

Open Elective Course [OE]

Course Code: CSO507

Winter 2023-24

Lecture#

Deep Learning

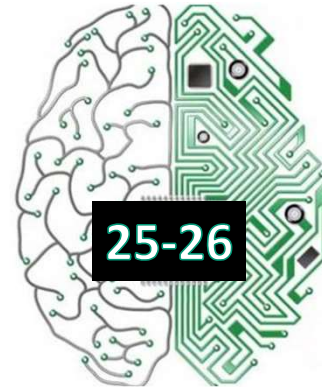
**Unit-5: Sequence Modeling with
Recurrent Neural Network (RNN) Part-VI&VII,
Attention Mechanism, Transformer (Part-I)**

Course Instructor:**Dr. Monidipa Das**

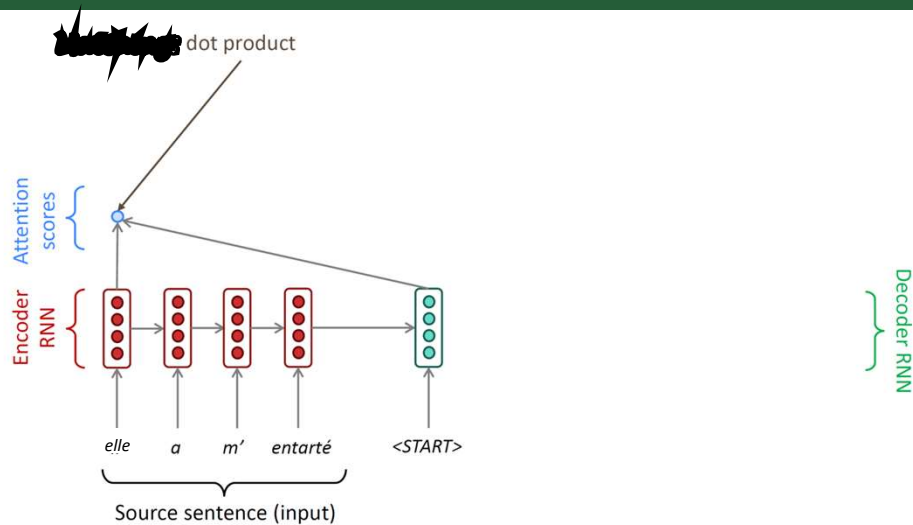
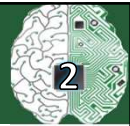
Assistant Professor

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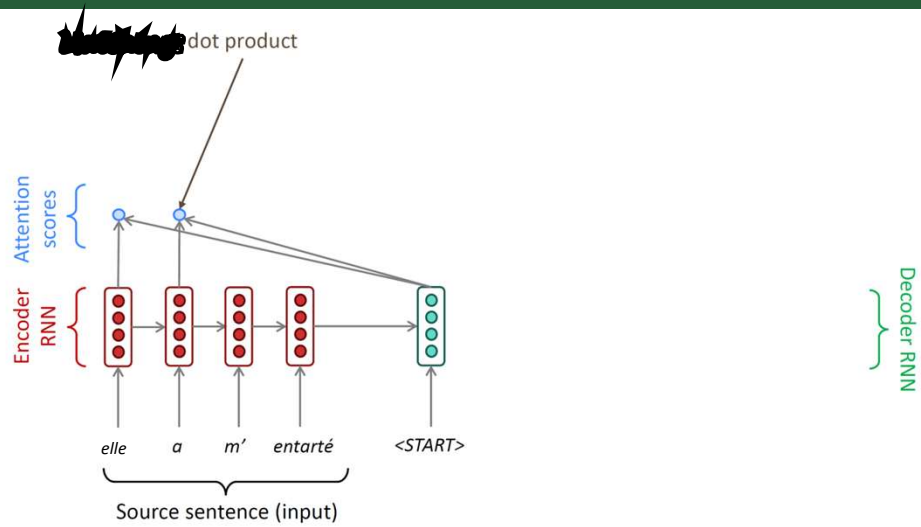


Attention Mechanism



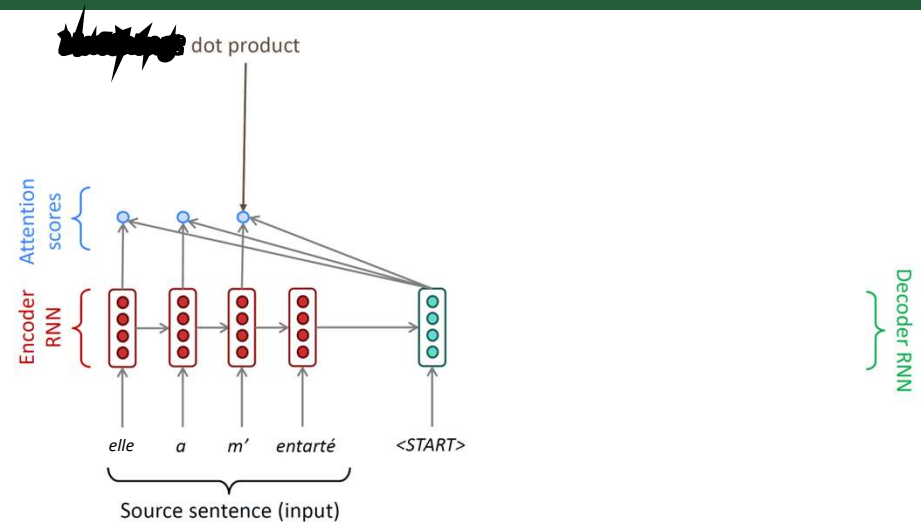
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Attention Mechanism



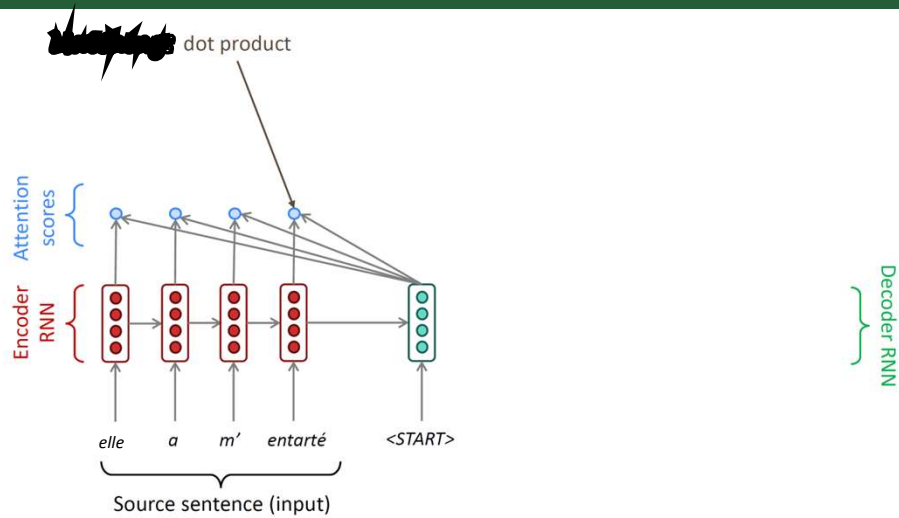
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Attention Mechanism



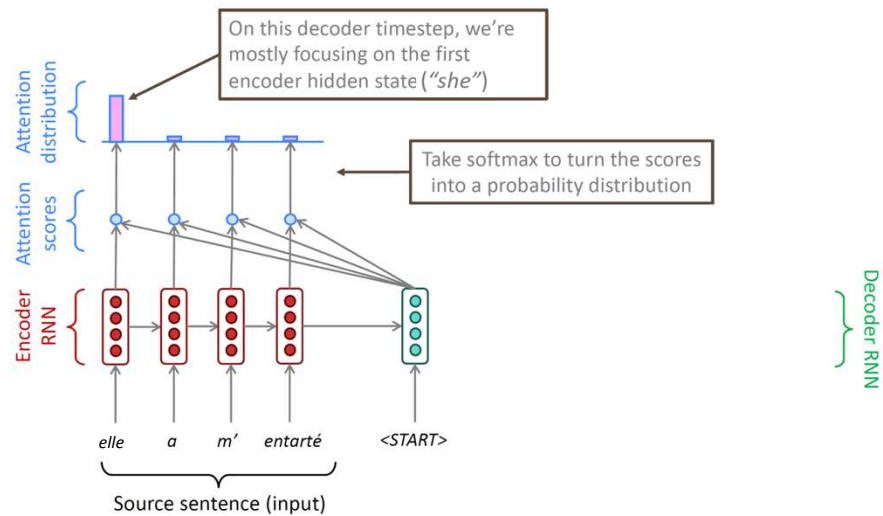
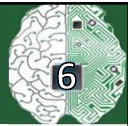
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Attention Mechanism



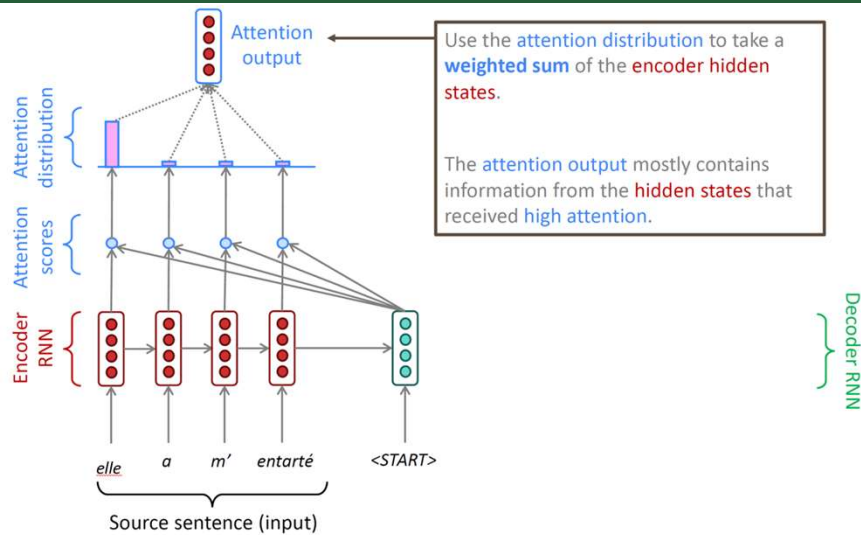
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Attention Mechanism



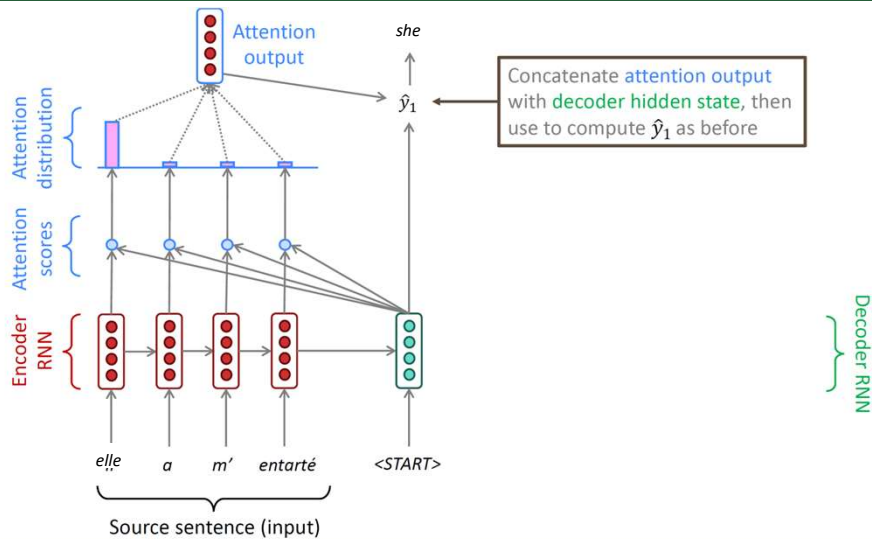
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Attention Mechanism



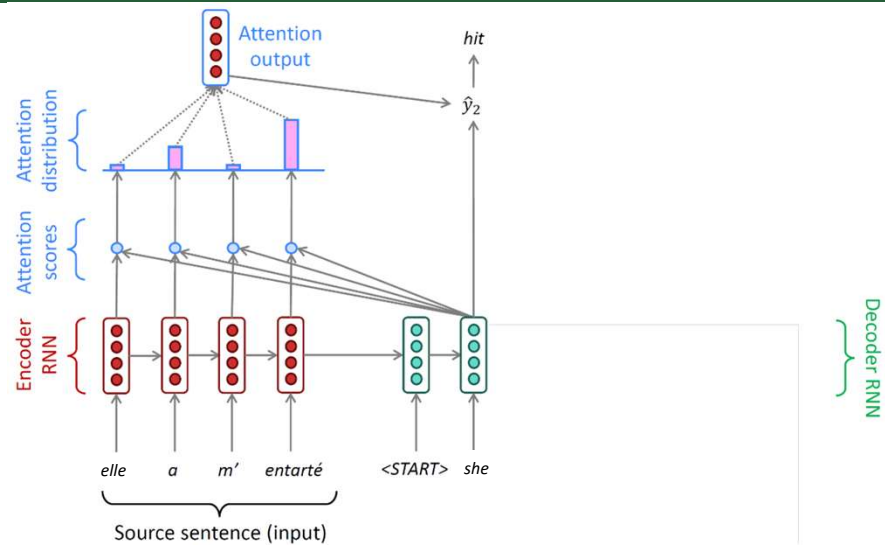
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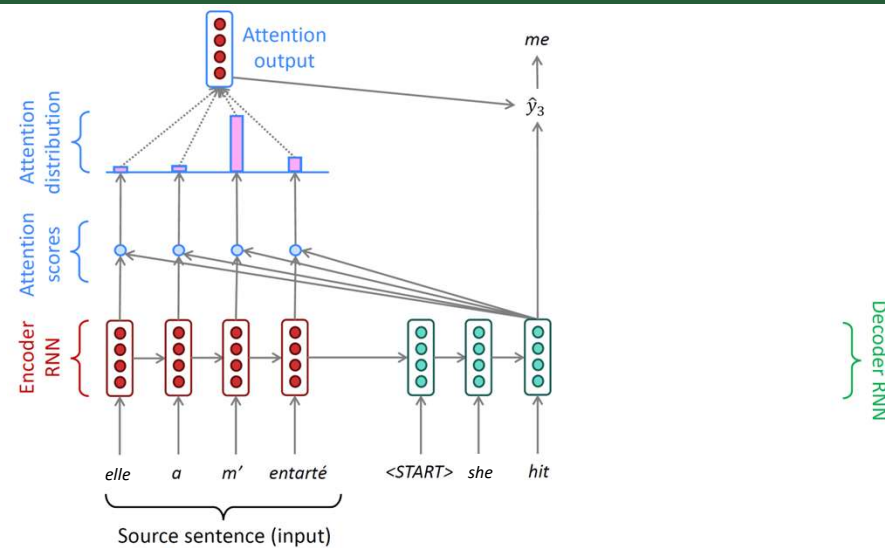
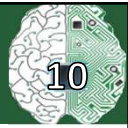
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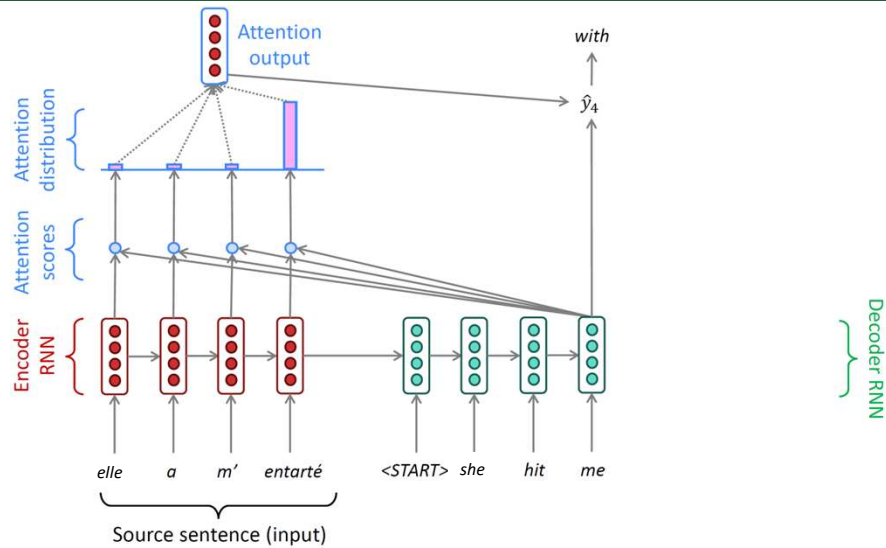
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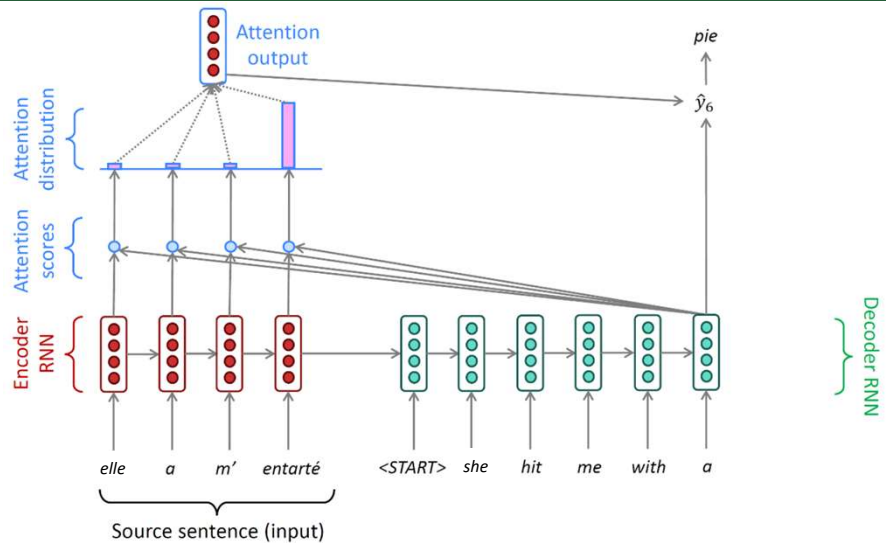
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Attention Mechanism



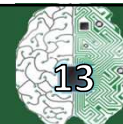
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Attention Mechanism



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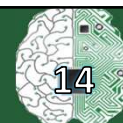
Attention Mechanism



- Input sequence X , encoder f_{enc} , and decoder f_{dec}
- $f_{enc}(X)$ produces hidden states $h_1^{enc}, h_2^{enc}, \dots, h_N^{enc}$
- On time step t , we have **decoder hidden state** h_t
- Compute attention score $\alpha_i = h_t^T h_i^{enc}$ //dot product attention
- Compute attention distribution $\hat{\alpha}_i = P_{att}(X_i) = softmax(\alpha_i)$
- Attention output: $h_{att}^{enc} = \sum_i \hat{\alpha}_i h_i^{enc}$
- $Y_t \sim g(h_t, h_{att}^{enc}; \theta)$
 - Sample an output using both

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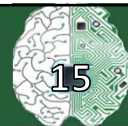
Attention Mechanism



- **Attention solves the bottleneck problem**
 - Attention allows decoder to look directly at source; bypass bottleneck
- **Attention helps with vanishing gradient problem**
 - Provides shortcut to faraway states
- **Attention provides some interpretability**
 - By inspecting attention distribution, we can see what the decoder was focusing on

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Self Attention



“I am going to the **bank** to deposit the cheque”

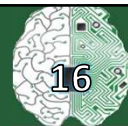
“The boat went down the river **bank**”

The vector representation used as input to RNN cannot differentiate context

Problems with RNNs: **Sequential computation inhibits parallelization**

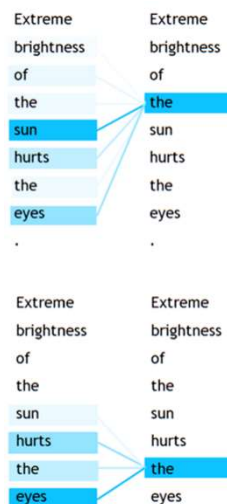
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Self Attention



- Self attention**

- Re-express representation in terms of the context the word occurs in
- Construct Probability distribution of importance - Dot product and normalization with only the input
- Re-express word vectors weighted by the probabilities as weights



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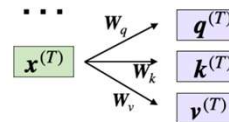
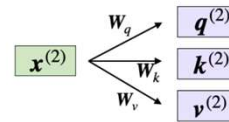
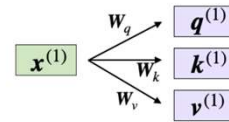
Self Attention

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Defining the Weight Matrices

- Three matrices serve to project the inputs into **query**, **key**, and **value** components

- Query sequence: $\mathbf{q}^{(i)} = \mathbf{W}_q \mathbf{x}^{(i)}$ for $i \in [1, T]$
- Key sequence: $\mathbf{k}^{(i)} = \mathbf{W}_k \mathbf{x}^{(i)}$ for $i \in [1, T]$
- Value sequence: $\mathbf{v}^{(i)} = \mathbf{W}_v \mathbf{x}^{(i)}$ for $i \in [1, T]$

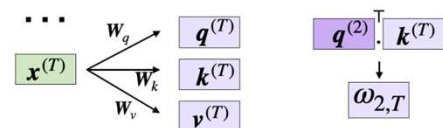
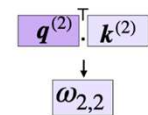
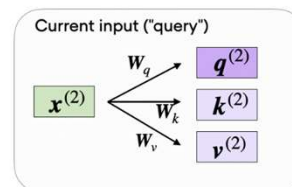
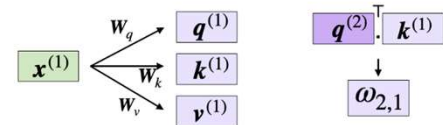


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Self Attention

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Computing the Unnormalized Attention Weights

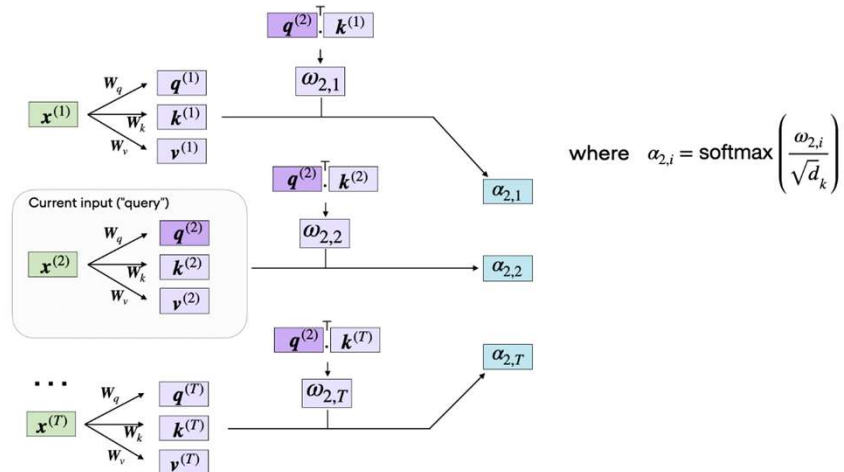


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Self Attention

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Computing the Attention Scores

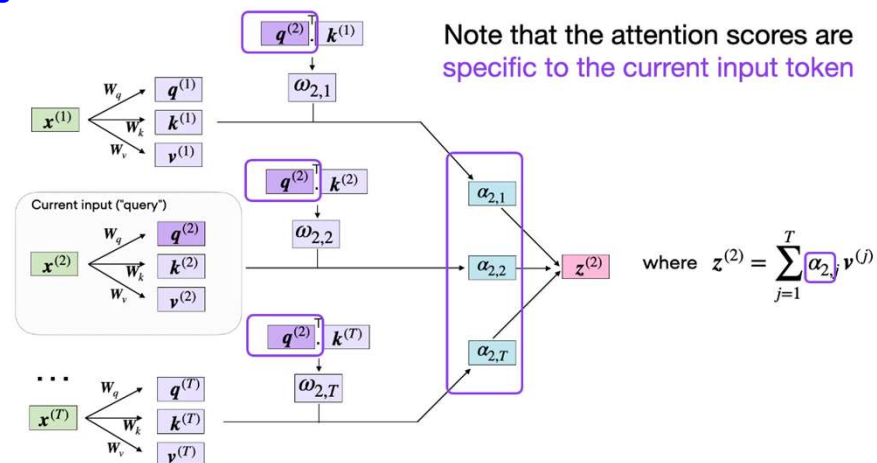


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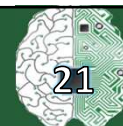
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Computing the Context Vector

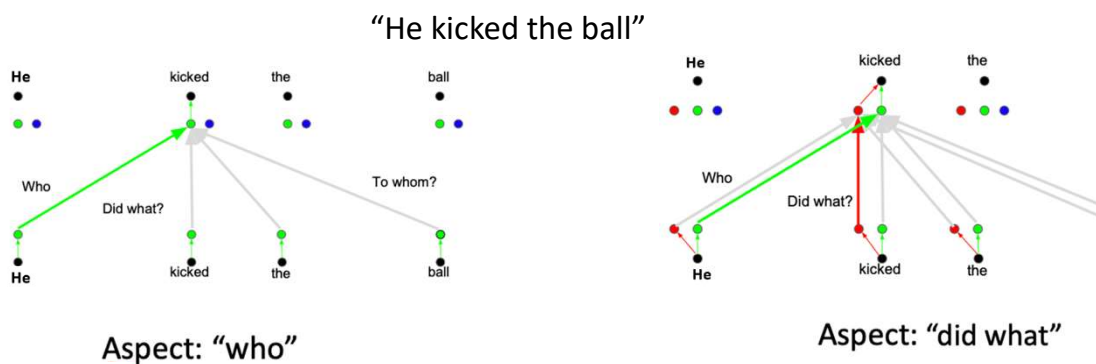


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Multi-Head Attention

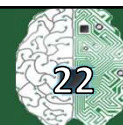


- All similarities do not encode the same aspects
- Multi-head Attention: Each notion of similarity is represented by an attention head

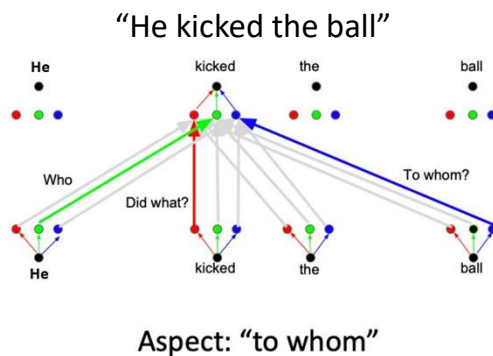


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Multi-Head Attention



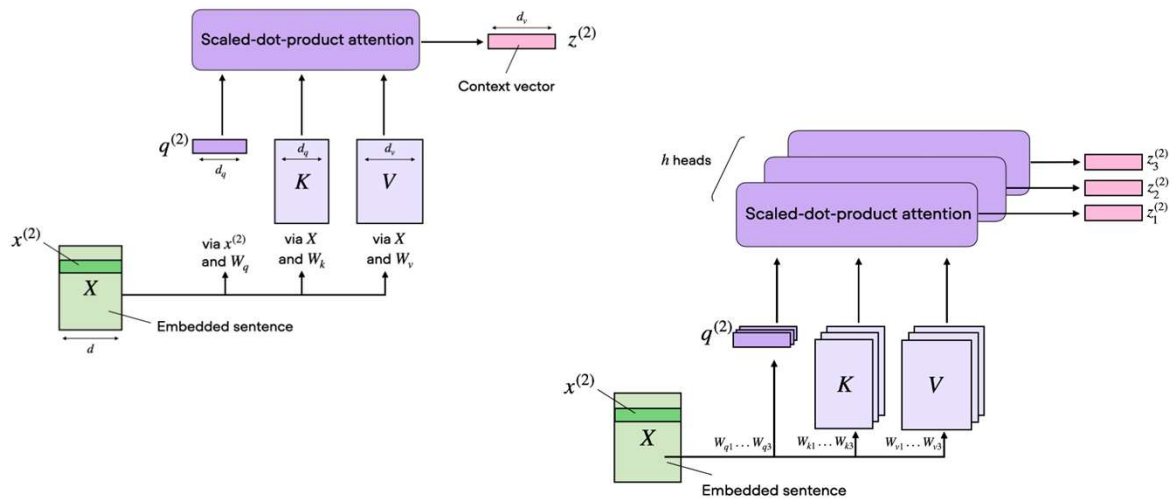
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Multi-Head Attention

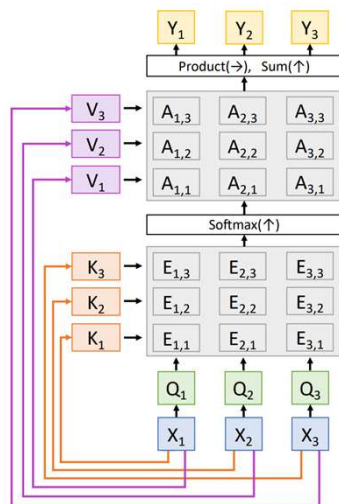
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Self Attention: Permutation Invariant!

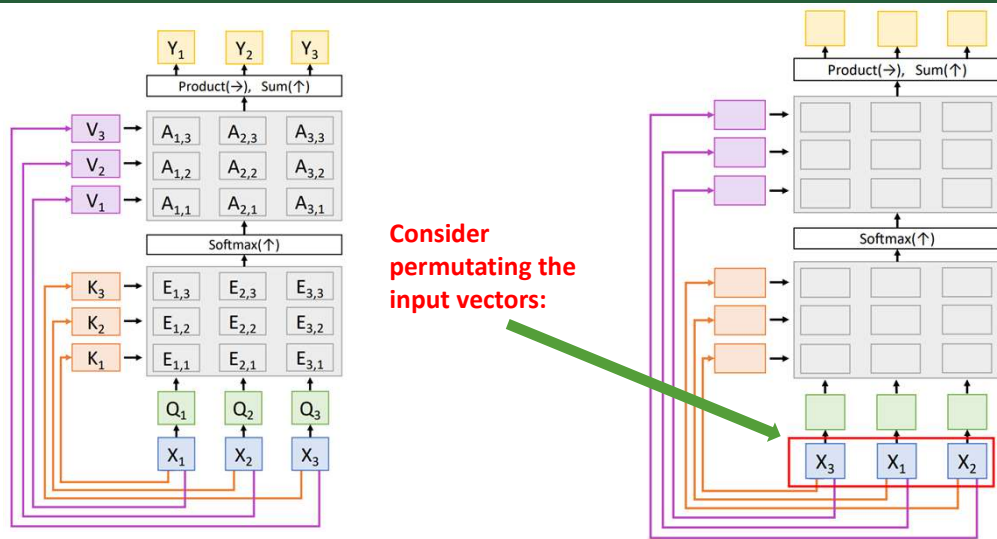
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Self Attention: Permutation Invariant!

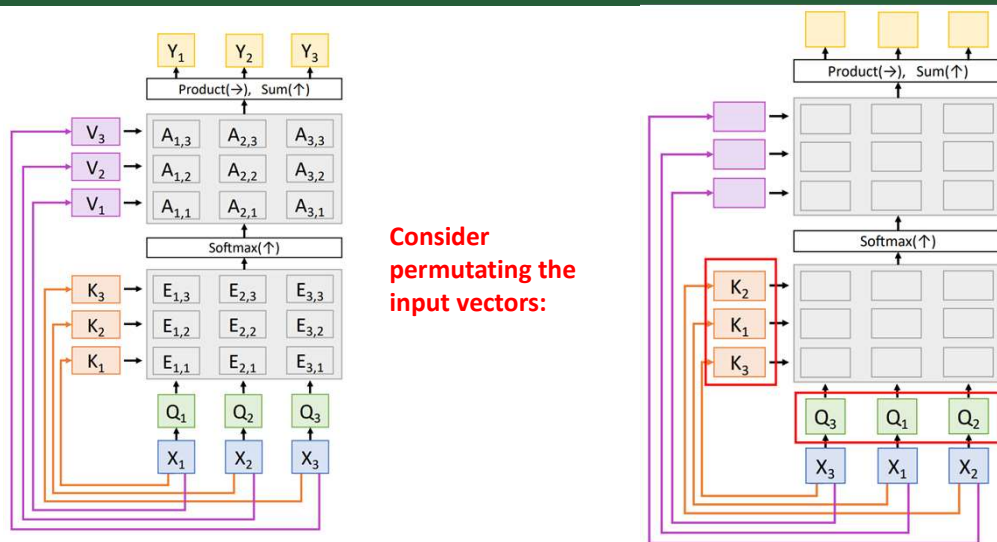
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Self Attention: Permutation Invariant!

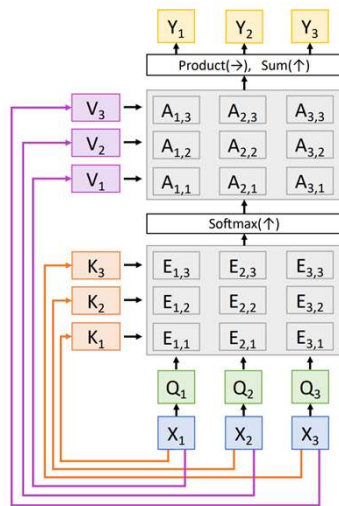
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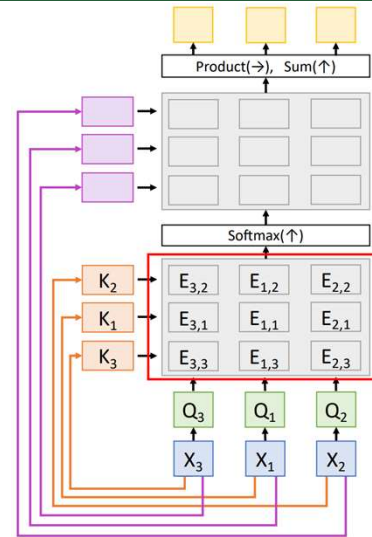
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Self Attention: Permutation Invariant!

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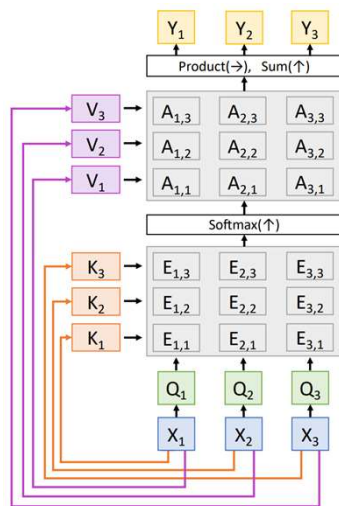
Consider
permuting the
input vectors:



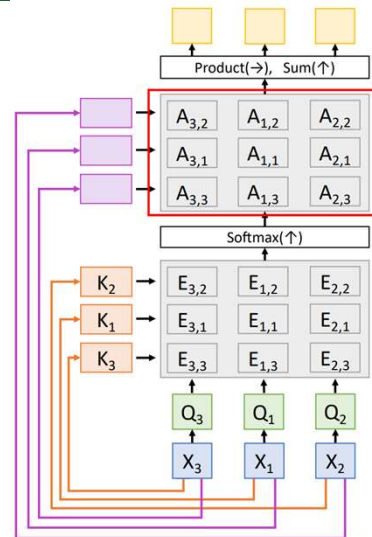
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Self Attention: Permutation Invariant!

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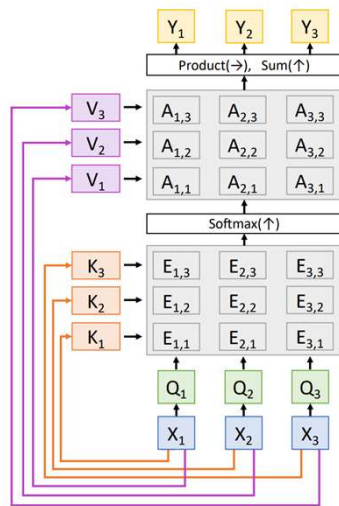
Consider
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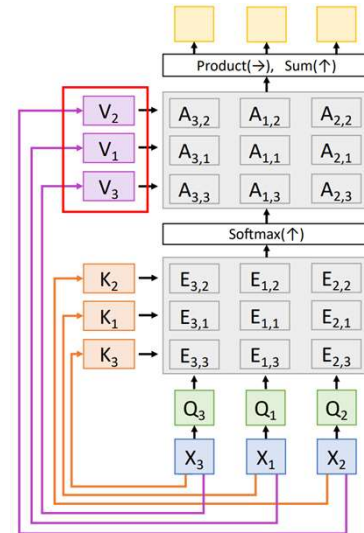
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Self Attention: Permutation Invariant!

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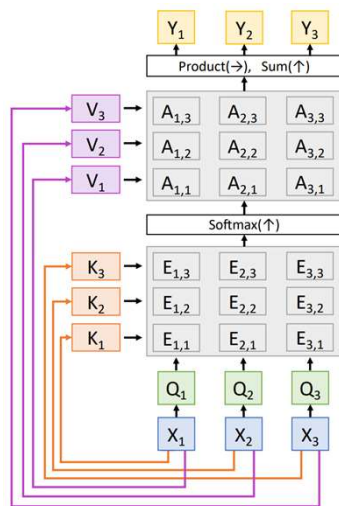
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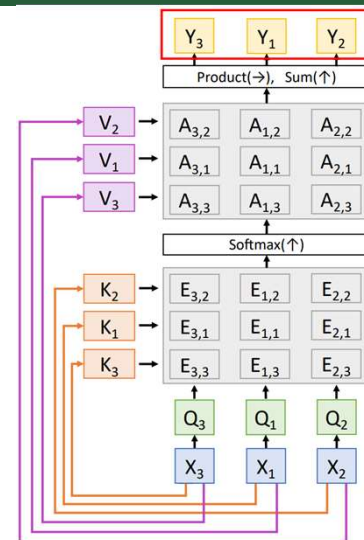
Self Attention: Permutation Invariant!

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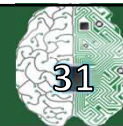
Consider
permuting the
input vectors:

The output is the
same put permuted!



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Self Attention: Permutation Invariant!



- Self attention doesn't "know" the order of the vectors it is processing!
- But what if the ordering of the input vectors conveys information as well?
 - The position of a word in a sentence matters!

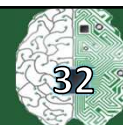
"The man ate a fish"

"The fish ate a man"

- Solution: Positional Encoding**

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Self Attention: Permutation Invariant!



- Add positional embeddings to input embeddings
 - Same dimension
 - Can be learned or fixed

Options for $\text{pos}(\cdot)$

- Learn a lookup table:
 - Learn parameters to use for $\text{pos}(t)$ for $t \in [0, T)$
 - Lookup table contains $T \times d$ parameters.

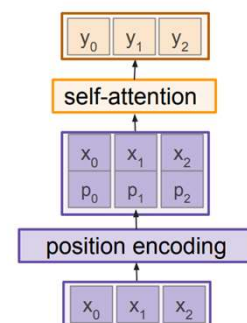
- Design a fixed function with the desiderata

Desiderata of $\text{pos}(\cdot)$:

- It should output a **unique** encoding for each time-step (word's position in a sentence)
- Distance** between any two time-steps should be consistent across sentences with different lengths.
- Our model should generalize to **longer** sentences without any efforts. Its values should be bounded.
- It must be **deterministic**.

$$\text{pos}(j) = \begin{bmatrix} \sin(\omega_1 \cdot t) \\ \cos(\omega_1 \cdot t) \\ \sin(\omega_2 \cdot t) \\ \cos(\omega_2 \cdot t) \\ \vdots \\ \sin(\omega_{d/2} \cdot t) \\ \cos(\omega_{d/2} \cdot t) \end{bmatrix}_d$$

$$\text{where } \omega_k = \frac{1}{10000^{2k/d}}$$



Concatenate special positional encoding p_j to each input vector x_j

We use a function $\text{pos}: \mathbb{N} \rightarrow \mathbb{R}^d$ to process the position j of the vector into a d -dimensional vector

So, $p_j = \text{pos}(j)$

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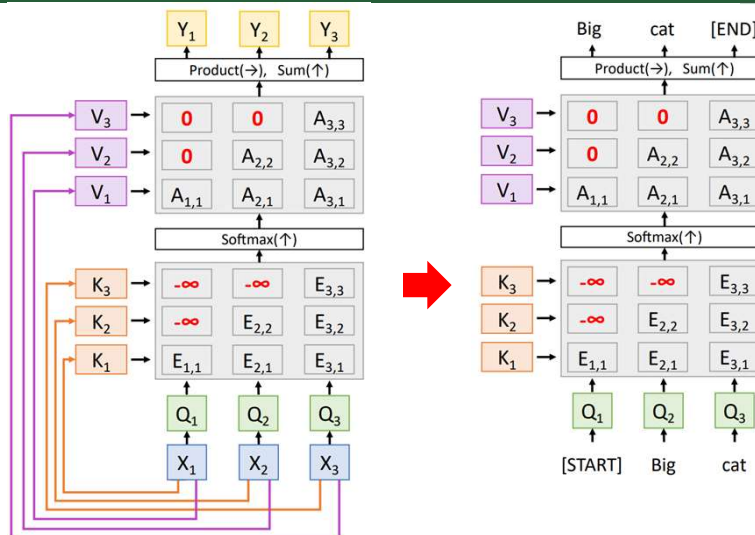
Masked Self-Attention Layer



Prevent vectors from looking at future vectors.

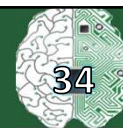
Manually set alignment scores to $-\infty$

Used for language modeling (predict next word)



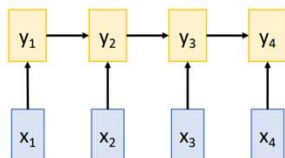
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RNN vs. 1D Convolution vs. Self-Attention



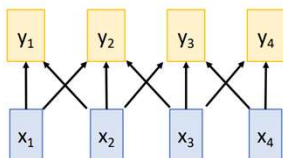
Three Ways of Processing Sequences

Recurrent Neural Network



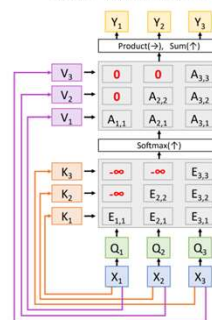
Works on **Ordered Sequences**
 (+) Good at long sequences: After one RNN layer, h_T "sees" the whole sequence
 (-) Not parallelizable: need to compute hidden states sequentially

1D Convolution



Works on **Multidimensional Grids**
 (-) Bad at long sequences: Need to stack many conv layers for outputs to "see" the whole sequence
 (+) Highly parallel: Each output can be computed in parallel

Self-Attention



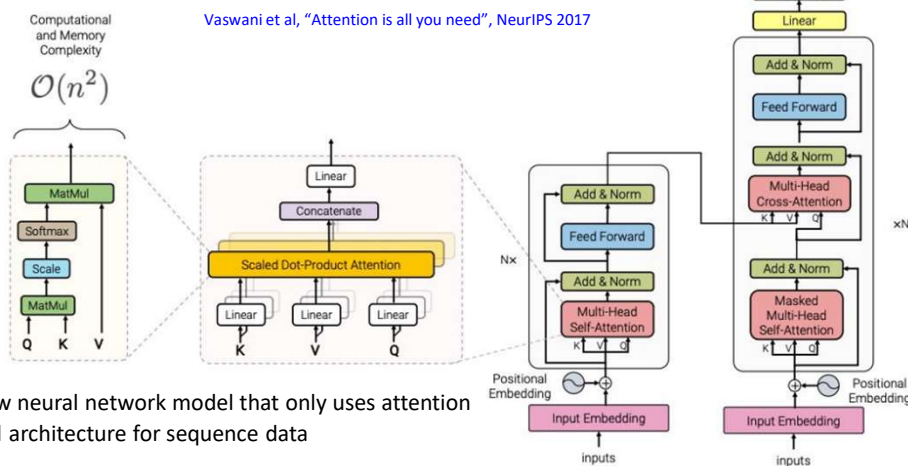
Works on **Sets of Vectors**
 (-) Good at long sequences: after one self-attention layer, each output "sees" all inputs!
 (+) Highly parallel: Each output can be computed in parallel
 (-) Very memory intensive

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The Transformer

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Architecture of a Standard Transformer



- Transformers are a new neural network model that only uses attention
- a fully attention-based architecture for sequence data

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Transformer Block

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Transformer Block:

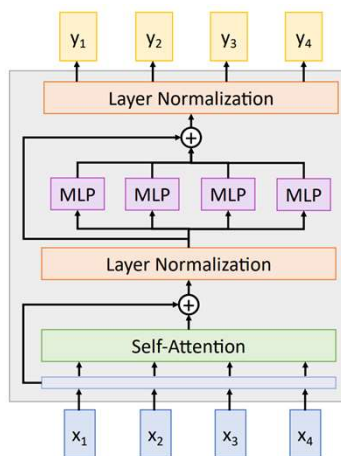
Input: Set of vectors x

Output: Set of vectors y

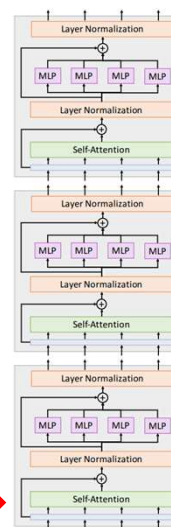
Self-attention is the only interaction between vectors!

Layer norm and MLP work independently per vector

Highly scalable, highly parallelizable

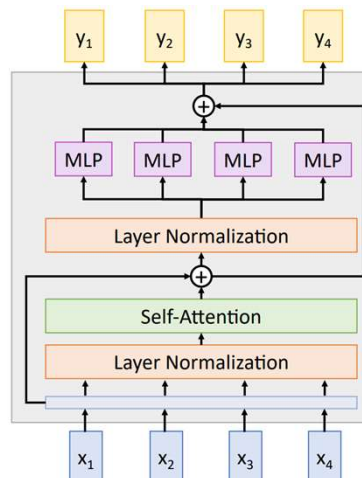
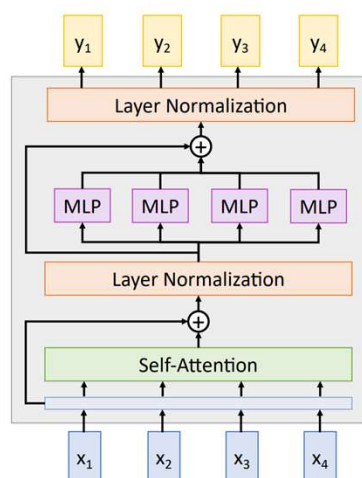
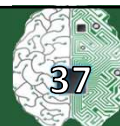


A Transformer is a sequence of transformer blocks



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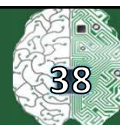
Post-Norm Transformer and Pre-Norm Transformer



Baevski & Auli, "Adaptive Input Representations for Neural Language Modeling", arXiv 2018

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Scaling up Transformers



Model	Layers	Width	Heads	Params
Transformer-Base	12	512	8	65M
Transformer-Large	12	1024	16	213M
BERT-Base	12	768	12	110M
BERT-Large	24	1024	16	340M
XLNet-Large	24	1024	16	~340M
RoBERTa	24	1024	16	355M
GPT-2	48	1600	?	1.5B
Megatron-LM	72	3072	32	8.3B
Turing-NLG	78	4256	28	17B
GPT-3	96	12,288	96	175B
Gopher	80	16,384	128	280B

Data 10.55 TB 4096x TPUv3 (38 days) Training time

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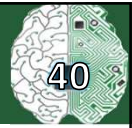
Advantages of Transformers



- **Great for modelling context**
 - Each token can have access to all other tokens in the sequence
- **A generic architecture:**
 - Operates on any inputs that can be tokenized!
- **Parallelizable**
- **Empirically shown to perform excellently at scale**

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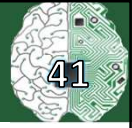
Weaknesses of Transformers



- **Quadratic complexity**
 - Each token attends to every other token
 - N tokens $\rightarrow N^2$ operations
 - Prohibitive as the number of tokens increases!
- **Most powerful language models are extremely expensive**
- **Large body of work on more efficient transformers.**
- **Transformers can overfit easily on smaller datasets**

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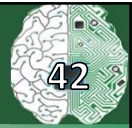
RNNs to Transformer



- **RNNs**
 - LSTMs work reasonably well for long sequences.
 - Expects an ordered sequences of inputs
 - Sequential computation: subsequent hidden states can only be computed after the previous ones are done.
- **Transformer:**
 - Good at long sequences. Each attention calculation looks at all inputs.
 - Can operate over unordered sets or ordered sequences with positional encodings.
 - Parallel computation: All alignment and attention scores for all inputs can be done in parallel
 - Requires a lot of memory: $N \times M$ alignment and attention scalars need to be calculated and stored for a single self-attention head.

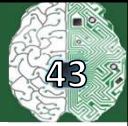
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Transformers for Vision



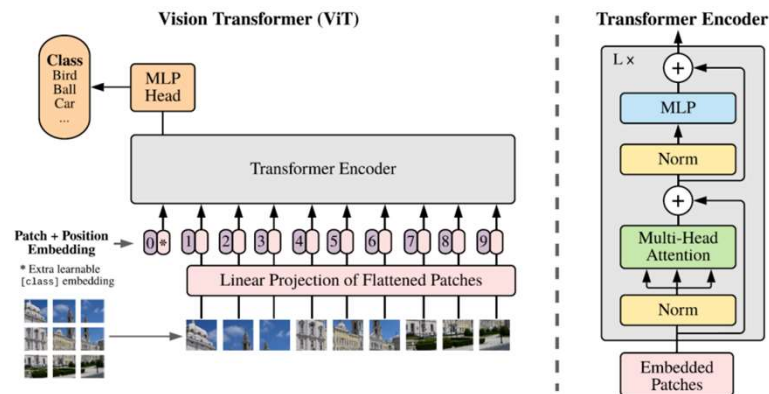
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Image Classification



- **Vision Transformer ('21) [ViT]**

- Decompose an image to $N \times N$ patches and then apply transformer encoder



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Questions?

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