Get the Transformation Matrices from DH

```
 A = \{\{ \cos[\theta], -\sin[\theta] * \cos[\alpha], \sin[\theta] * \sin[\alpha], a * \cos[\theta] \}, \{ \sin[\theta], \cos[\theta] * \cos[\alpha], -\cos[\theta] * \sin[\alpha], a * \sin[\theta] \}, \{ 0, \sin[\alpha], \cos[\alpha], d \}, \{ 0, 0, 0, 1 \} \};   A1 = A \ /. \  \{ a \to \theta, \alpha \to \text{Pi} \ / 2, d \to \theta.2, \theta \to q_1[t] \};   A2 = A \ /. \  \{ a \to \theta.36, \alpha \to \theta, d \to \theta, \theta \to (\text{Pi} \ / 2 + q_2[t]) \};   A3 = A \ /. \  \{ a \to \theta, \alpha \to \text{Pi} \ / 2, d \to \theta, \theta \to q_3[t] \};   A4 = A \ /. \  \{ a \to \theta, \alpha \to -\text{Pi} \ / 2, d \to \theta.38, \theta \to q_4[t] \};   A5 = A \ /. \  \{ a \to \theta, \alpha \to \text{Pi} \ / 2, d \to \theta, \theta \to q_5[t] \};   A6 = A \ /. \  \{ a \to \theta, \alpha \to \theta, d \to \theta.065, \theta \to q_6[t] \};   R_{12} = A2[[1; 3, 1; 3]];   R_{23} = A3[[1; 3, 1; 3]];   R_{34} = A4[[1; 3, 1; 3]];   R_{45} = A5[[1; 3, 1; 3]];   R_{56} = A6[[1; 3, 1; 3]];
```

```
T<sub>01</sub> = A1;

T<sub>02</sub> = Simplify[A1.A2];

T<sub>03</sub> = Simplify[T<sub>02</sub>.A3];

T<sub>04</sub> = Simplify[T<sub>03</sub>.A4];

T<sub>05</sub> = Simplify[T<sub>04</sub>.A5];

T<sub>06</sub> = Simplify[T<sub>05</sub>.A6];

R<sub>01</sub> = T<sub>01</sub>[[1;; 3, 1;; 3]];

R<sub>02</sub> = T<sub>02</sub>[[1;; 3, 1;; 3]];

R<sub>03</sub> = T<sub>03</sub>[[1;; 3, 1;; 3]];

R<sub>04</sub> = T<sub>04</sub>[[1;; 3, 1;; 3]];

R<sub>05</sub> = T<sub>05</sub>[[1;; 3, 1;; 3]];

R<sub>06</sub> = T<sub>06</sub>[[1;; 3, 1;; 3]];
```

```
zvec = {0, 0, 1};
b<sub>1</sub> = Transpose[R<sub>01</sub>].zvec;
b<sub>2</sub> = Simplify[Transpose[R<sub>02</sub>].R<sub>01</sub>.zvec];
b<sub>3</sub> = Simplify[Transpose[R<sub>03</sub>].R<sub>02</sub>.zvec];
b<sub>4</sub> = Simplify[Transpose[R<sub>04</sub>].R<sub>03</sub>.zvec];
b<sub>5</sub> = Simplify[Transpose[R<sub>05</sub>].R<sub>04</sub>.zvec];
b<sub>6</sub> = Simplify[Transpose[R<sub>06</sub>].R<sub>05</sub>.zvec];
```

General Parameters

```
rho = 3200;
g_0 = \{0, 0, -g\};
*qdes = {q_1[t], q_2[t], q_3[t], q_4[t], q_5[t], q_6[t]};
qdotdes = \{q_1'[t],q_2'[t],q_3'[t],q_4'[t],q_5'[t],q_6'[t]\};
qdotdotdes = \{q_1''[t], q_2''[t], q_3''[t], q_4''[t], q_5''[t], q_6''[t]\};*)
qdes = \{0, -Pi/2, Pi/2, 0, 0, 0\};
qdotdes = \{0, 0, 0, 0, 0, 0\};
qdotdotdes = \{0, 0, 0, 0, 0, 0\};
payload = 6;
```

Link Parameters

Link I

```
r1 = 0.098;
h1 = 0.2;
r_{01} = \{0, 0.2, 0\};
r1c1 = \{0, -0.1, 0\};
r0c1 = r_{01} + r1c1;
m_1 = \text{rho} * \text{Pi} * \text{r1}^2 * \text{h1};
```

```
12 = 0.36;
b2 = 0.15;
h2 = 0.15;
r_{12} = \{0.36, 0, 0\};
r2c2 = \{-0.18, 0, 0\};
r1c2 = r_{12} + r2c2;
m_2 = rho * 12 * b2 * h2;
           \begin{pmatrix} \frac{m_2}{12} * (b2^2 + h2^2) & 0 & 0 \\ 0 & \frac{m_2}{12} * (12^2 + h2^2) & 0 \\ 0 & 0 & \frac{m_2}{12} * (b2^2 + 12^2) \end{pmatrix}
```

```
r_{23} = \{0, 0, 0\};
r3c3 = \{0, 0, 0\};
r2c3 = r_{23} + r3c3;
m_3 = 0;
I_{3} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix};
```

Link 4

```
14 = 0.38;
b4 = 0.146;
h4 = 0.146;
r_{34} = \{0, -0.38, 0\};
r4c4 = \{0, 0.19, 0\};
r3c4 = r_{34} + r4c4;
m_4 = rho * 14 * b4 * h4;
```

```
r_{45} = \{0, 0, 0\};
r5c5 = \{0, 0, 0\};
r4c5 = r_{45} + r5c5;
m_5 = 0;
I_5 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix};
```

```
 r6 = 0.108; \\ h6 = 0.065; \\ r_{56} = \{0, 0, 0.065\}; \\ r6c6 = \{0, 0, -0.0325\}; \\ r5c6 = r_{56} + r6c6; \\ m_6 = rho * Pi * r6^2 * h6; \\ I_6 = \begin{pmatrix} \frac{m_6}{12} * \left(3 * r6^2 + h6^2\right) & 0 & 0 \\ & 0 & \frac{m_6}{12} * (3 * r6^2 + h6^2) & 0 \\ & 0 & 0 & \frac{m_6}{2} * r6^2 \end{pmatrix};
```

Forward Recursion

Link I

```
\begin{array}{l} \omega_{0} \ = \ \{0,\,0,\,0\}; \\ \alpha_{0} \ = \ \{0,\,0,\,0\}; \\ a_{0} \ = \ \{0,\,0,\,0\}; \\ \omega_{1} \ = \ Transpose[R_{01}] . \omega_{0} \ + \ q_{1} \ '[t] \ * \ b_{1}; \\ \alpha_{1} \ = \ Simplify[Transpose[R_{01}] . \alpha_{0} \ + \ q_{1} \ '[t] \ * \ b_{1} \ + \ (Transpose[R_{01}] . \omega_{0}) \ \times \ \left(q_{1} \ '[t] \ * \ b_{1}\right)]; \\ a_{1} \ = \ Transpose[R_{01}] . a_{0} \ + \ \alpha_{1} \ \times r_{01} \ + \ \omega_{1} \times (\omega_{1} \times r_{01}); \\ a_{c1} \ = \ a_{1} \ + \ \alpha_{1} \times r1c1 \ + \ \omega_{1} \times \left(\omega_{1} \times r1c1\right); \end{array}
```

Link 2

```
\begin{array}{l} \omega_3 = \text{Transpose}[R_{23}].\omega_2 + \mathsf{q}_3\,'[t] * \mathsf{b}_3; \\ \alpha_3 = \text{Simplify}\big[\text{Transpose}[R_{23}].\alpha_2 + \mathsf{q}_3\,'[t] * \mathsf{b}_3 + (\text{Transpose}[R_{23}].\omega_2) \times \big(\mathsf{q}_3\,'[t] * \mathsf{b}_3\big)\big]; \\ a_3 = \text{Simplify}\big[\text{Transpose}[R_{23}].a_2 + \alpha_3 \times r_{23} + \omega_3 \times (\omega_3 \times r_{23})\big]; \\ a_{c3} = \text{Simplify}\big[a_3 + \alpha_3 \times r_{3} + \omega_3 \times (\omega_3 \times r_{3})\big]; \end{array}
```

```
\omega_4 = Transpose[R<sub>34</sub>].\omega_3 + q<sub>4</sub>'[t] * b<sub>4</sub>;
    \alpha_4 = Simplify[Transpose[R_{34}].\alpha_3 + q_4''[t] * b_4 + (Transpose[R_{34}].\omega_3) \times (q_4''[t] * b_4)];
    a_4 = Transpose[R_{34}].a_3 + \alpha_4 \times r_{34} + \omega_4 \times (\omega_4 \times r_{34});
    a_{c4} = a_4 + \alpha_4 \times r4c4 + \omega_4 \times (\omega_4 \times r4c4);
Link 5
    \omega_5 = \text{Transpose}[R_{45}] \cdot \omega_4 + q_5'[t] * b_5;
    \alpha_5 = Simplify [Transpose[R_{45}].\alpha_4 + q_5''[t] * b_5 + (Transpose[R_{45}].\omega_4) \times (q_5'[t] * b_5)];
    a_5 = \text{Transpose}[R_{45}] \cdot a_4 + \alpha_5 \times r_{45} + \omega_5 \times (\omega_5 \times r_{45});
    a_{c5} = a_5 + \alpha_5 \times r5c5 + \omega_5 \times (\omega_5 \times r5c5);
Link 6
    \omega_6 = Transpose[R<sub>56</sub>].\omega_5 + q<sub>6</sub>'[t] * b<sub>6</sub>;
    \alpha_6 = \text{Transpose}[R_{56}] \cdot \alpha_5 + q_6''[t] * b_6 + (\text{Transpose}[R_{56}] \cdot \omega_5) \times (q_6'[t] * b_6);
    a_6 = Transpose[R_{56}].a_5 + \alpha_6 \times r_{56} + \omega_6 \times (\omega_6 \times r_{56});
    a_{c6} = a_6 + \alpha_6 \times r6c6 + \omega_6 \times (\omega_6 \times r6c6);
```

Backward Recursion

Link 6

```
g_6 = Transpose[R_{06}].g_0;
f_{67} = -payload * g_6;
f_{56} = f_{67} - m_6 * g_6 + m_6 * a_{c6};
\tau_{56} = -\text{r6c6} \times f_{67} + \text{r5c6} \times f_{56} + I_6.\alpha_6 + \omega_6 \times (I_6.\omega_6);
```

Link 5

```
g_5 = Transpose[R_{05}].g_0;
f_{45} = R_{56} \cdot f_{56} - m_5 * g_5 + m_5 * a_{c5};
\tau_{45} = (R_{56}.\tau_{56}) - r5c5 \times (R_{56}.f_{56}) + r4c5 \times f_{45} + I_5.\alpha_5 + \omega_5 \times (I_5.\omega_5);
```

```
g_4 = Transpose[R_{04}].g_0;
f_{34} = R_{45} \cdot f_{45} - m_4 * g_4 + m_4 * a_{c4};
\tau_{34} = R_{45} \cdot \tau_{45} - r4c4 \times (R_{45} \cdot f_{45}) + r3c4 \times f_{34} + I_4 \cdot \alpha_4 + \omega_4 \times (I_4 \cdot \omega_4);
```

```
g_3 = Transpose[R_{03}].g_0;
f_{23} = R_{34} \cdot f_{34} - m_3 * g_3 + m_3 * a_{c3};
\tau_{23} = R_{34} \cdot \tau_{34} - r_{3}c_{3} \times (R_{34} \cdot f_{34}) + r_{2}c_{3} \times f_{23} + I_{3} \cdot \alpha_{3} + \omega_{3} \times (I_{3} \cdot \omega_{3});
```

Link 2

```
g_2 = Transpose[R_{02}].g_0;
f_{12} = R_{23} \cdot f_{23} - m_2 * g_2 + m_2 * a_{c2};
\tau_{12} = R_{23} \cdot \tau_{23} - r2c2 \times (R_{23} \cdot f_{23}) + r1c2 \times f_{12} + I_2 \cdot \alpha_2 + \omega_2 \times (I_2 \cdot \omega_2);
```

Link I

```
g_1 = Transpose[R_{01}].g_0;
f_{01} = R_{12} \cdot f_{12} - m_1 * g_1 + m_1 * a_{c1};
\tau_{01} = R_{12} \cdot \tau_{12} - r1c1 \times (R_{12} \cdot f_{12}) + r0c1 \times f_{01} + I_{1} \cdot \alpha_{1} + \omega_{1} \times (I_{1} \cdot \omega_{1});
```

Computation

```
takeg = 9.81;
t1 = \tau_{01} /. \{q_1[t] \rightarrow qdes[[1]], q_2[t] \rightarrow qdes[[2]], q_3[t] \rightarrow qdes[[3]],
      q_4[t] \rightarrow qdes[[4]], q_5[t] \rightarrow qdes[[5]], q_6[t] \rightarrow qdes[[6]], q_1'[t] \rightarrow qdotdes[[1]],
      q_2'[t] \rightarrow qdotdes[[2]], q_3'[t] \rightarrow qdotdes[[3]], q_4'[t] \rightarrow qdotdes[[4]],
      q_5'[t] \rightarrow qdotdes[[5]], q_6'[t] \rightarrow qdotdes[[6]], q_1''[t] \rightarrow qdotdotdes[[1]],
      q_2''[t] \rightarrow qdotdotdes[[2]], q_3''[t] \rightarrow qdotdotdes[[3]], q_4''[t] \rightarrow qdotdotdes[[4]],
      q_5''[t] \rightarrow qdotdotdes[[5]], q_6''[t] \rightarrow qdotdotdes[[6]], g \rightarrow takeg\};
t2 = \tau_{12} /. \{q_1[t] \rightarrow qdes[[1]], q_2[t] \rightarrow qdes[[2]], q_3[t] \rightarrow qdes[[3]],
      q_4[t] \rightarrow qdes[[4]], q_5[t] \rightarrow qdes[[5]], q_6[t] \rightarrow qdes[[6]], q_1'[t] \rightarrow qdotdes[[1]],
      q_2'[t] \rightarrow qdotdes[[2]], q_3'[t] \rightarrow qdotdes[[3]], q_4'[t] \rightarrow qdotdes[[4]],
      q_5'[t] \rightarrow qdotdes[[5]], q_6'[t] \rightarrow qdotdes[[6]], q_1''[t] \rightarrow qdotdotdes[[1]],
      q_2''[t] \rightarrow qdotdotdes[[2]], q_3''[t] \rightarrow qdotdotdes[[3]], q_4''[t] \rightarrow qdotdotdes[[4]],
      q<sub>5</sub>''[t] → qdotdotdes[[5]], q<sub>6</sub>''[t] → qdotdotdes[[6]], g → takeg};
t3 = \tau_{23} /. \{q_1[t] \rightarrow qdes[[1]], q_2[t] \rightarrow qdes[[2]], q_3[t] \rightarrow qdes[[3]],
      q_4[t] \rightarrow qdes[[4]], q_5[t] \rightarrow qdes[[5]], q_6[t] \rightarrow qdes[[6]], q_1'[t] \rightarrow qdotdes[[1]],
      q_2'[t] \rightarrow qdotdes[[2]], q_3'[t] \rightarrow qdotdes[[3]], q_4'[t] \rightarrow qdotdes[[4]],
      q_5'[t] \rightarrow qdotdes[[5]], q_6'[t] \rightarrow qdotdes[[6]], q_1''[t] \rightarrow qdotdotdes[[1]],
      q_2''[t] \rightarrow qdotdotdes[[2]], q_3''[t] \rightarrow qdotdotdes[[3]], q_4''[t] \rightarrow qdotdotdes[[4]],
      q_5''[t] \rightarrow qdotdotdes[[5]], q_6''[t] \rightarrow qdotdotdes[[6]], g \rightarrow takeg\};
t4 = \tau_{34} /. \{q_1[t] \rightarrow qdes[[1]], q_2[t] \rightarrow qdes[[2]], q_3[t] \rightarrow qdes[[3]],
      q_4[t] \rightarrow qdes[[4]], q_5[t] \rightarrow qdes[[5]], q_6[t] \rightarrow qdes[[6]], q_1'[t] \rightarrow qdotdes[[1]],
      q_2'[t] \rightarrow qdotdes[[2]], q_3'[t] \rightarrow qdotdes[[3]], q_4'[t] \rightarrow qdotdes[[4]],
      q_5'[t] \rightarrow qdotdes[[5]], q_6'[t] \rightarrow qdotdes[[6]], q_1''[t] \rightarrow qdotdotdes[[1]],
      q_2''[t] \rightarrow qdotdotdes[[2]], q_3''[t] \rightarrow qdotdotdes[[3]], q_4''[t] \rightarrow qdotdotdes[[4]],
      q_5''[t] \rightarrow qdotdotdes[[5]], q_6''[t] \rightarrow qdotdotdes[[6]], g \rightarrow takeg\};
t5 = \tau_{45} /. {q<sub>1</sub>[t] \rightarrow qdes[[1]], q<sub>2</sub>[t] \rightarrow qdes[[2]], q<sub>3</sub>[t] \rightarrow qdes[[3]],
      q_4[t] \rightarrow qdes[[4]], q_5[t] \rightarrow qdes[[5]], q_6[t] \rightarrow qdes[[6]], q_1'[t] \rightarrow qdotdes[[1]],
      q_2'[t] \rightarrow qdotdes[[2]], q_3'[t] \rightarrow qdotdes[[3]], q_4'[t] \rightarrow qdotdes[[4]],
      q_5'[t] \rightarrow qdotdes[[5]], q_6'[t] \rightarrow qdotdes[[6]], q_1''[t] \rightarrow qdotdotdes[[1]],
      q_2''[t] \rightarrow qdotdotdes[[2]], q_3''[t] \rightarrow qdotdotdes[[3]], q_4''[t] \rightarrow qdotdotdes[[4]],
      q_5''[t] \rightarrow qdotdotdes[[5]], q_6''[t] \rightarrow qdotdotdes[[6]], g \rightarrow takeg\};
t6 = \tau_{56} /. \{q_1[t] \rightarrow qdes[[1]], q_2[t] \rightarrow qdes[[2]], q_3[t] \rightarrow qdes[[3]],
      q_4[t] \rightarrow qdes[[4]], q_5[t] \rightarrow qdes[[5]], q_6[t] \rightarrow qdes[[6]], q_1'[t] \rightarrow qdotdes[[1]],
      q_2'[t] \rightarrow qdotdes[[2]], q_3'[t] \rightarrow qdotdes[[3]], q_4'[t] \rightarrow qdotdes[[4]],
      q_5'[t] \rightarrow qdotdes[[5]], q_6'[t] \rightarrow qdotdes[[6]], q_1''[t] \rightarrow qdotdotdes[[1]],
      q_2''[t] \rightarrow qdotdotdes[[2]], q_3''[t] \rightarrow qdotdotdes[[3]], q_4''[t] \rightarrow qdotdotdes[[4]],
      q<sub>5</sub>''[t] → qdotdotdes[[5]], q<sub>6</sub>''[t] → qdotdotdes[[6]], g → takeg};
```

Actual Torques Required

```
\tau_{z1} = TrigReduce[b_1.t1];
\tau_{z2} = TrigReduce[b_2.t2];
\tau_{z3} = TrigReduce[b_3.t3];
\tau_{z4} = TrigReduce[b_4.t4];
\tau_{z5} = TrigReduce[b_5.t5];
\tau_{z6} = TrigReduce[b_6.t6];
Torq = \{\tau_{z1}, \tau_{z2}, \tau_{z3}, \tau_{z4}, \tau_{z5}, \tau_{z6}\}
{0., 290.765, 105.348, 0., 6.25594, 0.}
```

Following sections should only be used to extract the Manipulator equations

Configuration Dependent Mass Matrix

```
m_{11} = \tau_{z1} / .
      \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0, q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 1,
        q_2''[t] \rightarrow 0, q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{21} = \tau_{z2} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 1, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{31} = \tau_{z3} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 1, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{41} = \tau_{z4} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 1, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{51} = \tau_{z5} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 1, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{61} = \tau_{z6} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 1, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{12} = \tau_{z1} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 1,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{22} = \tau_{z2} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 1,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{32} = \tau_{z3} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 1,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{42} = \tau_{z4} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 1,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0};
m_{52} = \tau_{z5} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 1,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
```

```
m_{62} = \tau_{z6} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 1,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{13} = \tau_{z1} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 1, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{23} = \tau_{z2} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 1, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{33} = \tau_{z3} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3 ''[t] \rightarrow 1, q_4 ''[t] \rightarrow 0, q_5 ''[t] \rightarrow 0, q_6 ''[t] \rightarrow 0, g \rightarrow 0};
m_{43} = \tau_{z4} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 1, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{53} = \tau_{z5} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 1, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0};
m_{63} = \tau_{z6} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 1, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{14} = \tau_{z1} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 1, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{24} = \tau_{z2} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 1, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{34} = \tau_{z3} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 1, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{44} = \tau_{z4} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 1, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{54} = \tau_{z5} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 1, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{64} = \tau_{z6} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 1, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0, g \rightarrow 0};
m_{15} = \tau_{z1} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 1, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{25} = \tau_{z2} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 1, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{35} = \tau_{z3} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 1, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{45} = \tau_{z4} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 1, q_6''[t] \rightarrow 0, g \rightarrow 0;
```

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m_{55} = \tau_{z5} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 1, q_6''[t] \rightarrow 0, g \rightarrow 0;
m_{65} = \tau_{z6} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 1, q_6''[t] \rightarrow 0, g \rightarrow 0};
m_{16} = \tau_{z1} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 1, g \rightarrow 0;
m_{26} = \tau_{z2} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
       q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 1, g \rightarrow 0;
m_{36} = \tau_{z3} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
       q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 1, g \rightarrow 0;
m_{46} \ = \ \tau_{z4} \ /. \ \{q_1\,'[t] \ \rightarrow \ 0, \ q_2\,'[t] \ \rightarrow \ 0, \ q_3\,'[t] \ \rightarrow \ 0, \ q_4\,'[t] \ \rightarrow \ 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 1, g \rightarrow 0};
m_{56} = \tau_{z5} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
       q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 1, g \rightarrow 0;
m_{66} = \tau_{z6} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0,
        q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0, q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0,
        q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 1, g \rightarrow 0;
          m_{11} m_{12} m_{13} m_{14} m_{15} m_{16}
          m_{21} \ m_{22} \ m_{23} \ m_{24} \ m_{25} \ m_{26}
          m_{31} m_{32} m_{33} m_{34} m_{35} m_{36}
          m_{41} \ m_{42} \ m_{43} \ m_{44} \ m_{45} \ m_{46}
          m_{51} m_{52} m_{53} m_{54} m_{55} m_{56}
        (m_{61} m_{62} m_{63} m_{64} m_{65} m_{66})
\{\{0., 0., 0., 0., 0., 0.\}, \{290.765, 290.765, 290.765, 290.765, 290.765, 290.765\},
  \{105.348, 105.348, 105.348, 105.348, 105.348, 105.348\}, \{0., 0., 0., 0., 0., 0.\}
  \{6.25594, 6.25594, 6.25594, 6.25594, 6.25594, 6.25594\}, \{0., 0., 0., 0., 0., 0.\}\}
```

Gravitational Terms

```
g6 = \tau_{z6} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0, q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0,
                                             q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0, q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0;
g5 = \tau_{z5} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0, q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0,
                                             q_1^{\,\,\prime\prime}[t] \,\,\rightarrow\,\, 0,\,\, q_2^{\,\,\prime\prime}[t] \,\,\rightarrow\,\, 0,\,\, q_3^{\,\,\prime\prime}[t] \,\,\rightarrow\,\, 0,\,\, q_4^{\,\,\prime\prime}[t] \,\,\rightarrow\,\, 0,\,\, q_5^{\,\,\prime\prime}[t] \,\,\rightarrow\,\, 0,\,\, q_6^{\,\,\prime\prime}[t] \,\,\rightarrow\,\, 0\};
 g4 = \tau_{z4} /. \{q_1'[t] \rightarrow 0, q_2'[t] \rightarrow 0, q_3'[t] \rightarrow 0, q_4'[t] \rightarrow 0, q_5'[t] \rightarrow 0, q_6'[t] \rightarrow 0,
                                               q_1^{\,\prime\,\prime}[t] \,\,\rightarrow\,\, 0,\,\, q_2^{\,\prime\,\prime}[t] \,\,\rightarrow\,\, 0,\,\, q_3^{\,\prime\,\prime}[t] \,\,\rightarrow\,\, 0,\,\, q_4^{\,\prime\,\prime}[t] \,\,\rightarrow\,\, 0,\,\, q_5^{\,\prime\,\prime}[t] \,\,\rightarrow\,\, 0,\,\, q_6^{\,\prime\,\prime}[t] \,\,\rightarrow\,\, 0\};
g3 = \tau_{z3} \ /. \ \{q_1'[t] \rightarrow 0, \, q_2'[t] \rightarrow 0, \, q_3'[t] \rightarrow 0, \, q_4'[t] \rightarrow 0, \, q_5'[t] \rightarrow 0, \, q_6'[t] \rightarrow 0, \, q_6'[t] \rightarrow 0, \, q_8'[t] \rightarrow 0, \,
                                             q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0, q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0);
g2 = \tau_{z2} \ /. \ \{q_1'[t] \to 0, \, q_2'[t] \to 0, \, q_3'[t] \to 0, \, q_4'[t] \to 0, \, q_5'[t] \to 0, \, q_6'[t] \to 0, \, q_6'[t] \to 0, \, q_8'[t] \to 0, \,
                                             q_1''[t] \rightarrow 0, q_2''[t] \rightarrow 0, q_3''[t] \rightarrow 0, q_4''[t] \rightarrow 0, q_5''[t] \rightarrow 0, q_6''[t] \rightarrow 0;
g1 = \tau_{z1} \ /. \ \{q_1\,'[t] \ \rightarrow \ 0, \ q_2\,'[t] \ \rightarrow \ 0, \ q_3\,'[t] \ \rightarrow \ 0, \ q_4\,'[t] \ \rightarrow \ 0, \ q_5\,'[t] \ \rightarrow \ 0, \ q_6\,'[t] \ \rightarrow \ 0, \ q_6\,
                                               q_1^{\,\,\prime\,\prime}[t] \,\,\rightarrow\,\, 0,\,\, q_2^{\,\,\prime\,\prime}[t] \,\,\rightarrow\,\, 0,\,\, q_3^{\,\,\prime\,\prime}[t] \,\,\rightarrow\,\, 0,\,\, q_4^{\,\,\prime\,\prime}[t] \,\,\rightarrow\,\, 0,\,\, q_5^{\,\,\prime\,\prime}[t] \,\,\rightarrow\,\, 0,\,\, q_6^{\,\,\prime\,\prime}[t] \,\,\rightarrow\,\, 0\};
G = \{g1, g2, g3, g4, g5, g6\}
   {0., 290.765, 105.348, 0., 6.25594, 0.}
```

Coriolis Terms

```
CDq = Torq - M.qdotdotdes - G
\{0., 0., 0., 0., 0., 0.\}
```