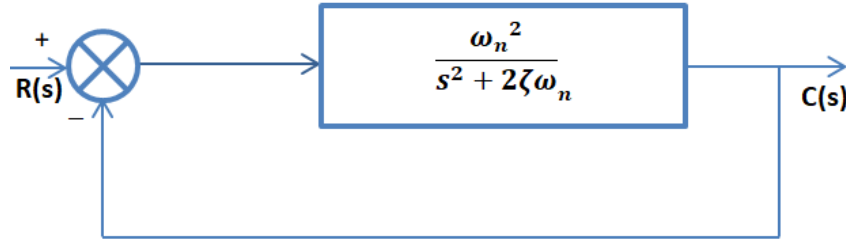


Experiment 4

Aim: To study about systems of second order and analyse their time response.

- Effect of damping ratio ζ on performance measure and plot the step response for the given block diagram for $\zeta = 0.1, 0.3, 0.5, 1, 2$.



- Calculate t_r , t_p , t_d , M_p with change in ζ
- To analyse the effect of addition of the following poles together and zeros subsequently to transfer function such that the transfer function becomes

$$\frac{\omega_n^2}{(s^2 + 2\zeta\omega_n + \omega_n^2)} \frac{\prod(1 + sT_z)}{\prod(1 + sT_p)}$$

Software: Matlab 2018a

Equations/Formula:

- $t_r = \frac{\pi - \phi}{\omega_n \sqrt{1 - \zeta^2}}$
- $t_s = \frac{4}{\zeta \omega_n}$
- $M_p = 1 - \frac{e^{-\zeta \omega_n t}}{\sqrt{1 - \zeta^2}} \sin \{ (\omega_n \sqrt{1 - \zeta^2})t + \phi \}$

Theory: The order of a control system is determined by the power of s in the denominator of its transfer function. If the power of s in the denominator of transfer function of a control system is 2, then the system is said to be second-order control system. The general expression of transfer function of a second order control system is given as

$$\frac{c(s)}{e(s)} = \frac{\omega_n^2}{(s^2 + 2\zeta\omega_n)}$$

Here ζ and ω_n are damping ratio and natural frequency of the system respectively. After giving unity feedback to the system the transfer equation becomes

$$\frac{c(s)}{e(s)} = \frac{\omega_n^2}{(s^2 + 2\zeta\omega_n + \omega_n^2)}$$

There are number of common terms in transient response characteristics and which are

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1. **Delay time** (t_d) is the time required to reach at 50% of its final value by a time response signal during its first cycle of oscillation.
2. **Rise time** (t_r) is the time required to reach at final value by a under damped time response signal during its first cycle of oscillation. If the signal is over damped, then rise time is counted as the time required by the response to rise from 10% to 90% of its final value.
3. **Peak time** (t_p) is simply the time required by response to reach its first peak i.e. the peak of first cycle of oscillation, or first overshoot.
4. **Maximum overshoot** (M_p) is straight way difference between the magnitude of the highest peak of time response and magnitude of its steady state. Maximum overshoot is expressed in term of percentage of steady-state value of the response. As the first peak of response is normally maximum in magnitude, maximum overshoot is simply normalized difference between first peak and steady-state value of a response.

MATLAB Code:

```
clc;
close all;
clear all;
wn = 1;
z = [0.1 0.3 0.5 0.7 1 2];
G1 = tf([0 0 wn],[1 2*z(1) 0]);
G2 = tf([0 0 wn],[1 2*z(2) 0]);
G3 = tf([0 0 wn],[1 2*z(3) 0]);
G4 = tf([0 0 wn],[1 2*z(4) 0]);
G5 = tf([0 0 wn],[1 2*z(5) 0]);
G6 = tf([0 0 wn],[1 2*z(6) 0]);
Y1 = feedback(G1,1);
Y2 = feedback(G2,1);
Y3 = feedback(G3,1);
Y4 = feedback(G4,1);
Y5 = feedback(G5,1);
Y6 = feedback(G6,1);
S = stepinfo(Y1)
subplot(2,3,1),
step(Y1);title('z = 0.1');
subplot(2,3,2),step(Y2);title('z = 0.3');
subplot(2,3,3),step(Y3);title('z = 0.5');
subplot(2,3,4),step(Y4);title('z = 0.7');
subplot(2,3,5),step(Y5);title('z = 1');
subplot(2,3,6),step(Y6);title('z = 3');
```

Result:

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