

Convolutional Neural Networks for Computer Vision Tasks

Kate Saenko

March 24, 2020

Today

Convolutional Neural Networks (CNNs) for vision

- Example network architecture for image classification
- CNNs for semantic segmentation, object detection (using slides from [Stanford's cs231n](#), spring 2019, Lecture 12, [video](#))

Today: Applications of CNNs to Computer Vision

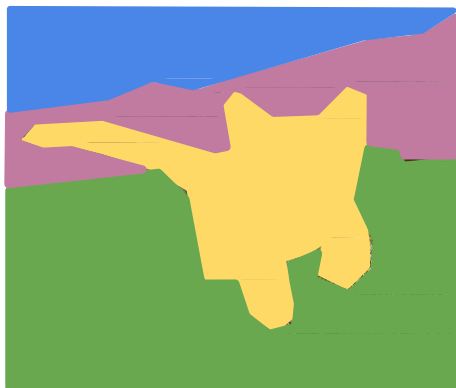
Classification



CAT

No spatial extent

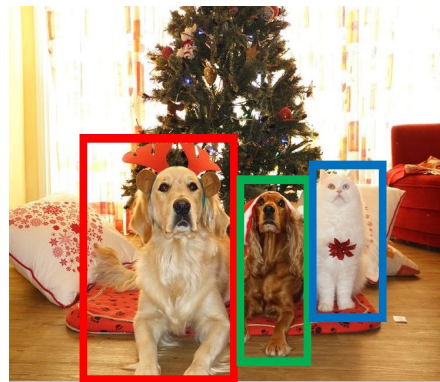
Semantic Segmentation



GRASS, CAT, TREE, SKY

No objects, just pixels

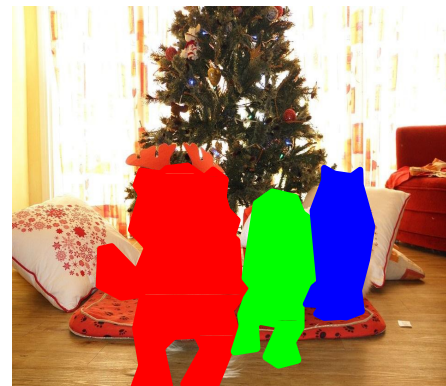
Object Detection



DOG, DOG, CAT

Multiple Object

Instance Segmentation



DOG, DOG, CAT

[This image.js](#) CC0 public domain

Last time: CNN for classification

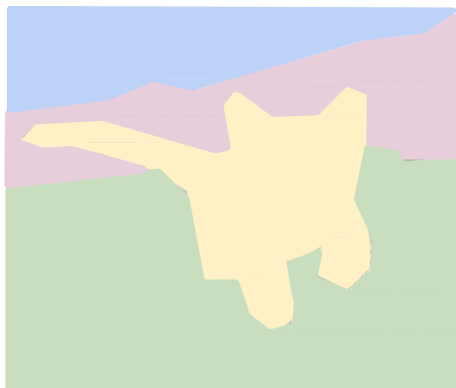
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No spatial extent

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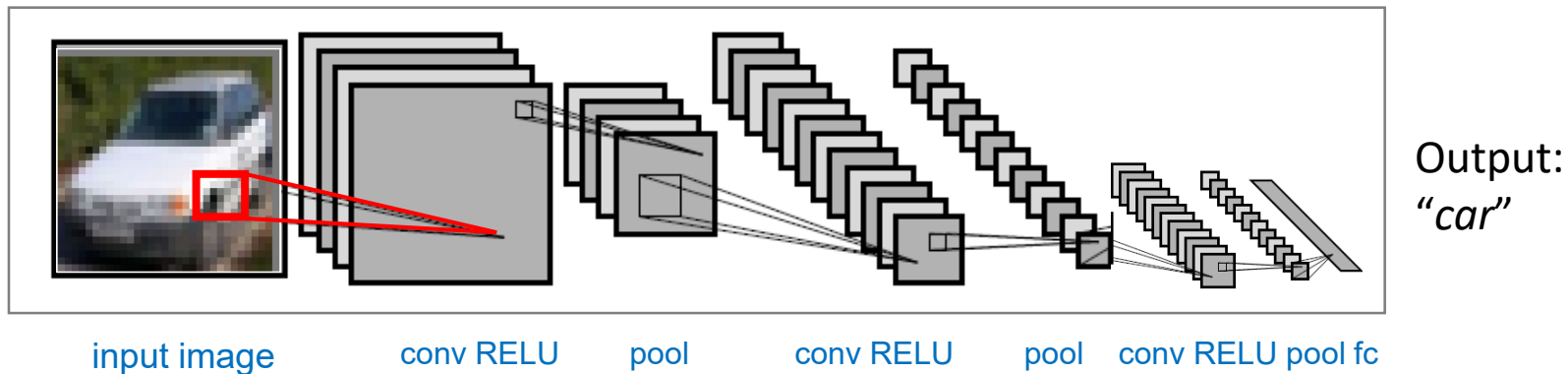
Instance Segmentation



DOG, DOG, CAT

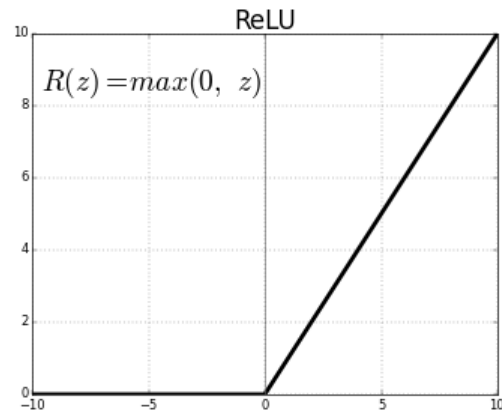
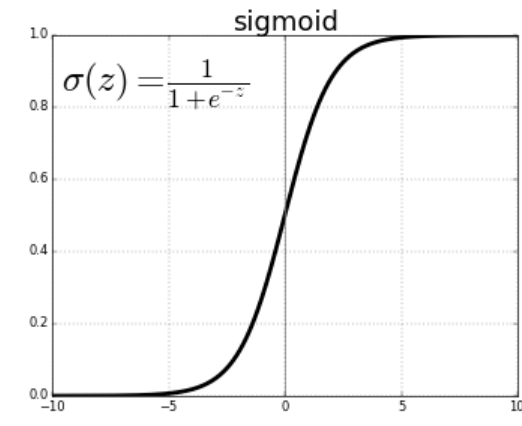
[This image.js](#) CC0 public domain

Example: CNN architecture for classification

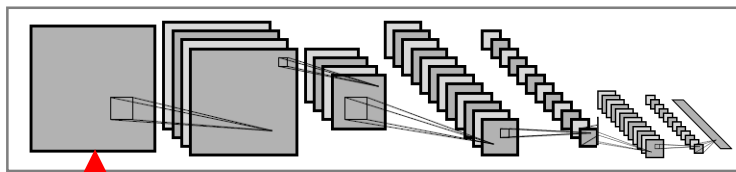


CIFAR-10 Demo ConvJS Network

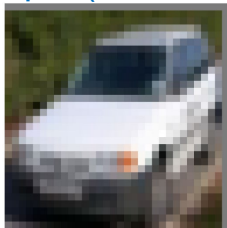
Nonlinear activation functions



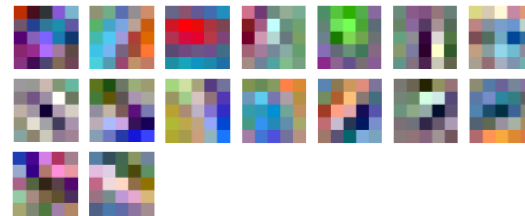
ReLU function $g(x) = \max(0, x)$

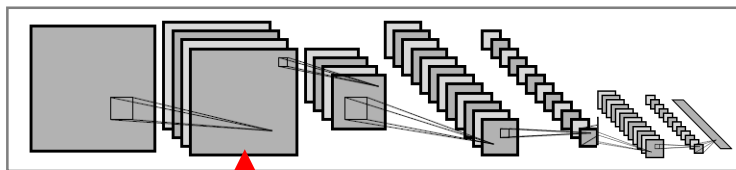


input (32x32x3)

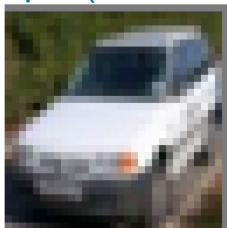


filter size 5x5x3, stride 1

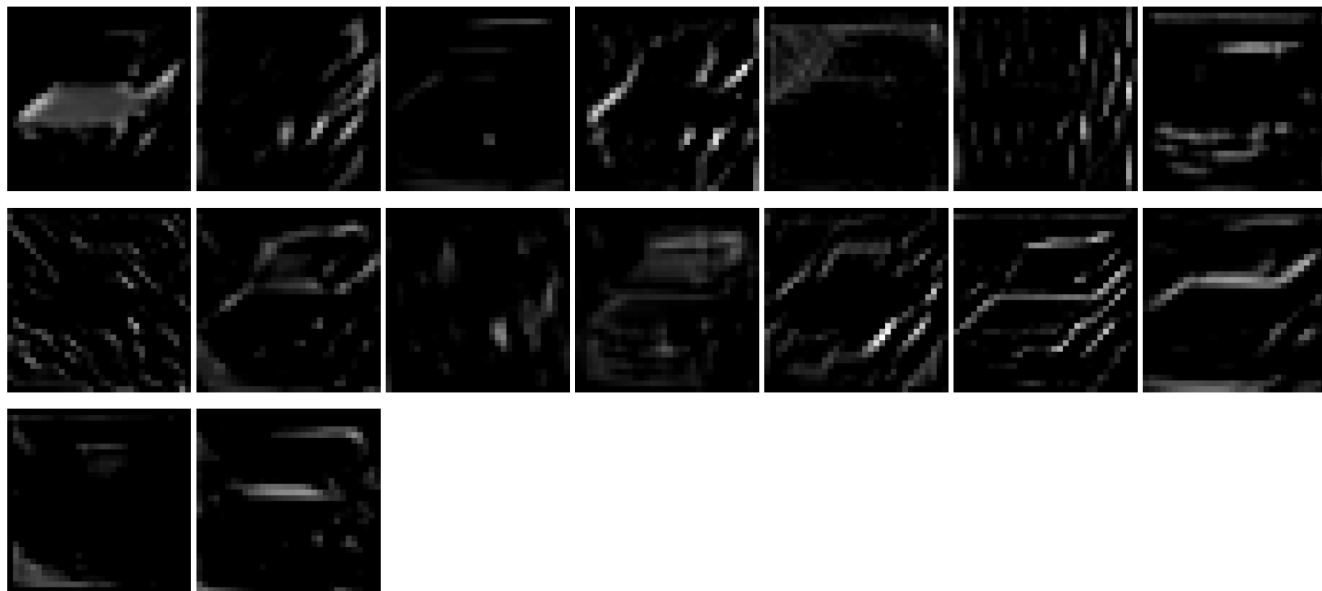




input (32x32x3)



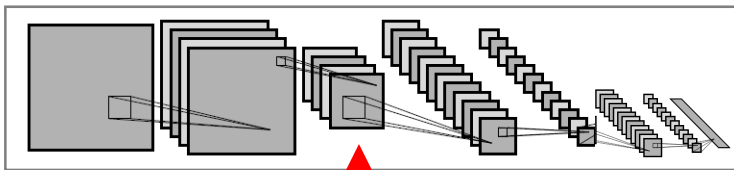
RELU



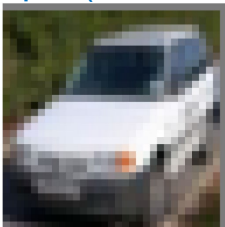
conv (32x32x16) params: $16 \times 5 \times 5 \times 3 + 16 = 1216$

filter size 5x5x3, stride 1





input (32x32x3)

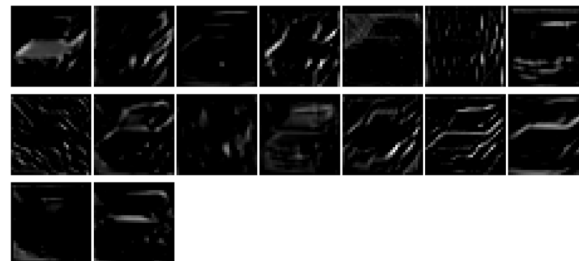


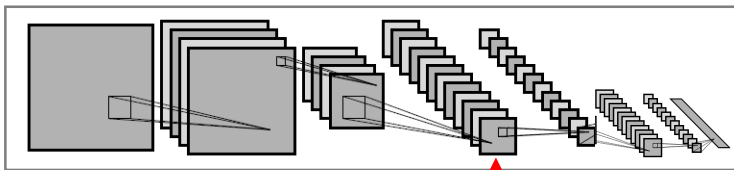
pool (16x16x16)
pooling size 2x2, stride 2

filter size 5x5x3, stride 1

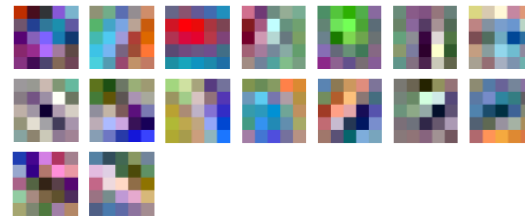


conv (32x32x16) params: $16 \times 5 \times 5 \times 3 + 16 = 1216$

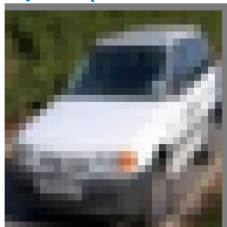




filter size $5 \times 5 \times 3$, stride 1

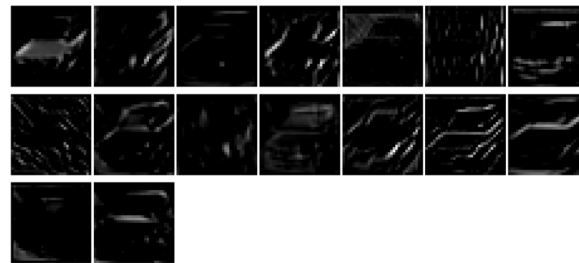


input ($32 \times 32 \times 3$)

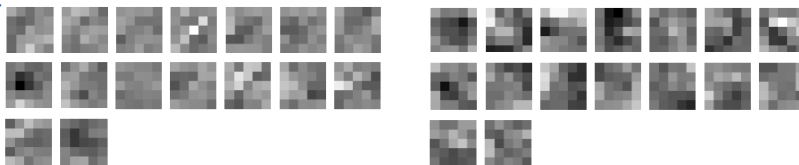


pool ($16 \times 16 \times 16$)
pooling size 2×2 , stride 2

conv ($32 \times 32 \times 16$) params: $16 \times 5 \times 5 \times 3 + 16 = 1216$



filter size $5 \times 5 \times 16$, stride 1



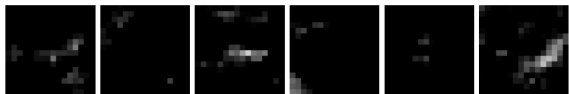
...

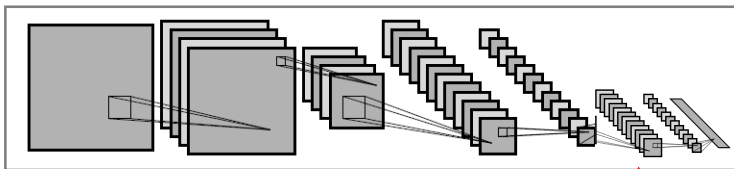
RELU

conv ($16 \times 16 \times 20$) params: $20 \times 5 \times 5 \times 16 + 20 = 8020$

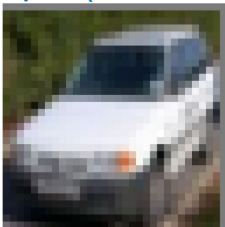


pool ($8 \times 8 \times 20$)
pooling size 2×2 , stride 2





input (32x32x3)



One more conv+RELU+pool:

conv (8x8x20)

filter size 5x5x20, stride 1

relu (8x8x20)

pool (4x4x20)

pooling size 2x2, stride 2

parameters: $20 \times 5 \times 5 \times 20 + 20 = 10020$

fc (1x1x10); parameters: $10 \times 320 + 10 = 3210$



softmax (1x1x10)



dog

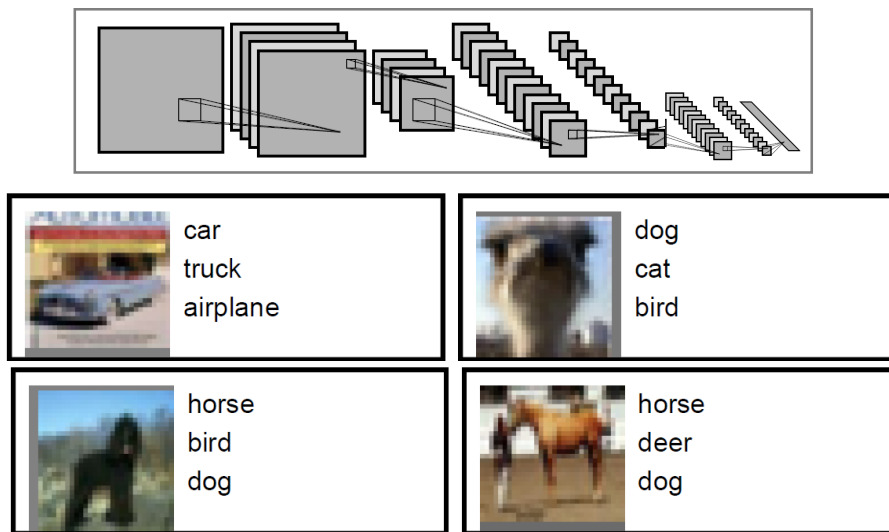
car

cat

⋮

Testing the network

- Show top three most likely classes



<http://cs.stanford.edu/people/karpathy/convnetjs/demo/cifar10.html>

Today: Segmentation, Detection

Computer Vision Tasks

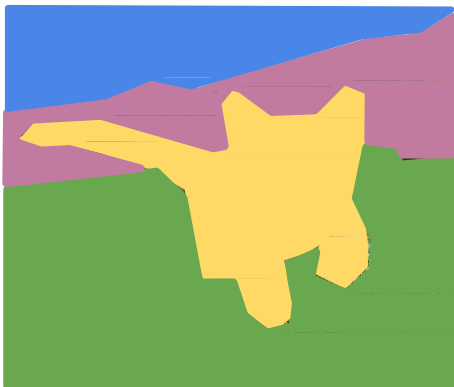
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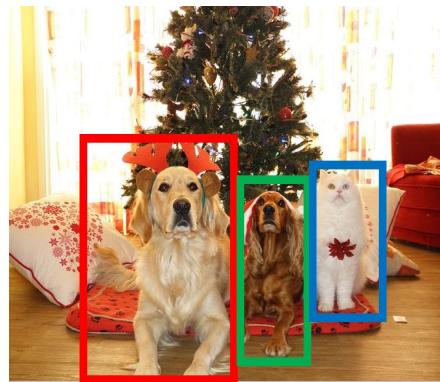
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Multiple Object

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[This image.js](#) CC0 public domain

Semantic Segmentation

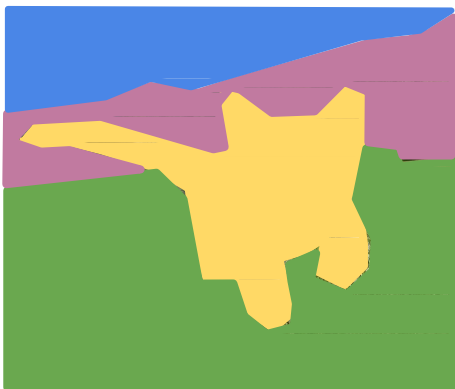
Classification



CAT

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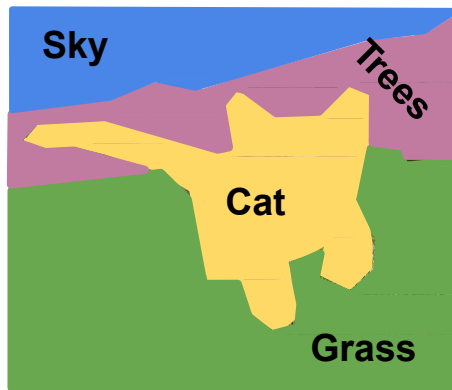


DOG, DOG, CAT

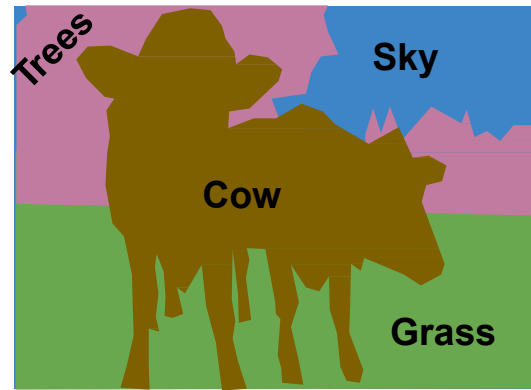
Semantic Segmentation

Label each pixel in the image with a category label

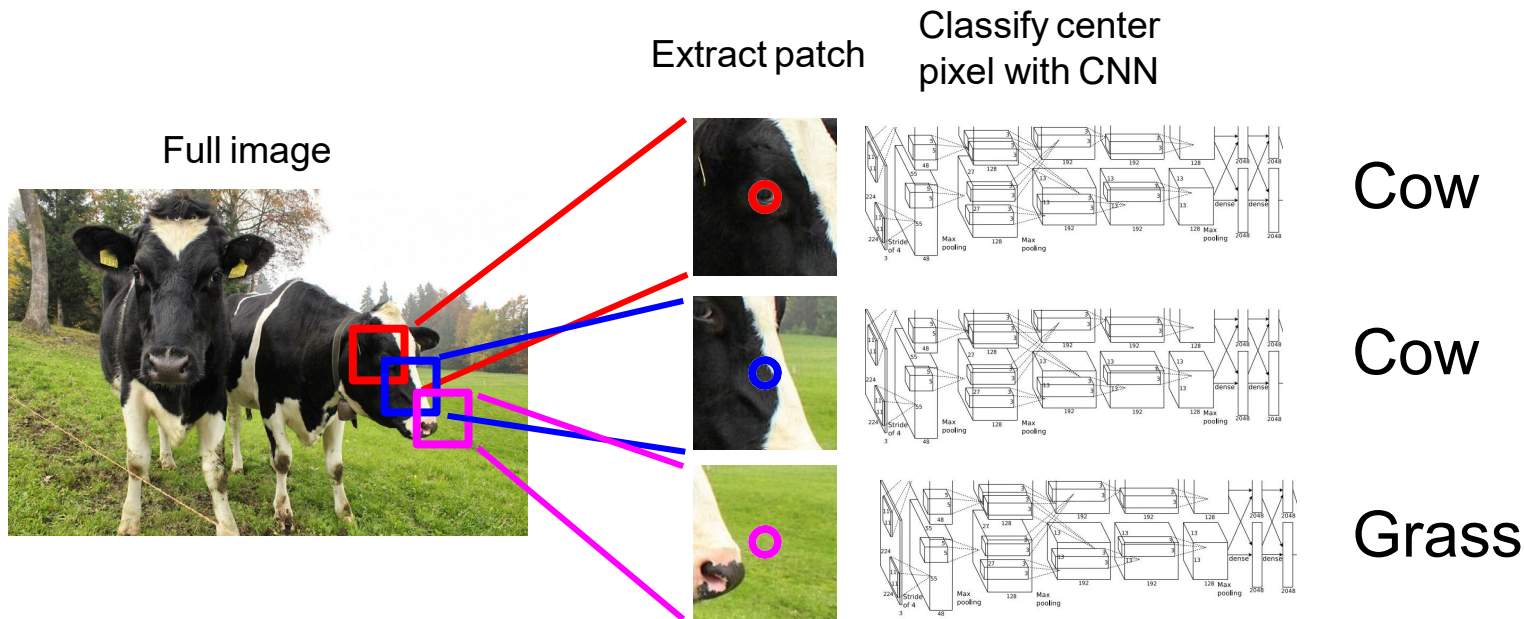
Don't differentiate instances, only care about pixels



[This image is CC0 public domain](#)



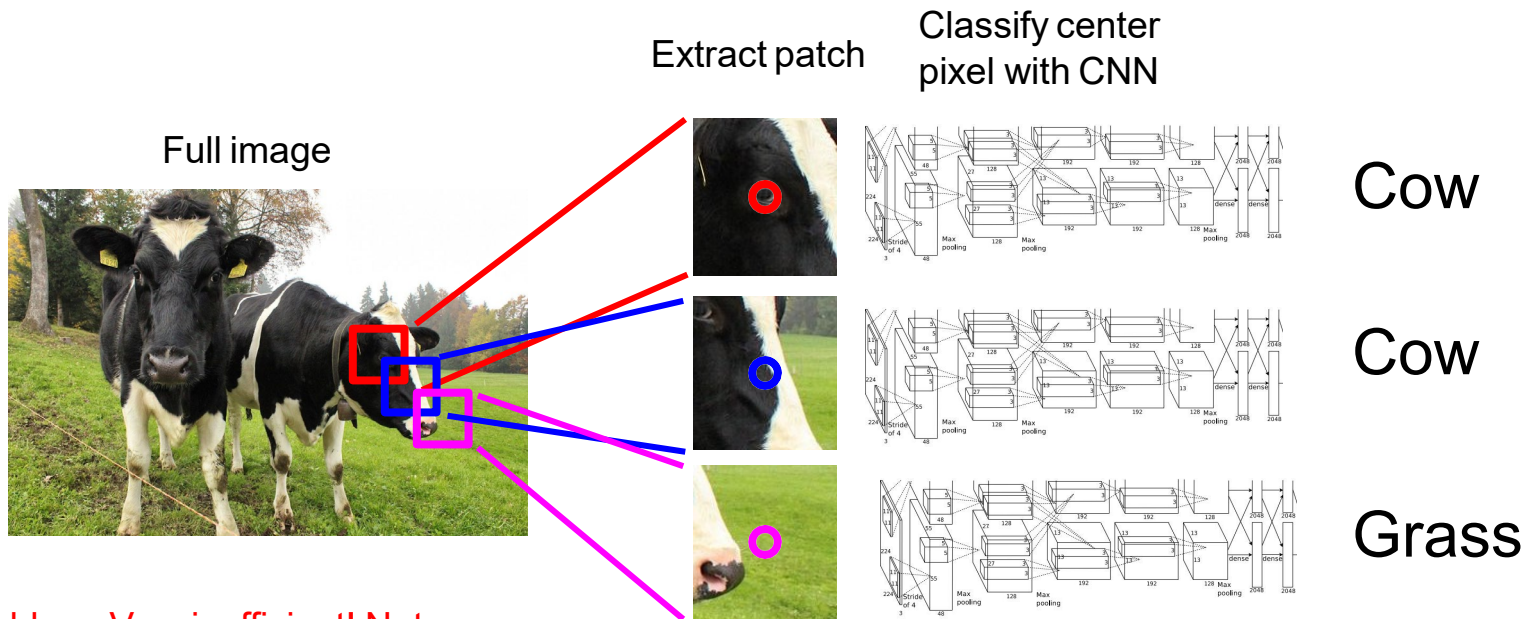
Semantic Segmentation Idea: Sliding Window



Farabet et al, "Learning Hierarchical Features for Scene Labeling," TPAMI 2013

Pinheiro and Collobert, "Recurrent Convolutional Neural Networks for Scene Labeling", ICML 2014

Semantic Segmentation Idea: Sliding Window

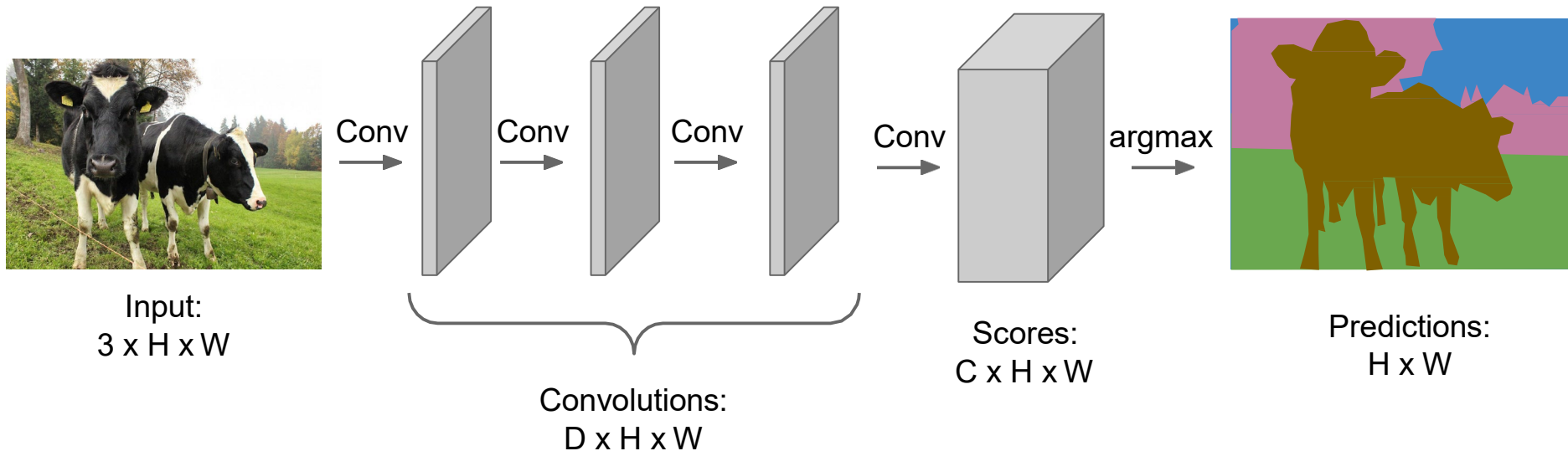


Problem: Very inefficient! Not reusing shared features between overlapping patches

Farabet et al, "Learning Hierarchical Features for Scene Labeling," TPAMI 2013
Pinheiro and Collobert, "Recurrent Convolutional Neural Networks for Scene Labeling", ICML 2014

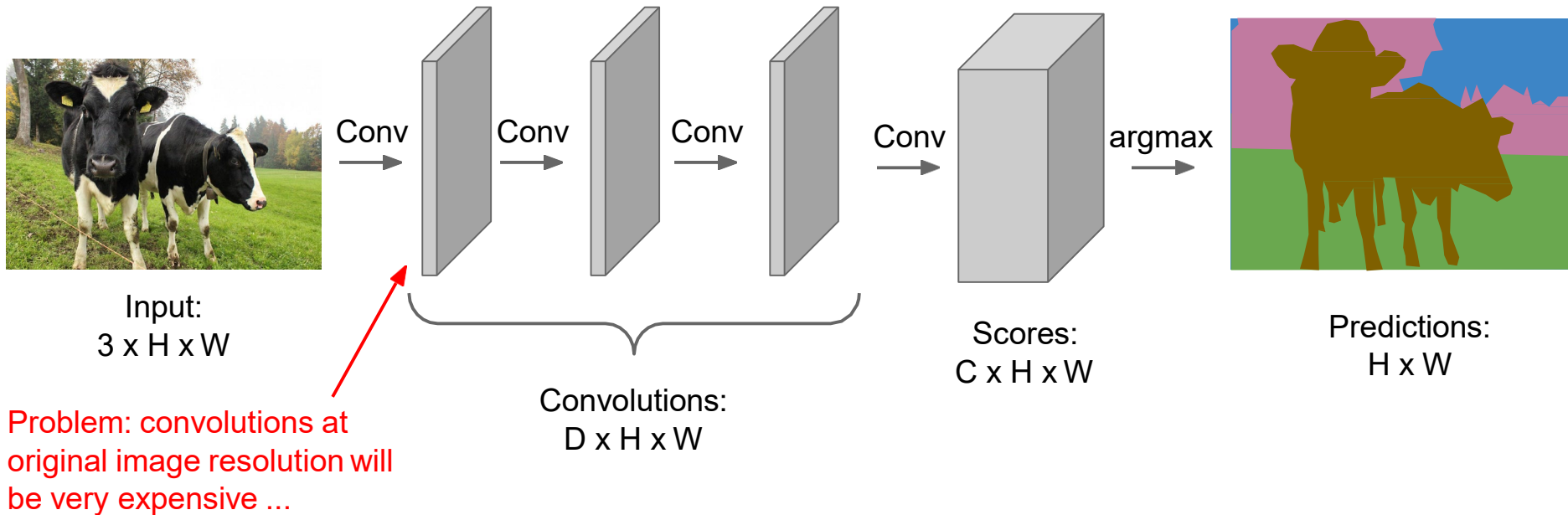
Semantic Segmentation Idea: Fully Convolutional

Design a network as a bunch of convolutional layers to make predictions for pixels all at once!



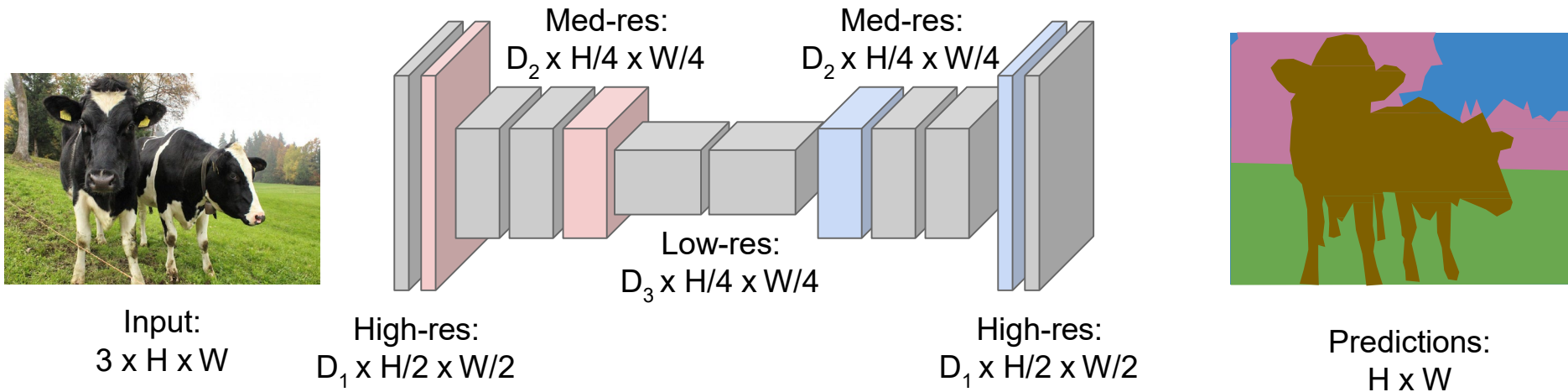
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Design a network as a bunch of convolutional layers to make predictions for pixels all at once!



Semantic Segmentation Idea: Fully Convolutional

Design network as a bunch of convolutional layers, with **downsampling** and **upsampling** inside the network!



Long, Shelhamer, and Darrell, "Fully Convolutional Networks for Semantic Segmentation", CVPR 2015
Noh et al, "Learning Deconvolution Network for Semantic Segmentation", ICCV 2015

Semantic Segmentation Idea: Fully Convolutional

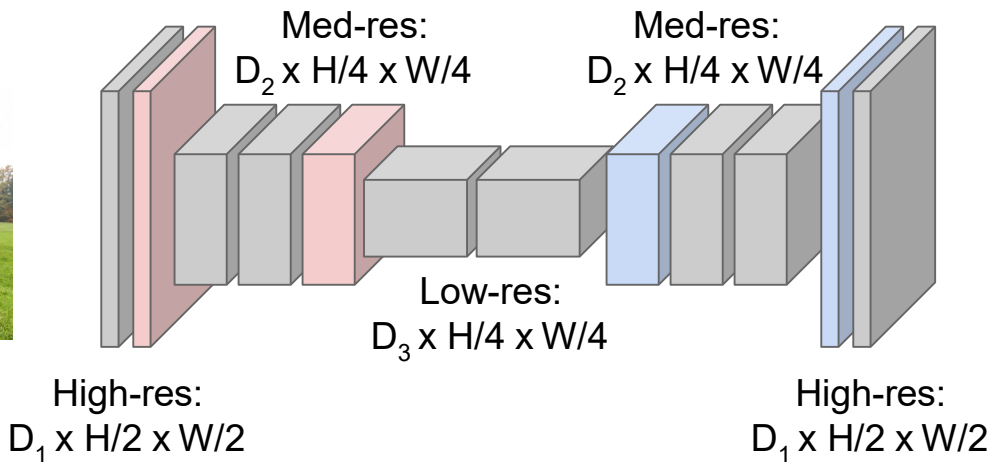
Downsampling:
Pooling, strided
convolution

Design network as a bunch of convolutional layers, with **downsampling** and **upsampling** inside the network!

Upsampling:
???



Input:
 $3 \times H \times W$



Predictions:
 $H \times W$

Long, Shelhamer, and Darrell, "Fully Convolutional Networks for Semantic Segmentation", CVPR 2015
Noh et al, "Learning Deconvolution Network for Semantic Segmentation", ICCV 2015

In-Network upsampling: “Unpooling”

Nearest Neighbor

1	2
3	4



1	1	2	2
1	1	2	2
3	3	4	4
3	3	4	4

Input: 2 x 2

Output: 4 x 4

“Bed of Nails”

1	2
3	4

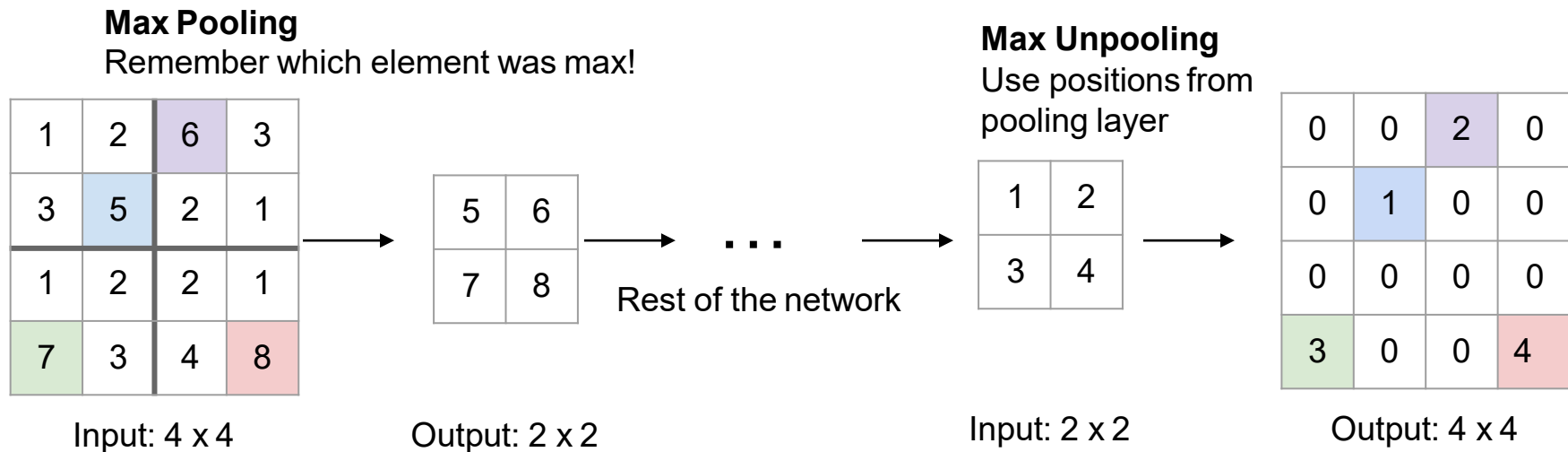


1	0	2	0
0	0	0	0
3	0	4	0
0	0	0	0

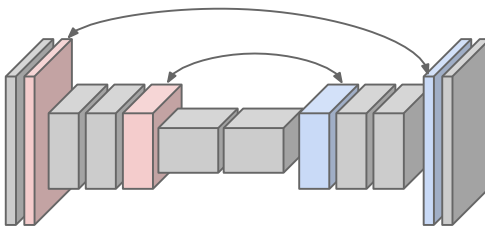
Input: 2 x 2

Output: 4 x 4

In-Network upsampling: “Max Unpooling”

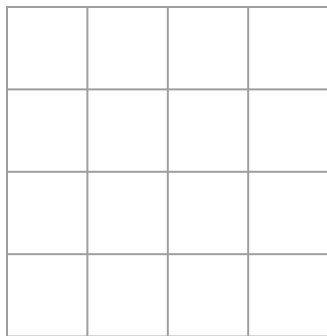


Corresponding pairs of
downsampling and
upsampling layers

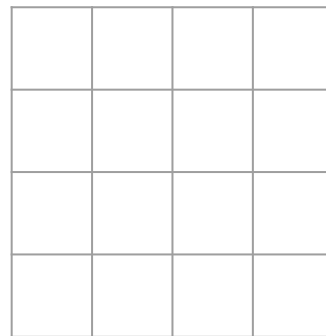


Learnable Upsampling: Transpose Convolution

Recall: Normal 3 x 3 convolution, stride 1 pad 1



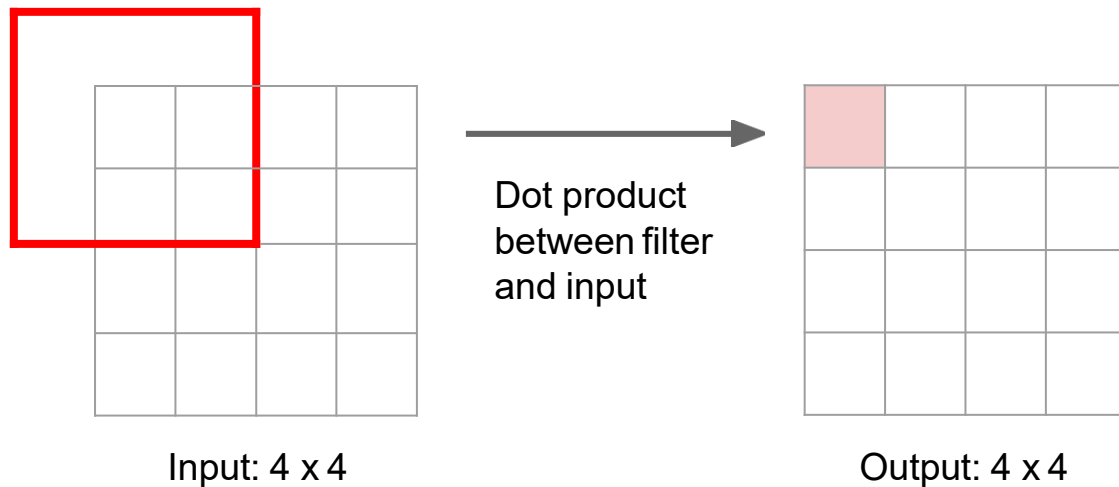
Input: 4 x 4



Output: 4 x 4

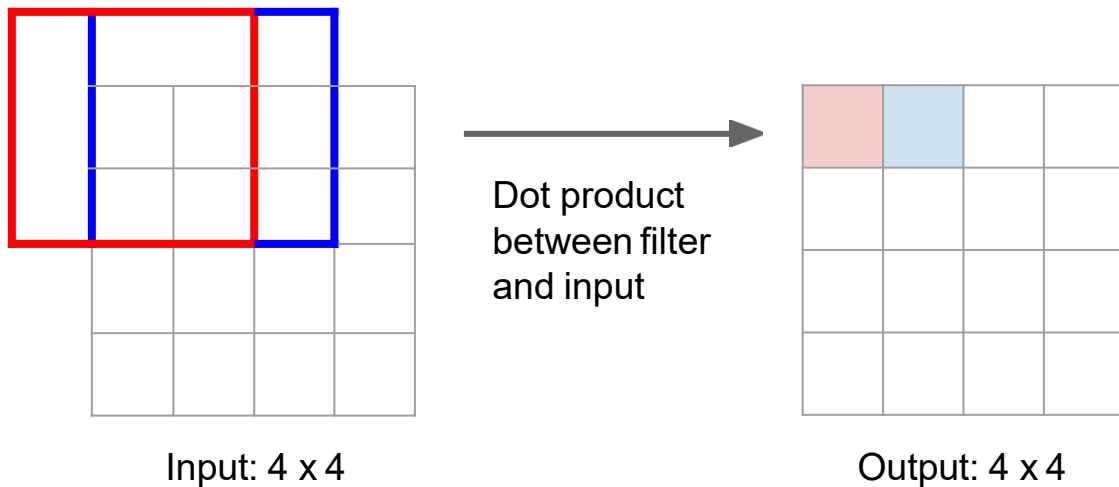
Learnable Upsampling: Transpose Convolution

Recall: Normal 3 x 3 convolution, stride 1 pad 1



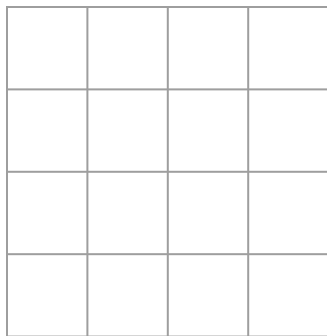
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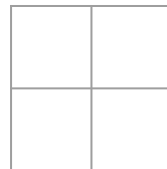


Learnable Upsampling: Transpose Convolution

Recall: Normal 3 x 3 convolution, stride 2 pad 1



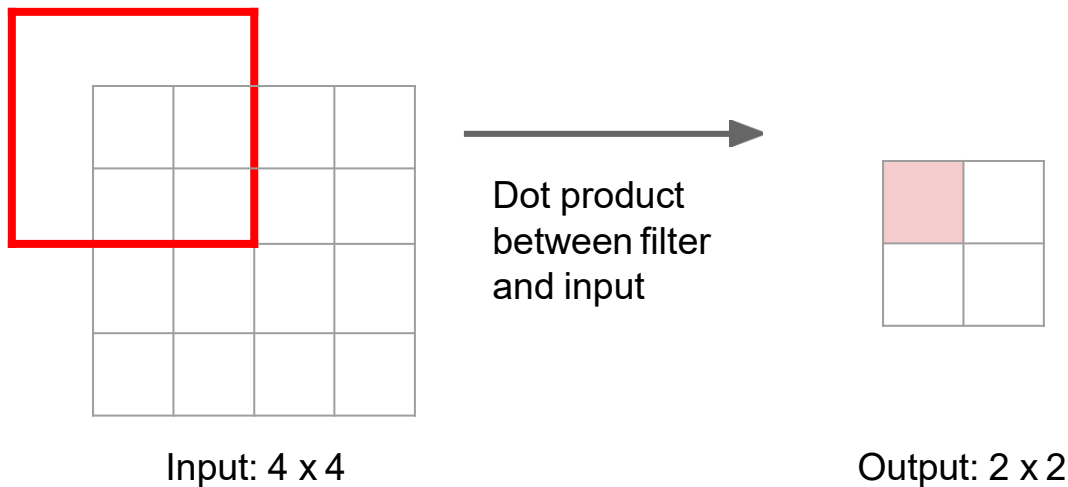
Input: 4 x 4



Output: 2 x 2

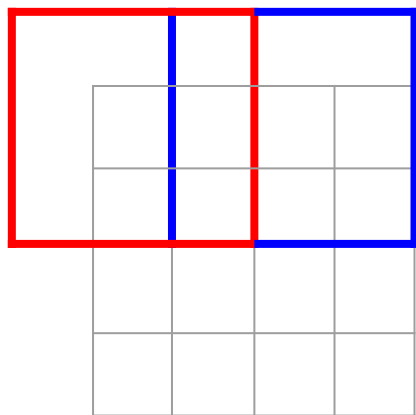
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Learnable Upsampling: Transpose Convolution

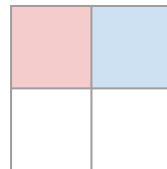
Recall: Normal 3 x 3 convolution, stride 2 pad 1



Input: 4 x 4



Dot product
between filter
and input



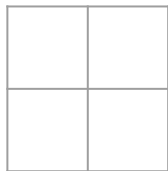
Output: 2 x 2

Filter moves 2 pixels in
the input for every one
pixel in the output

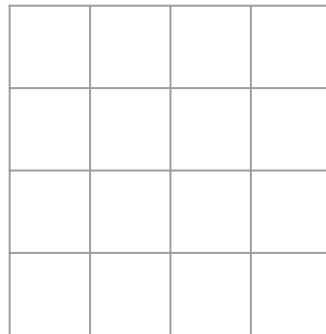
Stride gives ratio between
movement in input and
output

Learnable Upsampling: Transpose Convolution

3 x 3 **transpose** convolution, stride 2 pad 1



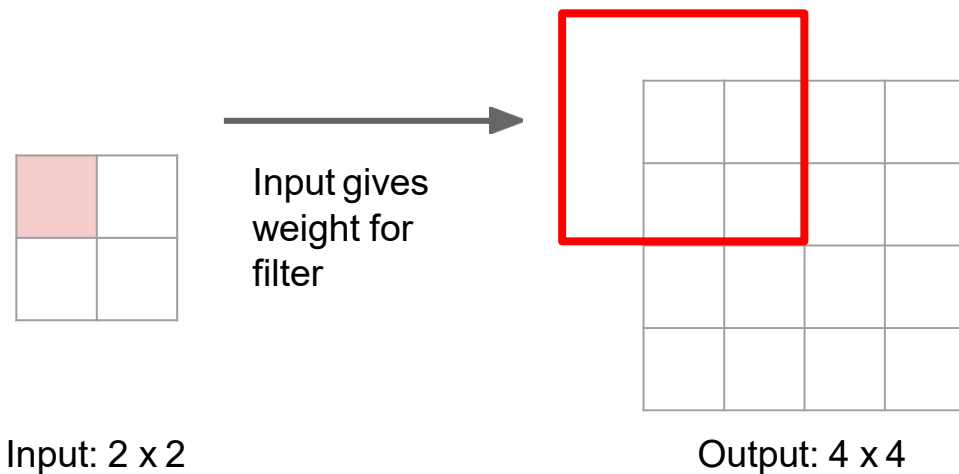
Input: 2 x 2



Output: 4 x 4

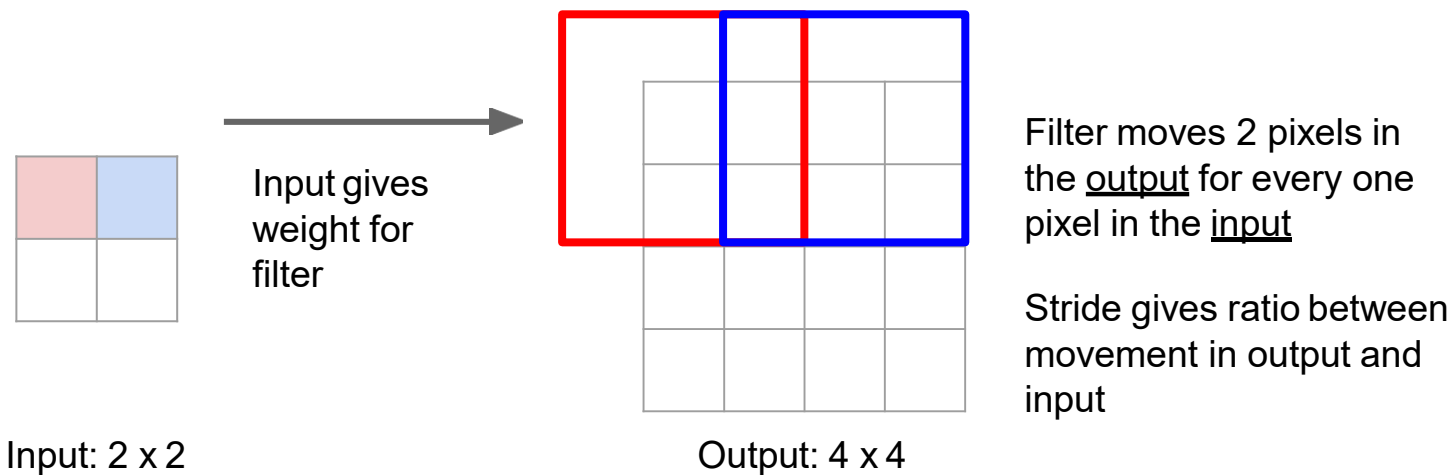
Learnable Upsampling: Transpose Convolution

3 x 3 **transpose** convolution, stride 2 pad 1

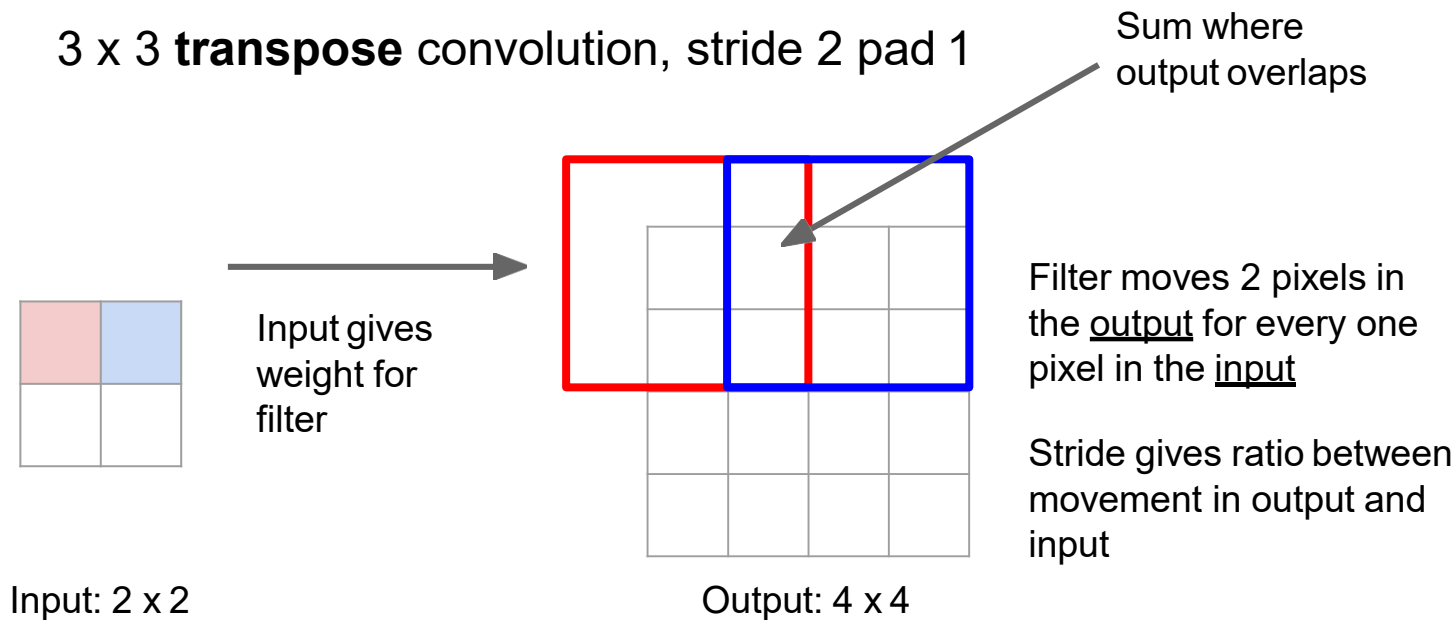


Learnable Upsampling: Transpose Convolution

3 x 3 **transpose** convolution, stride 2 pad 1



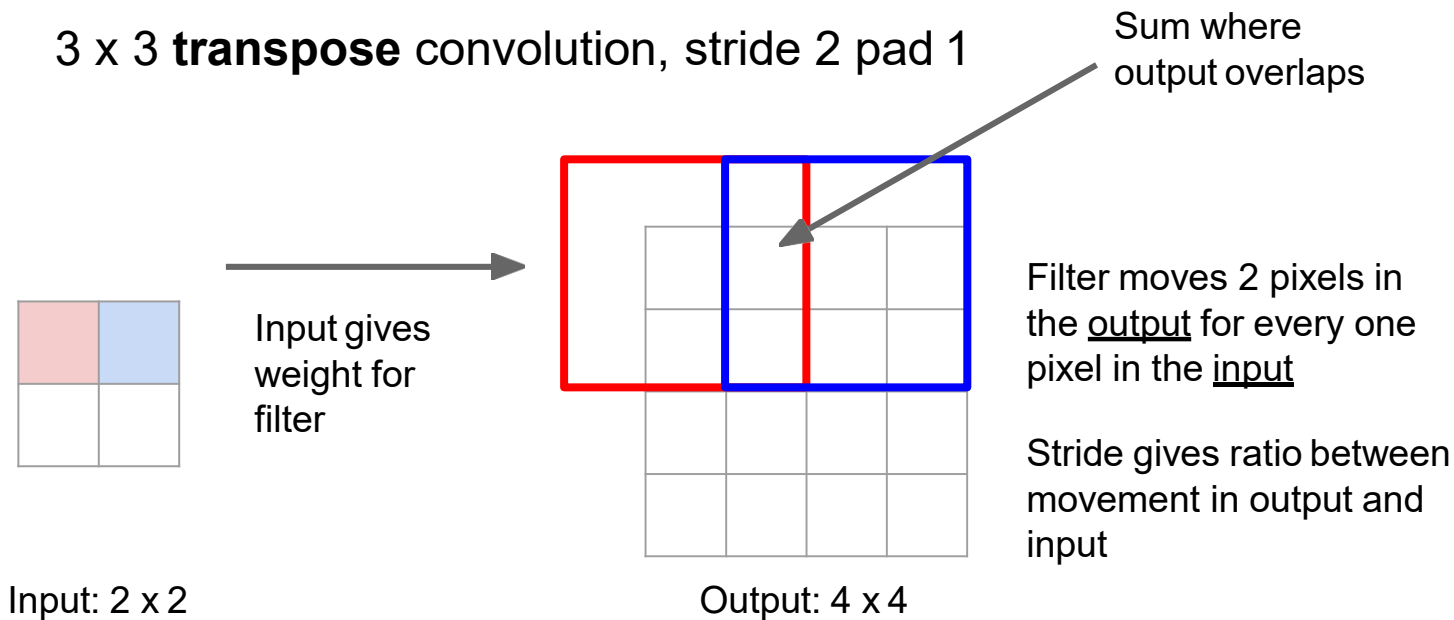
Learnable Upsampling: Transpose Convolution



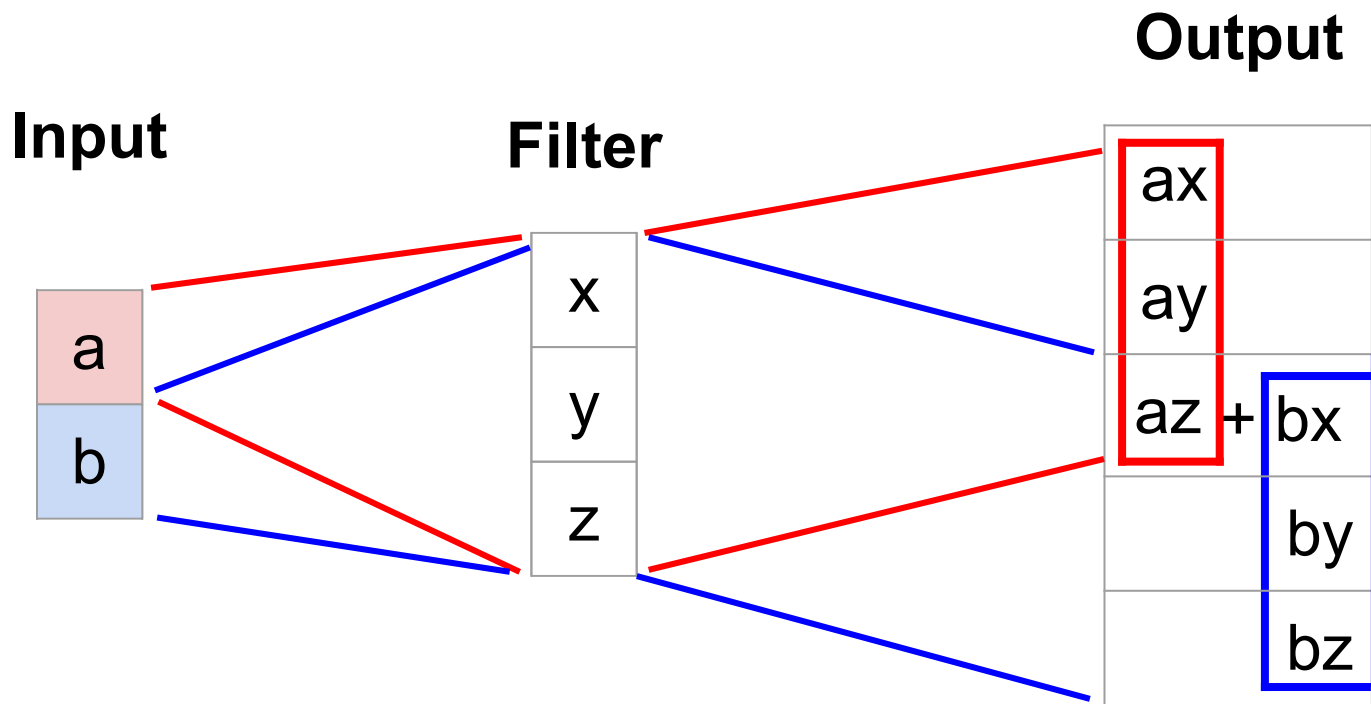
Learnable Upsampling: Transpose Convolution

Other names:

- Deconvolution (bad)
- Upconvolution
- Fractionally strided convolution
- Backward strided convolution



Learnable Upsampling: 1D Example



Output contains copies of the filter weighted by the input, summing at where it overlaps in the output

Need to crop one pixel from output to make output exactly 2x input

Convolution as Matrix Multiplication (1D Example)

We can express convolution in terms of a matrix multiplication

$$\vec{x} * \vec{a} = X\vec{a}$$

$$\begin{bmatrix} x & y & x & 0 & 0 & 0 \\ 0 & x & y & x & 0 & 0 \\ 0 & 0 & x & y & x & 0 \\ 0 & 0 & 0 & x & y & x \end{bmatrix} \begin{bmatrix} 0 \\ a \\ b \\ c \\ d \\ 0 \end{bmatrix} = \begin{bmatrix} ay + bz \\ ax + by + cz \\ bx + cy + dz \\ cx + dy \end{bmatrix}$$

Example: 1D conv, kernel
size=3, stride=1, padding=1

Convolution as Matrix Multiplication (1D Example)

We can express convolution in terms of a matrix multiplication

$$\vec{x} * \vec{a} = X \vec{a}$$

$$\begin{bmatrix} x & y & x & 0 & 0 & 0 \\ 0 & x & y & x & 0 & 0 \\ 0 & 0 & x & y & x & 0 \\ 0 & 0 & 0 & x & y & x \end{bmatrix} \begin{bmatrix} 0 \\ a \\ b \\ c \\ d \\ 0 \end{bmatrix} = \begin{bmatrix} ay + bz \\ ax + by + cz \\ bx + cy + dz \\ cx + dy \end{bmatrix}$$

Example: 1D conv, kernel
size=3, stride=1, padding=1

Convolution transpose multiplies by the transpose of the same matrix:

$$\vec{x} *^T \vec{a} = X^T \vec{a}$$

$$\begin{bmatrix} x & 0 & 0 & 0 \\ y & x & 0 & 0 \\ z & y & x & 0 \\ 0 & z & y & x \\ 0 & 0 & z & y \\ 0 & 0 & 0 & z \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = \begin{bmatrix} ax \\ ay + bx \\ az + by + cx \\ bz + cy + dx \\ cz + dy \\ dz \end{bmatrix}$$

When stride=1, convolution transpose is just a regular convolution (with different padding rules)

Convolution as Matrix Multiplication (1D Example)

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$$\vec{x} * \vec{a} = X\vec{a}$$

$$\begin{bmatrix} x & y & x & 0 & 0 & 0 \\ 0 & 0 & x & y & x & 0 \end{bmatrix} \begin{bmatrix} 0 \\ a \\ b \\ c \\ d \\ 0 \end{bmatrix} = \begin{bmatrix} ay + bz \\ bx + cy + dz \end{bmatrix}$$

Example: 1D conv, kernel
size=3, stride=2, padding=1

Convolution as Matrix Multiplication (1D Example)

We can express convolution in terms of a matrix multiplication

$$\vec{x} * \vec{a} = X \vec{a}$$

$$\begin{bmatrix} x & y & x & 0 & 0 & 0 \\ 0 & 0 & x & y & x & 0 \end{bmatrix} \begin{bmatrix} 0 \\ a \\ b \\ c \\ d \\ 0 \end{bmatrix} = \begin{bmatrix} ay + bz \\ bx + cy + dz \end{bmatrix}$$

Example: 1D conv, kernel size=3, stride=2, padding=1

Convolution transpose multiplies by the transpose of the same matrix:

$$\vec{x} *^T \vec{a} = X^T \vec{a}$$

$$\begin{bmatrix} x & 0 \\ y & 0 \\ z & x \\ 0 & y \\ 0 & z \\ 0 & 0 \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} ax \\ ay \\ az + bx \\ by \\ bz \\ 0 \end{bmatrix}$$

When stride>1, convolution transpose is no longer a normal convolution!

Semantic Segmentation Idea: Fully Convolutional

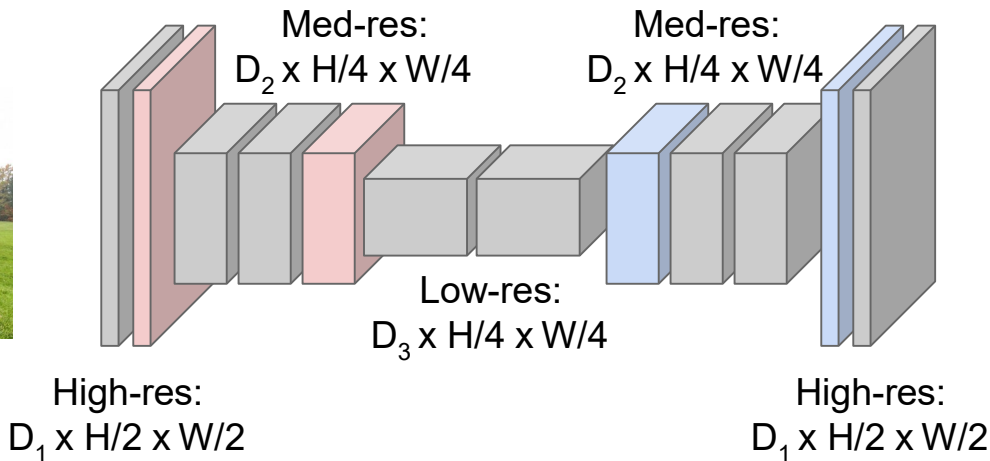
Downsampling:
Pooling, strided
convolution

Design network as a bunch of convolutional layers, with **downsampling** and **upsampling** inside the network!

Upsampling:
Unpooling or strided
transpose convolution



Input:
 $3 \times H \times W$



Predictions:
 $H \times W$

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Noh et al, "Learning Deconvolution Network for Semantic Segmentation", ICCV 2015

Object Detection

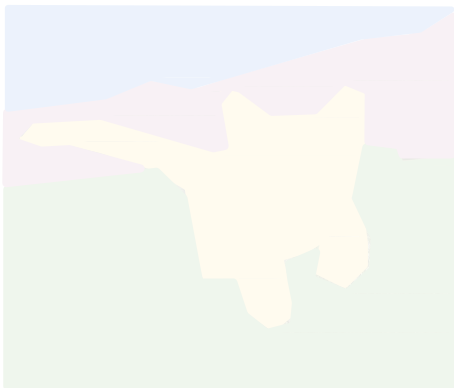
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CAT

No spatial extent

Semantic Segmentation



GRASS, CAT,
TREE, SKY

No objects, just pixels

Object Detection



DOG, DOG, CAT

Multiple Object

Instance Segmentation



DOG, DOG, CAT

Object Detection: Impact of Deep Learning

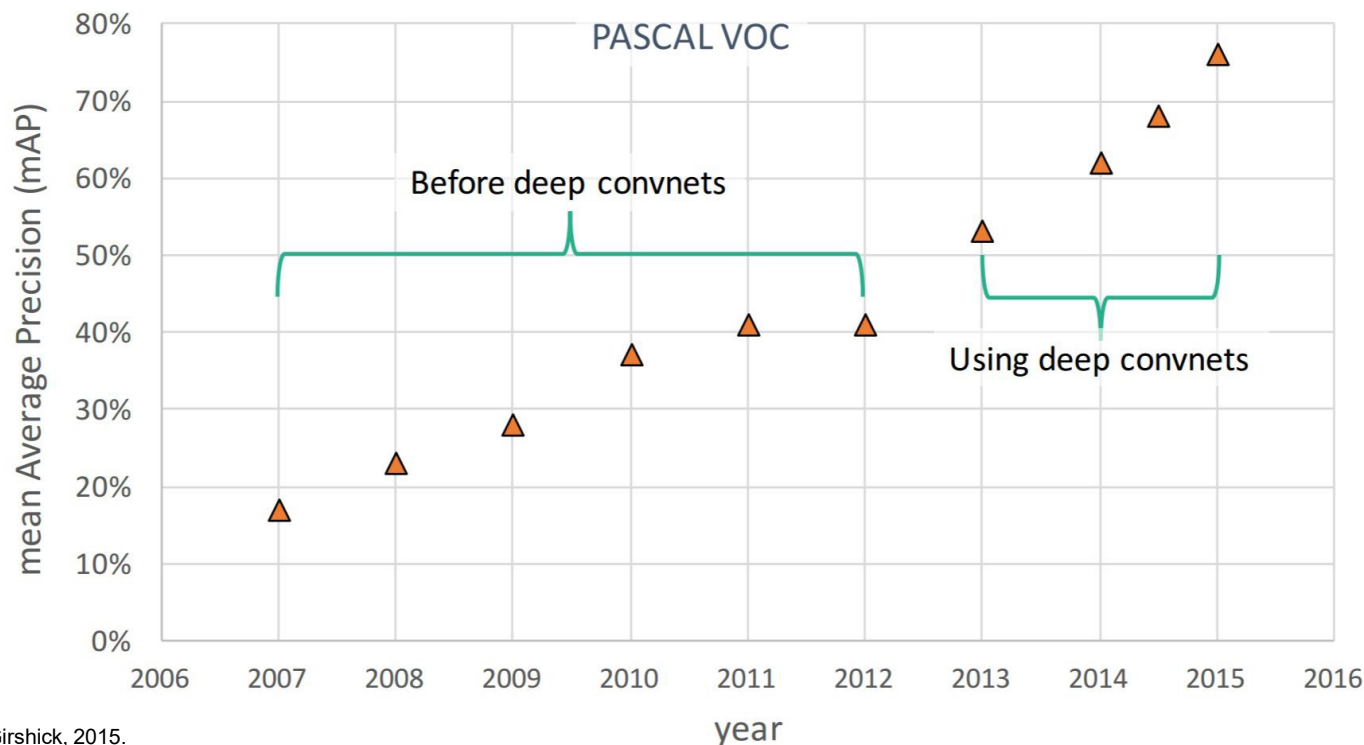


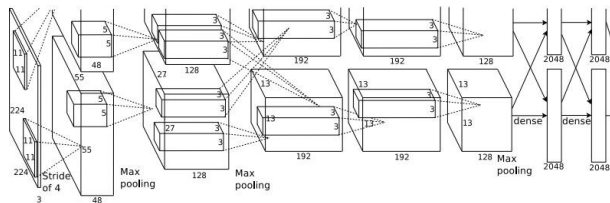
Figure copyright Ross Girshick, 2015.
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Object Detection: Single Object

(Classification + Localization)



[This image is CC0 public domain](#)



Fully Connected:
4096 to 1000

Class Scores

Cat: 0.9
Dog: 0.05
Car: 0.01
...

Correct label:
Cat

Softmax Loss

Vector:
4096

Fully Connected:
4096 to 4

Box Coordinates
(x, y, w, h)

L2 Loss

Correct box:
(x', y', w', h')

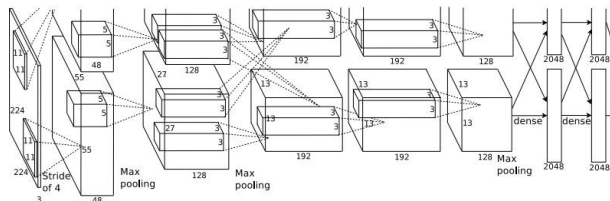
Treat localization as a regression problem!

Object Detection: Single Object

(Classification + Localization)



[This image is CC0 public domain.](#)



Fully
Connected:
4096 to 1000

Class Scores

Cat: 0.9
Dog: 0.05
Car: 0.01
...

Correct label:
Cat

Softmax
Loss

Multitask Loss

+

Loss

Vector:
4096

Fully
Connected:
4096 to 4

Box
Coordinates
(x, y, w, h)

L2 Loss

Correct box:
(x', y', w', h')

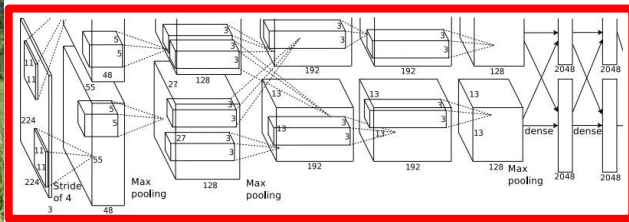
Treat localization as a
regression problem!

Object Detection: Single Object

(Classification + Localization)



[This image is CC0 public domain](#)



Often pretrained on ImageNet
(Transfer learning)

Treat localization as a
regression problem!

Fully
Connected:
4096 to 1000

Class Scores

Cat: 0.9
Dog: 0.05
Car: 0.01
...

Correct label:
Cat

Softmax
Loss

+ → Loss

Vector:
4096

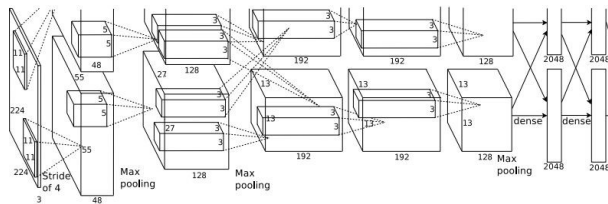
Fully
Connected:
4096 to 4

Box
Coordinates
(x, y, w, h)

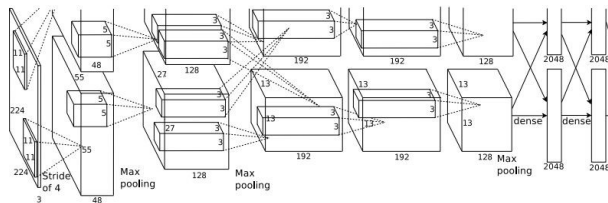
L2 Loss

Correct box:
(x', y', w', h')

Object Detection: Multiple Objects



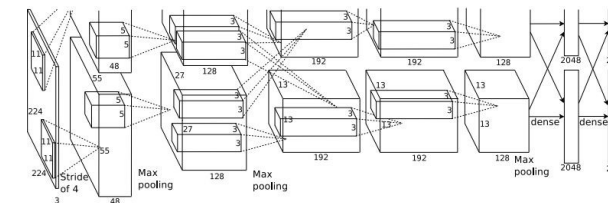
CAT: (x, y, w, h)



DOG: (x, y, w, h)

DOG: (x, y, w, h)

CAT: (x, y, w, h)



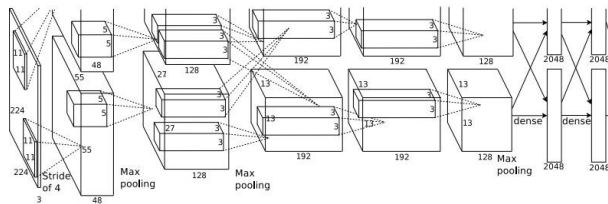
DUCK: (x, y, w, h)

DUCK: (x, y, w, h)

....

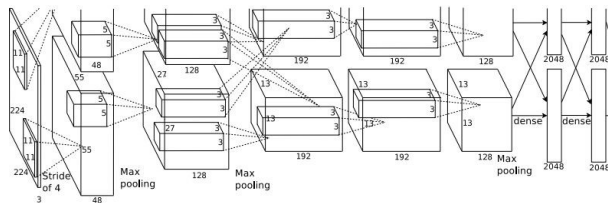
Object Detection: Multiple Objects

Each image needs a
different number of outputs!



CAT: (x, y, w, h)

4 numbers

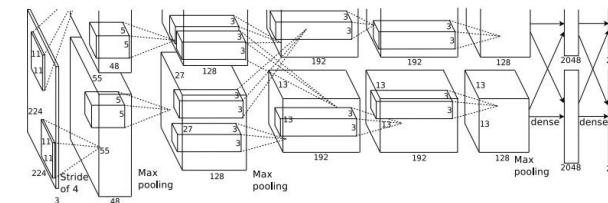


DOG: (x, y, w, h)

DOG: (x, y, w, h)

CAT: (x, y, w, h)

16 numbers



DUCK: (x, y, w, h)

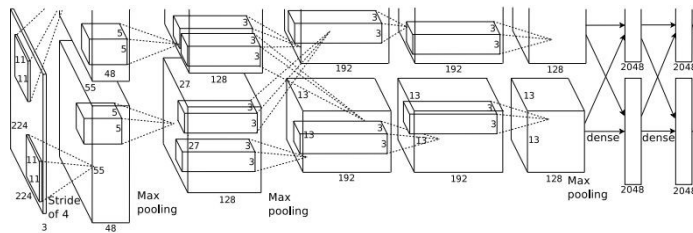
DUCK: (x, y, w, h)

Many
numbers!

....

Object Detection: Multiple Objects

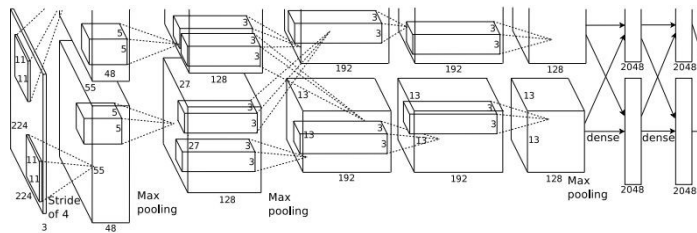
Apply a CNN to many different crops of the image, CNN classifies each crop as object or background



Dog? NO
Cat? NO
Background? YES

Object Detection: Multiple Objects

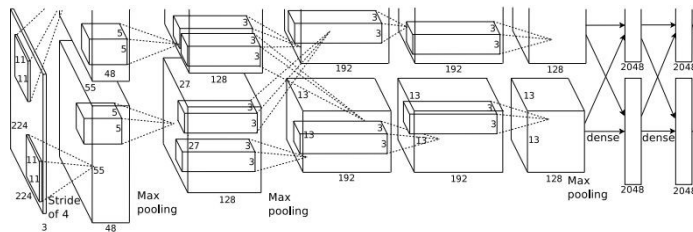
Apply a CNN to many different crops of the image, CNN classifies each crop as object or background



Dog? YES
Cat? NO
Background? NO

Object Detection: Multiple Objects

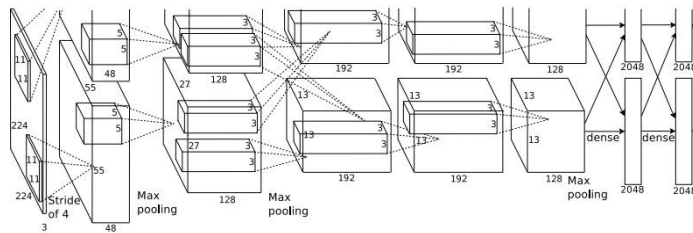
Apply a CNN to many different crops of the image, CNN classifies each crop as object or background



Dog? YES
Cat? NO
Background? NO

Object Detection: Multiple Objects

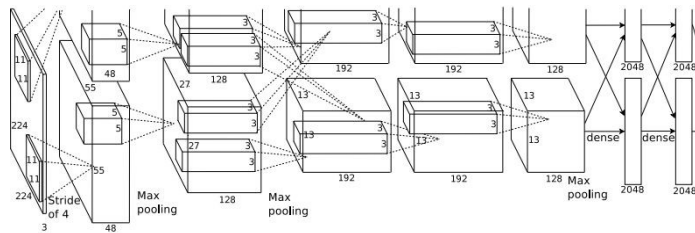
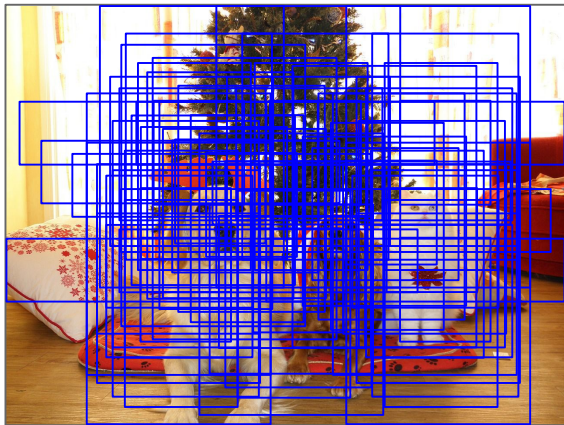
Apply a CNN to many different crops of the image, CNN classifies each crop as object or background



Dog? NO
Cat? YES
Background? NO

Object Detection: Multiple Objects

Apply a CNN to many different crops of the image, CNN classifies each crop as object or background

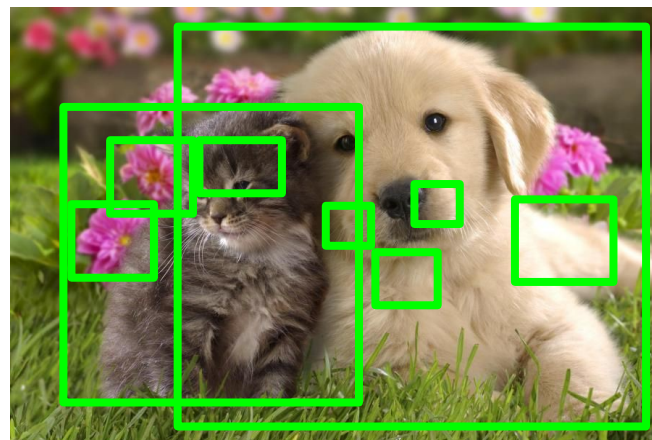


Dog? NO
Cat? YES
Background? NO

Problem: Need to apply CNN to huge number of locations, scales, and aspect ratios, very computationally expensive!

Region Proposals: Selective Search

- Find “blobby” image regions that are likely to contain objects
- Relatively fast to run; e.g. Selective Search gives 2000 region proposals in a few seconds on CPU



Alexe et al, “Measuring the objectness of image windows”, TPAMI 2012

Uijlings et al, “Selective Search for Object Recognition”, IJCV 2013

Cheng et al, “BING: Binarized normed gradients for objectness estimation at 300fps”, CVPR 2014

Zitnick and Dollar, “Edge boxes: Locating object proposals from edges”, ECCV 2014

R-CNN



Input image

Girshick et al, "Rich feature hierarchies for accurate object detection and semantic segmentation", CVPR 2014.
Figure copyright Ross Girshick, 2015; [source](#). Reproduced with permission.

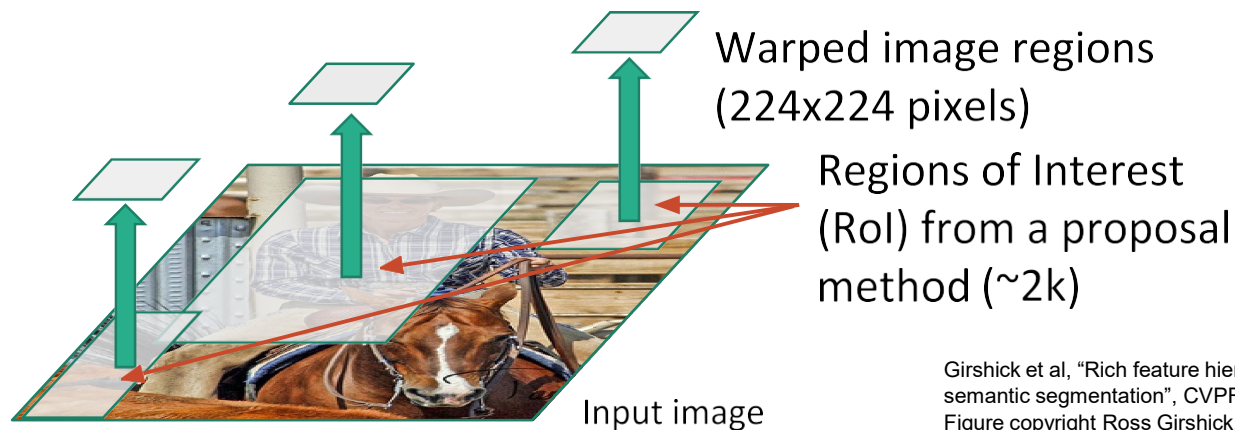
R-CNN



Regions of Interest
(RoI) from a proposal
method (~2k)

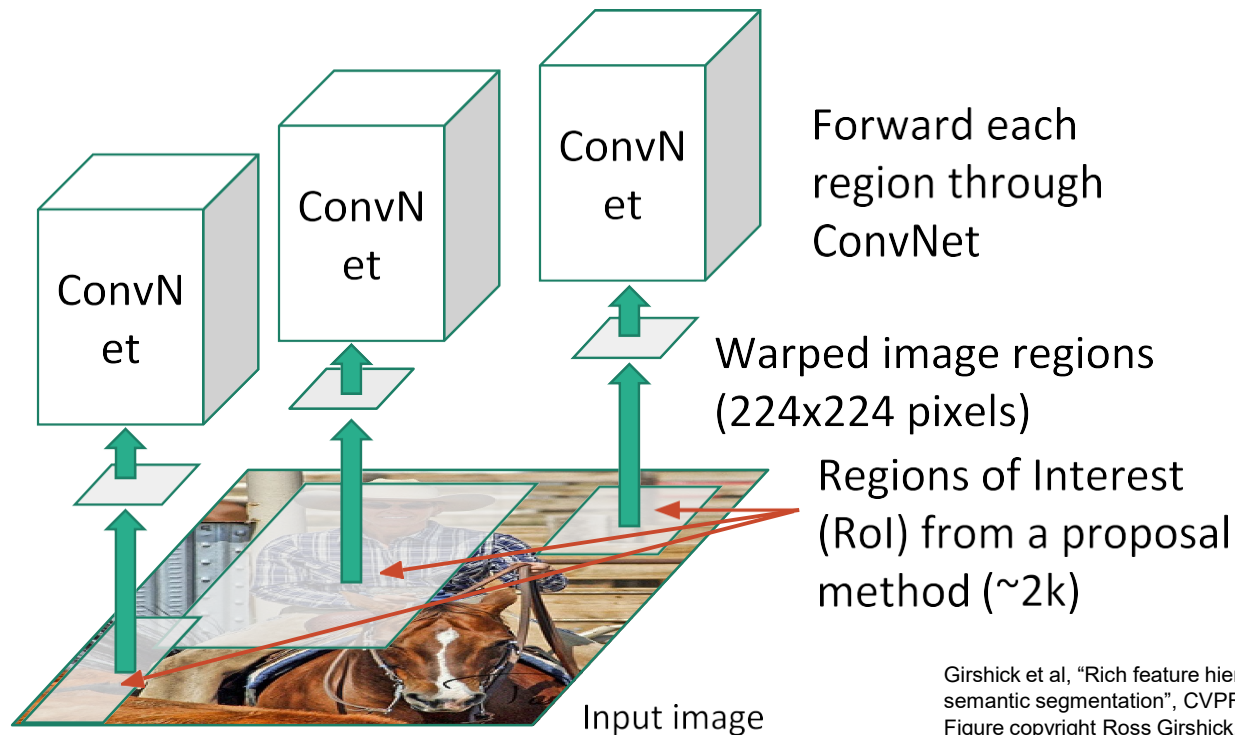
Girshick et al, "Rich feature hierarchies for accurate object detection and semantic segmentation", CVPR 2014.
Figure copyright Ross Girshick, 2015; [source](#). Reproduced with permission.

R-CNN



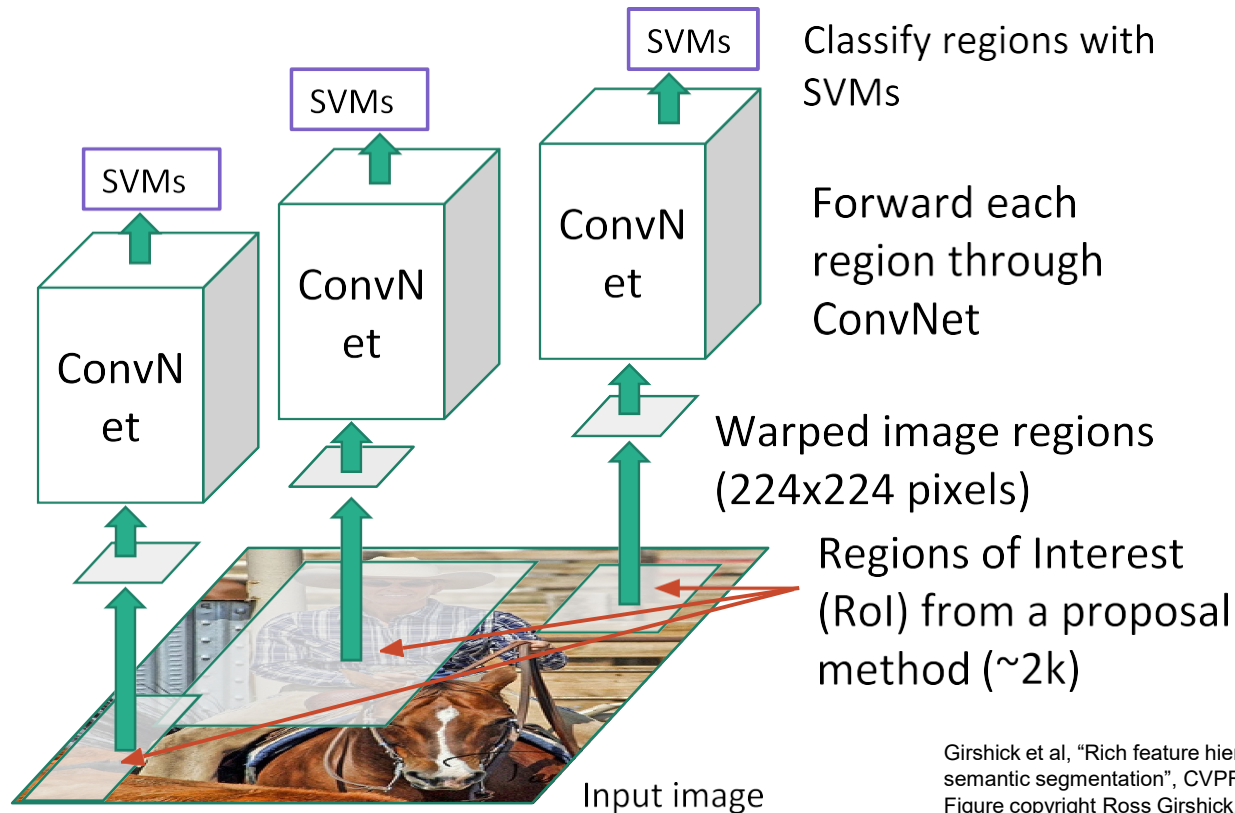
Girshick et al, "Rich feature hierarchies for accurate object detection and semantic segmentation", CVPR 2014.
Figure copyright Ross Girshick, 2015; [source](#). Reproduced with permission.

R-CNN



Girshick et al, "Rich feature hierarchies for accurate object detection and semantic segmentation", CVPR 2014.
Figure copyright Ross Girshick, 2015; [source](#). Reproduced with permission.

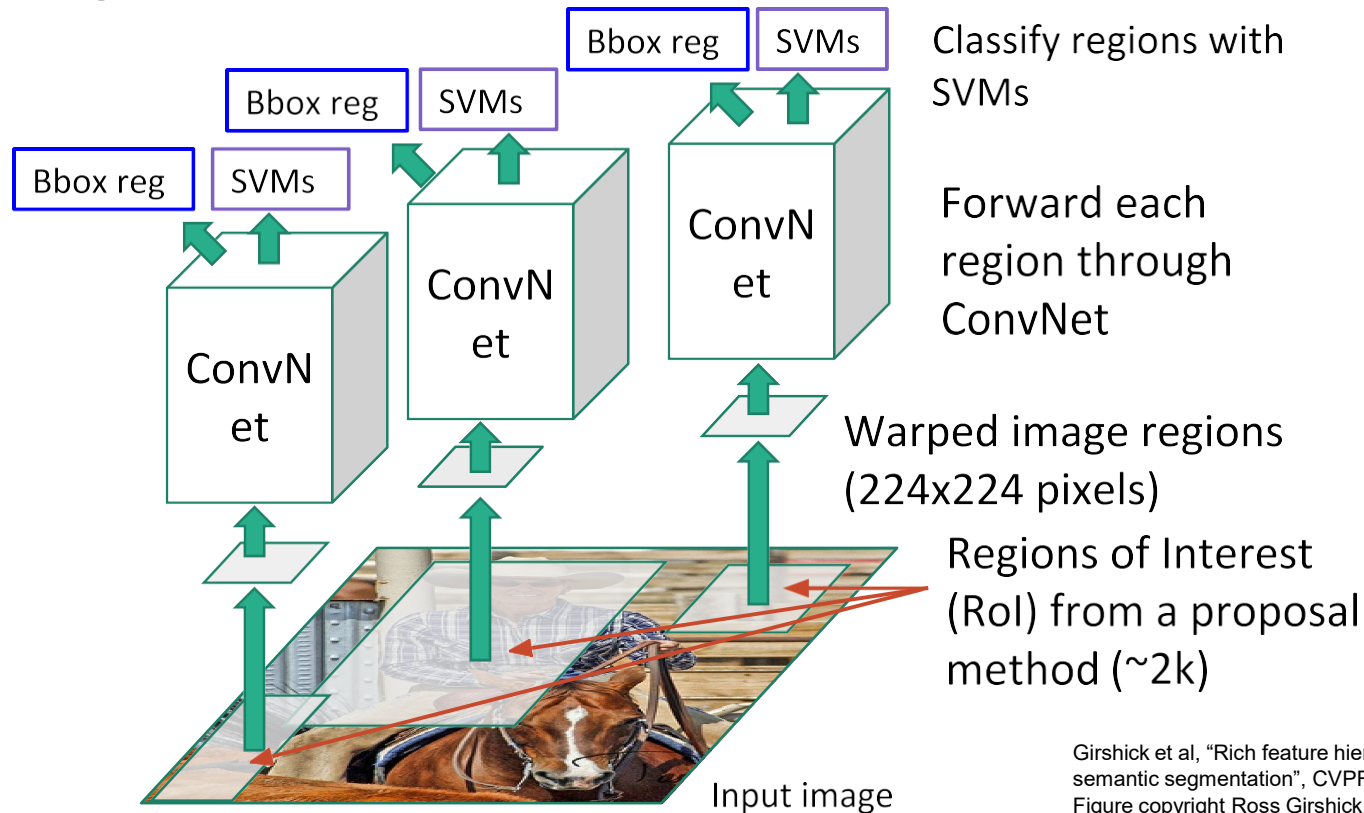
R-CNN



Girshick et al, "Rich feature hierarchies for accurate object detection and semantic segmentation", CVPR 2014.
Figure copyright Ross Girshick, 2015; [source](#). Reproduced with permission.

R-CNN

Predict “corrections” to the RoI: 4 numbers: (dx, dy, dw, dh)



Girshick et al, “Rich feature hierarchies for accurate object detection and semantic segmentation”, CVPR 2014.
Figure copyright Ross Girshick, 2015; [source](#). Reproduced with permission.

The end

- This is all we had time for, but..
- ..see the rest of the Stanford lecture for other variants of CNNs for object detection