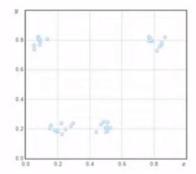
## K-means Clustering

### Data science for Engineers

## What is K-means clustering?

- A technique to partition N observations into K clusters (K≤N) in which each observation belongs to cluster with nearest mean
- One of the simplest unsupervised algorithms
- Works well for all distance metrics where mean is defined (ex. Euclidean distance)



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## Description of K-means clustering

Given N observations  $(x_1,x_2,...,x_N)$ , K-means clustering will partition n observations into K (K $\leq$ N) sets S= $\{s_1,...,s_k\}$  so as to minimize the within cluster sum of squares (WCSS)

$$\mathop{\arg\min}_{\mathbf{S}} \sum_{i=1}^k \sum_{\mathbf{x} \in S_i} \|\mathbf{x} - \boldsymbol{\mu}_i\|^2$$

Where  $\mu(i)$  is the mean of points in s(i)

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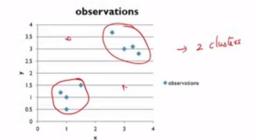


Where  $\mu(i)$  is the mean of points in s(i)  $S_i$ 

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# Algorithm with an example

Obervation	×	У
1	1	1
2	1.5	1.5
3	1	0.5
4	0.8	1.2
5	3.3	3.1
6	2.58	3.68
7	3.5	2.8
8	3	3





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## Example continued...

Step 1: Randomly choose two points as the cluster centers

	Individual	Mean x	Mean y
Group 1	1	(1	1
Group 2	8	8	X

Step 2: Compute the distances and group the closest ones

	300	20	,	
Observation	distance 1	distance 2	Group	
1	0	2.8284271	1	
2	0.7071068	2.1213203	1	
3	0.5	3.2015621	1	
4	0.2828427	2.8425341	1	
5	3.1144823	0.3162278	2	
6	3.111077	0.7992496	2	
7	3.0805844	0.5385165	2	
(8)	2.8284271	0	2	

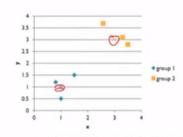


Fig: Plot of groups after step I & 'x' - mean

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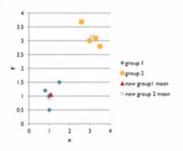
## Example continued...

Step 3: Compute the new mean and repeat step 2

	Individual	Mean x	Mean y
Group1	1,2,3,4	1.075	1.05
Group 2	5,6,7,8	3.095	3.145

Step 4: If change in mean is negligible or no reassignment then stop the process

Observation	distance 1	distance 2	Group
1	0.0901388	2.9983412	1
2	0.6189709	2.2912988	1
3	0.5550901	3.374174	1
4	0.3132491	3.0083301	1
5	3.0254132	0.2098809	2
6	3.0301691	0.7425968	2
7	2.9905058	0.5320244	2
8	2.7400958	0.1733494	2





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## Determining number of clusters(K)

- Elbow method looks at percentage of variance explained as a function of number of clusters
- The point where marginal decrease plateaus is an indicator of the optimal number of clusters
- We will see a demonstration of this in the example



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# Disadvantages of K-means

- This algorithm could converge to a local minima, therefore role of initial position is very important
- If the clusters are not spherical, then K-means can fail to identify the correct number of clusters

