## 1.1 Newton's Laws

Isaac Newton introduced the three basic laws of mechanics that are known as Newton's Laws.

### Newton's Second Law

$$\vec{\mathbf{F}}_{net} = m\vec{\mathbf{a}}$$

Sometimes this equation is written as

$$\vec{\mathbf{F}}_{net} = \frac{d\vec{\mathbf{p}}}{dt}$$

to account for a changing mass, where  $\vec{\mathbf{p}} = m\vec{\mathbf{v}}$ .

#### Newton's First Law

Newton's first law is a special case of the second law:

If 
$$\vec{\mathbf{F}}_{net} = \vec{\mathbf{0}}$$
, the motion is uniform

which means that velocity is constant and accusation is 0.

## Gravity

Acceleration caused by gravity is the same on every object. This seems contradictory to what we have seen from Newton's second law,  $\vec{\mathbf{a}} = \vec{\mathbf{F}}_{new}/m$ , but since the force of gravity is proportional to the mass, the acceleration is independent of the mass.

#### Hooke's Law

The equation for spring force is F = -kx. So,

$$-kx = m\frac{d^2x}{dt}$$

The solution of this differential equation is

$$x(t) = A\sin(\omega t + \varphi)$$

where A is the amplitude of the motion, and  $\varphi$  is the textitphase. Both of these quantities are determined by the initial conditions.  $\omega$  is determined by the spring and the mass:

$$\omega = \sqrt{k/m}$$

where  $\omega$  is the angular frequency, which is related to the period T and frequency f.

$$T = \frac{1}{f}$$

so  $f = \omega/2\pi$ .

# Newton's Third Law

Every force has an equal and opposite reaction force.

$$\vec{\mathbf{F}}_1 2 = -\vec{\mathbf{F}}_2 1$$

This can be restated in terms of momentum.

$$\frac{d\vec{\mathbf{p_1}}}{dt} = -\frac{d\vec{\mathbf{p_2}}}{dt} \text{ or } \frac{d}{dt}(\vec{\mathbf{p_1}} + \vec{\mathbf{p_2}}) = 0$$

So,

$$\vec{\mathbf{P}}_{tot} = \mathbf{a}$$
 constant vector