## Week 2: Solve with instructor

Calculus

Let 
$$f(x) = \begin{cases} \frac{\sqrt{9x^4 + x^2}}{5x^2 + 3x + 1} & \text{if } x \le 0; \\ x & \text{if } x < 0. \end{cases}$$
. Is  $f$  continuous at  $x = 0$ ?



Let 
$$f(x) = \begin{cases} x^2 \sin\left(\frac{1}{x}\right) + 3 & \text{if } x \neq 0; \\ 1 & \text{if } x = 0. \end{cases}$$
. Is  $f$  continuous at  $x = 0$ ?



Let 
$$f(x) = \begin{cases} -x + c & \text{if } x \le 1; \\ 6 - 2x^2 & \text{if } x > 1. \end{cases}$$
 Find a value of  $c$  so that  $f(x)$  is continuous at  $x = 1$ .

Let 
$$f(x) = \begin{cases} \frac{x^2 - 9}{x - 3} & \text{if } x < 3; \\ cx^2 + 10 & \text{if } x \ge 3. \end{cases}$$
 Find the value of  $c$  so that  $f(x)$  is continuous at  $x = 3$ .



$$\text{Let } G(x) = \left\{ \begin{array}{l} \frac{1}{(x+3)^2} & \text{, if } x \leq -1; \\ 2-x & \text{, if } -1 < x \leq 1; \\ \frac{3}{x+2} & \text{, if } x > 1. \end{array} \right. \text{Find all values of } x \text{ where } G \text{ is not continuous.}$$

What is the approximate value of  $\sqrt{9.1}$  (up to four decimal places)?



Find the linearization of  $\sqrt[3]{x}$  at x = 8?



Compute the linear approximation of  $f(x) = (1+x)^n$  at x=0.



Use the linear approximation obtained in the previous question to compute an approximate value of  $(1.01)^3$ .



## Drag your dot to how you are feeling:







Compute the cubic approximation of  $f(x) = \sqrt{(1+x)} at a = 0$ .



Find the linearization of  $f(x) = e^x \sin(x - y)$  at the point (0, 0).



Compute the derivative of  $f(x, y) = x^2y$  in the direction of (1, 2) at the point (3, 2).



For the function in the previous question (i. e.,  $f(x, y) - x^2y$ ), compute the derivative of f in the direction of (2, 1) at the same point, i. e., (3, 2).



For the function in the previous question (i. e.,  $f(x, y) = x^2y$ ), in which direction is the derivative maximum?



For the function in the previous question (i. e.,  $f(x, y) = x^2y$ ), what is the value of the maximal derivative?



For the function in the previous question (i. e.,  $f(x) = x^2y$ ), what is the derivative in the direction of (-3, 4) at the point (3, 2)?



For the function in the previous question (i. e.,  $f(x, y) = x^2y$ ), what is the derivative in the direction of (-4, -3) at the point (3, 2)?



Without computing, tell whether  $x \cdot y = ||x|| ||y||$  if x = [2, 5, 6] and y = [16, 40, 48].

## Were you able to understand how to solve these questions?





