

Ques. Consider the grammar

$$S' \rightarrow CC$$

$$C \rightarrow aC \mid d$$

- (i) Construct LR(1) set of items for the above grammar
- (ii) Construct LR(1) parsing table
- (iii) Parse the string  $aadd$  with the help of LR(1) table.

Solution

$$S \rightarrow CC$$

$$C \rightarrow aC \mid d$$

Step-1 First make the augmented grammar by adding production  $S' \rightarrow S$ .

The purpose of this grammar is to indicate the acceptance of input. That is when parser is about to reduce  $S' \rightarrow S$  it reaches to acceptance state.

Step-2 Now the augmented grammar becomes

$$S' \rightarrow S$$

$$S \rightarrow CC$$

$$C \rightarrow aC$$

$$C \rightarrow d$$

} augmented grammar

Now place  $(\cdot)$  at first position of R.H.S in each production



$S' \rightarrow \cdot S$  ,  $\underline{\$}$   $\longrightarrow$  lookahead symbol  
 which is calculated in LR(1)  
 & which makes it different  
 from LR(0).

\* Now it is noted that lookahead of starting production  
 i.e. production which we add to make the augmented  
 grammar is  $\$$  by default.

$S' \rightarrow \cdot S, \underline{\$}$   
 $S \rightarrow \cdot CC, \$$   
 $C \rightarrow \cdot aC, -$   
 $C \rightarrow \cdot d, -$

For calculating lookahead for other production we  
 compare  $S' \rightarrow \cdot S, \underline{\$}$  with

$A \rightarrow \alpha \cdot X \beta, a$

we get

$A = S'$  ,  $X = S$  ,  $\beta = \epsilon$  ,  $a = \$$

Now calculate  $FIRST(\beta a) = FIRST(\epsilon \$)$   
 $= FIRST(\$)$   
 $= \{\$ \}$



$$S' \rightarrow \cdot S, \underline{\$} \leftarrow \text{by default}$$

$$S \rightarrow \cdot CC, \underline{\$} \leftarrow \text{calculated by using above production}$$

$$C \rightarrow \cdot aC, \underline{\quad}$$

$$C \rightarrow \cdot d, \underline{\quad}$$

Now, again do the same process for calculation of lookahead for production  $C \rightarrow \cdot aC$

$$S \rightarrow \cdot CC, \underline{\$}$$

Compare with:

$$A \rightarrow \alpha \cdot X \beta, a$$

$$A = S, X = C, \beta = C, a = \$$$

$$\text{FIRST}(\beta a) = \text{FIRST}(C \$)$$

$$= \text{FIRST}(C)$$

$$= \{a, d\} \leftarrow \text{using rule for calculation of FIRST from grammar.}$$

For every product which start with C copy this lookahead  
ie,

$$C \rightarrow \cdot aC, \underline{a/d}$$

$$C \rightarrow \cdot d, \underline{a/d}$$

Now, the complete picture becomes

$S' \rightarrow \cdot S, \underline{\$}$
$S \rightarrow \cdot CC, \underline{\$}$
$C \rightarrow \cdot aC, \underline{a/d}$
$C \rightarrow \cdot d, \underline{a/d}$

State  $I_0$

~~Step~~ Now apply goto on state  $I_0$ .

goto ( $I_0, S$ ) [means shift the dot one place to right where (.) is followed by  $S$ ]

$S' \rightarrow S \cdot, \$$   $I_1$

goto ( $I_0, C$ ) [since (.) is followed by non terminal after applying goto then repeat the production of non-terminal mentioned in  $I_0$ .]

$S \rightarrow C \cdot C, \$$

$C \rightarrow \cdot aC, \$$

$C \rightarrow \cdot d, \$$

(by default since it is first production)

→ For calculation of lookahead for this production

compare  $S \rightarrow C \cdot C, \$$  with

$A \rightarrow \alpha \cdot \beta, a$ , we get

$A = S, \alpha = C, \beta = C, a = \$$

$FIRST(\beta a) = FIRST(CC)$

$= FIRST(\$)$

$= \{\$ \}$

Now copy this lookahead in all production with derive from  $C$ . therefore

$S \rightarrow C \cdot C, \$$   
 $C \rightarrow \cdot aC, \$$   
 $C \rightarrow \cdot d, \$$   $I_2$



goto ( $I_0, a$ )

$C \rightarrow a \cdot C, \underline{a/d}$

← This lookahead copy from the  $I_0$ .

These productions repeat as in first production

$C \rightarrow \cdot aC, \underline{a/d}$

$C \rightarrow \cdot d, \underline{a/d}$

→ This lookahead copy from above production because we copy lookahead for all production derive by same non-terminal.

( $\cdot$ ) is followed by non-terminal  $C$  therefore repeat production derive by  $C$  in state  $I_0$ .

$C \rightarrow a \cdot C, \underline{a/d}$	$I_3$
$C \rightarrow \cdot aC, \underline{a/d}$	
$C \rightarrow \cdot d, \underline{a/d}$	

goto ( $I_0, d$ )

$C \rightarrow d \cdot, \underline{a/d}$   $I_4$

$\therefore$  After applying goto on state  $I_0$  we get  $I_1, I_2, I_3$  &  $I_4$  similarly apply goto on state  $I_1, I_2, I_3$  &  $I_4$  & calculate new states. as

Note: since goto is not applicable on state  $I_1$ , as  $(\cdot)$  is already at least in R.H.S. therefore.

goto ( $I_2, C$ )

$S \rightarrow CC\cdot, \$$   $I_5$

This lookahead copy from state  $I_2$ .

goto ( $I_2, a$ )

$C \rightarrow a\cdot C, \$$   
 $C \rightarrow \cdot aC, \$$   
 $C \rightarrow \cdot d, \$$   $I_6$

This situation again becomes that  $(\cdot)$  is followed by non-terminal after applying goto therefore repeat production of non-terminal from  $I_0$ .

As these production derives by non-terminal 'C' therefore write or copy lookahead of first production.

goto ( $I_2, d$ )

$C \rightarrow d\cdot, \$$   $I_7$

This is new state because this lookahead is different from lookahead in  $I_4$ .

After applying goto on state  $I_2$  we get  $I_5, I_6$  &  $I_7$ .

→ Now apply goto on state  $I_3$ .

goto ( $I_3, C$ )

$C \rightarrow aC\cdot, \underline{a/d}$   $I_0$



goto ( $I_3$ , a)

$$\left\{ \begin{array}{l} C \rightarrow a \cdot C, \underline{a/d} \\ C \rightarrow \cdot aC, \underline{\cancel{a/d}} \\ C \rightarrow \cdot d, \underline{a/d} \end{array} \right\}$$

← This state is  $I_3$  repeated as state  $I_3$  so need not give as new state.

goto ( $I_3$ , d)

$$C \rightarrow d \cdot, \underline{a/d} \} I_4 \text{ [this is also repeated as state } I_4]$$

After goto on state  $I_3$  we get new state  $I_3$  & old state  $I_3$  &  $I_4$ .

Now again apply goto on state  $I_4$  but in this state (.) is already at last place in R.H.S. so need of goto on state  $I_4$  similarly in state  $I_5$  therefore apply goto on state  $I_6$

goto ( $I_6$ , C)

$$\boxed{C \rightarrow aC \cdot, \underline{\$}}$$

$I_9$  (New state)

goto ( $I_6$ , a)

$$C \rightarrow a \cdot C, \underline{\$}$$

$$C \rightarrow \cdot aC, \underline{\$}$$

$$C \rightarrow \cdot d, \underline{\$}$$

← old state ( $I_6$ )

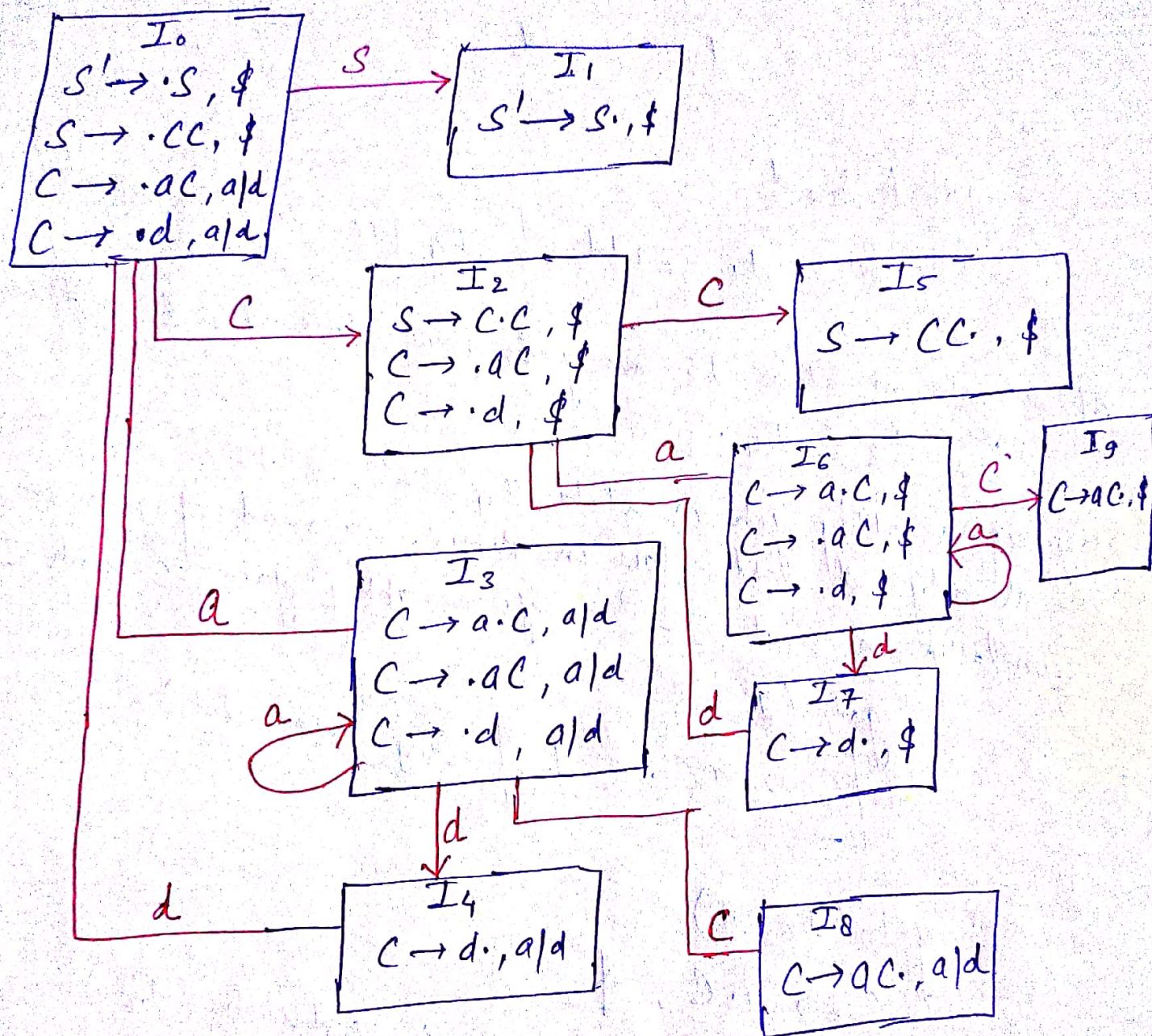
goto ( $I_6$ , d)

$$C \rightarrow d \cdot, \underline{\$} \} \leftarrow \text{old state } (I_7)$$

so, after applying goto on state  $I_6$  we get new state  $I_9$  & old state  $I_6$  &  $I_7$ .



Now goto on state  $I_7$ ,  $I_8$  &  $I_9$  produce no states because there is no scope of shifting of  $(\cdot)$  in R.H.S. therefore after completion of step-2.



The LR(0) graph for Grammar

This is the answer of LR(0) items of the given grammar.