# Proximal Policy Optimization with Dynamic Clipping

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## Background

#### Reinforcement Learning

- A set of algorithms that seek to replicate behavioral learning.
- Basic vocabulary:
  - Environment: a general setting with changeable parameters in which actions can be performed that affect these parameters
  - State (denoted s): a specific configuration (i.e. "snapshot") of an environment
  - Agent: an entity that learns to accomplish a task in a specific evironment
  - Action (denoted a): a decision made by the agent that is intended to affect subsequent states
  - **Episode**: a sequence of states and actions in an environment
  - **Reward** (denoted r): a number associated with a state-action pair
- Overall goal: train an agent that picks actions such that the sum of the rewards over an episode is maximimized.

- Example: cart-pole demo

#### Policy Gradient Methods

- An agent can be provided with a **policy**, usually denoted  $\pi$ , that completely specifies the probabilty distribution of the action that should be taken at any particular state.
- $\pi$  is parameterized by some vector  $\theta$  and can be any function of a state  $s_t$ .
- The task of the agent is to learn  $\theta$ .

#### Generic Policy Gradient Algorithm

### Algorithm Generic Policy Gradient

```
Initialize \theta arbitrarily
```

#### while True do

▷ loop forever

$$\theta_{\textit{old}} \leftarrow \theta$$

 $rollout \leftarrow (s, a, r)$  from multiple  $\pi_{\theta}$  episodes

Set  $\theta$  to maximize the loss function  $L(rollout, \theta, \theta_{old})$ 

#### Trust Region Policy Optimization (TRPO)

The theory behind TRPO suggests using the loss function:

$$L_{\theta_{old}}(\theta) - CD_{KL}^{max}(\theta, \theta_{old})$$

where C is a constant and

$$L_{ heta_{old}}( heta) = \mathbb{E}_t \left[ rac{\pi_{ heta}(a_t|s_t)}{\pi_{ heta_{old}}(a_t|s_t)} A_t 
ight]$$

.

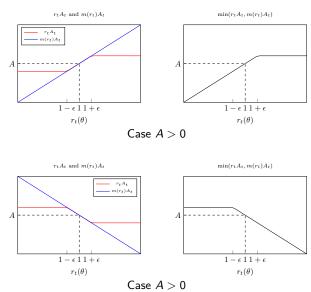
- Using this loss function guarantees monotonic improvement.
- Using the penalty term  $CD_{KL}^{max}(\theta,\theta_{old})$  leads to small step sizes in practice, so TRPO uses a hard constraint on the KL divergence.

### Proximal Policy Optimization (PPO)

 PPO uses a loss function that is an approximation to the TRPO loss:

$$L^{CLIP}( heta) = \mathbb{E}\left[\min\left(r_t A_t, \operatorname{clip}(r_t, 1-\epsilon, 1+\epsilon) A_t
ight)
ight]$$
 where  $r_t( heta) = rac{\pi_{ heta}(a_t|s_t)}{\pi_{ heta_{old}}(a_t|s_t)}$ .

- Resultant clipping behavior:



 Research question: how can we more precisely control penalties introduced through the clipping objective?

## Potential Shortcoming of PPO

 We can separate the loss into its positive and negative components:

$$\begin{split} L^{CLIP}(\theta) &= \mathbb{E}_t \left[ \min \left( r_t A_t, \text{clip}(r_t, 1 - \epsilon, 1 + \epsilon) A_t \right) \right] \\ &= \mathbb{E}_t \left[ \begin{cases} \min \left( r_t, \text{clip}(r_t, 1 + \epsilon) \right) A_t & A_t > 0 \\ \max \left( r_t, \text{clip}(r_t, 1 - \epsilon) \right) A_t & A_t < 0 \end{cases} \right] \end{split}$$

Let:

$$egin{aligned} r_{t,\textit{CLIP}}^+ &= \min \left( r_t, \operatorname{clip}(r_t, 1 + \epsilon) 
ight) \ r_{t,\textit{CLIP}}^- &= \max \left( r_t, \operatorname{clip}(r_t, 1 - \epsilon) 
ight) \end{aligned}$$

- We know that:

$$\mathbb{E}_t[r_{t,CLIP}^+] < 1$$

$$\mathbb{E}_t[r_{t,CLIP}^-] > 1$$

## Potential Shortcoming of PPO (contd.)

 Now, we can define the "expected penalty contributions" of positive and negative advantages:

$$1 - \mathbb{E}_t[r_{t,CLIP}^+]$$

and

$$\mathbb{E}_t[r_{t,CLIP}^-] - 1$$

- Because r<sub>t</sub> and A<sub>t</sub> are not independent, these expected penalty contributions do not suggest actual penalty contributions.
- However, they can indicate inherent imbalances in the system.

# Potential Shortcoming of PPO (contd.)

#### Conceptual Example

- Consider a typical example in reinforcement learning where:
  - We have an agent using a continuous action space (continuous control).
  - The policy is encoded by a gaussian with state-dependent means but constant standard deviation.

# Potential Shortcoming of PPO (contd.)

What happens as we learn?



## Results

## **Future Directions**