Matching and Re-weighting

When X differ...

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Recap: Potential outcomes and Identification

To identify treatment effects one could **just** compare potential outcomes in two states:

- with treatment
- without treatment

Mathematically, average treatment effects would be:

$$ATE = E(Y_i(1) - Y_i(0))$$

the problem: with real data, we are only able to see one outcome. The counter factual is not observed:

$$Y_i = Y_i(1) * D + Y_i(0) * (1 - D)$$

and simple differences may not capture ATE, because of selection bias and heterogeneity in effects.

Recap: Gold Standard - RCT

The easiest, but most expensive, way to deal with the problem is using **Randomized Control Trials**.

Effectively, you randomize Treatment, so that potential outcomes are independent of treatment:

$$Y(1), Y(0) \perp D$$

In other words, the distribution of potential outcomes is the same for those treated or untreated units.

$$\begin{split} E(Y,D=1) &= E(Y(1),D=1) = E(Y(1),D=0) \\ E(Y,D=0) &= E(Y(0),D=1) = E(Y(0),D=0) \\ ATT &= E(Y,D=1) - E(Y,D=0) \end{split}$$

But what if you can't Randomize

When unconditional fails

More often than not, specially if we didn't construct the data, it would be impossible to find that unconditional independence assumption holds.

For example, treatment (say having health insurance) may vary by age, gender, race, location, etc.

This is similar to the selection bias: Outcomes across treated and untreated groups will be different because:

- Composition: Characteristics of people among the treated could be different than those among the untreated For example, they could be older, more educated, mostly men, etc.
- Other factors: There could be factors we cannot control for, that also affect outcomes.

There is conditional

When unconditional independence assumption fails, we can call on Conditional independence assumption:

$$Y(1), Y(0) \perp D|X$$

In other words, If we can look into specific groups (given X), it may be possible to impose the Independence assumption.

This relaxes the independence condition, but assumes selection is due to observable characteristics only. (it still needs to be as good as randomized given X)

Implications:

$$E(Y|D=1,X) = E(Y(1)|D=1,X) = E(Y(1)|D=0,X)$$

 $E(Y|D=0,X) = E(Y(0)|D=1,X) = E(Y(0)|D=0,X)$

Intuition

Matching is a methodology that falls within quasi-experimental designs. You cannot or could not decide the assignment rules, so now are using data as given.

The idea is to construct an artificial control and use it as a counter-factual, so that both treated and control groups "look similar" in terms of observables.

Once a group of synthetic controls has been constructed, treatment effects can be calculated for the whole population:

$$ATE(X) = E(Y|D=1,X) - E(Y|D=0,X)$$

$$ATE = \int ATE(X) dFx$$

How can we do this?

we just need to find observational twins!

Matching Twins



Prince Charles

- Male
- Born in 1948
- Raised in the UK
- Married twice
- Lives in a castle
- Wealthy & famous



Ozzy Osbourne

- Male
- Born in 1948
- Raised in the UK
- Married twice
- Lives in a castle
- Wealthy & famous

Figure 1: Matching on Observables

Subclassification or stratification

Consider the following dataset:

```
frause titanic, clear
expand freq
drop if freq==0
gen class1=class==1
tab survived class1 , nofreq col
```

<IPython.core.display.HTML object>

(Data downloaded from R base)
(8 zero counts ignored; observations not deleted)
(2,177 observations created)
(8 observations deleted)

Survived	 	class1 0	1		Total
No Yes	 -	72.92 27.08	37.54 62.46	•	67.70 32.30
Total			100.00		100.00

If we assume full Independence assumption we would believe that being in first class increased chance of survival in 35.4%. but is that the case?

What if the composition of individuals differs across classes (women and children)

```
tab age class1, nofreq col
tab sex class1, nofreq col
```

class1		
0 +	1	Total
5.49 94.51	1.85 98.15	4.95 95.05
100.00	100.00	100.00
class1 0	1	Total
	0 +	0 1 +

Male Female	İ	17.32	55.38 44.62	İ	21.35
	:	100.00			100.00

There were fewer children, but more women in first class. Perhaps that explains the difference in survival rates

A better approach would be to look into the survival probabilities stratifying the data:

```
gen surv=survived==2
bysort age sex class1:egen sr_mean=mean(survived==2)
table (age sex) (class1), stat(mean surv) nototal
```

 +	class1 0	
I		
l		
1 .40	67797	1
.61	36364	1
I		
l		
.18	83378	.3257143
.62	63345	.9722222
	.61 .18	0 + .4067797

So even within each group, the survival probability is larger in first class. What about Average?

```
bysort age sex:egen sr_mean_class1=max(sr_mean*(class1==1))
bysort age sex:egen sr_mean_class0=max(sr_mean*(class1==0))
gen teff = sr_mean_class1-sr_mean_class0
sum teff if class1==1 // ATT
sum teff if class1==0 // ATU
sum teff // ATE
```

Max	Min	Std. dev.	Mean	Variable
.5932204	.1373765	.1125033	.2375421	teff
Max	Min	Std. dev.	Mean	Variable
.5932204	.1373765	.1089261	.1887847	teff
Max	Min	Std. dev.	Mean	 Variable
.5932204	.1373765	.1107948	.1959842	teff

What did we do?

The procedure above is a simple stratification approach, aka matching, to analyze the true impact of the treatment (being a 1st class passenger).

- 1. Stratified the sample in groups by age and gender.
 - Identify the shares of each group by class1
- 2. Predict probability of survival per strata and class1
- 3. Obtain the Strata level Effects
- 4. Aggregate as needed.
 - Here, we could estimate ATE, ATT or ATU!

Where could things go wrong?

Overlapping

The procedure describe above works well whenever there is data overlapping.

- For every combination of X, you see data on the control and treated group 0 < P(D|X) < 1

When this fails, you wont be able to estimate ATE's, although ATT's or ATU's might still be possible:

for ATT: P(D|X) < 1
 for ATU: 0 < P(D|X)

For example:

```
frause hhprice, clear
keep price rooms type_h
tab rooms type_h
```

		=0 if house	e, =1		
Number of		TownHous	se		
rooms		0	1		Total
1	-+- 	37	 72	·+- 	109
2	İ	1,134	751	İ	1,885
3		4,634	648		5,282
4		2,465	115		2,580
5	1	465	2	1	467
6	1	46	0	1	46
7	1	7	0		7
	-+-			+-	
Total		8,788	1,588		10,376

Would not be able to estimate ATE nor ATU. Only ATT for townhouses.

Curse of dimensionality

There is a second problem in terms of stratification. How would we deal with Multiple dimensions? Would it be possible to find "twins" for every observation?

The answer is, probably no. Too many groups to track, to many micro cells to make use of:

```
frause oaxaca, clear
drop if lnwage==.
egen strata=group(educ isco)
bysort strata:egen flag=mean(female)
list educ isco female if (flag==0 | flag==1) & educ == 10, sep(0)
```

(Excerpt from the Swiss Labor Market Survey 1998) (213 observations deleted)

```
+----+
| educ isco female |
```

	-			
158.		10	1	0
159.		10	1	0
197.		10	7	0
198.		10	7	0
199.		10	9	1
200.		10	9	1
	+-			+

Alternative: Matching as a weighted

The problem of curse of dimensional states that as the number of desired characteristics to match increase, fewer "twins" will be available in the data. At the end...no one will be like you!

The alternative, is to look into People that are sufficiently close so they can be used for matching.

$$\begin{split} ATT_i &= Y_i - \sum_{j \in C} w(x_j, x_i) Y_j \\ ATT &= \frac{1}{N_T} \sum (ATT_i) \\ ATT &= E(Y|D=1) - E_i \left(\sum_{j \in C} w(x_j, x_i) Y_j \middle| D = 0 \right) \end{split}$$

Depending how w(.) is defined, we would be facing different kinds of matching estimators.

Types of Matching

Matching on covariates

The first decision to take is whether one should find matches based on covariates, or based on scores (propensity scores).

Using covariates implies that will aim to find the closest "twin" possible, based on multiple dimensions:

$$\begin{split} Eclidean &= d(x_i,x_j) = \sqrt{(x_i-x_j)'(x_i-x_j)} \\ WEclidean &= d(x_i,x_j) = \sqrt{(x_i-x_j)'W(x_i-x_j)} \\ Maha &= d(x_i,x_j) = \sqrt{(x_i-x_j)'S^{-1}(x_i-x_j)} \end{split}$$

Distance measures are used to identify the closest matches to a given observation, and thus the weight assigned to that observation.

Has the advantage of looking at individuals who are indeed close to each other, but becomes more difficult as the dimensionality of X's increase. (you will not find close matches)

Matching on Scores

A second approach is to match individuals based on some summary index that condenses the information in X into a single scalar h(x), reducing the dimensionality problem from K to 1.

Few candidates:

- Propensity Score: P(D|X) based on a logit/probit/binomial model. Most common approach!
- Predicted Mean: $X\beta$ if there is information on outcome to be predicted
- PCA: Using Principal components to reduce dimensionality before Matching

Since there is only 1 dimension to consider, multiple distance measures are possible:

• nearest neighbors, kernel weight matching, radious matching.

But one has to be careful with the approach. King and Nielsen (2019) Argue about the risks of PSM

1 vs K matching; With and without replacement

Two additional questions remain regarding matching. How many "twins" to use, and if twins will be obtained with/without replacement.

- Fewer matches reduce bias (choosing only the closest observation), but increase variance.
- More matches increase bias, but reduce variance. (because of less optimal matches)
- with replacement: control units may be used more than once. This will improve matching
 quality reducing bias. But by using the same units multiple times, it will increase
 variance.
- without replacement: Control units are used once, potentially reducing matching quality, but reducing variance. It will be order dependent.

see Caliendo and Kopeing (2008)

What about SE? and Statistical inference?

Well....this is one of the few cases where Bootstrapping WON'T work!

Standard errors are more cumbersome. So we will just rely on software results

Other considerations

Once you have chosen your matching method, find your "statistical twins", and estimate your differences you are done! (or are you)

Not yet...common practice: Evaluate the balance of your data

Matching aims to reduce or eliminate differences in characteristics between treatment and control units. Thus, one should evaluate the differences (before and after match) of your characteristis

- 1. Check for overlapping condition.
- either variable by variable or with pscore
- 2. Assess Matching Quality: Have differences across groups vanished?
- Check Standardized differences $\frac{\mu_1 \mu_2}{\sqrt{0.5*(V_1 + V_2)}}$
- t-tests
- PR2 of regression with matched data

Implementation

In Stata, there are at least two approaches that can be used for matching:

- psmatch2 (from ssc)
- teffects (Official Stata command)

We will use this to answer a simple question:

What is the impact of Traing Jobs on Earnings?

Example

This file contains information on experimental and observed data for the analysis of training on earnings program:

```
use https://friosavila.github.io/playingwithstata/drdid/lalonde.dta, clear
keep if year==1978
drop if dwincl==0
label define sample 1 "exper" 2 "CPS" 3 "PSID"
label values sample sample
tab sample treated,m
```

(19,204 observations deleted)
(277 observations deleted)

	1	treated		
sample	0	1	•	Total
	+			+
exper	260	185	0	445
CPS	0	0	15,992	15,992
PSID	0	0	2,490	1 2,490
	+			+
Total	l 260	185	18,482	18,927

First Experimental design - RCT

```
reg re treated
tabstat age educ black married nodegree , by(treated)
logit treated age educ black hisp married nodegree
```

Source		df	MS	Number of ob	_	445
	·			1(1, 110)	=	8.04
Model		1	348013183		=	0.0048
Residual	1.9178e+10	443	43290369.3	1	= d =	0.0178
	1.9526e+10	444	43976681.9	naj n bquare	a = =	0.0156 6579.5
re	Coefficient			P> t [95%		interval]

treated	1794.342	632.8534	2.84	0.005	550.5745	3038.11
_cons	4554.801	408.0459	11.16	0.000	3752.855	5356.747

Summary statistics: Mean Group variable: treated

treated	age		black		nodegree
0 1	25.05385 25.81622	10.08846 10.34595	.8269231 .8432432	.1538462	.7081081
Total	25.37079				

Iteration 0: log likelihood = -302.1 Iteration 1: log likelihood = -294.72908 Iteration 2: log likelihood = -294.71464 Iteration 3: log likelihood = -294.71464

Logistic regression

Number of obs = 445 LR chi2(6) = 14.77 Prob > chi2 = 0.0221 Pseudo R2 = 0.0244

Log likelihood = -294.71464

treated		Std. err.	z	P> z	[95% conf.	interval]
age educ black hisp married nodegree cons	.0059171063959725436898291587 .23424158385524 1.053028	.0142668 .071354 .3639735 .5042305 .2661824 .3093833	0.41 -0.90 -0.70 -1.64 0.88 -2.71	0.678 0.370 0.485 0.100 0.379 0.007 0.315	0220452 203811 9677438 -1.817432 2874665 -1.444933 9998064	.0338794 .0758916 .4590061 .159115 .7559495 2321722 3.105862

Then using PScore Matching CPS

```
keep if treated == 1 | sample ==2
replace treated=0 if treated==.
reg re treated
tabstat age educ black hisp married nodegree , by(treated)
```

(2,750 observations deleted)
(15,992 real changes made)

Source	SS	df	MS		er of obs 16175)	=	16,177 142.43
Model Residual	1.3206e+10	1 16,175	1.3206e+10) Prob	> F uared	=	0.0000
	1.5129e+12	16,176	93528158.4	- Adj	R-squared MSE	=	0.0087 9629
re	Coefficient			P> t		onf.	interval]
treated _cons		712.0207 76.14292		0.000	-9893.15	-	-7101.877 14995.91

Summary statistics: Mean Group variable: treated

treated	J	educ		-	married	nodegree
0 1	33.22524 25.81622	12.02751 10.34595	.0735368 .8432432	.072036 .0594595	.1891892	.7081081
+- Total		12.00828				

We need to do trimming

```
bysort educ black hisp married:egen n11=sum(treated==1)
bysort age black hisp married:egen n22=sum(treated==1)
drop if n11==0 | n22 ==0
```

tabstat age educ ${\color{red} black}$ hisp married nodegree , by(treated) reg re treated

(13,536 observations deleted)

Summary statistics: Mean Group variable: treated

treated		_	educ t			_		ied	node	gre	e
1	24.241 25.816	45 11.69 22 10.34	9788 .25 4595 .843	52443 32432	.0260	586 595	.3346				
·		76 11.60	0318 .293	38281	.0283	983	.3244	983	. 288	527	1
			d1				Number F(1, 2				2,641 73.89
	·						Prob >				
			2,639				R-squa				0.0272
	+					-	Adj R-	squa	red	=	0.0269
Tota	1 2.	1151e+11	2,640	801	17339.	3	Root M	SE		=	8829.8
			Std. err								
treate	d -5	786.584	673.1834	1 -	8.60	0.0	000	-710	6.605	;	-4466.564
_con	s 1	2135.73	178.1702	2 6	88.11	0.0	000	117	86.36	5	12485.1

Lets do some matching

```
teffects nnmatch (re age educ black married nodegree ) (treated)
tebalance summarize
teffects nnmatch (re age educ black married nodegree ) (treated), nn(2)
tebalance summarize
teffects psmatch (re) (treated age educ black married nodegree )
tebalance summarize
```

teffects psmatch (re) (treated age educ $\frac{black}{black}$ married nodegree), nn(2) tebalance summarize

Treatment-effe Estimator Outcome model Distance metr:	: nearest-ne : matching		of obs = requested = min = max =	2,641 1 1 138		
	 Coefficient +				2 - 7	interval]
ATE treated						-1355.923
(refitting the	e model using	the generate	e() opti	on)		

Covariate balance summary

	Raw	Matched
Number of obs =	2,641	5,282
Treated obs =	185	2,641
Control obs =	2,456	2,641

	Raw		s Vari Raw	ance ratio Matched
age educ black married nodegree	.2342346 7684118	015417 0812288 0 0008087	1.305844 1.881909 .7039609 .6923501 1.088086	.8410946 .8598207 1 .999393

Treatment-effect	s estimation	Number of obs	=	2,641
Estimator :	nearest-neighbor matching	Matches: requested	=	2
Outcome model :	matching	min	=	2
Distance metric:	Mahalanobis	max	=	138

 re	Coefficient		z		[95% conf.	interval]
ATE						
treated	_5166 000	1107 652	_1 66	0 000	_7227 0/10	_2005_020
(1 VS 0)	-5100.000		-4.00		-7337.848 	-2990.929
(refitting the	model using	the generate	e() opti	ion)		
Covariate bala	nce summary					
	Ra	w Match	ned			
Number of obs	= 2,64	.1 5,2	282			
Treated obs						
Control obs	= 2,45	66 2,6	641 			
		ed difference w Matche			ance ratio Matched	
	+					
_	e .234234				.7345997	
	c 768411 k 1.47310				.8978301 1 006716	
	d 335131					
	e 1.01039			1.088086		
Treatment-effe	cts estimation	n		Number o	f obs =	2,641
	: propensity	-score match	ning	Matches:	requested =	1
Outcome model	: matching				min =	1
Treatment mode	1: logit				max =	138
1		AI robust				
re		std. err.			[95% conf.	interval]
ATE						
treated						
(1 vs 0)	-4278.549	1135.847	-3.77	0.000	-6504.768	-2052.331
(£:++: + 1						

(refitting the model using the generate() option)

Covariate balance summary

	Raw	Matched
Number of obs =	2,641	5,282
Treated obs =	185	2,641
Control obs =	2,456	2,641

| Standardized differences | Variance ratio | Raw | Matched | Raw | Matched | Raw | Matched | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw | Matched | Raw |

(refitting the model using the generate() option)

Covariate balance summary

	Raw	Matched
Number of obs =	2,641	5,282
Treated obs =	185	2,641
Control obs =	2,456	2,641

	I	Raw	differences Matched	R	aw	ance ratio Matched
age educ black married nodegree	1	.2342346 7684118 1.473105 3351313 1.010393	06133 1321518 0698339 0414439 .0939209	1.3058 1.8819 .70396 .69235 1.0880	44 09 09 01	.8834346 1.021302 .933348 .9674741 1.080951

A missing variable? Earnings in previous year. May capture information of Need to do treatment (selection)

```
tabstat age educ black hisp married nodegree re74, by(treated)
gen dre = re-re74
teffects nnmatch (dre age educ black married nodegree ) (treated)

teffects nnmatch (dre age educ black married nodegree ) (treated), nn(2)

teffects psmatch (dre) (treated age educ black married nodegree )

teffects psmatch (dre) (treated age educ black married nodegree ), nn(2)
```

Summary statistics: Mean Group variable: treated

treated	age		black	-	married	nodegree
0 1	24.24145 25.81622	11.69788 10.34595	. 252443 . 8432432	.0260586 .0594595	.3346906 .1891892	.7081081
Total	24.35176					

treated | re74

0 93 1 20	95.574					
Total 88	339.421					
Treatment-effects estimation Estimator : nearest-neighbor matching Outcome model : matching Distance metric: Mahalanobis					min =	
					[95% conf.	interval]
ATE treated					-917.4997	6150.806
Treatment-effects estimation Estimator : nearest-neighbor matching Outcome model : matching Distance metric: Mahalanobis				Matches:	min =	2 2 138
	Coefficient	AI robust			[95% conf.	
ATE treated (1 vs 0)	'	1674.91	0.44	0.663	-2552.47 	4013.055
Treatment-effects estimation Estimator : propensity-score matching Outcome model : matching Treatment model: logit				min =		1 1 138
dre	Coefficient	AI robust std. err.	z	P> z	[95% conf.	
ATE treated					-1248.262	5572.884

Treatment-effects estimation Estimator : propensity-score matching Outcome model : matching Treatment model: logit				Number o	2,641 2 2 138	
	 Coefficient				2	interval]
ATE treated (1 vs 0)	 	1739.496	1.05	0.292	-1576.318	5242.379

In this case, Matching alone could not get the right answer. Who were the most likely to "go to the training?"

So instead we change the question: How much the change in earnings compare across groups.

Wait: What about Reweighting?

An alternative method to Matching is to do Re-weighting.

We have seen this!

Your control group has a distribution g(x) and your treatment f(x). We can use some weighting factors h(x) that reshapes $g(x) \to \hat{f}(x)$.

How? Using Propensity scores

Why does it work? Just as matching, your goal is to compare distributions of outcomes, forcing differences in observed characteristics to be the same.

IPW, does this by reweighting the distribution! (rather than matching)

Inverse Probability Weighting: IPW

s1: Estimate Pscore

$$p(D = 1|X) = F(X\beta)$$

S2: Estimate IPW

For ATT:
$$W(D=1,x) = 1 \& W(D=0,X) = \frac{\hat{p}(x)}{1-\hat{p}(x)}$$

For ATU:
$$W(D=0,x)=1$$
 & $W(D=1,X)=\frac{1-\hat{p}(x)}{\hat{p}(x)}$

For ATE:
$$W(D=0,x)=\frac{1}{1-\hat{p}(x)}~\&~W(D=1,X)=\frac{1}{\hat{p}(x)}$$

s3: Estimate Treatment effect:

$$TE = \sum_{i \in D=1} w_i^s(1) Y_i - \sum_{i \in D=0} w_i^s(0) Y_i$$

Even Better: Go DR!

An interesting advantage of IPW approach is that you can gain efficiency using Doubly Robust Methods. Namely, instead of comparing outcomes directly, you could compare predicted outcomes!

$$\begin{split} ATT &= \frac{1}{N_t} \sum (Y_1 - X' \hat{\beta}_w^0) \\ ATU &= \frac{1}{N_c} \sum (X' \hat{\beta}_w^1 - Y_0) \\ ATE &= \frac{1}{N} \sum (X' \hat{\beta}_w^1 - X' \hat{\beta}_w^0) \end{split}$$

where $\hat{\beta}_w^k$ can be modeled using weighted least squares

Comparing to Matching

```
teffects ipw (re) (treated age educ black married nodegree), iter(3) nolog teffects ipwra (re age educ black married nodegree) (treated age educ black married nodegree) teffects ipw (dre) (treated age educ black married nodegree), iter(3) nolog teffects ipwra (dre age educ black married nodegree) (treated age educ black married nodegree)
```

ATE treated (1 vs 0)	•	1088.667	-4.44	0.000	-6967.101	-2699.603		
POmean treated	+ 							
0	11979.19	179.1903	66.85	0.000	11627.99	12330.4		
Treatment-effe Estimator Outcome model Treatment mode	: IPW regres : linear	Number	of obs =	2,641				
re		std. err.			[95% conf.	interval]		
ATE treated (1 vs 0)	-4835.38				-6820.036	-2850.724		
POmean treated 0		179.0958	66.87	0.000	11625.49	12327.54		
Warning: Convergence not achieved.								
Treatment-effects estimation Estimator : inverse-probability weights Outcome model : weighted mean Treatment model: logit					of obs =	2,641		
dre	Coefficient	Robust std. err.			[95% conf.	interval]		
ATE treated (1 vs 0)					-2037.382	4988.802		
POmean treated								

	0	-	2746.475	161.2845	17.03	0.000	2430.363	3062.587
Warning: Convergence not achieved.								
Treatment-effects estimation Estimator : IPW regression adjustment Outcome model : linear Treatment model: logit						Number	of obs =	2,641
			Coefficient				[95% conf.	interval]
ATE tre	ated 0)	 		1516.493	0.85	0.396	-1685.666	4258.875
POmean	ated	- -					2438.338	3071.173
Warning: Convergence not achieved.								

Next: Regression Discontinuity