

Advanced Data Structure and Algorithms for Problem Solving

Lecture # 04

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Recursion

- Recursion is a mathematical technique that evaluates a function by calling the same function repeatedly on smaller inputs.
- Most programming languages support such a style of programming.
 - Often very elegant to study.
- Helps in problem solving too.

Recursion

- **Q:** How many twists does it take to screw in a light bulb?

A: Is it already screwed in? Then zero. If not, then twist it once, ask me again, and add 1 to my answer.

Recursion

- Relates to mathematical induction
- Divide and Conquer algorithms

Lets start with an examples

- A mathematical view of computer science
- $\text{factorial}(n) = n * \text{factorial}(n-1)$

Three Laws of Recursion

- $\text{factorial}(n) = n * \text{factorial}(n-1)$
- A recursive algorithm must change its state and move toward the base case.
- A recursive algorithm must call itself, recursively.

Factorial – deeper look

Factorial – deeper look

- Space and time complexity

Inductive Reasoning

- A recursive algorithm must have a **base case**.
- If I call `factorial(n)` with $n=1$, I am done
- If I call `factorial(n)` with $n>1$, it makes a recursive call with a smaller value of n ; must eventually reach $n=1$.

Recursion and Induction

Recursion with multiple base cases

Recursion with multiple base cases

Fibonacci deeper look

- Time and space complexity

Recursion is not always good

Recursion with memoization

Exponentiation

Modular Exponentiation

Thank You