

Course: Machine Learning - Foundations  
Week 4: Test questions

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1. (1 point)

**Answer:** A

2. (1 point)

**Answer:** The determinant, column space and rank of a matrix are not affected by row operations on the matrix

3. (1 point)

**Answer:** D

4. (1 point)

**Answer:** A,D

5. (1 point)

**Answer:** Determinant= product of eigen values

6. (1 point)

**Answer:** Trace=sum of eigen values

7. (1 point) If the eigenvalues of a matrix are -1, 0 and 4, then its trace and determinant are

Trace:\_\_\_\_\_

Determinant:\_\_\_\_\_

**Answer:** Determinant= product of eigen values

Trace=sum of eigen values

8. (1 point)

**Answer:** To find characteristic polynomial obtain  $|A - \lambda I|$

9. (1 point)

**Answer:** Solve for  $\lambda$ ,  $|A - \lambda I| = 0$

10. (1 point)

**Answer:** If  $\lambda$  is an eigen value of  $A$  then  $\lambda^n$  is eigen value of  $A^n$  and vice versa

11. (1 point)

**Answer:** A

12. (1 point)

**Answer:** B

13. (2 points)

**Answer:** 0, 5

14. (2 points)

**Answer:** solve  $(A - \lambda I)x = 0$ , where  $\lambda$  is the eigen value and x is corresponding eigen vector

15. (2 points)

**Answer:** Let us consider  $P^{-1}AP = B$ , Here B is an upper triangular matrix, So the eigenvalues are same as principal diagonal elements. Now, the eigenvalues of B are the eigenvalues of A. So eigenvalues of  $A^2$  are eigenvalues of B squared.

16. (2 points)

**Answer:** 
$$\begin{bmatrix} \theta_0 \\ \theta_1 \\ \theta_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1.3 & 1.69 \\ 1 & 4 & 16 \end{bmatrix}^{-1} \begin{bmatrix} 0 \\ 1.5 \\ 2 \end{bmatrix}$$