

LoRaSp

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# Chapter 1

## Class Index

### 1.1 Class Hierarchy

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# Chapter 2

## Class Index

### 2.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

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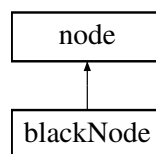
## Chapter 3

# Class Documentation

### 3.1 blackNode Class Reference

Class `blackNode`.

`#include <blackNode.h>`Inheritance diagram for `blackNode::`



#### Public Member Functions

- `blackNode ()`  
*Default constructor.*
- `blackNode (redNode *, tree *, int, int)`  
*Constructor::*
- `~blackNode ()`  
*Destructor.*
- `redNode * parent () const`  
*Returns parent\_.*
- `int * OuterIndex () const`  
*Returns outer\_index\_ptr\_.*
- `int * InnerIndex () const`  
*Returns inner\_index\_ptr\_.*
- `redNode * leftChild () const`  
*Returns pointer to the left child.*

- `redNode * rightChild () const`  
*Returns pointer to the right child.*
- `superNode * superChild () const`  
*Returns pointer to the super child.*
- `redNode * redParent ()`  
*Returns pointer to its parent.*
- `redNode * redParent (int)`  
*overloaded version for many levels up*
- `double mergeChildren ()`  
*Merge left and right redNodes to a [superNode](#).*
- `void mergeRHS ()`  
*Merge RHS of children.*
- `timeTuple2 schurComp ()`  
*Apply schur-complement.*

### 3.1.1 Detailed Description

Class [blackNode](#). Inherited from the general class [node](#). It is a [node](#) corresponding to the local variables, and multipole equations.

### 3.1.2 Constructor & Destructor Documentation

#### 3.1.2.1 `blackNode::blackNode (redNode * P, tree * T, int first, int last)`

Constructor:.. input arguments: pointer to the [redNode](#) parent, pointer to the [tree](#), range of belonging rows/cols

Array of start indices in edgetab

Adjacency array of every vertex

### 3.1.3 Member Function Documentation

#### 3.1.3.1 `double blackNode::mergeChildren ()`

Merge left and right redNodes to a [superNode](#). Output is the time elapsed.

#### 3.1.3.2 `timeTuple2 blackNode::schurComp ()`

Apply schur-complement. This function is called immediately after its [superNode](#) child is eliminated.

The documentation for this class was generated from the following files:

- blackNode.h
- blackNode.cpp

## 3.2 diagPC Class Reference

This is the diagonal preconditioner.

```
#include <diagPC.h>
```

### Public Member Functions

- [diagPC](#) ()  
*Default constructor.*
- [diagPC](#) (spMat \*A)  
*constructor*
- [~diagPC](#) ()  
*Destructor.*
- VectorXd & [solve](#) (VectorXd &b)  
*Solve function.*

### 3.2.1 Detailed Description

This is the diagonal preconditioner.

### 3.2.2 Constructor & Destructor Documentation

#### 3.2.2.1 [diagPC::diagPC \(spMat \\* A\)](#) `[inline]`

constructor Takes pointer to the sparse matrix

The documentation for this class was generated from the following file:

- [diagPC.h](#)

## 3.3 edge Class Reference

Class `edge`.

```
#include <edge.h>
```

### Public Member Functions

- `edge ()`  
*Default constructor.*
- `edge (node *, node *)`  
*Constructr.*
- `node * source () const`  
*Returns pointer to the source `node`.*
- `node * destination () const`  
*Returns pointer to the destination `node`.*
- `bool isWellSeparated ()`  
*Check if `edge` is between two spearated nodes.*
- `void compress ()`  
*Compress the `edge`.*
- `bool isEliminated ()`  
*Check if the `edge` is eliminated.*
- `bool isCompressed () const`  
*Returns the compressed flag.*

### Public Attributes

- `densMat * matrix`  
*Pointer to the interaction matrix.*

#### 3.3.1 Detailed Description

Class `edge`. An `edge` can connect any two nodes (red, black, `superNode`). It has the data of the corresponding interaction block. Convention: Edge is created by its source `node`.

#### 3.3.2 Constructor & Destructor Documentation

##### 3.3.2.1 `edge::edge (node * s, node * d)`

Constructr. Constructor inputs are: pointer to the source `node`, pointer to the destination `node`,

### 3.3.3 Member Function Documentation

#### 3.3.3.1 void edge::compress ()

Compress the [edge](#). This function should be called after an [edge](#) is compressed, and moved to the parent level. As a result the following steps happen:

- Set the compressed\_ flag to [true]
- Free the matrix memory

#### 3.3.3.2 bool edge::isEliminated ()

Check if the [edge](#) is eliminated. An [edge](#) is eliminated during the elimination process iff either its source or destination [node](#) is eliminated

#### 3.3.3.3 bool edge::isWellSeparated ()

Check if [edge](#) is between two separated nodes. This function check if the edges source and separation are well separated. The adjacency list of nodes are used to determine that. Note that source and dest. can be different [node](#) types at different levels.

### 3.3.4 Member Data Documentation

#### 3.3.4.1 densMat\* edge::matrix

Pointer to the interaction matrix. a pointer to a dense m by n matrix note: n is the number of columns (variables at source [node](#)), and m is the number of rows ( equations at destination [node](#)).

The documentation for this class was generated from the following files:

- edge.h
- edge.cpp



## 3.4 eyePC Class Reference

This is the default preconditioner.

```
#include <eyePC.h>
```

### Public Member Functions

- [eyePC](#) ()  
*Default constructor.*
- [~eyePC](#) ()  
*Destructor.*
- VectorXd & [solve](#) (VectorXd &b)  
*Solve function.*

#### 3.4.1 Detailed Description

This is the default preconditioner. Essentially, this preconditioner = no preconditioner!

The documentation for this class was generated from the following file:

- eyePC.h

## 3.5 gmres< precondition > Class Template Reference

Class [gmres](#).

```
#include <gmres.h>
```

### Public Member Functions

- [gmres](#) ()  
*Default constructor.*
- [~gmres](#) ()  
*Destructor.*
- [gmres](#) (spMat \*, precondition \*, VectorXd \*, VectorXd \*, int, double, bool)  
*Constructor with input parameters.*
- void [solve](#) ()  
*solve: start iteration until:*
- VectorXd \* [residuals](#) ()  
*Returns vector of residuals.*
- VectorXd \* [retVal](#) ()  
*Returns solution.*
- int [totalIters](#) () const  
*Returns total number of iterations.*
- double [totalTime](#) () const  
*Returns total time to solve.*

### 3.5.1 Detailed Description

```
template<class precondition> class gmres< precondition >
```

Class [gmres](#). This class get a sparse matrix, and a rhs, apply the GMRES method until convergence.

### 3.5.2 Constructor & Destructor Documentation

**3.5.2.1** `template<class precondition > gmres< precondition >::gmres (spMat * A, precondition * P, VectorXd * rhs, VectorXd * x0, int m, double eps, bool verb) [inline]`

Constructor with input parameters. Pointer to the sparse matrix. Pointer to the preconditioner. Pointer to the RHS vector. Pointer to the initial guess vector. Maximum number of iterations. Accuracy threshold.

Allocate memory to matrices and vectors

### 3.5.3 Member Function Documentation

#### 3.5.3.1 `template<class precondition > void gmres< precondition >::solve () [inline]`

solve: start iteration until: 1) Krylov sub-space stops growing or 2) Reach maximum number of iteration or 3) Reach desired accuracy

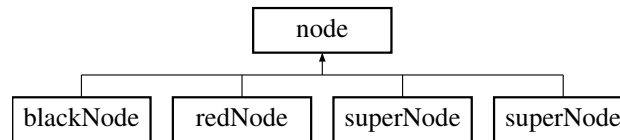
The documentation for this class was generated from the following file:

- gmres.h

### 3.6 node Class Reference

Class [node](#).

`#include <node.h>`Inheritance diagram for `node::`



#### Public Member Functions

- [node](#) ()  
*Default constructor.*
- [node](#) ([node](#) \*, [tree](#) \*, int, int)  
*Constructor:.*
- virtual [~node](#) ()  
*Destructor.*
- [node](#) \* [parent](#) () const  
*Returns parent\_.*
- int [IndexFirst](#) () const  
*Returns index\_first\_.*
- int [IndexLast](#) () const  
*Returns index\_last\_.*
- [tree](#) \* [Tree](#) () const  
*Returns tree\_ptr\_.*
- bool [isEmpty](#) ()  
*True if this [node](#) contains no column of the matrix.*
- bool [isEliminated](#) () const  
*True if this [node](#) is eliminated.*
- void [eliminate](#) ()  
*Set the elimination flag to [true].*
- void [deEliminate](#) ()  
*Set the elimination flag to [false].*
- int [m](#) () const  
*Returns m\_.*

- `int n () const`  
*Returns  $n_{\_}$ .*
- `void m (int val)`  
*Set  $m_{\_}$ .*
- `void n (int val)`  
*Set  $n_{\_}$ .*
- `virtual redNode * redParent ()=0`  
*Returns pointer to the redParent (pure virtual).*
- `virtual redNode * redParent (int)=0`  
*Overload: int is the lvl of grand parent.*
- `void eraseCompressedEdges ()`  
*Erase removed edges from the list of incoming/outgoing edges.*
- `VectorXd * RHS ()`  
*Access to the pointer of the RHS vector.*
- `void RHS (VectorXd *in)`  
*Set the pointer of the RHS vector.*
- `VectorXd * VAR ()`  
*Access to the pointer of the variables vector.*
- `void VAR (VectorXd *in)`  
*Set the pointer of the VAR vector.*
- `void solveL ()`  
*solve  $L z = b$*
- `void solveU ()`  
*solve  $U VAR = RHS$*

## Public Attributes

- `std::vector< edge * > inEdges`  
*List of incoming edges.*
- `std::vector< edge * > outEdges`  
*List of outgoing edges.*
- `bool eliminated_`  
*A boolean flag to keep track of elimination.*
- `densMat * invPivot`

*The inverse of the selfEdge matrix (i.e., pivot).*

- bool `rhsUpdated_`

*A boolean flag to keep track of updated RHS.*

- int `order`

*The order of elimination.*

### 3.6.1 Detailed Description

Class `node`. This (virtual) class is an interface for the three inherited classes `blackNode`, `redNode`, and `superNode`

### 3.6.2 Constructor & Destructor Documentation

#### 3.6.2.1 `node::node (node * P, tree * T, int first, int last)`

Constructor:.. input arguments: pointer to parent, pointer to the `tree`, range of belonging rows/cols Constructor by passing the ptr to the `tree`, and range of belonging columns

### 3.6.3 Member Function Documentation

#### 3.6.3.1 `virtual redNode* node::redParent () [pure virtual]`

Returns pointer to the redParent (pure virtual). `redNode` -> returns itself `blackNode` -> returns `parent()` `superNode` -> returns `parent()` of parent()

Implemented in `blackNode`, `redNode`, `superNode`, and `superNode`.

#### 3.6.3.2 `void node::solveL ()`

solve  $Lz = b$  This function updates RHS, which is solve for  $z$  in  $Lz = b$  It uses the order of elimination.

#### 3.6.3.3 `void node::solveU ()`

solve  $U \text{ VAR} = \text{RHS}$  Solve for unknowns of this cluster. It uses the order of elimination.

The documentation for this class was generated from the following files:

- `node.h`
- `node.cpp`

## 3.7 params Class Reference

Parameters class.

```
#include <params.h>
```

### Public Member Functions

- `std::string Input_Matrix_File () const`  
*Public function to access to input matrix file.*
- `params ()`  
*Default constructor.*
- `params (char *)`  
*Constructor.*
- `params (char *, int, int, int, double, int, double, double, int, double, int, double, int, bool)`  
*Constructor.*
- `~params ()`  
*Destructor.*
- `unsigned int treeLevelThreshold () const`  
*Returns subdividing\_threshold\_.*
- `double epsilon () const`  
*Returns epsilon\_.*
- `int lowRankMethod () const`  
*Returns lowRankMethod\_.*
- `int cutOffMethod () const`  
*Returns cutOffMethod\_.*
- `double aPrioriRank () const`  
*Returns aPrioryRank\_.*
- `double rankCapFactor () const`  
*Returns rankCapFactor\_.*
- `double deployFactor () const`  
*Returns deployFactor\_.*
- `int gmresMaxIters () const`  
*Returns GMRES maximum number of iterations.*
- `double gmresEpsilon () const`  
*Returns GMRES residual threshold.*

- int `gmresPC` () const  
*Returns GMRES preconditioner.*
- bool `gmresVerbose` () const  
*Returns GMRES verbose.*
- double `ILUDropTol` () const  
*Returns ILU drop tol.*
- int `ILUFil` () const  
*Returns ILU Fill.*
- int `normCols` () const  
*Returns normCols\_.*

### 3.7.1 Detailed Description

Parameters class. This class loads an input parameter file, and store different parameters. All other classes can access to the parameters using this class.

### 3.7.2 Constructor & Destructor Documentation

#### 3.7.2.1 `params::params (char * address)`

Constructor. Should construct a parameter object with the char\* of \ the path to the input parameter file  
In the input parameter file, empty line and lines starting \ with # will be ignored

#### 3.7.2.2 `params::params (char * matrixFile, int depth, int lrmeth, int cometh, double eps, int aprank, double rankCap, double depFac, int gmresMI, double gmresEps, int gmresPrec, double ILUDT, int ILUFil, bool normCols)`

Constructor. With this constructor we directly provide parameters

The documentation for this class was generated from the following files:

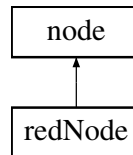
- `params.h`
- `params.cpp`



## 3.8 redNode Class Reference

Class `redNode`.

`#include <redNode.h>`Inheritance diagram for `redNode`::



### Public Member Functions

- `redNode ()`  
*Default constructor.*
- `redNode (blackNode *, tree *, bool, int, int)`  
*Constructor::.*
- `~redNode ()`  
*Destructor.*
- `blackNode * child () const`  
*Returns child\_.*
- `bool IsLeaf () const`  
*True if this is leaf node.*
- `blackNode * parent () const`  
*Return parent\_.*
- `unsigned int level () const`  
*Returns level\_.*
- `bool which () const`  
*Returns which\_.*
- `void createBlackNode ()`
- `std::set< redNode * > * AdjList ()`
- `redNode * redParent ()`  
*Returns pointer to it self.*
- `redNode * redParent (int)`  
*overloaded version for many levels up*

### 3.8.1 Detailed Description

Class `redNode`. Inherited from the general class `node`. It is a `node` corresponding to the multipole variables, and local equations.

## 3.8.2 Constructor & Destructor Documentation

### 3.8.2.1 redNode::redNode (blackNode \* *P*, tree \* *T*, bool *W*, int *first*, int *last*)

Constructor:.. input arguments: pointer to the [blackNode](#) parent, pointer to the [tree](#), which child, range of belonging rows/cols

The documentation for this class was generated from the following files:

- redNode.h
- redNode.cpp

## 3.9 RedSVD::RedPCA< \_MatrixType > Class Template Reference

### Public Types

- typedef \_MatrixType **MatrixType**
- typedef MatrixType::Scalar **Scalar**
- typedef MatrixType::Index **Index**
- typedef Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic > **DenseMatrix**
- typedef Eigen::Matrix< Scalar, Eigen::Dynamic, 1 > **ScalarVector**

### Public Member Functions

- **RedPCA** (const MatrixType &A)
- **RedPCA** (const MatrixType &A, const Index rank)
- void **compute** (const DenseMatrix &A, const Index rank)
- DenseMatrix **components** () const
- DenseMatrix **scores** () const

**template<typename \_MatrixType> class RedSVD::RedPCA< \_MatrixType >**

The documentation for this class was generated from the following file:

- rsvd.h

### 3.10 RedSVD::RedSVD<\_MatrixType> Class Template Reference

#### Public Types

- typedef \_MatrixType **MatrixType**
- typedef MatrixType::Scalar **Scalar**
- typedef MatrixType::Index **Index**
- typedef Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic > **DenseMatrix**
- typedef Eigen::Matrix< Scalar, Eigen::Dynamic, 1 > **ScalarVector**

#### Public Member Functions

- **RedSVD** (const MatrixType &A)
- **RedSVD** (const MatrixType &A, const Index rank)
- void **compute** (const MatrixType &A, const Index rank)
- DenseMatrix **matrixU** () const
- ScalarVector **singularValues** () const
- DenseMatrix **matrixV** () const

**template<typename \_MatrixType> class RedSVD::RedSVD<\_MatrixType>**

The documentation for this class was generated from the following file:

- rsvd.h

## 3.11 RedSVD::RedSymEigen< \_MatrixType > Class Template Reference

### Public Types

- typedef \_MatrixType **MatrixType**
- typedef MatrixType::Scalar **Scalar**
- typedef MatrixType::Index **Index**
- typedef Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic > **DenseMatrix**
- typedef Eigen::Matrix< Scalar, Eigen::Dynamic, 1 > **ScalarVector**

### Public Member Functions

- **RedSymEigen** (const MatrixType &A)
- **RedSymEigen** (const MatrixType &A, const Index rank)
- void **compute** (const MatrixType &A, const Index rank)
- ScalarVector **eigenvalues** () const
- DenseMatrix **eigenvectors** () const

template<typename \_MatrixType> class RedSVD::RedSymEigen< \_MatrixType >

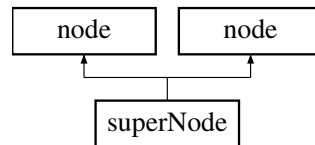
The documentation for this class was generated from the following file:

- rsvd.h

## 3.12 superNode Class Reference

Class [superNode](#).

`#include <superNode.h>`Inheritance diagram for `superNode::`



### Public Member Functions

- [superNode](#) ()  
*Default constructor.*
- [superNode](#) ([blackNode](#) \*, [tree](#) \*, int, int)  
*Constructor:.*
- [~superNode](#) ()  
*Destructor.*
- [blackNode](#) \* [parent](#) () const  
*Returns parent\_.*
- [redNode](#) \* [redParent](#) ()  
*Returns pointer to its parent.*
- [redNode](#) \* [redParent](#) (int)  
*overloaded version for many levels up*
- unsigned int [level](#) () const  
*Returns level\_.*
- [timeTuple2](#) [compress](#) ()  
*Compress all well separated interactions.*
- [timeTuple2](#) [schurComp](#) ()  
*Actually eliminate the [node](#), and its parent.*
- void [splitVAR](#) ()  
*Split the solution to left/right redNodes.*
- void [addRandomCols](#) (densMat &, int)  
*Pad some random columns to the matrix (on the right).*
- void [addRandomRows](#) (densMat &, int)  
*Pad some random rows to the matrix (at the bottom).*

- void [extendOrthoCols](#) (densMat &, int)  
*Pad some random columns and apply QR (on the right ).*
- void [extendOrthoRows](#) (densMat &, int)  
*Pad some random rows and apply QR (at the bottom ).*
- bool [criterionCheck](#) (int, double, [RedSVD::RedSVD](#)< densMat > &, densMat &, int)  
*check if the approximation is fine*
- [superNode](#) ()  
*Default constructor.*
- [superNode](#) ([blackNode](#) \*, [tree](#) \*, int, int)  
*Constructor:.*
- [~superNode](#) ()  
*Destructor.*
- [blackNode](#) \* [parent](#) () const  
*Returns parent\_.*
- [redNode](#) \* [redParent](#) ()  
*Returns pointer to its parent.*
- [redNode](#) \* [redParent](#) (int)  
*overloaded version for many levels up*
- unsigned int [level](#) () const  
*Returns level\_.*
- void [compress](#) ()  
*Compress all well separated interactions.*
- void [schurComp](#) ()  
*Actually eliminate the [node](#), and its parent.*
- void [splitVAR](#) ()  
*Split the solution to left/right redNodes.*
- void [addRandomCols](#) (densMat &, int)  
*Pad some random columns to the matrix (on the right).*
- void [addRandomRows](#) (densMat &, int)  
*Pad some random rows to the matrix (at the bottom).*
- void [extendOrthoCols](#) (densMat &, int)  
*Pad some random columns and apply QR (on the right ).*
- void [extendOrthoRows](#) (densMat &, int)  
*Pad some random rows and apply QR (at the bottom ).*

- bool `criterionCheck` (int, double, `RedSVD::RedSVD< densMat > &`, `densMat &`, int)  
*check if the approximation is fine*

### 3.12.1 Detailed Description

Class `superNode`. Inherited from the general class `node`. It is a `node` corresponding to particles

### 3.12.2 Constructor & Destructor Documentation

#### 3.12.2.1 `superNode::superNode (blackNode * P, tree * T, int first, int last)`

Constructor:. input arguments: pointer to the `blackNode` parent, pointer to the `tree`, range of belonging rows/cols

#### 3.12.2.2 `superNode::superNode (blackNode *, tree *, int, int)`

Constructor:. input arguments: pointer to the `blackNode` parent, pointer to the `tree`, range of belonging rows/cols

### 3.12.3 Member Function Documentation

#### 3.12.3.1 `timeTuple2 superNode::compress ()`

Compress all well separated interactions. Exit is a timeTuple: (lowRank time, everything else time)

#### 3.12.3.2 `void superNode::extendOrthoCols (densMat &, int)`

Pad some random columns and apply QR (on the right ). We assume the input matrix consists of orthonormal columns.

#### 3.12.3.3 `void superNode::extendOrthoCols (densMat & A, int p)`

Pad some random columns and apply QR (on the right ). We assume the input matrix consists of orthonormal columns.

#### 3.12.3.4 `void superNode::extendOrthoRows (densMat &, int)`

Pad some random rows and apply QR (at the bottom ). We assume the input matrix consists of orthonormal rows.

#### 3.12.3.5 `void superNode::extendOrthoRows (densMat & A, int p)`

Pad some random rows and apply QR (at the bottom ). We assume the input matrix consists of orthonormal rows.



### 3.12.3.6 void superNode::schurComp ()

Actually eliminate the [node](#), and its parent. Eliminating a [node](#) involves going through all edges, and create new edges based on schur complement

### 3.12.3.7 timeTuple2 superNode::schurComp ()

Actually eliminate the [node](#), and its parent. Eliminating a [node](#) involves going through all edges, and create new edges based on schur complement

The documentation for this class was generated from the following files:

- superNode.h
- superNode\_rsvd.h
- superNode.cpp
- superNode\_general.cpp
- superNode\_QR.cpp
- superNode\_rsvd.cpp
- superNode\_svd.cpp

### 3.13 tree Class Reference

```
#include <tree.h>
```

#### Public Member Functions

- [tree](#) ()  
*Constructor (for root [node](#)).*
- [tree](#) ([params](#) \*)  
*Constructor with parameters as input.*
- [~tree](#) ()  
*Destructor.*
- [params](#) \* [Parameters](#) () const  
*Provide a submatrix with given range of columns.*
- spMat \* [Matrix](#) () const  
*Returns matrix\_.*
- spMatBool \* [SymbMatrix](#) () const  
*Returns symb\_matrix\_.*
- int [n](#) () const
- std::vector< redNodeStrList > \* [redNodeList](#) ()  
*Returns pointer to the list of redNodes.*
- std::vector< superNodeStrList > \* [superNodeList](#) ()  
*Returns pointer to the list of superNodes.*
- std::vector< double > \* [meanRanks](#) ()  
*Returns pointer to mean rank list.*
- std::vector< int > \* [minRanks](#) ()  
*Returns pointer to min rank list.*
- std::vector< int > \* [maxRanks](#) ()  
*Returns pointer to max rank list.*
- unsigned int [maxLevel](#) ()  
*Returns the maximum level number.*
- void [addRedNode](#) (unsigned int, [redNode](#) \*)  
*Add a new [redNode](#) to the list.*
- void [addSuperNode](#) (unsigned int, [superNode](#) \*)  
*Add a new [superNode](#) to the list.*

- void `createAdjList` ()  
*Form the adjacency list for all redNodes.*
- void `createCol2LeafMap` ()  
*Using a Map we create key-value pairs for all leaf nodes.*
- void `createLeafEdges` ()  
*Load the data to edges between *tree* leaves.*
- double `createSuperNodes` (unsigned int)  
*Creating superNodes.*
- timeTuple4 `eliminate` (unsigned int)  
*Eliminate variables at level [l] in the *tree*.*
- void `setRHS` (VectorXd &)  
*Set the RHS for all nodes.*
- void `setLeafRHS` (VectorXd &)  
*Dedicate memory, and set the RHS for leaf nodes.*
- void `setLeafRHSVAR` ()  
*Dedicate memory, and set the VAR for leaf nodes.*
- void `solveL` (unsigned int)  
*SolveL for black, super, and red Nodes in a level.*
- void `solveU` (unsigned int)  
*SolveU for black, super, and red Nodes in a level.*
- VectorXd & `solve` ()  
*Top to bottom traverse to solve for a given RHS.*
- VectorXd & `solve` (VectorXd &)
- void `factorize` ()  
*Bottom to Top traverse to decompose  $A = L U$ .*
- VectorXd & `computeSolution` ()  
*Compute solution.*
- VectorXd \* `VAR` ()  
*Access to the pointer of the variables vector.*
- void `setRanks` ()  
*set ranks*
- void `log` (std::string)  
*store everything in a log file*
- void `computeFrobNorm` (unsigned int)

*Compute the Frob. norm at level l.*

- VectorXd \* `retVal` ()  
*Returns a pointer to the solution.*
- void `normalize_cols` (spMat \*)  
*Divide each col of the matrix by its maximum value.*

## Public Attributes

- VectorXi \* `permutationVector`  
*The vecotr contains required permutation of the last level.*
- double `assembleTime`  
*Tree assembling time.*
- double `precondFactTime`  
*Time for preconditioner factorization time ( solve ).*
- double `accuracy`  
*GMRES final relative accuracy.*
- double `residual`  
*GMRES final relative residual.*
- VectorXd \* `residuals`  
*GMRES residuals.*
- int `gmresTotalIters`  
*GMRES total iterations.*
- double `gmresTotalTime`  
*GMRES total time.*
- bool `padding`  
*Padding happend?*
- bool `largePivot`  
*Large pivots happend?*
- std::vector< double > `frobNorms`  
*Store Forb. of each level.*
- std::vector< double > `totalSizes`  
*Totoal size of each level.*
- double `globFrobNorm`  
*global frob norm = sum(frobNorms)*

- double `globSize`  
*global size = sum(totalSizes)*
- int `count`  
*COUNT the number of eliminated nodes (so far).*

### 3.13.1 Detailed Description

Class `tree` This class represents a `tree` of nodes, and provide necessary information/routines for `tree`. The full matrix is also stored as a member of this class, only one version that is globally accessible.

### 3.13.2 Constructor & Destructor Documentation

#### 3.13.2.1 `tree::tree () [inline]`

Constructor (for root `node`). In the constructor we read the matrix data from input files (in market-matrix format), and store it as EigenSparse matrix. Also, the nodes of the `tree` will be generated in the constructor.

Default constructor

#### 3.13.2.2 `tree::tree (params * par)`

Constructor with parameters as input.

Constructing the root

The root of the `tree` is a `redNode`. We need to pass the range of columns that belong to each `node`. The `tree` will be created in a BFS order. The order of things need to be done:

- create the root
- When a `redNode` born it will be added to the `redNodelist`
- for the last created level do the permutation
- for the last created level decide if further subdividing is required (based on `threshold_level`)
- if yes for all `redNodes` in the last level call `createBlacknode()`

set the global frob norm = 0 initially

Initially no `node` is eliminated

Initially no padding and no large pivot is assumed

### 3.13.3 Member Function Documentation

#### 3.13.3.1 `void tree::addRedNode (unsigned int l, redNode * ptr)`

Add a new `redNode` to the list. The `blackNode` will use this function to create its red children. The first argument is the level of the new red `node` and the second is the pointer to it

### 3.13.3.2 void tree::addSuperNode (unsigned int *l*, superNode \* *ptr*)

Add a new [superNode](#) to the list. The [blackNode](#) will use this function to create its [superNode](#) child. The first argument is the level of the new [superNode](#) and the second is the pointer to it

### 3.13.3.3 VectorXd & tree::computeSolution ()

Compute solution. i.e., collect the solution of all leaves

### 3.13.3.4 void tree::createAdjList ()

Form the adjacency list for all redNodes. Note that this is the list of original interactions induced by children. Later on during the elimination, nodes may have new interactions, and will be stored through edges. Only symbolic matrix will be used here.

### 3.13.3.5 void tree::createCol2LeafMap ()

Using a Map we create key-value pairs for all leaf nodes. For each non-empty leaf the key is the index of the first columns it posses, and the value is the pointer to the leaf.

### 3.13.3.6 void tree::createLeafEdges ()

Load the data to edges between [tree](#) leaves. After the [tree](#), and adjacency lists are created, load the sub block of matrix to the edges between leaves.

### 3.13.3.7 double tree::createSuperNodes (unsigned int *l*)

Creating superNodes. This function combine sibling redNodes at level [*l*] of the [tree](#), and create a new [superNode](#). By construction, the parent of the resulted [superNode](#) is a [blackNode](#). Note that in order to access pairs of sibling redNodes at level [*l*] of the [tree](#), we go through the redNodes at level [*l*-1] in the [tree](#), and look at their grand red children. Output is the time elapsed: tuple( compression, schurComp ).

### 3.13.3.8 timeTuple4 tree::eliminate (unsigned int *l*)

Eliminate variables at level [*l*] in the [tree](#). Output is the time elapsed.

### 3.13.3.9 void tree::factorize ()

Bottom to Top traverse to decompose  $A = L U$ . Bottom to top traverse.

At each level, first create the superNodes (i.e., combine two redNodes), and then eliminate (and compress) all superNodes, as well as their black [node](#) parents.

### 3.13.3.10 params\* tree::Parameters () const [inline]

Provide a submatrix with given range of columns. The order of input arguments: first column, last column, InnerIndex list, OuterIndex list Note: The indices in the in/out-er lists always start from 0! Returns 0 if successful, returns 1 otherwise Returns param\_

**3.13.3.11 void tree::setRanks ()**

set ranks At each level compute mean, min, and max size of the redNodes

**3.13.3.12 VectorXd & tree::solve (VectorXd & *RHS*)**

bottom to top traverse to solve  $Lz = b$

top to bottom traverse to solve  $Ux = z$

**3.13.3.13 VectorXd & tree::solve ()**

Top to bottom traverse to solve for a given RHS. Top to bottom traverse.

If no RHS is provided it uses the RHS from input [params](#), and automatically permute it. For the overloaded version, it takes a permuted RHS as an input.

Start from the top, solve the first set of equations directly (e.g., direct LU), Then back-propagate toward leaves, and solve all unknowns. This version uses the RHS provided in the input [params](#).

**3.13.3.14 void tree::solveL (unsigned int *l*)**

SolveL for black, super, and red Nodes in a level. This functions work from bottom to top

**3.13.3.15 void tree::solveU (unsigned int *l*)**

SolveU for black, super, and red Nodes in a level. This functions work from top to the bottom

**3.13.4 Member Data Documentation****3.13.4.1 std::vector<double> tree::frobNorms**

Store Forb. of each level. The frob. norm of level  $l$  is defined as:  $\sqrt{\sum_{e \text{ is edge between two superNodes}} e.matrix.frob^2}$

**3.13.4.2 std::vector<double> tree::totalSizes**

Total size of each level. For each level,  $l$ , it computes: sum of sizes (=  $m*n$  for a  $m$ -by- $n$  matrix) of all blocks in that level

The documentation for this class was generated from the following files:

- tree.h
- tree.cpp

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