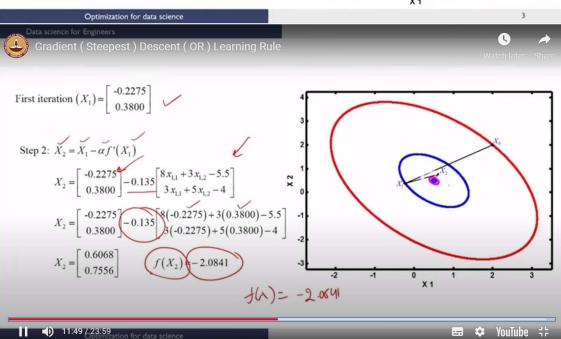


Data science for Engineers Constant objective function contour plots $f'(X) = \begin{bmatrix} 8x_1 + 3x_2 - 5.5 \\ 3x_1 + 5x_2 - 4 \end{bmatrix}$ Learning parameter (α) = 0.135 Constant objective function contour plots $f(X) = 4x_1^2 + 3x_1x_2 + 2.5x_2^2 - 5.5x_1 - 4x_2 = K$ Quadratic in this case - ellipse Initial guess $(X_0) = \begin{bmatrix} 2 \\ 2 \end{bmatrix}$ $f(X_0) = 19$ Step $X_1 = X_0 - aff(X_0)$ Gradient Descent (or) Learning Rule in ML. $X_{1} = \begin{bmatrix} 2 \\ 2 \end{bmatrix} - 0.135 \begin{bmatrix} 8x_{0,1} + 3x_{0,2} - 5.5 \\ 3x_{0,1} + 5x_{0,2} - 4 \end{bmatrix}$ $\begin{bmatrix} -0.2275 \\ 0.3800 \end{bmatrix} f(X_1) = 0.0399$ Optimization for data science



Data science for Engineers

Second iteration
$$(X_2) = \begin{bmatrix} 0.6068 \\ 0.7556 \end{bmatrix}$$

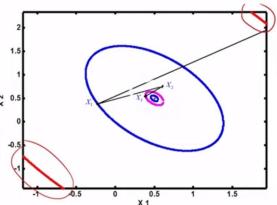
Step 3:
$$X_3 = X_2 - (f'(X_2))$$

Step 3:
$$X_3 = X_2 - (f'(X_2))$$

$$X_3 = \begin{bmatrix} 0.6068 \\ 0.7556 \end{bmatrix} -0.135 \begin{bmatrix} 8x_{2,1} + 3x_{2,2} - 5.5 \\ 3x_{2,1} + 5x_{2,2} - 4 \end{bmatrix}$$

$$X_3 = \begin{bmatrix} 0.6068 \\ 0.7556 \end{bmatrix} - 0.135 \begin{bmatrix} 8(0.6068) + 3(0.7556) - 5.5 \\ 3(0.6068) + 5(0.7556) - 4 \end{bmatrix}$$

$$X_3 = \begin{bmatrix} 0.3879 \\ 0.5398 \end{bmatrix}$$
 $f(X_3) \neq -2.3342$



Optimization for data science

Data science for Engineers

Third iteration $(X_3) = \begin{bmatrix} 0.3879 \\ 0.5398 \end{bmatrix}$

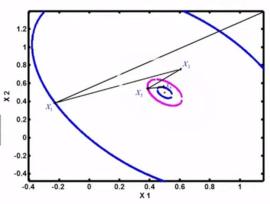
Step 4:
$$X_4 = X_3 + g(f'(X_3))$$

Step 4:
$$X_4 = X_3$$
 $G(X_3)$
 $X_4 = \begin{bmatrix} 0.3879 \\ 0.5398 \end{bmatrix} - 0.135 \begin{bmatrix} 8x_{3,1} + 3x_{3,2} \\ 3x_{3,1} + 5x_{3,2} - 4 \end{bmatrix}$

$$X_4 = \begin{bmatrix} 0.3879 \\ 0.5398 \end{bmatrix} - 0.135 \begin{bmatrix} 8 \big(0.3879 \big) + 3 \big(0.5398 \big) - 5.5 \\ 3 \big(0.3879 \big) + 5 \big(0.5398 \big) - 4 \end{bmatrix}$$

$$X_4 = \begin{bmatrix} 0.4928 \\ 0.5583 \end{bmatrix}$$
 $f(X_4) = -2.3675$

Optimal solution $(X_{opti}) = \begin{bmatrix} 0.5\\0.5 \end{bmatrix}$ $f(X_{opti}) = -2.3750$



Optimization for data science