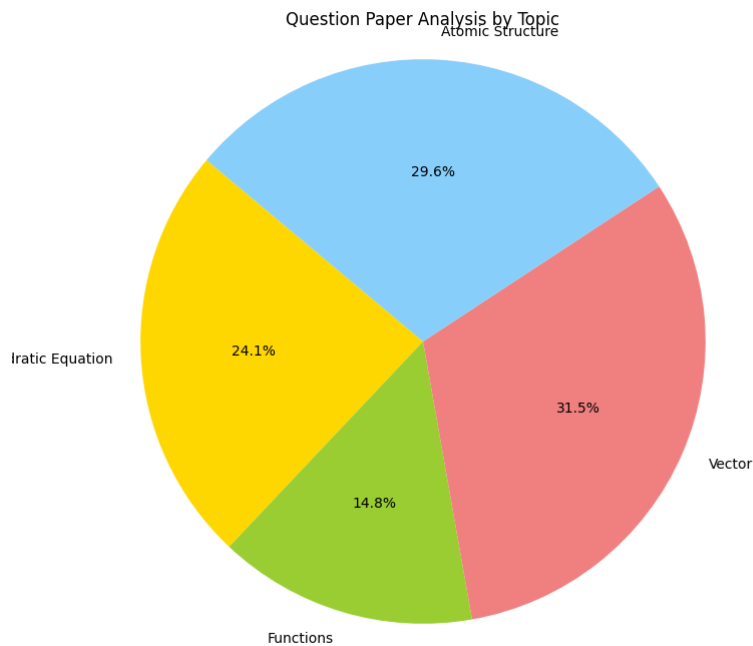
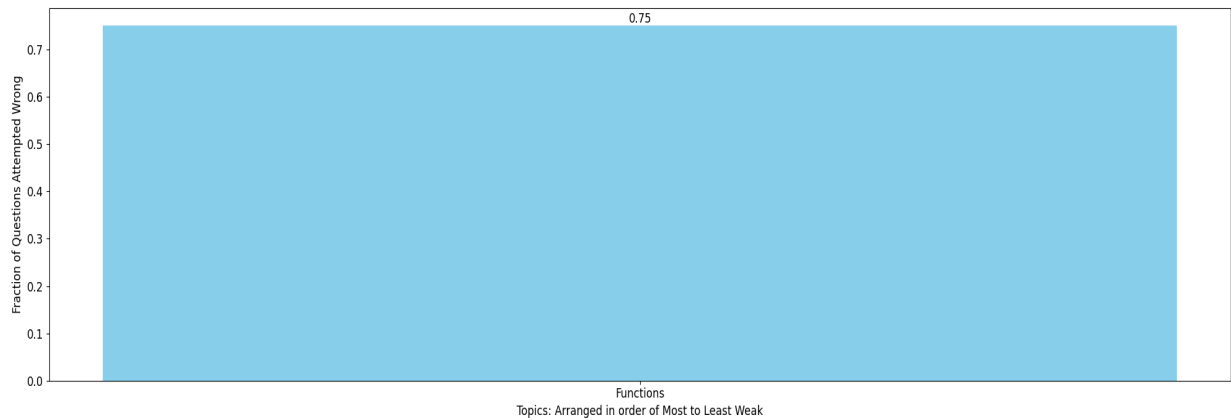


Mahika Total  
MLAssist - Personalised DPP

Question Paper Analysis:



Weak Topic Analysis:



## Practice Questions:

### Functions:

29. Let  $A = \{1, 2, 3, \dots, 10\}$  and  $f: A \rightarrow A$  be defined as  $f(k) = \begin{cases} k+1 & \text{if } k \text{ is odd} \\ k & \text{if } k \text{ is even} \end{cases}$ . Then the number of possible function  $g: A \rightarrow A$  such that  $g \circ f = f$  is [JEE - Main 2021]  
 (A) 105 (2)  $^{10}C_5$  (3) 55 (4)  $5!$

7. Let  $f(x) = \sin\left(\frac{\pi}{6} \sin\left(\frac{\pi}{2} \sin x\right)\right)$  for all  $x \in \mathbb{R}$  and  $g(x) = \frac{\pi}{2} \sin x$  for all  $x \in \mathbb{R}$ . Let  $(f \circ g)(x)$  denote  $f(g(x))$  and  $(g \circ f)(x)$  denote  $g(f(x))$ . Then which of the following is (are) true? [JEE Ad. 2015]

- (A) Range of  $f$  is  $\left[-\frac{1}{2}, \frac{1}{2}\right]$  (B) Range of  $f \circ g$  is  $\left[-\frac{1}{2}, \frac{1}{2}\right]$   
 (C)  $\lim_{x \rightarrow 0} \frac{f(x)}{g(x)} = \frac{\pi}{6}$  (D) There is an  $x \in \mathbb{R}$  such that  $(g \circ f)(x) = 1$

3. If  $f(x)$  is defined on  $(0, 1)$ , then the domain of definition of  $f(e^x) + f(\ln|x|)$  is  
 (A)  $(-e, -1)$  (B)  $(-e, -1) \cup (1, e)$   
 (C)  $(-\infty, -1) \cup (1, \infty)$  (D)  $(-e, e)$

14. If  $f(x) = \left(\frac{1-x}{1+x}\right)$ ,  $|x| < 1$ , then  $f\left(\frac{2x}{1+x^2}\right)$  is equal to [JEE - Main 2019]  
 (A)  $2f(x)$  (B)  $2f(x^2)$  (C)  $(f(x))^2$  (D)  $-2f(x)$

7. The function  $f: \mathbb{R} \rightarrow \left[-\frac{1}{2}, \frac{1}{2}\right]$  defined as  $f(x) = \frac{x}{1+x^2}$ , is : [JEE - Main 2017]  
 (A) neither injective nor surjective. (B) invertible  
 (C) injective but not surjective (D) surjective but not injective.