

Naive Baye's Algorithm (Classification)

- ① Probability [Independent And Dependent Events]
- ② Baye's Theorem
- ③ Naive Baye's Mathematical Intuition.
- ④ Variants of Naive Baye's

① Probability [Independent And Dependents Events]

Independent Events

Rolling a Dice {1, 2, 3, 4, 5, 6}

$$Pr(1) = \frac{1}{6} \quad Pr(2) = \frac{1}{6} \quad Pr(3) = \frac{1}{6}.$$

Tossing a Coin. {H, T}

$$Pr(H) = \frac{1}{2} \quad Pr(T) = \frac{1}{2}.$$

Dependent Event

① What is the probability of first removing a orange marble and then removing a yellow marble



1st Event
 \downarrow
 $Pr(O) = \frac{3}{5}$



$$\left[Pr(Y/O) = \frac{2}{4} \right] \Rightarrow \text{conditional probability}$$



$$Pr(O \text{ and } Y) = Pr(O) * Pr(Y/O) \stackrel{\downarrow}{=} \text{conditional probability.}$$

$$= \frac{3}{5} * \frac{2}{4} = \frac{6}{20} = \boxed{\frac{3}{10}}$$

$$\boxed{\Pr(A \text{ and } B) = \Pr(A) * \Pr(B/A).}$$

↓
Dependent

$$\boxed{\Pr(A \text{ or } B) = \Pr(A) + \Pr(B)}$$

↓
Independent

② Bayes Theorem

$$\Pr(A \text{ and } B) = \Pr(B \text{ and } A)$$

$$\Pr(A) * \Pr(B/A) = \Pr(B) * \Pr(A/B)$$

$$\boxed{\Pr(A/B) = \frac{\Pr(A) * \Pr(B/A)}{\Pr(B)}} \Rightarrow \text{Bayes Theorem}$$

$\Pr(A/B)$ = Probability of Event A given B has occurred

$\Pr(A)$ = Probability of Event A

$\Pr(B)$ = " " " B

$\Pr(B/A)$ = Probability of Event B given A has occurred.

Dataset			$\Pr(Y/(x_1, x_2, x_3))$
x_1	x_2	x_3	
-	-	-	Yes
-	-	-	No
-	-	-	Yes
-	-	-	No
-	-	-	Yes

$$\Pr(Y/(x_1, x_2, x_3)) = \frac{\Pr(Y) * \Pr(x_1, x_2, x_3)/y}{\Pr(x_1, x_2, x_3)}$$

$$= \frac{\Pr(y) * \Pr(x_1/y) * \Pr(x_2/y) * \Pr(x_3/y)}{\Pr(x_1) * \Pr(x_2) * \Pr(x_3)}$$

$$\Pr(Y=y_{\text{Yes}}/(x_1, x_2, x_3)) = \frac{\Pr(y_{\text{Yes}}) * \Pr(x_1/y_{\text{Yes}}) * \Pr(x_2/y_{\text{Yes}}) * \Pr(x_3/y_{\text{Yes}})}{\Pr(x_1) * \Pr(x_2) * \Pr(x_3)}$$

Remove

$$\Pr(Y = No \mid (x_1, x_2, x_3)) = \frac{\Pr(No) * \Pr(x_1/No) * \Pr(x_2/No) * \Pr(x_3/No)}{\Pr(x_1) * \Pr(x_2) * \Pr(x_3)} \quad \text{Remove.}$$

Outlook

Day	Outlook	Temperature	Humidity	Wind	PlayTennis
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

Outlook	Yes	No	$P(E/Yes)$	$P(E/No)$
Sunny	2	3	2/9	3/5
Overcast	4	0	4/9	0/5
Rain.	3	2	3/9	2/5

Temperature

	Yes	No	$P(E/Yes)$	$P(E/No)$
Hot	2	2	2/9	2/5
Mild	4	2	4/9	2/5
Cool	3	1	3/9	1/5

$$\Pr(Y_{Yes} \mid (\text{Sunny}, \text{Hot})) = \frac{\Pr(\text{Yes}) * \Pr(\text{Sunny}/\text{Yes}) * \Pr(\text{Hot}/\text{Yes})}{\Pr(\text{Sunny}) * \Pr(\text{Hot})}$$

$$\begin{aligned}
 &= \frac{9/14 * 2/9 * 2/5}{3/14 * 2/5} \\
 &= \frac{2}{63} = \boxed{0.031} \%
 \end{aligned}$$

$\frac{0.031}{0.031 + 0.085}$

$$\Pr(N_{No} \mid (\text{Sunny}, \text{Hot})) = \frac{\Pr(\text{No}) * \Pr(\text{Sunny}/\text{No}) * \Pr(\text{Hot}/\text{No})}{\Pr(\text{Sunny}) * \Pr(\text{Hot})}$$

Constant

$$= 5/14 * 3/5 * 2/5$$

$$= 0.085$$

$$\Pr(Y_0 | (\text{Sunny}, \text{hot})) = \frac{0.031}{0.031 + 0.085} = 0.27 = 27\%.$$

$$\Pr(W_0 | (\text{Sunny}, \text{hot})) = \frac{0.085}{0.031 + 0.085} = 0.73 = 73\%.$$

$[\text{Sunny, hot}] \Rightarrow \underline{\text{No}}$

$\Rightarrow \text{Outlook} \rightarrow \text{Rain}$ }
 $\text{Temperature} \rightarrow \text{Mild}$ }.

Variants of Naive Baye's

- ① Bernoulli Naive Baye's
- ② Multinomial Naive Baye's
- ③ Gaussian Naive Baye's

① Bernoulli Naive Baye's

Whenever your features are following Bernoulli's Distribution, then we use Bernoulli Naive Baye's

$f_1 \ f_2 \ f_3 \ f_4 \quad \underline{O/p}$

Yes Male Pass

No Female Fail

② Multinomial Naive Bayes $\Rightarrow I/p \Rightarrow Text$

Dataset \Rightarrow Sentiment Analysis, Spam ham classification.

Text \Rightarrow Numerical Values \Rightarrow NLP

- ① Bag
- ② TFIDF
- ③ Word2Vec

③ Gaussian Naive Bayes

Independent features \Rightarrow Gaussian Distribution

Age Height Weight O/p

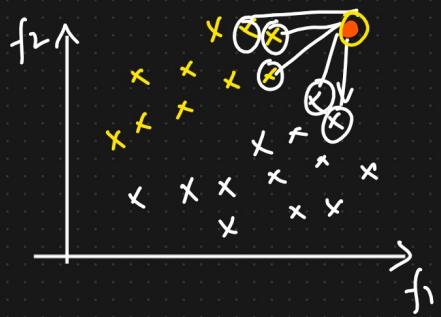
② K Nearest Neighbour (KNN)

① Classification

$$\begin{cases} \text{NLLW} \\ K=10 \end{cases}$$

② Regression

Classification $\begin{cases} 1 \text{ million} \\ \text{Iterations} \end{cases}$ $K=5 \Rightarrow$ Hyperparameters



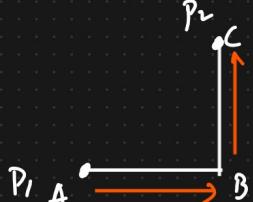
① Euclidean Distance

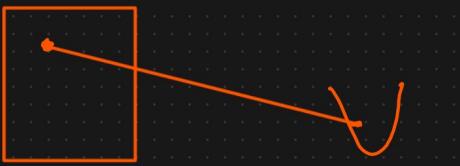
$$P_2(x_2, y_2) \\ P_1(x_1, y_1)$$

Distance Metrics



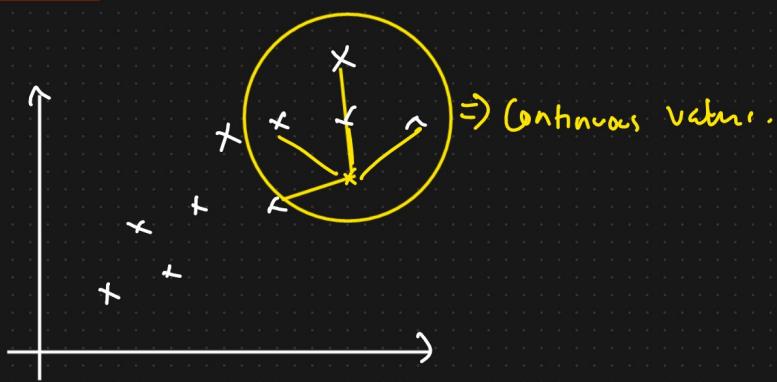
② Manhattan Distance





$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\boxed{|x_2 - x_1| + |y_2 - y_1|}$$



Variants of KNN

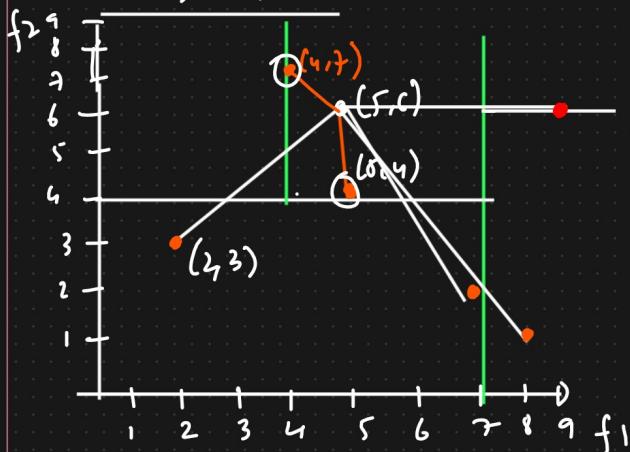
Two Variants

① K Dimension Tree

② Ball Tree

$$K=4$$

① K-D Tree



(2,3) (4,7) (5,4) (7,2) (8,1) (9,6)

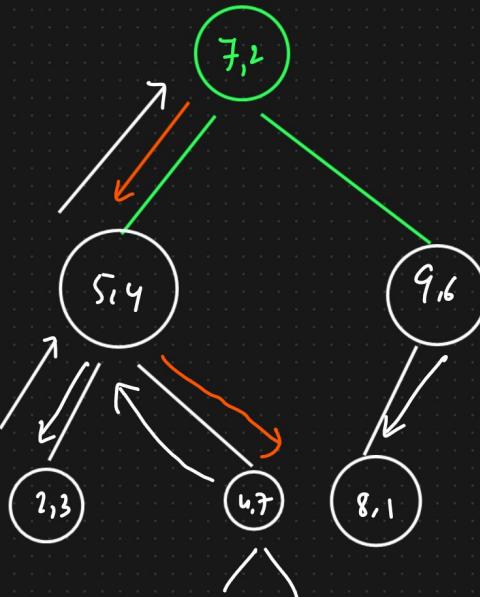
$$2,4, \boxed{5,7}, 8,9 \quad \frac{5+7}{2} = 6$$

3, 7, 4, 2, 1, 6

1, 2, 3, 4, 6, 7

$$\frac{3+4}{2} = 3.5$$

$$K=5$$



② Ball Tree



Final Group

C_{41}

b^2

p_1

p_2

p_3

p_4