

## 1.1 Newton's Laws

Isaac Newton introduced the three basic laws of mechanics that are known as Newton's Laws.

### Newton's Second Law

:

$$\vec{\mathbf{F}}_{net} = m\vec{\mathbf{a}} \quad (1.1)$$

Sometimes this equation is written as

$$\vec{\mathbf{F}}_{net} = \frac{d\vec{\mathbf{p}}}{dt} \quad (1.2)$$

to account for a changing mass, where  $\vec{\mathbf{p}} = m\vec{\mathbf{v}}$ .

### Newton's First Law

Newton's first law is a special case of the second law:

$$\text{If } \vec{\mathbf{F}}_{net} = \vec{\mathbf{0}}, \text{ the motion is uniform} \quad (1.3)$$

which means that velocity is constant and acceleration is 0.

### Gravity

Acceleration caused by gravity is the same on every object. This seems contradictory to what we have seen from Newton's second law,  $\vec{\mathbf{a}} = \vec{\mathbf{F}}_{new}/m$ , but since the force of gravity is proportional to the mass, the acceleration is independent of the mass.

### Hooke's Law

The equation for spring force is  $F = -kx$ . So,

$$-kx = m \frac{d^2x}{dt^2} \quad (1.4)$$

The solution of this differential equation is

$$x(t) = A \sin(\omega t + \varphi) \quad (1.5)$$

where  $A$  is the *amplitude* of the motion, and  $\varphi$  is the *textitphase*. Both of these quantities are determined by the initial conditions.  $\omega$  is determined by the spring and the mass:

$$\omega = \sqrt{k/m} \quad (1.6)$$

where  $\omega$  is the *angular frequency*, which is related to the *period*  $T$  and *frequency*  $f$ .

$$T = \frac{1}{f} \quad (1.7)$$

so  $f = \omega/2\pi$ .

### Newton's Third Law

Every force has an equal and opposite reaction force.

$$\vec{\mathbf{F}}_{12} = -\vec{\mathbf{F}}_{21} \quad (1.8)$$

This can be restated in terms of momentum.

$$\frac{d\vec{\mathbf{p}}_1}{dt} = -\frac{d\vec{\mathbf{p}}_2}{dt} \text{ or } \frac{d}{dt}(\vec{\mathbf{p}}_1 + \vec{\mathbf{p}}_2) = 0 \quad (1.9)$$

So,

$$\vec{\mathbf{P}}_{tot} = \text{a constant vector} \quad (1.10)$$