

Gradient - descent

Properties

- If $\eta_t = \frac{1}{t+1}$, the algorithm converges
- Gradient descent converges to "LOCAL MINIMUM"

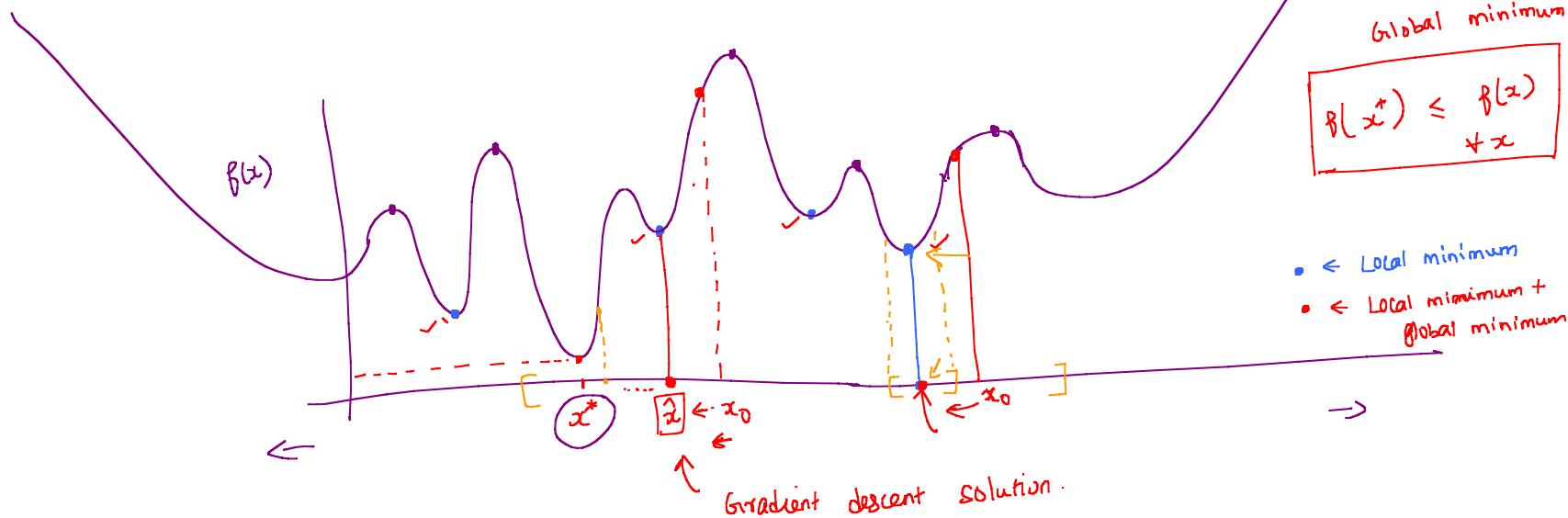
Local minimum

$$\exists \epsilon > 0 \text{ s.t.}$$

$$f(\hat{x}) \leq f(x) \quad \forall x \in [\hat{x} - \epsilon, \hat{x} + \epsilon]$$

Global minimum

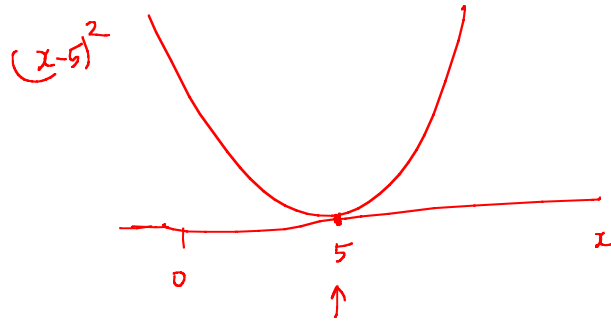
$$f(x^*) \leq f(x) \quad \forall x$$



Functions for which

local minimum
 \Updownarrow
Global minimum

CONVEX
FUNCTIONS



What is special about

$$d = \boxed{-f'(x)}$$