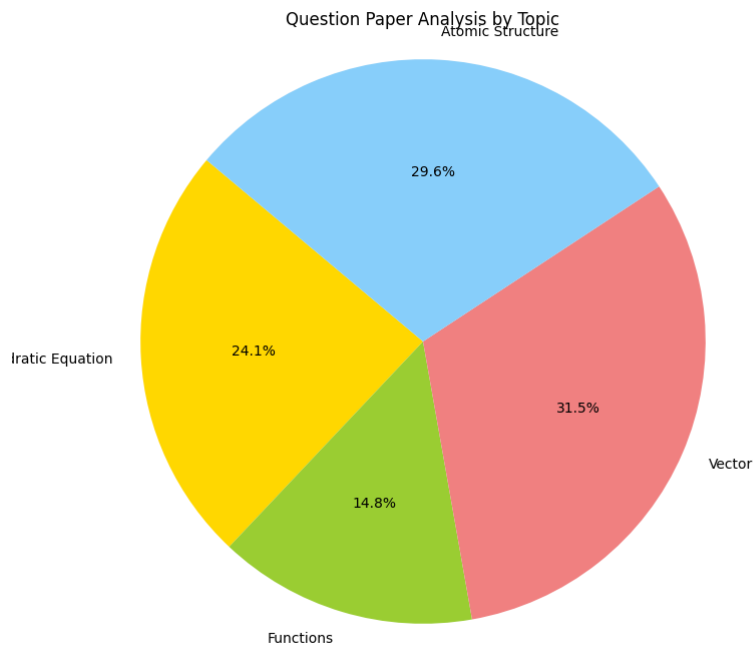
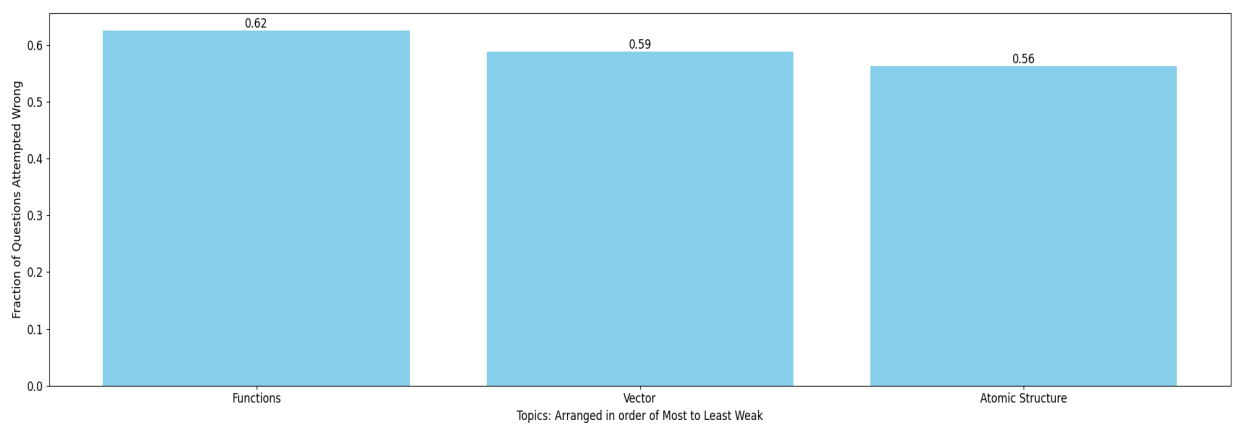


# Ayush dhar dubey Total MLAssist - Personalised DPP

## Question Paper Analysis:



## Weak Topic Analysis:



## Practice Questions:

### Functions:

13. Compute the inverse of the functions:

(a)  $f(x) = \ln(x + \sqrt{x^2 + 1})$

(b)  $f(x) = 2^{\frac{x}{x-1}}$

(c)  $y = \frac{10^x - 10^{-x}}{10^x + 10^{-x}}$

1. If  $f(x) = 4x^3 - x^2 - 2x + 1$  and  $g(x) = \begin{cases} \min\{1(x), 0 \leq x \leq 1\} & , 0 \leq x \leq 1 \\ 3 - x & ; 1 < x \leq 2 \end{cases}$  then find the value of  $\lambda$  if  $2\lambda = g(1/4) + g(3/4) + g(5/4)$

8. Let 'f' be a function defined in  $[-2, 3]$  given as  $f(x) = \begin{cases} -(x-1), & 0 \leq x < 1 \\ 2(x-1)^2, & 1 \leq x < 2 \\ -x^2 + 4x - 3, & 2 \leq x \leq 3 \end{cases}$

#### List-I

- (P) The number of integers in the range of  $f(x)$  is  
 (Q) The number of integral values of  $x$  which are in the domain of  $f(1 - |x|)$ , is  
 (R) The number of integers in the range of  $|f(-|x|)|$ , is  
 (S) The number of integral values of  $k$  for which the equation  $f(|x|) = k$  has exactly four distinct solutions is

#### List-II

- (1) 2  
 (2) 4  
 (3) 6  
 (4) 7

Code :

- |                        |                        |
|------------------------|------------------------|
| (A) P-3, Q-3, R-2, S-1 | (B) P-4, Q-4, R-2, S-1 |
| (C) P-3, Q-4, R-2, S-1 | (D) P-3, Q-4, R-2, S-2 |

14. The period of the function

$$f(x) = \left( \sec^2 \left( \frac{\pi x}{10} \right) - \tan^2 \left( \frac{\pi x}{10} \right) \right)^{\cos^4 4\pi x + 100\{x\}}$$

(where  $\{.\}$  denotes fractional part function) is  $\lambda$ , then  $(\lambda/2)$  is equal to

36. For  $p, q \in \mathbb{R}$ , consider the real valued function  $f(x) = (x - p)^2 - q$ ,  $x \in \mathbb{R}$  and  $q > 0$ . Let  $a_1, a_2, a_3$  and  $a_4$  be in an arithmetic progression with mean  $p$  and positive common difference. If  $|f(a_i)| = 500$  for all  $i = 1, 2, 3, 4$ , then the absolute difference between the roots of  $f(x) = 0$  is: **[JEE - Main 2022]**

### Vector:

23. Let  $\vec{a}, \vec{b}, \vec{c}$  be vectors of length 3, 4, 5 respectively. Let  $\vec{a}$  be perpendicular to  $\vec{b} + \vec{c}$ ,  $\vec{b}$  to  $\vec{c} + \vec{a}$  and  $\vec{c}$  to  $\vec{a} + \vec{b}$ . Then  $|\vec{a} + \vec{b} + \vec{c}|$  is :

(A)  $2\sqrt{5}$  (B)  $2\sqrt{2}$  (C)  $10\sqrt{5}$  (D)  $5\sqrt{2}$

58. If  $A(-4, 0, 3)$ ;  $B(14, 2, -5)$  then which one of the following points lie on the bisector of the angle between  $\vec{OA}$  and  $\vec{OB}$  ( $O$  is the origin of reference)
- (A)  $(2, 1, -1)$  (B)  $(2, 11, 5)$  (C)  $(10, 2, -2)$  (D)  $(1, 1, 2)$

6. (a) Two adjacent sides of a parallelogram ABCD are given by  $\vec{AB} = 2\hat{i} + 10\hat{j} + 11\hat{k}$  and  $\vec{AD} = -\hat{i} + 2\hat{j} + 2\hat{k}$ . The side AD is rotated by an acute angle  $\alpha$  in the plane of the parallelogram so that AD becomes AD'. If AD' makes a right angle with the side AB then the cosine of the angle  $\alpha$  is given by –

(A)  $\frac{8}{9}$  (B)  $\frac{\sqrt{17}}{9}$  (C)  $\frac{1}{9}$  (D)  $\frac{4\sqrt{5}}{9}$

- (b) If  $\vec{a}$  and  $\vec{b}$  are vectors in space given by  $\vec{a} = \frac{\hat{i} - 2\hat{j}}{\sqrt{5}}$  and  $\vec{b} = \frac{2\hat{i} + \hat{j} + 3\hat{k}}{\sqrt{14}}$ , then the value of

$$(2\vec{a} + \vec{b}) \cdot [(\vec{a} \times \vec{b}) \times (\vec{a} - 2\vec{b})]$$

**[JEE 2010, 5 + 3]**

26. A, B, C & D are four points in a plane with pv's  $\vec{a}, \vec{b}, \vec{c}$  &  $\vec{d}$  respectively such that  $(\vec{a} - \vec{d}) \cdot (\vec{b} - \vec{c}) = (\vec{b} - \vec{d}) \cdot (\vec{c} - \vec{a}) = 0$ . Then for the triangle ABC, D is its  
 (A) incentre (B) circumcentre (C) orthocentre (D) centroid
40. Let the volume of a parallelepiped whose coterminal edges are given by  $\vec{u} = \hat{i} + \hat{j} + \lambda \hat{k}$ ,  $\vec{v} = \hat{i} + \hat{j} + 3\hat{k}$  and  $\vec{w} = 2\hat{i} + \hat{j} + \hat{k}$  be 1 cu. unit. If  $\theta$  be the angle between the edge  $\vec{u}$  and  $\vec{w}$ , then  $\cos\theta$  can be : [JEE (Main)-2020]
- (1)  $\frac{7}{6\sqrt{6}}$  (2)  $\frac{5}{3\sqrt{3}}$  (3)  $\frac{7}{6\sqrt{3}}$  (4)  $\frac{5}{7}$

### Atomic Structure:

8. Which of the following sets of quantum number is correct for an electron in 4f orbital ? [AIEEE-2004]
- (1)  $n = 3, l = 2, m = -2, s = +\frac{1}{2}$  (2)  $n = 4, l = 4, m = -4, s = -\frac{1}{2}$   
 (3)  $n = 4, l = 3, m = +1, s = +\frac{1}{2}$  (4)  $n = 4, l = 3, m = +4, s = +\frac{1}{2}$
- 
17. Statement-1: Energy emitted when an electron jump from  $5 \rightarrow 2$  (energy level) is less than when an electron jump from  $2 \rightarrow 1$  in all 'H' like atom.  
 Statement-2: The [total energy difference] between 1<sup>st</sup> & 2<sup>nd</sup> energy level is greater than that of any two energy level provided level '1' is not part of those two energy levels.  
 (A) Statement-1 is true, statement-2 is true and statement-2 is correct explanation for statement-1.  
 (B) Statement-1 is true, statement-2 is true and statement-2 is NOT the correct explanation for statement-1.  
 (C) Statement-1 is true, statement-2 is false.  
 (D) Statement-1 is false, statement-2 is true.

36. The ground state energy of hydrogen atom is  $-13.6$  eV. The energy of second excited state  $\text{He}^+$  ion in eV is : [JEE Main (Jan.) 2019]

(1)  $-54.4$                       (2)  $-6.04$                       (3)  $-3.4$                       (4)  $-27.2$

21. In an atom, two electrons move round the nucleus in circular orbits of radii  $R$  and  $4R$ . The ratio of the time taken by them to complete one revolution is: (Consider Bohr model to be valid)

(A)  $1 : 4$                       (B)  $4 : 1$                       (C)  $1 : 8$                       (D)  $8 : 1$

11. Select the correct curve(s):

If  $v$  = velocity of electron in Bohr's orbit

$r$  = Radius of electron in Bohr's orbit

P.E. = Potential energy of electron in Bohr's orbit

K.E. = Kinetic energy of electron in Bohr's orbit

