

## Performance measures

## Results : confusion matrix

```
# confusion matrix
> confusionMatrix(crashTest_1_TEST$LogisPred,crashTest_1_TEST$carType)
Confusion Matrix and Statistics

          Reference
Prediction  Hatchback  SUV
Hatchback      10      1
SUV              0      9

      Accuracy : 0.95
      95% CI : (0.7513, 0.9987)
    No Information Rate : 0.5
    P-value [Acc > NIR] : 2.003e-05

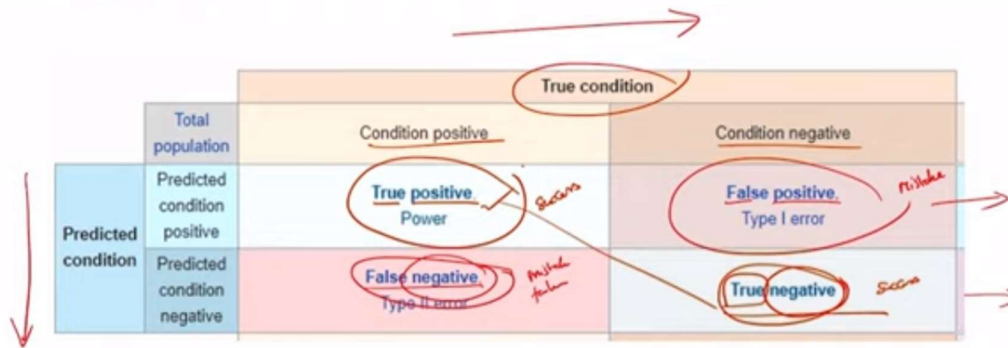
      Kappa : 0.9
  Mcnemar's Test P-value : 1

      Sensitivity : 1.0000
      Specificity : 0.9000
    Pos Pred Value : 0.9091
    Neg Pred Value : 1.0000
      Prevalence : 0.5000
    Detection Rate : 0.5000
Detection Prevalence : 0.5500
    Balanced Accuracy : 0.9500

'Positive' class : Hatchback
```



## Confusion matrix



Source: [https://en.wikipedia.org/wiki/Receiver\\_operating\\_characteristic](https://en.wikipedia.org/wiki/Receiver_operating_characteristic)

## Measures of performance

### Terminology

- $TP$  → true positives,  $TN$  → true negatives,
  - $FP$  → false positives,  $FN$  → false negatives
- $$N = TP + TN + FP + FN$$
- $TP$  – Correct identification of positive labels
  - $TN$  – Correct identification of negative labels
  - $FP$  – Incorrect identification of positive labels
  - $FN$  – Incorrect identification of negative labels

## Measures of performance

- Accuracy: Overall effectiveness of a classifier

- $A = \frac{TP+TN}{N}$

TP, TN, FP, FN

- Maximum value that accuracy can take is 1
- This happens when the classifier exactly classifies two groups (i.e,  $FP = 0$  and  $FN = 0$ )

- Remember

- Total number of true positive labels =  $TP+FN$

- Similarly

- Total number of true negative labels =  $TN+FP$



## Measures of performance

- Sensitivity: Effectiveness of a classifier to identify positive labels

- $S_e = \frac{TP}{TP+FN}$

TP, TN, FP, FN

- Specificity: Effectiveness of a classifier to identify negative labels

- $S_p = \frac{TN}{FP+TN}$

- Both  $S_e$  and  $S_p$  lie between 0 and 1, 1 is an ideal value for each of them

- Balanced accuracy.

- $BA = (sensitivity + specificity)/2$



## Measures of performance

- Prevalence: How often does the yes condition actually occur in our sample

$$P = \frac{TP + FN}{N}$$



- Positive predictive value: Proportion of correct results in labels identified as positive

$$PPV = \frac{(sensitivity * prevalence)}{((sensitivity * prevalence) + ((1 - specificity) * (1 - prevalence)))}$$

- Negative prediction value: Proportion of correct results in labels identified as negative

$$NPV = \frac{specificity * (1 - prevalence)}{(((1 - sensitivity) * prevalence) + ((specificity) * (1 - prevalence)))}$$



## Measures of performance

- Detection rate:

$$DR = \frac{TP}{N}$$

- Detection prevalence: prevalence of predicted events

$$DP = \frac{TP + FP}{N}$$

- The Kappa statistic (or value) is a metric that compares an **observed accuracy** with an **expected accuracy** (random chance)

$$Kappa = \frac{observed\ accuracy - expected\ accuracy}{1 - expected\ accuracy}$$



## Measures of performance

- Observed accuracy

- $OA = \frac{a+d}{N}$

- Expected accuracy

- $EA = \frac{(a+c)(a+b) + (b+d)(c+d)}{N}$

- Kappa = 
$$\frac{\frac{(a+d)}{N} - \left( \frac{(a+c)(a+b) + (b+d)(c+d)}{N} \right)}{\left( 1 - \left( \frac{(a+c)(a+b) + (b+d)(c+d)}{N} \right) \right)}$$

- Where  $a, b, c$  and  $d$  are  $TP, FP, FN$  and  $TN$  respectively



## Results : confusion matrix

```
# confusion matrix.
> confusionMatrix(crashTest_1_TEST$LogisPred, crashTest_1_TEST$carType)
Confusion Matrix and Statistics
```

	Reference		
Prediction	Hatchback	SUV	
Hatchback	10	1	TP=10, FP=1
SUV	0	9	FN=0, TN=9

Accuracy : 0.95  
 95% CI : (0.7513, 0.9987)  
 No Information Rate : 0.5  
 P-value [Acc > NIR] : 2.003e-05

Kappa : 0.9  
 McNemar's Test P-value : 1

Sensitivity : 1.0000  
 Specificity : 0.9000  
 Pos Pred Value : 0.9091  
 Neg Pred Value : 1.0000  
 Prevalence : 0.5000  
 Detection Rate : 0.5000  
 Detection Prevalence : 0.5500  
 Balanced Accuracy : 0.9500

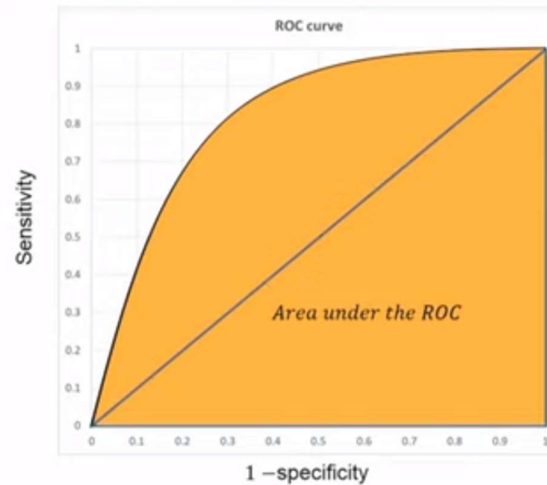
'Positive' class : Hatchback

Handwritten calculations:  
 $\frac{TP}{TP+FP} = \frac{10}{10+1} = \frac{10}{11}$   
 $\frac{TN}{TN+FN} = \frac{9}{9+0} = \frac{9}{9}$



## ROC

- ROC can be used to
  - See the classifier performance at different threshold levels (from 0 to 1)
  - AUC- Area under the ROC
    - An area of 1 represents a perfect test; an area of 0.5 represents a worthless model.
    - .90 – 1 = excellent ✓
    - .80 – .90 = good ✓
    - .70 – .80 = fair ✓
    - .60 – .70 = poor ✓
  - $AUC < 0.5$ , check whether your labels are marked in opposite



## ROC

- ROC can be used to
  - Compare different classifiers at one threshold or overall threshold levels
  - Performance
  - Model 3 > Model 2 > Model 1

