

TYPES FOR UNTYPED LANGUAGES

Matthias Felleisen (PLT)
Northeastern University

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-- anonymous friend from TLDI, 06/nov/2009

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types are bad for pl research.

-- me, many times

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types are bad for pl research.

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if i ran a company, i'd use a typed programming language.

-- me, also many times

it turns out that PLT is like running a company: start with two major components, glue them together with a few lines, and pretty soon you have several widely used apps and you need to maintain them.

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and now think how many other apps run on JavaScript, Lua, Perl, PHP, Python, Ruby (on Rails), and similar scripting languages

choice I: make fun of these languages,
their lack of type systems, their mistakes
with LAMBDA etc, the lack of PL
background of their designers, the
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types for untyped languages:
gradually enrich “scripts”
with explicit and sound types
without changing code

Goal: explicit types for “scripts” via a mixed typed/untyped language

problem I: programmers will convert only small pieces (“modules”) into explicitly typed form, but this “mixed” programming language should be as type sound as a plain typed language -- what does type soundness mean?

Goal: explicit types for “scripts” via a mixed typed/untyped language

problem 1: programmers will convert only small pieces (“modules”) into explicitly typed form, but this “mixed” programming language should be as type sound as a plain typed language -- what does type soundness mean?

problem 2: programmers will not wish to modify code to accommodate the type checker, so the type system must accommodate the existing idioms of the scripting language, though adding type declarations to functions, structures, methods, fields etc. is acceptable -- what makes a type system practical?

TYPE SOUNDNESS FOR MIXED PROGRAMS

T

#lang STLC

inc : int → int
inc(x) = x + 1

provide inc

U

#lang LC

require T

f(x) = ... inc(true) ...

T

```
#lang STLC
```

```
inc : int → int  
inc(x) = x + 1
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```
provide inc
```

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```
#lang LC
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```
require T
```

```
f(x) = ... inc(true) ...
```

T

#lang STLC

encode : (int → int) → int
encode(f) = ... f(42) + 21 ...

provide encode

U

#lang LC

require T

f(x) = ... x + 1 ... return "hello"

main(x) = ... encode(f) ...

T

#lang STLC

encode : (int → int) → int
encode(f) = ... f(42) + 21 ...

provide encode

U

#lang LC

require T

f(x) = ... x + 1 ... return "hello"

main(x) = ... encode(f) ...

T

#lang STLC

encode : (int → int) → int
encode(f) = ... f(42) + 21 ...

provide encode

bang!

U

#lang LC

require T

f(x) = ... x + 1 ... return "hello"

main(x) = ... encode(f) ...

U

#lang LC

inc(x) = x + 1

provide inc

T

#lang STLC

require U

f(x) = ... inc(???) ??? | 0 ...

U

#lang LC

inc(x) = x + 1

provide inc

T

#lang STLC

require U

f(x) = ... inc(???) ??? | 0 ...

U

#lang LC

inc(x) = x + 1

provide inc

T

#lang STLC

require U [inc : int → int]

f(x) = ... inc(42) + 10 ...

U

```
#lang LC
```

```
inc(x) = if x = 0  
           "hello"  
else  
           x + 1
```

```
provide inc
```

T

```
#lang STLC
```

```
require U [inc : int → int]
```

```
f(x) = ... inc(42) + 10 ...
```

U

```
#lang LC
```

```
inc(x) = if x = 0  
          "hello"  
      else  
          x + 1
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provide inc
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require U [inc : int → int]
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f(x) = ... inc(42) + 10 ...
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inc(x) = if x = 0  
          "hello"  
      else  
          x + 1
```

```
provide inc
```

T

```
#lang STLC
```

```
require U [inc : int ->
```

```
f(x) = ... inc(42) + 10 ...
```

bang

step I: typed ‘modules’ must specify types for all imported variables and specify types for all exports

step 1: typed ‘modules’ must specify types for all imported variables and specify types for all exports

step 2: type checking converts these ‘interface types’ into run-time checks that ‘blame’ the violator i.e., contracts [Findler, Felleisen ICFP 2002]

Theorem: Let P be a mixed program with checked types at **import** interpreted as contracts. Then

- P yields to a value,
- P diverges, or
- P signals an error that blames an untyped module.

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- P yields to a value,
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- P signals an error that blames an untyped module.

the “Blame Theorem”
Tobin-Hochstadt & Felleisen (2006)
improved: Wadler-Findler (2009)

question: what about polymorphism?

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answer 1: use generative data to protect access at run-time and get relationally parametric contracts [Guha, Matthews, Findler, Krishnamurthi, DLS 2003]

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answer 1: use generative data to protect access at run-time and get relationally parametric contracts [Guha, Matthews, Findler, Krishnamurthi, DLS 2003]

answer 2: this imposes a new implementation of all primitives and thus a large cost on the language -- it is an open problem and a very real one

PRACTICAL TYPES

adding types to structure fields and type declarations for functions is acceptable

```
#lang scheme
```

```
(define-struct circle (radius))
```

```
; Circle = (make-circle Number)
```

```
; Circle → Number
```

```
(check-within
```

```
(circle-area (make-circle 1)) pi .1)
```

```
(define (circle-area c)
```

```
(* pi (circle-radius c) (circle-radius c)))
```

```
#lang scheme
```

```
(define-struct circle (radius))
;; Circle = (make-circle Number)

;; Circle → Number
```

```
(check-within
  (circle-area (make-circle 1)) pi .1)

(define (circle-area c)
  (* pi (circle-radius c) (circle-radius c)))
```

```
#lang typed-scheme
```

```
(define-struct: circle ({radius : Number}))
```



```
(: circle-area (circle → Number))

(check-within
  (circle-area (make-circle 1)) pi .1)

(define (circle-area c)
  (* pi (circle-radius c) (circle-radius c)))
```

Scheme demands different types for
different occurrences of parameters

```
#lang scheme
```

```
(define-struct circle (radius))  
;; Circle = (make-circle Number)
```

```
...
```

```
(define-struct square (length))  
;; Square = (make-square Number)
```

```
...
```

```
;; Shape is one of:
```

```
;; -- Circle  
;; -- Square
```

```
;; ...
```

```
;; Shape → Number
```

```
(define (shape-area s)  
  (cond  
    [(circle? s) (circle-area s)]  
    [(square? s) (square-area s)])))
```

```
#lang scheme
```

```
(define-struct circle (radius))  
;; Circle = (make-circle Number)
```

```
...
```

```
(define-struct square (length))  
;; Square = (make-square Number)
```

```
...
```

```
;; Shape is one of:
```

```
;; -- Circle  
;; -- Square
```

```
;; ...
```

```
;; Shape → Number
```

```
(define (shape-area s)
```

```
  (cond
```

```
    [(circle? s) (circle-area s)] ; programmers knows s : Circle
```

```
    [(square? s) (square-area s)])])
```

```
#lang typed-scheme
```

```
(define-struct: circle ({radius : Number}))
```

```
...
```

```
(define-struct: square ({length : Number}))
```

```
...
```

```
(define-type-alias: shape
```

```
  (U
   circle
   square))
```

```
(: shape-area (shape → Number))
```

```
(define (shape-area s)
```

```
  (cond
```

```
    [(circle? s) (circle-area s)] ;; and so does our type system !
```

```
    [(square? s) (square-area s)]))
```

```
#lang scheme
...
;; (Listof shape) → Number
;; compute the areas of all squares in a list of arbitrary shapes
(define (sum-squares l)
  (foldl + 0
    (map square-area
      (filter square? l))))
```

```
#lang scheme  
...  
;; (Listof shape) → Number  
;; compute the areas of all squares in a list of arbitrary shapes  
(define (sum-squares l)  
  (foldl + 0  
    (map square-area ;; programmer knows: (listof square)  
      (filter square? l))))
```

```
#lang scheme  
...  
;; (Listof shape) → Number  
;; compute the areas of all squares in a list of arbitrary shapes  
(define (sum-squares l)  
  (foldl + 0 ;; programmer also knows: (listof number)  
        (map square-area ;; programmer knows: (listof square)  
             (filter square? l))))
```

```
#lang typed-scheme  
...  
(: sum-squares ((Listof shape) → Number))  
;; compute the areas of all squares in a list of arbitrary shapes  
(define (sum-squares l)  
  (foldl + 0  
    (map square-area ;  
         ; and so does our type system  
         (filter square? l))))
```

“occurrence typing” is also necessary for paths into data structures

```
#lang scheme

;; Atom is either Number or false

;; [Listof Atom] → Number
;; sum the numbers in this list

(check-expect (sum (list 2 3 #f 4)) 9)

(define (sum l)
  (cond
    [(empty? l) 0]
    [(not (first l)) (sum (rest l))]
    [else (+ (first l) (sum (rest l))))]))
```

```
#lang scheme
```

```
; ; Atom is either Number or false
```

```
; ; [Listof Atom] → Number
```

```
; ; sum the numbers in this list
```

```
(check-expect (sum (list 2 3 #f 4)) 9)
```

```
(define (sum l)
```

```
  (cond
```

```
    [(empty? l) 0]
```

```
    [(not (first l)) (sum (rest l))] ; programmer knows: (first l) = #f
```

```
    [else (+ (first l) (sum (rest l)))]))
```

```
#lang scheme
```

```
; ; Atom is either Number or false
```

```
; ; [Listof Atom] → Number
```

```
; ; sum the numbers in this list
```

```
(check-expect (sum (list 2 3 #f 4)) 9)
```

```
(define (sum l)
```

```
  (cond
```

```
    [(empty? l) 0]
```

```
    [(not (first l)) (sum (rest l))]
```

```
    [else (+ (first l) (sum (rest l))))])
```

; programmer: (first l) : Number

```
#lang typed-scheme
```

```
(define-type-alias Atom (U Number #f))
```

```
(: sum ([Listof Atom] → Number))
```

```
;; sum the numbers in this list
```

```
(check-expect (sum (list 2 3 #f 4)) 9)
```

```
(define (sum l)
```

```
  (cond
```

```
    [(empty? l) 0]
```

```
    [(not (first l)) (sum (rest l))] ; and so does our type system
```

```
    [else (+ (first l) (sum (rest l)))]))
```

the type system needs some simple
propositional reasoning

;Atom is either Number or #f.

; [Listof Atom] [Listof Atom] → [Listof Number]
;; add corresponding numbers, drop false, stop at end of shortest list

(check-expect (mrg (list 1 false 2) (list 3 4 5 false 10)) (list 4 4 7))

(define (mrg l k)

(cond

[(or (empty? l) (empty? k))
empty]

[(and (not (first l)) (not (first k)))
(cons 0 (mrg (rest l) (rest k))))]

[(not (first l))
(cons (first k) (mrg (rest l) (rest k))))]

[(not (first k))
(cons (first l) (mrg (rest l) (rest k))))]

[else
(cons (+ (first l) (first k)) (mrg (rest l) (rest k))))])

;Atom is either Number or #f.

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empty]

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(cons 0 (mrg (rest l) (rest k)))]

[(not (first l))
(cons (first k) (mrg (rest l) (rest k)))]

[(not (first k))
(cons (first l) (mrg (rest l) (rest k)))]

[else
(cons (+ (first l) (first k)) (mrg (rest l) (rest k))))])

;Atom is either Number or #f.

; [Listof Atom] [Listof Atom] → [Listof Number]
;; add corresponding numbers, drop false, stop at end of shortest list

(**check-expect** (mrg (list 1 false 2) (list 3 4 5 false 10)) (list 4 4 7))

(**define** (mrg l k)

(**cond**

[(or (empty? l) (empty? k))
empty]

[(and (not (first l)) (not (first k)))
(cons 0 (mrg (rest l) (rest k)))]

[(**not (first l)**)

(cons (**first k**) (mrg (rest l) (rest k))))]

[(**not (first k)**)

(cons (first l) (mrg (rest l) (rest k))))]

[**else**

(cons (+ (first l) (first k)) (mrg (rest l) (rest k))))])

;Atom is either Number or #f.

; [Listof Atom] [Listof Atom] → [Listof Number]
;; add corresponding numbers, drop false, stop at end of shortest list

(check-expect (mrg (list 1 false 2) (list 3 4 5 false 10)) (list 4 4 7))

(define (mrg l k)

(cond

[**(or** (**empty?** l) (**empty?** k))
empty]

[**(and** (**not** (**first** l)) (**not** (**first** k)))
(**cons** 0 (mrg (**rest** l) (**rest** k))))]

[**(not** (**first** l))
(**cons** (**first** k) (mrg (**rest** l) (**rest** k))))]

[**(not** (**first** k))
(**cons** (**first** l) (mrg (**rest** l) (**rest** k))))]

[**else**
(**cons** (+ (**first** l) (**first** k)) (mrg (**rest** l) (**rest** k))))])

;Atom is either Number or #f.

;; [Listof Atom] [Listof Atom] → [Listof Number]
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(**check-expect** (mrg (list 1 false 2) (list 3 4 5 false 10)) (list 4 4 7))

(**define** (mrg l k)

(**cond**

[(or (empty? l) (empty? k))
empty]

[(and (not (first l)) (not (first k)))
(cons 0 (mrg (rest l) (rest k)))]

[(not (first l))
(cons (first k) (mrg (rest l) (rest k)))]

[(not (first k))
(cons (first l) (mrg (rest l) (rest k)))]

[else ; programmers knows (first l) : Number, (first k) : Number
(cons (+ (first l) (first k)) (mrg (rest l) (rest k))))])

(define-type-alias Atom (U Number #f))

(: mrg ([Listof Atom] [Listof Atom] → [Listof Number]))

;; add corresponding numbers, drop false, stop at end of shortest list

(check-expect (mrg (list 1 false 2) (list 3 4 5 false 10)) (list 4 4 7))

(define (mrg l k)

(cond

[[(or (empty? l) (empty? k))
empty]

[(and (not (first l)) (not (first k)))
(cons 0 (mrg (rest l) (rest k)))]

[(not (first l))
(cons (first k) (mrg (rest l) (rest k)))]

[(not (first k))
(cons (first l) (mrg (rest l) (rest k)))]

[else ;; as does our type system
(cons (+ (first l) (first k)) (mrg (rest l) (rest k))))])

and programmers wish to abstract over predicates and paths in such programs

(define-type-alias Atom (U Number #f))

(: naughty ((Pair Atom Any) → Boolean : #f @ car))
(define (naughty l) (not (first l)))

(: mrg ([Listof Atom] [Listof Atom] → [Listof Number]))

(define (mrg l k)

(cond

[(or (empty? l) (empty? k))
empty]

[(and (not (first l)) (not (first k)))
(cons 0 (mrg (rest l) (rest k)))]

[(naughty? l)]

(cons (first k) (mrg (rest l) (rest k))))]

[(naughty? k)]

(cons (first l) (mrg (rest l) (rest k))))]

[else

(cons (+ (first l) (first k)) (mrg (rest l) (rest k))))])

all of this comes with the standard
polymorphic functions (ML)

plus some very Scheme-specific twists

```
#lang scheme
```

```
:: (A ... → Void) (Listof A) ... → Void
;; process the worklists until one of them is exhausted
```

```
(define (process-work-list f . wl)
```

```
  (cond
```

```
    [(ormap empty? wl) (void)]
```

```
    [else (begin
```

```
      (apply f (map first wl))
```

```
      (apply process-work-list f (map rest wl))))]))
```

```
#lang scheme

;; (A ... → Void) (Listof A) ... → Void
;; process the worklists until one of them is exhausted

(define (process-work-list f . wl) ;; variable number of arguments
  (cond
    [(ormap empty? wl) (void)]
    [else (begin
              (apply f (map first wl))
              (apply process-work-list f (map rest wl))))]))
```

```
#lang typed-scheme

(: process-work-list (forall ((A ...)) ((A ... -> Void) (Listof A) ... -> Void)))
;; process the worklists until one of them is exhausted

(define (process-work-list f . wl) ;; variable number of arguments
  (cond
    [(ormap empty? wl) (void)]
    [else (begin
              (apply f (map first wl))
              (apply process-work-list f (map rest wl))))]))
```

```
#lang typed-scheme

(: process-work-list (forall ((A ...) ((A ... -> Void) (Listof A) ... -> Void)))
;; process the worklists until one of them is exhausted

(define (process-work-list f . wl) ;; variable number of arguments
  (cond
    [(ormap empty? wl) (void)]
    [else (begin
              (apply f (map first wl))
              (apply process-work-list f (map rest wl))))]))
```

THEORETICAL TYPES

$TEnv \vdash \text{expression} : type$

where *type* includes “true union” types

$$\frac{TEnv(x) = t}{TEnv \vdash x : t}$$

$TEnv \vdash \text{expression} : \text{type}$

where *type* includes “true union” types

$$\frac{TEnv(x) = t}{TEnv \vdash x : t}$$

(: find-path ([Listof String] -> (U Path #f))
define (find-path los) ...)

$TEnv \vdash \text{expression} : \text{type}; \textcolor{red}{Filter+}, \textcolor{blue}{Filter-}$

where

$\textcolor{red}{Filter+}$ is a proposition for the case when expression evaluates to a true value

$\textcolor{blue}{Filter-}$ is a proposition for the case when expression evaluates to #f (false)

$TEnv \vdash \text{expression} : \text{type}; \textcolor{red}{Filter+}, \textcolor{blue}{Filter-}$

where

$\textcolor{red}{Filter+}$ is a proposition for the case when expression evaluates to a true value

$\textcolor{blue}{Filter-}$ is a proposition for the case when expression evaluates to #f (false)

$TEnv \vdash \text{tst} : t; Ftst+, Ftst-$

$TEnv * \textcolor{red}{Ftst+} \vdash tn : t; Ftn+, Ftn-$

$TEnv * \textcolor{blue}{Ftst-} \vdash tn : t; Fel+, Fel-$

$TEnv \vdash \mathbf{if} \text{tst} \mathbf{then} \ tn \ \mathbf{else} \ el : t; F+, F-$

$TEnv \vdash \text{expression} : \text{type}; \text{Filter}+, \text{Filter}-; \text{Subject}$

where

Subject is the path that expression explores, starting at some variable

Filter+ is a proposition for the case when expression evaluates to a true value

Filter- is a proposition for the case when expression evaluates to #f (false)

$TEnv \vdash \text{expression} : \text{type}; Filter+, Filter-; \text{Subject}$

where

Subject is the path that expression explores, starting at some variable

Filter+ is a proposition for the case when expression evaluates to a true value

Filter- is a proposition for the case when expression evaluates to #f (false)

$TEnv \vdash rator : (d \rightarrow r; F; O); Ftst+,Ftst-; Orator$

$TEnv \vdash tn : t; Ftn+,Ftn-; Orand$

$Oapp = \text{PathRator}(\text{PathRand}(x)) \text{ if } O = \text{PathRator} \text{ & } Orand = \text{PathRand}(x)$

$TEnv \vdash (rator\ rand) : t; F+,F-; Oapp$

$TEnv \vdash \text{expression} : \text{type}; Filter+, Filter-; \text{Subject}$

where

Subject is the path that expression explores, starting at some variable

Filter+ is a proposition for the case when expression evaluates to a true value

Filter- is a proposition for the case when expression evaluates to #f (false)

$TEnv \vdash rator : (d \rightarrow r; F; O); Ftst+,Ftst-; Orator$

$TEnv \vdash tn : t; Ftn+,Ftn-; Orand$

$Oapp = \text{PathRator}(\text{PathRand}(x)) \text{ if } O = \text{PathRator} \& \text{Orand} = \text{PathRand}(x)$

$TEnv \vdash (rator\ rand) : t; F+,F-; Oapp$

Example: assume x has type

```
(if (number? (first x))
    ;; path for number?: *
    ;; path for (first x): (first x)
    ;; combined: (first x)
    (add1 (first x)) ; combine path with filter and get (first x) : Number
    ...)
```

$TEnv \vdash (\lambda (x) \text{ expression}) : \text{dom} \rightarrow \text{rng}; \text{LatentFilter+}, \text{LatentFilter-}; \text{LatentSubject}$
where

LatentSubject is the path that *body* explores (when applied), starting at parameter

LatentFilter+ is a proposition for the case when *body* evaluates to a true value
(when applied)

LatentFilter- is a proposition for the case when *body* evaluates to #f (false)

(when applied)

$TEnv; \textcolor{red}{PropEnv} \vdash \text{expression} : \text{type}; \text{Filter}+, \text{Filter}-; \text{Subject}$

where

PropEnv is a collection of implications between filters

Subject is the path that expression explores, starting at some variable

$\text{Filter}+$ is a proposition for the case when expression evaluates to a true value

$\text{Filter}-$ is a proposition for the case when expression evaluates to $\#f$ (false)

$TEnv; \text{PropEnv} \vdash \text{expression} : \text{type}; \text{Filter}+, \text{Filter}-; \text{Subject}$

where

PropEnv is a collection of implications between filters

Subject is the path that expression explores, starting at some variable

$\text{Filter}+$ is a proposition for the case when expression evaluates to a true value

$\text{Filter}-$ is a proposition for the case when expression evaluates to $\#f$ (false)

$TEnv; \text{PropEnv} \vdash \text{tst} : t; \text{Ftst}+, \text{Ftst}-; \text{otst}$

$\text{PropEnv} * \text{Ftst}+ \vdash \text{Ftst}++$

$TEnv * \text{Ftst}++; \text{PropEnv} * \text{Ftst}+ \vdash \text{tn} : t; \text{Ftn}+, \text{Ftn}-; \text{otn}$

$\text{PropEnv} * \text{Ftst}- \vdash \text{Ftst}--$

$TEnv * \text{Ftst}--; \text{PropEnv} * \text{Ftst}- \vdash \text{tn} : t; \text{Fel}+, \text{Fel}-; \text{oel}$

$TEnv \vdash \mathbf{if} \text{ tst } \mathbf{then} \text{ tn } \mathbf{else} \text{ el} : t; \text{F}+, \text{F}-$

Theorem: The type system satisfies the usual type soundness theorem wrt to a standard CBV semantics.

Proof

- mechanized proof for part (Isabelle/Hol, Redex)
- proof requires “dead code” rules

EXPERIENCE

	Squad	Metrics	Acct	Spam	Sys	Rand	Total
LINES	2369	511	407	315	1290	618	5510
INCREASE	7%	25%	7%	6%	1%	3%	7%
USEFUL ANN	96	51	25	16	53	26	267
λ : ANN	34	22	2	8	22	0	88
OTHER ANN	12	7	1	1	0	1	22
define-struct:	16	2	0	0	4	1	23
TYPE ALIAS	13	7	0	2	2	3	27
require/typed	3	1	0	0	5	0	9
ANN/100 LINE	7.3	18	6.9	8.6	6.7	5.0	7.9
FIXES	5	3	4	5	8	0	25
FIXES/100 LINE	0.21	0.59	0.98	1.6	0.62	0.0	0.45
PROBLEMS	7	4	3	1	0	1	16
PROB/100 LINE	0.29	0.78	0.73	0.32	0.0	0.16	0.29
DIFFICULTY	**	***	**	*	*	*	

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Metrics : inspect Scheme programs
 overuses a complex data structure
 for different purposes

CONCLUSION

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Foster & Hicks et al.: Ruby
Field et al.: “occurrence typing” for COBOL
Vitek & Field et al.: Thorn
Wadler: theory

Contrast

Types **in** Language Design & Implementation

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Types **after** Language Design & Implementation:
untyped languages are more popular than typed languages
people build large systems in these languages
and **then** they discover the **need for types**

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untyped languages are more popular than typed languages
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the game is different:
asking programmers to rewrite code to appease a type
checker will not work; the type system must accommodate the language

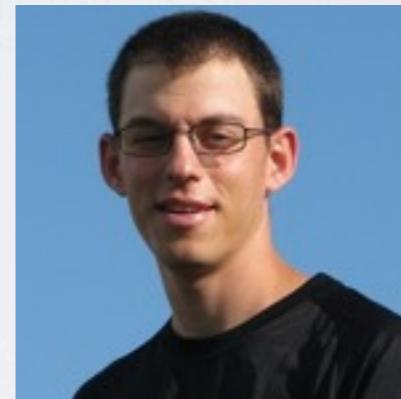
For Scheme we found these to be useful:

- “occurrence typing”
- separating positive and negative propositions
- separating out the subject of inspection
- basic propositional reasoning

Sam Tobin-Hochstadt,
Typed Scheme: From Scripts to Programs
NUPRL Dissertation, January 2010
<http://www.ccs.neu.edu/scheme/pubs/>

For other “scripting” languages
we may need these
and different techniques.
There’s plenty of work.

THE END



Sam Tobin-Hochstadt (NUPRL)



T. Stevie Strickland (NUPRL)

Ivan Gazeau (ENS)