Homework 1, due September 13th, 11:59pm

September 7, 2023

Use a programming language or package where decision trees and random forests can be trained and applied. Examples include Matlab, Python (scikit-learn package), or R.

- 1. Using the training and test sets specified in the syllabus, perform the following tasks:
 - a) On the madelon dataset, train decision trees of maximum depth 1, 2, up to 12, for a total of 12 decision trees. If your package does not allow the max depth as a parameter, train trees with $2^1, 2^2, ..., 2^{12}$ nodes, again a total of 12 trees. Use the trained trees to predict the class labels on the training and test sets, and obtain the training and test misclassification errors. Plot on the same graph the training and test misclassification errors vs tree depth (or log2 of nodes) as two separate curves. Report in a table the minimum test error and the tree depth (number of nodes or splits) for which the minimum was attained. (2 points)
 - b) Repeat point a) on the satimage dataset. (2 points)
 - c) On the madelon dataset, for each of $k \in \{3, 10, 30, 100, 300\}$ train a random forest with k trees where the split attribute at each node is chosen from a random subset of $\sim \sqrt{500}$ features. Use the trained trees to predict the class labels on the training and test sets, and obtain the training and test misclassification errors. Plot on the same graph the training and test errors vs number of trees k as two separate curves. Report the training and test misclassification errors in a table. (3 points)
 - d) Repeat point c) on the madelon dataset where the split attribute at each node is chosen from a random subset of $\sim \ln(500)$ features. (1 point)
 - e) Repeat point c) on the madelon dataset where the split attribute at each node is chosen from all 500 features. (1 point)