2.1 Discussion: Rearrangements of Infinite Series

Consider the infinite series

$$\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n} = 1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \frac{1}{5} - \frac{1}{6} + \dots$$

If we just add from left to right, we get a series of partial sums: $s_1=1,\ s_2=1/2,\ s_3=5/6,$ and so on. We also see that the sums oscillate such that $s_1>s_3>s_5>\dots$ and $s_2< s_4< s_6<\dots$

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