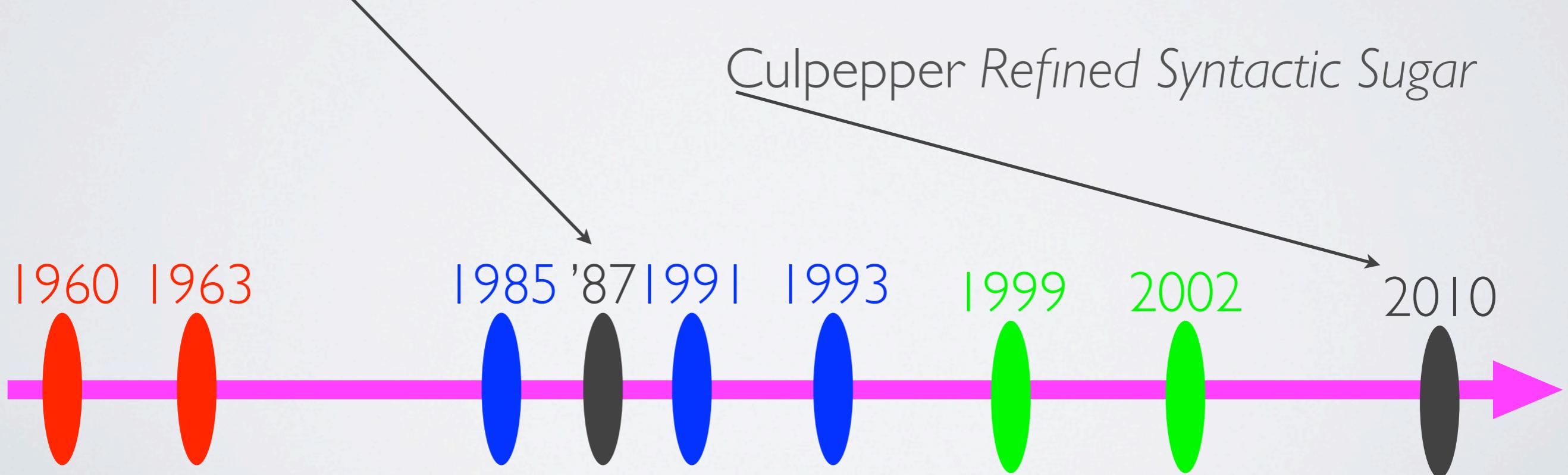
Flatt Composable and Compilable Macros



For easy macros, the specification should be the implementation. For others, you may need the power of the entire language.

## Kohlbecker & Wand Macros by Example

Culpepper Refined Syntactic Sugar



## 65, Lisp

```
(define-macro (let . stx)
  (define decls (second stx))
  (define binds (map first decls))
  (define vals  (map second decls))
  (define body (rest (rest stx)))
  ;;; -- IN --
  `((lambda ,@binds . body) ,@vals))
```

```
(let ((x 8) (y 5))
  (+ x y))
```

```
(let ((x 8 'BAD) (y 5))
  (+ x y))
```

```
(let ((|7 x) (y 5))
  (+ x y))
```

## 65, Lisp

```
(define-macro (let . stx)
  (define decls (second stx))
  (define binds (map first decls))
  (define vals  (map second decls))
  (define body (rest (rest stx)))
  ;; -- IN --
  `((lambda ,@binds . body) ,@vals))
```

```
(let ((x 8) (y 5))
  (+ x y))
```

```
(let ((x 8 'BAD) (y 5))
  (+ x y))
```

```
(let ((|7 x) (y 5))
  (+ x y))
```

## 87, Scheme

```
(define-syntax-rule
  (let ((lhs rhs) ...) body ...)
  ;; ==>
  ((lambda (lhs ...) body ...) rhs ....))
```

```
(let ((x 8) (y 5))
  (+ x y))
```

```
(let ((x 8 'BAD) (y 5))
  (+ x y))
```

```
(let ((|7 x) (y 5))
  (+ x y))
```

## 65, Lisp

```
(define-macro (let . stx)
  (define decls (second stx))
  (define binds (map first decls))
  (define vals (map second decls))
  (define body (rest (rest stx)))
  ;; -- IN --
  `((lambda ,@binds . body) ,@vals))
```

```
(let ((x 8) (y 5))
  (+ x y))
```

```
(let ((x 8 'BAD) (y 5))
  (+ x y))
```

```
(let ((|7 x) (y 5))
  (+ x y))
```

## 87, Scheme

```
(define-syntax-rule
  (let ((lhs rhs) ...) body ...)
  ;; ==>
  ((lambda (lhs ...) body ...) rhs ....))
```

```
(let ((x 8) (y 5))
  (+ x y))
```

```
(let ((x 8 'BAD) (y 5))
  (+ x y))
```

```
(let ((|7 x) (y 5))
  (+ x y))
```

## 94, R5RS

```
(define-syntax let
  (syntax-rules ()
    (_ ((lhs rhs) ...) body ...)
    ;; ==>
    ((lambda (lhs ...) body ...) rhs ....)))
```

```
(let ((x 8) (y 5))
  (+ x y))
```

```
(let ((x 8 'BAD) (y 5))
  (+ x y))
```

```
(let ((|7 x) (y 5))
  (+ x y))
```

## 95, Chez

```
(define-syntax (let stx)
  (syntax-case stx ()
    (_ ((lhs rhs) ...) body ...)
    #:==>
    #'((lambda (lhs ...) body ...) rhs ....))
```

```
(let ((x 8) (y 5))
  (+ x y))
```

```
(let ((x 8 'BAD) (y 5))
  (+ x y))
```

```
(let ((|7 x) (y 5))
  (+ x y))
```

95, Chez

```
(define-syntax (let stx)
  (syntax-case stx ()
    (_ ((lhs rhs) ...) body ...)
    ;;=;>
    #'((lambda (lhs ...) body ...) rhs ....))
```

```
(let ((x 8) (y 5))
  (+ x y))
```

```
(let ((x 8 'BAD) (y 5))
  (+ x y))
```

```
(let ((|7 x) (y 5))
  (+ x y))
```

| 0, PLT

```
(define-syntax (let stx)
  (syntax-parse stx
    (_ ((lhs:identifier rhs:expr) ...) 
       body:expr ...)
    ;;=;>
    #'((lambda (lhs ...) body ...) rhs ....)))
```

```
(let ((x 8) (y 5))
  (+ x y))
```

```
(let ((x 8 'BAD) (y 5))
  (+ x y))
```

```
(let ((|7 x) (y 5))
  (+ x y))
```

95, Chez

```
(define-syntax (let stx)
  (syntax-case stx ()
    (_ ((lhs rhs) ...) body ...)
    ;;=;>
    #'((lambda (lhs ...) body ...) rhs ....))
```

```
(let ((x 8) (y 5))
  (+ x y))
```

```
(let ((x 8 'BAD) (y 5))
  (+ x y))
```

```
(let ((|7 x) (y 5))
  (+ x y))
```

| 0, PLT

```
(define-syntax (let stx)
  (syntax-parse stx
    (_ ((lhs:identifier rhs:expr) ...) 
       body:expr ...)
    ;;=;>
    #'((lambda (lhs ...) body ...) rhs ....)))
```

```
(let ((x 8) (y 5))
  (+ x y))
```

```
(let ((x 8 'BAD) (y 5))
  (+ x y))
```

```
(let ((|7 x) (y 5))
  (+ x y))
```

automatic synthesis of  
syntactic checks  
and error messages

**And a true compiler API comes with a lot more power ...**

- automatic source tracking
- lifting definitions to module top-level
- local expansion
- module-body expansion

**Macro-implemented features are indistinguishable from *native* features now.**

- classes (two systems: Java-like, CLOS-like)
- keyword args, C ffi, first-class components
- scribble (plus reader)
- and of course Typed Scheme.

# MEANINGFUL TYPES FOR LISPERS

**Goal:** adding types to systems written in Scheme on a module-by-module basis

**Ungoal:** Types are optional compiler hints.

**Goal:** types are **explicit** and **checked**; the system is sound

**Goal:** adding types should demand as few changes to the code as possible.

**Goal:** these types are solid maintenance information for all programmers, including versions of our future selves.

But, adding these kinds of types is non-trivial.

problem I: what is type soundness in a system of typed and untyped Scheme modules? what do types mean?

But, adding these kinds of types is non-trivial.

problem 1: what is type soundness in a system of typed and untyped Scheme modules? what do types mean?

problem 2: programmers should not need to modify code to accommodate the type checker but vice versa. how can a type system accommodate Scheme?

# MEANINGFUL TYPES

...

T

```
#lang scheme
;; inc5: Integer -> Integer
(define (inc5 i) (+ i 5))
(sprintf "~a\n" (inc -3))

(provide inc5)
```

U

```
#lang scheme

(require T)

(sprintf "~a\n" (inc5 6))
```

~~#lang scheme~~

~~;; inc5: Integer -> Integer~~

~~(define (inc5 i) (+ i 5))~~

~~(printf “~a\n” (inc -3))~~

~~(provide inc5)~~

T

#lang scheme

(require T)

(printf “~a\n” (inc5 6))

U

#lang typed/scheme

(: inc5 (Integer -> Integer))

(define (inc5 i) (+ i 5))

(printf “~a\n” (inc -3))

(provide inc5)

T

U

## #lang scheme

(require **T**)

... (inc5 true) ...

T

## #lang typed/scheme

```
(: inc5 (Integer -> Integer))
(define (inc5 i) (+ i 5))
```

```
(provide inc5)
```

U

## #lang scheme

(require **T**)

... (inc5 true) ...

T

## #lang typed/scheme

```
(: inc5 (Integer -> Integer))
(define (inc5 i) (+ i 5))
```

```
(provide inc5)
```

U

## #lang scheme

(require **T**)

... (inc5 true) ...

T

## #lang typed/scheme

```
(: inc5 (Integer -> Integer))  
(define (inc5 i) (+ i 5))
```

```
(provide inc5)
```

bang!

**#lang** typed/scheme

```
(define (encode f)
  (+ (f 21) 42))

(provide encode)
```

T

**#lang** scheme

```
(require T)
```

```
(define (hello i)
  (format "~a: hello world" i))

(prin
```

U

T

#**lang** typed/scheme

```
(: encode ((Integer -> Integer) -> Integer))
(define (encode f)
  (+ (f 21) 42))

(provide encode)
```

U

#**lang** scheme

```
(require T)

(define (hello i)
  (format "~a: hello world" i))

printf "~a\n" (encode hello))
```

T

#**lang** typed/scheme

```
(: encode ((Integer -> Integer) -> Integer))
(define (encode f)
  (+ (f 21) 42))
(provide encode)
```

U

#**lang** scheme

```
(require T)
(define (hello i)
  (format "~a: hello world" i))
(sprintf "~a\n" (encode hello))
```

#**lang** typed/scheme

```
(: encode ((Integer -> Integer) -> Integer))  
  
(define (encode f)  
  (+ (f 21) 42))  
  
(provide encode)
```

T

#**lang** scheme

```
(require T)  
  
(define (hello i)  
  (format "~a: hello world" i))  
  
(printf "~a\n" (encode hello))
```

U

U

#lang scheme

```
(define (inc5 x) (+ x 5))
```

```
(provide inc)
```

T

#lang typed/scheme

```
(require U)
```

```
(define (f x)
... (inc5 ???) ??? 10 ... )
```

U

#lang scheme

(define (inc5 x) (+ x 5))

(provide inc)

T

#lang typed/scheme

(require U)

(define (f x)  
... (inc5 ???) ??? 10 ... )

T

#lang typed/scheme

(require/typed U  
(f (Integer -> Integer)))

(define (f x)  
... (inc5 ???) ... 10 ... )

U

#lang scheme

```
(define (inc5 x)
  (if (= 42 x)
      "hello world"
      (+ x 5)))
(provide inc)
```

T

#lang typed/scheme

```
(require/typed U
  (f (Integer -> Integer)))
(define (f x)
  (+ (inc5 42) 0))
```

U

#lang scheme

```
(define (inc5 x)
  (if (= 42 x)
      "hello world"
      (+ x 5)))

(provide inc)
```

T

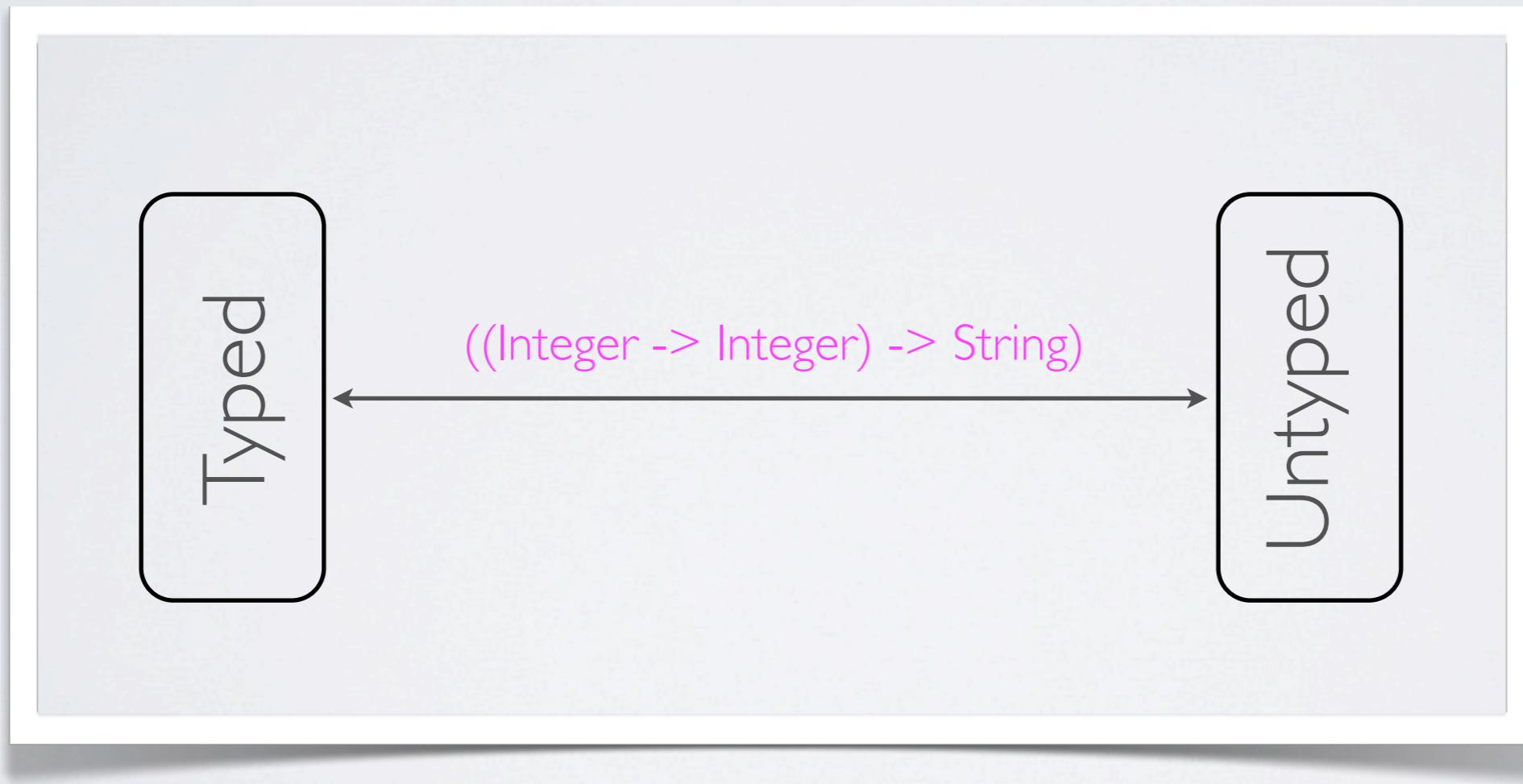
#lang typed/scheme

```
(require/typed U
  (f (Integer -> Integer)))

(define (f x)
  (+ (inc5 42) 0))
```

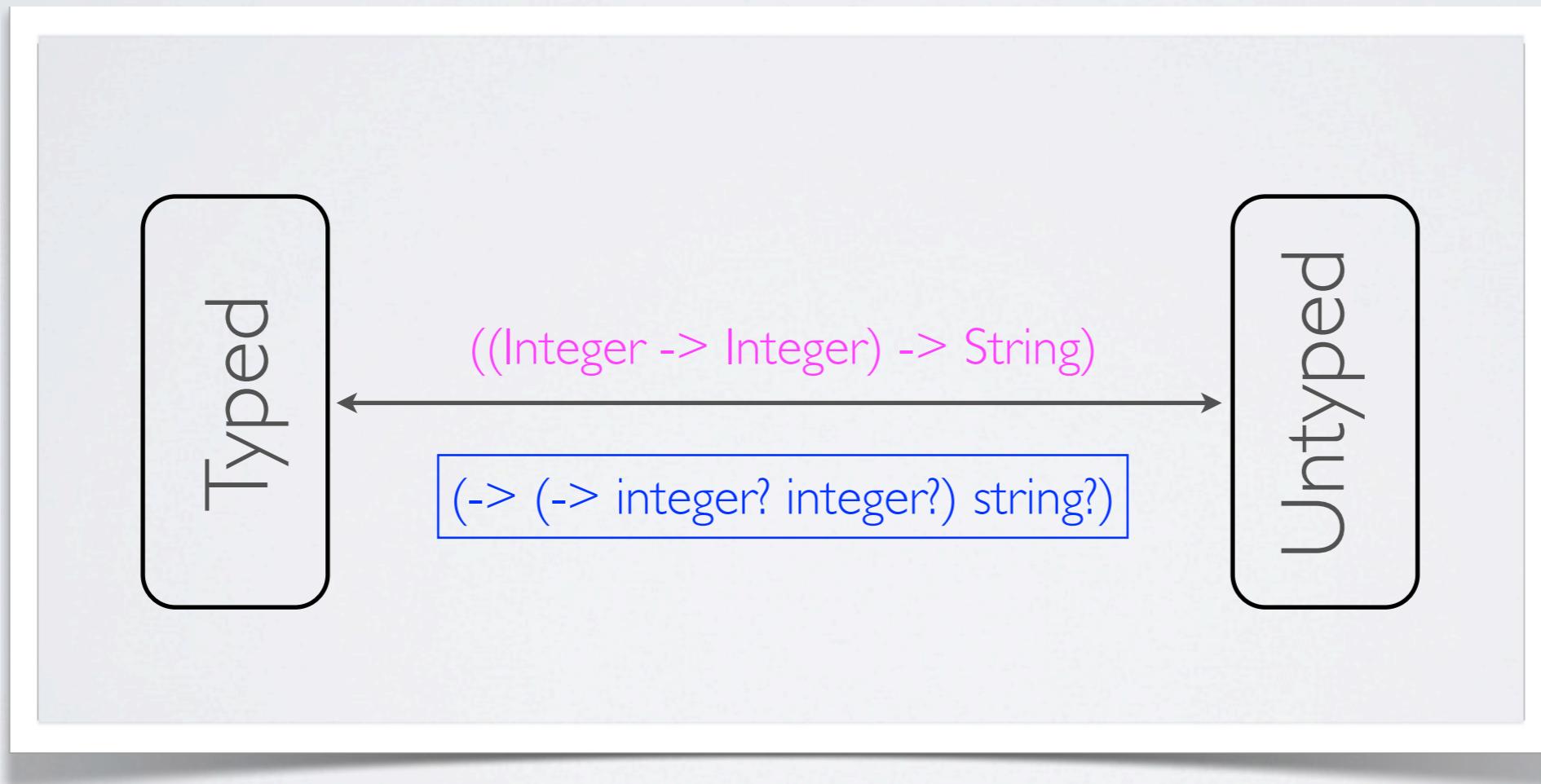
bang!

**step 1: typed ‘modules’ must specify types for all imported variables and specify types for all exports**



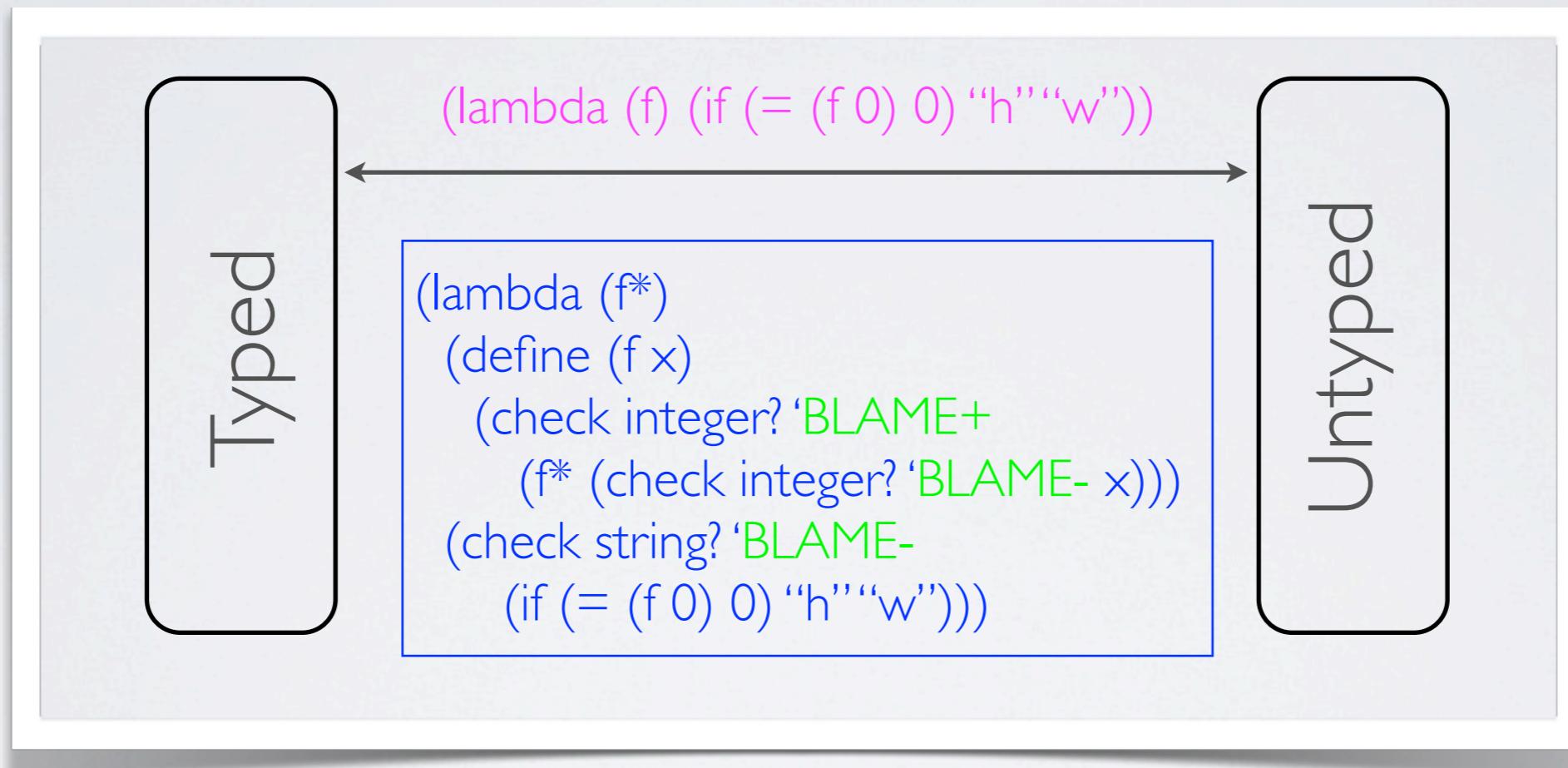
step 1: typed ‘modules’ must specify types for all imported variables and specify types for all exports

step 2: type checking converts ‘interface types’ into contracts that ‘blame’ the violating module --- when needed only!



at “contract boundaries” contracts are attached to a value

when functions are applied, contracts are checked



**Theorem:** Let  $P$  be a mixed program with checked types in interfaces interpreted as contracts. Then

- $P$  yields to a value,
- $P$  diverges, or
- $P$  signals an error that blames a specific untyped module.

**Theorem:** Let  $P$  be a mixed program with checked types in interfaces interpreted as contracts. Then

- $P$  yields to a value,
- $P$  diverges, or
- $P$  signals an error that blames a specific untyped module.

the “Blame Theorem”  
Tobin-Hochstadt & Felleisen (2006)

# ...TYPES FOR LISPERS

remember: adding types is good;  
changing code is bad

remember: adding types is good;  
changing code is bad

adding types to structure fields and type  
declarations for functions is acceptable

```
#lang scheme
```

```
(define-struct circle (radius))
```

```
;; Circle = (make-circle Number)
```

```
;; Circle → Number
```

```
(check-within
```

```
  (circle-area (make-circle 1)) pi .1)
```

```
(define (circle-area c)
```

```
  (* pi (circle-radius c) (circle-radius c)))
```

```
#lang scheme
```

```
(define-struct circle (radius))
```

```
; Circle = (make-circle Number)
```

```
; Circle → Number
```

```
(check-within
```

```
(circle-area (make-circle 1)) pi .1)
```

```
(define (circle-area c)
```

```
(* pi (circle-radius c) (circle-radius c)))
```

```
#lang typed/scheme
```

```
(define-struct: circle ({radius : Number}))
```

```
(: circle-area (circle → Number))
```

```
(check-within
```

```
(circle-area (make-circle 1)) pi .1)
```

```
(define (circle-area c)
```

```
(* pi (circle-radius c) (circle-radius c)))
```

**Scheme demands different types for  
different occurrences of parameters**

```
#lang scheme
```

```
(define-struct circle (radius))  
;; Circle = (make-circle Number)
```

```
...
```

```
(define-struct square (length))  
;; Square = (make-square Number)
```

```
...
```

```
;; Shape is one of:
```

```
;; -- Circle  
;; -- Square
```

```
;; ...
```

```
;; Shape → Number
```

```
(define (shape-area s)  
  (cond  
    [(circle? s) (circle-area s)]  
    [(square? s) (square-area s)])))
```

```
#lang scheme
```

```
(define-struct circle (radius))  
;; Circle = (make-circle Number)
```

```
...
```

```
(define-struct square (length))  
;; Square = (make-square Number)
```

```
...
```

```
;; Shape is one of:
```

```
;; -- Circle  
;; -- Square
```

```
;; ...
```

```
;; Shape → Number
```

```
(define (shape-area s)  
  (cond
```

```
    [(circle? s) (circle-area s)] ; programmers knows s : Circle  
    [(square? s) (square-area s)])
```

```
#lang typed/scheme
```

```
(define-struct: circle ({radius : Number}))
```

```
...
```

```
...
```

```
(define-struct: square ({length : Number}))
```

```
...
```

```
...
```

```
(define-type-alias shape
```

```
  (U circle
```

```
    square
```

```
    ...))
```

```
(: shape-area (shape → Number))
```

```
(define (shape-area s)
```

```
  (cond
```

```
    [(circle? s) (circle-area s)] ; and so does our type system !
```

```
    [(square? s) (square-area s)]))
```

Scheme demands different types for  
different occurrences of parameters

...

...  
and that must hold for **higher-order  
fragments** too

```
#lang scheme
...
;; (Listof shape) → Number
;; compute the areas of all squares in a list of arbitrary shapes
(define (sum-squares l)
  (foldl + 0
    (map square-area
      (filter square? l))))
```

```
#lang scheme  
...  
;; (Listof shape) → Number  
;; compute the areas of all squares in a list of arbitrary shapes  
(define (sum-squares l)  
  (foldl + 0  
    (map square-area ;; programmer knows: (listof square)  
      (filter square? l))))
```

```
#lang scheme
...
;; (Listof shape) → Number
;; compute the areas of all squares in a list of arbitrary shapes
(define (sum-squares l)
  (foldl + 0 ; programmer also knows: (listof number)
        (map square-area ; programmer knows: (listof square)
              (filter square? l))))
```

```
#lang typed-scheme  
...  
(: sum-squares ((Listof shape) → Number))  
;; compute the areas of all squares in a list of arbitrary shapes  
(define (sum-squares l)  
  (foldl + 0  
    (map square-area ;  
         ; and so does our type system  
         (filter square? l))))
```

“occurrence typing” is also necessary  
for paths into data structures

```
#lang scheme

;; Atom is either Number or false

;; [Listof Atom] → Number
;; sum the numbers in this list

(check-expect (sum (list 2 3 #f 4)) 9)

(define (sum l)
  (cond
    [(empty? l) 0]
    [(not (first l)) (sum (rest l))]
    [else (+ (first l) (sum (rest l))))]))
```

```
#lang scheme
```

```
; ; Atom is either Number or false
```

```
; ; [Listof Atom] → Number
```

```
; ; sum the numbers in this list
```

```
(check-expect (sum (list 2 3 #f 4)) 9)
```

```
(define (sum l)
```

```
  (cond
```

```
    [(empty? l) 0]
```

```
    [(not (first l)) (sum (rest l))] ; programmer knows: (first l) = #f
```

```
    [else (+ (first l) (sum (rest l)))]))
```

```
#lang scheme
```

```
; ; Atom is either Number or false
```

```
; ; [Listof Atom] → Number
```

```
; ; sum the numbers in this list
```

```
(check-expect (sum (list 2 3 #f 4)) 9)
```

```
(define (sum l)
```

```
  (cond
```

```
    [(empty? l) 0]
```

```
    [(not (first l)) (sum (rest l))]
```

```
    [else (+ (first l) (sum (rest l))))])
```

*; programmer: (first l) : Number*

```
#lang typed-scheme
```

```
(define-type-alias Atom (U Number #f))
```

```
(: sum ([Listof Atom] → Number))
```

```
;; sum the numbers in this list
```

```
(check-expect (sum (list 2 3 #f 4)) 9)
```

```
(define (sum l)
```

```
  (cond
```

```
    [(empty? l) 0]
```

```
    [(not (first l)) (sum (rest l))]
```

```
    [else (+ (first l) (sum (rest l)))])) ; and so does our type system
```

the type system needs some simple  
propositional reasoning

;Atom is either Number or #f.

; [Listof Atom] [Listof Atom] → [Listof Number]  
;; add corresponding numbers, drop false, stop at end of shortest list

(**check-expect** (mrg (list 1 false 2) (list 3 4 5 false 10)) (list 4 4 7))

(**define** (mrg l k)

(**cond**

[(or (empty? l) (empty? k))  
empty]

[(and (not (first l)) (not (first k)))  
(cons 0 (mrg (rest l) (rest k))))]

[(not (first l))  
(cons (first k) (mrg (rest l) (rest k))))]

[(not (first k))  
(cons (first l) (mrg (rest l) (rest k))))]

[else  
(cons (+ (first l) (first k)) (mrg (rest l) (rest k))))])

;Atom is either Number or #f.

; [Listof Atom] [Listof Atom] → [Listof Number]  
;; add corresponding numbers, drop false, stop at end of shortest list

(**check-expect** (mrg (list 1 false 2) (list 3 4 5 false 10)) (list 4 4 7))

(**define** (mrg l k)

(**cond**

[(or (empty? l) (empty? k))  
empty]

[(and (not (first l)) (not (first k)))  
(cons 0 (mrg (rest l) (rest k))))]

[(not (first l))  
(cons (first k) (mrg (rest l) (rest k))))]

[(not (first k))  
(cons (first l) (mrg (rest l) (rest k))))]

[else  
(cons (+ (first l) (first k)) (mrg (rest l) (rest k))))])

;Atom is either Number or #f.

; [Listof Atom] [Listof Atom] → [Listof Number]  
;; add corresponding numbers, drop false, stop at end of shortest list

(**check-expect** (mrg (list 1 false 2) (list 3 4 5 false 10)) (list 4 4 7))

(**define** (mrg l k)

(**cond**

[(or (empty? l) (empty? k))  
empty]

[(and (not (first l)) (not (first k)))  
(cons 0 (mrg (rest l) (rest k))))]

[**(not (first l))**

(cons **(first k)** (mrg (rest l) (rest k))))]

[**(not (first k))**

(cons (first l) (mrg (rest l) (rest k))))]

[**else**

(cons (+ (first l) (first k)) (mrg (rest l) (rest k))))])])

;Atom is either Number or #f.

; [Listof Atom] [Listof Atom] → [Listof Number]  
;; add corresponding numbers, drop false, stop at end of shortest list

(**check-expect** (mrg (list 1 false 2) (list 3 4 5 false 10)) (list 4 4 7))

(**define** (mrg l k)

(**cond**

[(or (empty? l) (empty? k))  
empty]

[(and (not (first l)) (not (first k)))  
(cons 0 (mrg (rest l) (rest k))))]

[(not (first l))  
(cons (first k) (mrg (rest l) (rest k))))]

[**(not (first k))**  
(cons (**first l**) (mrg (rest l) (rest k))))]

[**else**  
(cons (+ (first l) (first k)) (mrg (rest l) (rest k))))])

;Atom is either Number or #f.

;; [Listof Atom] [Listof Atom] → [Listof Number]  
;; add corresponding numbers, drop false, stop at end of shortest list

(**check-expect** (mrg (list 1 false 2) (list 3 4 5 false 10)) (list 4 4 7))

(**define** (mrg l k)

(**cond**

[(or (empty? l) (empty? k))  
empty]

[(and (not (first l)) (not (first k)))  
(cons 0 (mrg (rest l) (rest k)))]

[(not (first l))  
(cons (first k) (mrg (rest l) (rest k)))]

[(not (first k))  
(cons (first l) (mrg (rest l) (rest k)))]

[else ; programmers knows (first l) : Number, (first k) : Number  
(cons (+ (first l) (first k)) (mrg (rest l) (rest k))))])

**(define-type-alias** Atom (U Number #f))

(: mrg ([Listof Atom] [Listof Atom] → [Listof Number]))

;; add corresponding numbers, drop false, stop at end of shortest list

**(check-expect** (mrg (list 1 false 2) (list 3 4 5 false 10)) (list 4 4 7))

**(define** (mrg l k)

**(cond**

[[(or (empty? l) (empty? k))  
empty]

[(and (not (first l)) (not (first k)))  
(cons 0 (mrg (rest l) (rest k)))]

[(not (first l))  
(cons (first k) (mrg (rest l) (rest k)))]

[(not (first k))  
(cons (first l) (mrg (rest l) (rest k)))]

[else ;; as does our type system  
(cons (+ (first l) (first k)) (mrg (rest l) (rest k))))])

And a true “Lisp” type system comes with a lot more.

- abstraction over predicates
- explicit, first-class polymorphism
- *local* type inference to reduce annotation cost
- PLT Scheme-specific constructs (CL keywords, arity polymorphism, etc)

# CONCLUSION

### From PLT Scheme to LISP:

- from macros to languages
- types for Lispers

From PLT Scheme to LISP:

Macros are More than  
Functions on S-expressions.

- scope and macros
- modules and macros
- phases and macros
- specification and macros

From PLT Scheme to LISP:

Types are Promising.

- types for Lisp idioms
- sound types from contracts

# THE END

PLT Scheme *is* Racket.  
<http://racket-lang.org/>

Matthew Flatt (Utah)	language, compiler, macros
Shriram Krishnamurthi	macros and modules
Robby Findler (Northwestern)	contracts, IDE
Jay McCarthy (BYU)	macro-languages & web services
Ryan Culpepper (Utah)	macros
Sam Tobin-Hochstadt (Northeastern)	types
Stevie Strickland (Northeastern)	contracts & types

**(define-type-alias** Atom (U Number #f))

(: naughty ((Pair Atom Any) → Boolean : #f @ car))  
(define (naughty l) (not (first l)))

(: mrg ([Listof Atom] [Listof Atom] → [Listof Number]))

**(define** (mrg l k)

**(cond**

[(or (empty? l) (empty? k))  
empty]

[(and (not (first l)) (not (first k)))  
(cons 0 (mrg (rest l) (rest k)))]

[(naughty? l)]

(cons (first k) (mrg (rest l) (rest k))))]

[(naughty? k)]

(cons (first l) (mrg (rest l) (rest k))))]

[else

(cons (+ (first l) (first k)) (mrg (rest l) (rest k))))])