Picking on the Same Person: Does Algorithmic Monoculture lead to Outcome Homogenization?

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Abstract

As the scope of machine learning broadens, we observe a recurring theme of algorithmic monoculture: the same systems, or systems that share components (e.g., datasets, models), are deployed by multiple decision-makers. While sharing offers advantages like amortizing effort, it also has risks. We introduce and formalize one such risk, *outcome homogenization*: the extent to which particular individuals or groups experience the same outcomes across different deployments. If the same individuals or groups exclusively experience undesirable outcomes, this may institutionalize systemic exclusion and reinscribe social hierarchy. We relate algorithmic monoculture and outcome homogenization by proposing the *component* sharing hypothesis: if algorithmic systems are increasingly built on the same data or models, then they will increasingly homogenize outcomes. We test this hypothesis on algorithmic fairness benchmarks based on the US Census, demonstrating that increased data-sharing exacerbates homogenization, especially for small datasets. Further, given the current regime in AI of foundation models, i.e., pretrained models that can be adapted to myriad downstream tasks, we test whether model-sharing homogenizes outcomes across tasks. We observe mixed results: we find that for both vision and language settings, the specific methods for adapting a foundation model significantly influence the degree of outcome homogenization. We also identify societal challenges that inhibit the measurement, diagnosis, and rectification of outcome homogenization in deployed machine learning systems.

21 1 Introduction

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Machine learning is built on strong traditions of sharing: we share datasets (e.g., ImageNet), models 22 (e.g., BERT), libraries (e.g., PyTorch), optimizers (e.g., Adam), evaluations (e.g., SuperGLUE) and 23 much more. This ethos of sharing serves the field well: we are able to repeatedly capitalize on the effort required to build high-quality assets (e.g., ImageNet has supported thousands of researchers in computer 25 vision), and improvements to these assets have sweeping benefits (e.g., BERT raised all boats in NLP). 26 27 Yet does sharing also have risks? Could this central tenet of the field lead to undesirable outcomes? We observe that certain forms of sharing can be reinterpreted as monoculture: Kleinberg and Raghavan 28 [2021] define algorithmic monoculture as the state "in which many decision-makers all rely on the 29 same algorithm." In parts of society where algorithmic systems are ubiquitous, we see trends towards 30 such monoculture [Moore and Tambini, 2018, Engler, 2021]. Monocultures often pose serious risks: 31 Kleinberg and Raghavan [2021] show monoculture is suboptimal for decision-makers when their 33 decisions are interconnected, as when they compete to hire job candidates. Should we think of our practices of sharing assets in ML as monoculture and, if so, what harms should we worry about?

We investigate this question by proposing one potential risk we call *outcome homogenization*, i.e., the phenomenon of individuals (or groups) exclusively receiving negative outcomes from all ML models 36 they interact with. We view outcome homogenization as an important class of systemic harms that 37 arise when we study social systems, i.e., harms that require observing how individuals are treated by 38 many decision-makers. In §2, we conceptually motivate outcome homogenization in the context of 39 algorithmic hiring. In §3, we introduce the first mathematical formalism for outcome homogenization: 40 we measure homogenization as the observed probability of systemic failure normalized by the base rate. 41 To link the practice of sharing in ML with the proposed harm of homogenization, we pose and test 42 the component sharing hypothesis: algorithmic systems built using the same underlying components, 43 such as training data and machine learning models, will systematically exclude the same individuals 44 or groups. We see component sharing as a specific form of algorithmic monoculture, which generalizes 45 the definition in Kleinberg and Raghavan [2021] from decision-makers deploying the same system 46 to deploying similar systems in terms of how they are constructed. We investigate how two types of 47 shared components — training data and foundation models — contribute to homogeneous outcomes. In §4, we demonstrate that data-sharing reliably homogenizes outcomes for individuals and for racial 49 groups, especially for small training datasets involving US census data. In §5, we discuss how the rise 50 of foundation models [Bommasani et al., 2021], i.e., pretrained models that can be adapted to myriad 51 downstream tasks, could yield unprecedented homogenization. Based on experiments with foundation 52 models for vision (CLIP) and language (RoBERTa), to our surprise, we find the use of foundation 53 models does not always exacerbate outcome homogenization. Instead, we find the specific mechanism 54 for adapting the foundation model to the downstream task significantly influences homogenization: for example, linear probing consistently leads to more homogeneous outcomes than finetuning for 56 both modalities. Through these experiments, it is clear that the relationship between sharing and 57 homogenization is not fully explained by our hypothesis, but that there is some evidence that sharing 58 homogenizes outcomes. To advance the study of homogenization in practice, where systemic harms 59 are most consequential, we conclude by identifying key challenges for diagnosing, measuring, and 60 rectifying homogenization in society (§6). 61

Outcome Homogenization in Resume Screening

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To illustrate outcome homogenization and its potential causes, we will use the example of algorithmic resume screening. Companies use resumes to screen job applicants, choosing which candidates to interview and which to reject. Maximum homogenization occurs when every company makes the same decision about each candidate, such that each lucky candidate is interviewed by all companies and each unlucky candidate by no companies. We say that the unlucky candidates who receive no interviews experience a systemic failure.

What factors might homogenize outcomes? Historically, hiring managers at each company decided who to interview and often agreed in their decisions. This agreement can be attributed to multiple 70 sources: first, if the needs of each company were identical, then managers at different companies may 71 be incentivized to interview the same candidates, thereby homogenizing outcomes. Second, if hiring 72 managers' choices are influenced by the same social biases, they will mistakenly reject the same people, 73 thereby homogenizing their errors. Bias in resume screening is well-documented and remains signifi-74 cant [Jowell and Prescott-Clarke, 1970, Bertrand and Mullainathan, 2004, Kline et al., 2021, inter alia]. 75 However, neither explanation implies that systemic failures are inevitable. Since companies have 76 77 different needs and resumes are imperfect predictors of success in role, the "best" candidates will likely differ across companies. Further, bias is not uniform across companies: Kline et al. [2021] find that 78 21% of firms were responsible for 46% of the racial contact gap. Even if decisions are influenced 79 by the same group-level biases, different companies may choose different individual members of 80 the advantaged and disadvantaged groups. Variance in company needs, in prevalence of bias, and 81 in individual hiring manager preferences all make it more likely that different resumes survive the 82 screening stage at different companies, ensuring some diversity in resume screening outcomes. 83

How do these dynamics change with the introduction of automated decision-making? Most 84 large companies now use automated resume screening software to parse resumes and decide which 85 applicants advance. As a stylized example, if every company deploys the same deterministic system 86 and has the same hiring criteria, then outcomes will be necessarily homogeneous: individuals will either receive interviews at every company or be rejected by all of them (i.e., systemic failure). This

example is not far from reality: a few major vendors dominate the marketplace for algorithmic resume screening with 700 companies, including over 30% of Fortune 100 companies, relying on Hirevue [Hirevue, 2021]. This practice of different companies deploying the same system is defined as *algorithmic monoculture* by Kleinberg and Raghavan [2021].

More generally, different companies may instead deploy *similar*, but non-identical, systems. We 93 expand the definition of algorithmic monoculture to encapsulate this broader setting, which is also 94 alluded to in Kleinberg and Raghavan [2021]. Engler [2021] describe this as the reality for college 95 enrollment management algorithms, writing "there are a relatively small number (between five and 10) 96 of prominent vendors in the enrollment management algorithm market, ... their process and analytics 97 are markedly similar. Since their processes seem relatively consistent, the outcomes might be as well 98 potentially leading to consistently good results for students who match the historical expectations 99 of colleges, and consistently poor results for students who don't". 100

Component Sharing Hypothesis. In this work, we study systems that are related in how they are constructed, akin to what is described by Engler [2021]. We pose the component sharing hypothesis that relates such algorithmic monoculture with outcome homogenization: *If deployed algorithmic systems share components, outcome homogenization will increase (i.e., there will be more systemic failures)*. In this work, we empirically test this hypothesis for two prominent forms of component sharing: (i) the sharing of training data in training all deployed systems (§4) and (ii) the sharing of the same foundation model for building all deployed systems (§5).

3 Formalizing Outcome Homogenization

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While prior work [Kleinberg and Raghavan, 2021, Creel and Hellman, 2021, Bommasani et al., 2021] alludes to outcome homogenization, here we provide the first mathematical formalism of outcome homogenization. In line with our running example of resume screening, we formalize outcome homogenization for individuals in terms of *systemic failures* (i.e., every algorithmic system fails for an individual). We then generalize to the group setting, where groups are systemically excluded rather than individuals, with a discussion of how these metrics relate to established fairness, robustness, and accuracy metrics (§3.4).

3.1 Formalizing Outcome Homogenization for Individuals

Notation. Since we define outcome homogenization as a systemic phenomenon, we consider a social system $\{h^i\}_{i=1}^k$ where every individual j interacts with the k deployed models $h^1,...,h^k$. Specifically, an individual $j \in [N]$ will submit features x^i_j (e.g., their resume) as input to company $i \in [k]$ and receive an outcome $h^i(x^i_j) = \hat{y}^i_j$ (e.g., an interview). Let D^i be the empirical distribution of inputs x^i for company i.

To define a notion of failure, let $I^i(x^i_j)$ indicate if \hat{y}^i_j is a negative outcome, i.e., individual j experiences a negative outcome from model h^i . The failure rate for model h^i is

$$\operatorname{fail}(h^i) \triangleq \underset{x^i \sim D^i}{\mathbb{E}} I^i(x^i) = \underset{x^i \sim D^i}{\Pr} \left[I^i(x^i) = 1 \right]. \tag{1}$$

Experimentally, we consider classification errors as failures (i.e., $I^i(x^i) \triangleq \mathbb{I} \big[h^i(x^i) \neq y^i \big]$), but other negative outcomes (e.g., rejections from hiring or educational opportunities; $I^i(x^i) \triangleq \mathbb{I} \big[h^i(x^i) = -1 \big]$) also can be studied under our framework.

Systemic failures for individuals. If an individual exclusively experiences failure, we say they experience systemic failure. The observed rate of systemic failure S is

$$S \triangleq \underset{j}{\mathbb{E}} \left[\prod_{i} I^{i}(x_{j}^{i}) \right] = \Pr_{j} \left[I^{1}(x_{j}^{1}) = 1 \wedge \dots \wedge I^{k}(x_{j}^{k}) = 1 \right]. \tag{2}$$

¹The formal model of Kleinberg and Raghavan [2021] is related, but substantially distinct. Concretely, their formalism considers harms experienced by decision-makers, whereas we center decision-subjects.

²Note that our framework is general: we permit the deployed models to be for different tasks and for the individual's inputs to not be the same, though in our resume screening example all the models perform the same task and applicants often submit the same resume to different companies.

In other words, it is the fraction of individuals who are failed by every model.

Homogenization metric for individuals. S quantifies homogeneous outcomes but is difficult to compare across real-world systems with different underlying accuracies: S will in general be higher for less accurate systems independent of a *specific* tendency to pick on the same person. While we may sometimes want to combine accuracy and outcome homogenization into an overall measure of utility or social welfare, which S implicitly does, we focus on a *relative* measure of homogenization that disentangles accuracy from homogenization. In particular, we are interested in outcome homogenization even, and perhaps especially, in systems that are highly accurate.

As a result, we measure individual-level outcome homogenization for a social system $\{h^i\}_{i=1}^k$ by normalizing the *observed* rate of systemic failure by the *expected* rate of systemic failure.

$$H^{\text{individual}}(h^1, \dots, h^k) \triangleq \frac{S}{\prod\limits_{i=1}^k \text{fail}(h^i)} = \frac{\mathbb{E}\left[\prod\limits_{i} I^i(x^i_j)\right]}{\prod\limits_{i} \left[\mathbb{E}I^i(x^i_j)\right]} \tag{3}$$

This measure can be interpreted as the ratio between (i) the probability that an individual experiences systemic failure and (ii) the probability that randomly sampled outputs for each model are all misclassified. That is, the measure captures how the rate of systemic failure changes when we attend to the structure of individuals.

3.2 Formalizing Outcome Homogenization for Groups

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In addition to our individual-level metric, we also define a group-level metric for outcome homogenization. While our individual-level metric individualizes harm, complementing work on group-level harms like bias and inequity, we may also want to identify when broader social groups (e.g., Black women) are systemically excluded. This is especially relevant when we do not have access to individual-level information (e.g., due to privacy concerns; see §6) or when individuals are not shared across data distributions (e.g., hiring in different states).

Notation. For each input x^i , we denote the associated group as $G(x^i) \in \mathcal{G}$. Group identity may correspond with the data producer (e.g., the age of a user querying a search engine) or the data subject (e.g., the race of an individual subject to face recognition). Let D_g^i indicate restricting the data distribution to inputs to group g, i.e., $\forall x^i \in D_g^i$, $G(x^i) = g$. The group failure rate $\operatorname{fail}_g(h^i)$ is

$$\mathtt{fail}_g(h^i) \triangleq \underset{x^i \sim D_g^i}{\mathbb{E}} I^i(x^i). \tag{4}$$

Homogenization metric for groups. To measure group-level outcome homogenization for a social system $\left\{h^i\right\}_{i=1}^k$, we modify our individual-level metric to compute a weighted average over groups in place of a simple average over individuals.

$$H_{G}^{\mathbf{group}}(h^{1},...,h^{k}) = \frac{\frac{1}{\sum W(g)} \sum_{g} \left[W(g) \prod_{i} \mathtt{fail}_{g}(h^{i}) \right]}{\prod_{i=1}^{k} \mathtt{fail}(h^{i})} \tag{5}$$

Weight functions. We consider three weight functions $W: \mathcal{G} \to \mathbb{R}$ (full definitions in §A.1):

Average (H_{avg}) Each group g receives a weight proportional to its *frequency* across all deployments.

Uniform (H_{unif}) Each group g receives equal weight.

Worst (H_{worst}) The group with the highest rate of systemic failure receives a weight of 1 and all other groups receive a weight of 0.

We introduce these weight functions to clarify that, much like having both individual-level metrics and group-level metrics, we may want to weight groups differently in different circumstances. For example, weighting by frequency may provide a useful overall measurement of homogenization but obscure systemic exclusion experienced by minority groups or specifically the worst-off group.

3.3 Understanding our metrics

As a ratio of probabilities, our metrics take values in $[0,\infty)$ where 0 indicates no systemic failures, 1 indicates the observed rate matches the expected rate, and values greater than 1 indicate some degree of outcome homogenization. In the individual setting, we assume each individual generates exactly one input per deployment, which may not hold in practice (e.g., people may submit multiple resumes or not apply to every company). We appropriately generalize our individual-level metric to address this in Appendix A. Further, in the group setting, we recover the individual-level metric using the **uniform** weighting (or the **average** weighting) if each individual's inputs are treated as belonging to their own group.

3.4 Relationship with related concepts

Given that we introduce (several) metrics, we want to be cognizant of how they relate to existing metrics for related concepts (e.g., accuracy, fairness, robustness). This speaks to the convergent and divergent validity of our metrics [Campbell and Fiske, 1959, Messick, 1987, Jacobs and Wallach, 2021], i.e., whether they are adequately correlated with metrics of similar constructs and adequately uncorrelated with metrics of dissimilar constructs. Here, we discuss theoretical relationships, whereas in §5.2 we look at the empirical correlations.

Accuracy. We design our metrics to minimize correlation with accuracy to separate homogenization effects explicable by the accuracy of the underlying models from those that go beyond what is predicted by accuracy. While not theoretically guaranteed, we demonstrate in Table 1 that our metrics are consistently uncorrelated, or very weakly correlated, with accuracy.

Fairness and Robustness. Beyond accuracy, outcome homogenization is closely related to fairness and robustness. However, we emphasize that outcome homogenization is fundamentally about correlated outcomes for social *systems*, whereas almost all robustness or fairness metrics are defined for a single model. Recent work [Zhao and Chen, 2019, D'Amour et al., 2020, Wang et al., 2021] has initiated the study of fairness in multi-task learning, however these works focus on favorable overall trade-offs across tasks as opposed to systemic modes of failure. Conversely, our metrics cease to be interesting (e.g., $H^{individual}$ is always 1) in the single-model setting as systemic failures are single-model failures.

At a more fine-grained level, algorithmic fairness metrics [e.g., Dwork et al., 2012, Hardt et al., 2016, Corbett-Davies and Goel, 2018], as well as fairness metrics from other fields like the Gini coefficient, 193 emphasize discrepancies between individuals/groups. In contrast, our metrics do not (explicitly) center 194 these differences; we are interested in the observed rate of systemic failures across all deployments 195 (and whether this exceeds the expected rate). Performance differences across individuals/groups are 196 not sufficient for outcome homogenization: if the performance disparities for each deployment do not 197 align across deployments, then the observed rate of systemic failure may not exceed the expected rate. 198 For robustness metrics, our metric H_{worst} in the worst-case setting closely resembles the metrics studied 199 in work on worst-group robustness [e.g., Sagawa* et al., 2020]. In particular, when there is only one 200 201 deployment, our metric recovers the standard worst-group accuracy normalized by the overall accuracy.

202 3.5 Alternative metrics

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In Appendix A, we more extensively discuss desiderata for our metric, alternatives we considered, and how we arrived at the metrics we present in the main paper. With that said, we also note conditions where we may instead favor alternatives, as well as connections to familiar quantities like the covariance, Pearson correlation, and (pointwise) mutual information in the binary setting (k=2).

4 Data-Sharing Experiments

Having stated our mathematical formalism and metrics for outcome homogenization, we test if sharing training data leads to outcome homogenization. We choose to look at the US Census, which has been well-studied in work on algorithmic fairness and ensures we have individual-level outcomes.

Data. We work with the ACS PUMS data³ introduced by Ding et al. [2021], which contains US Census survey data recording 286 features (e.g., self-reported race and sex, occupation, average hours worked per week) for 3.6 million individuals. Ding et al. [2021] construct several classification tasks using

³Full reproducibility details are provided in §B.1.

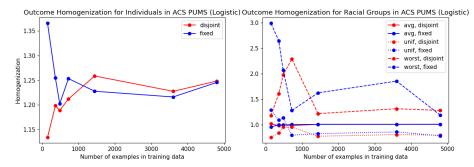


Figure 1: Results for data-sharing experiments showing homogenization (y) as a function of training dataset size (x). Training across tasks on the same data (**fixed**) yields more homogeneous outcomes than on non-identical but identically distributed data (**disjoint**), especially for small datasets.

this data, where each task uses some of an individual's features as inputs and one of their features as the label for the prediction task (e.g., predicting if an individual's income exceeds \$50000). We work with three such tasks: **ACSEmployment** (predict if an individual is employed), **ACSIncomePovertyRatio** (predict an individual's income normalized by the poverty threshold), and **ACSHealthInsurance** (predict if an individual has health insurance).

Individuals and Groups. For each individual, we have their true label for each of the three tasks, enabling us to measure individual-level homogenization. In the group setting, we measure how outcomes homogenize when grouping by the 9 self-identified racial categories (e.g., American Indian, Asian, Black/African American, White, two or more races).

Experimental Design. To test if data-sharing influences outcome homogenization, we formulate a controlled comparison by specifying two settings for the training data: fixed and disjoint. In the fixed setting, we sample n points without replacement from the entire ACS PUMS training dataset and set the training data for every task to this set. In the disjoint setting, we sample 3n points without replacement and randomly partition them across the three tasks. In other words, in the fixed setting, the three models are trained on data corresponding to exact same individuals, whereas in the disjoint setting, no pair of models is trained on data corresponding to the same individual. Having specified the training data, we train logistic regression models for each of three tasks following Ding et al. [2021]. To account for randomness, we report results averaged over 25 trials of the experiment (i.e., 5 samples of training data and 5 training runs per sample for every value of n we consider).

Results and Analysis. In Figure 1, we present our results for this controlled comparison. Across all of our homogenization metrics, we see clear trends (for both individuals and racial groups) that the **fixed** setting yields more homogeneous outcomes than the **disjoint** setting (i.e., blue line is above the corresponding red line). This provides clear evidence for our hypothesis: the use of the same training data leads to greater outcome homogenization than the use of different (but identically distributed) training data. Interestingly, our results also suggest that homogenization can be improved by randomly subsampling a dataset. Given a fixed dataset D, Figure 1 (**left**) suggests that homogenization is better (lower) if each of the three applications randomly subsamples a third of D rather than using the entire dataset D. However, subsampling can reduce accuracy, which poses a tradeoff we discuss in §6. Further, we see that these effects wane as the amount of training data increases (i.e., gap between blue and red lines from left to right). This comes as no surprise: the two distributions converge due to concentration of measure, hence the distinction between the training data in the **fixed** and in the **disjoint** settings is increasingly small for larger amounts of data.

Picking on the same person. Further, we contrast the degree of homogenization in the individual and group settings. (Recall the **average** and **uniform** metrics are the group-level analogues of our individual-level metric.) Outcomes are consistently more homogeneous at the individual-group than for racial groups. This has significant ramifications for many works on algorithmic fairness, which only consider social groups (e.g., race): these works may miss systemic failures for particular individuals that are obscured at the group-level [cf. Kearns et al., 2018, Hashimoto et al., 2018]. Even

⁴We provide results on two additional datasets and for three additional model families (gradient boosted trees, SVMs, neural networks) in Appendix C, which reinforce the findings here.

intersectional approaches may not suffice to surface these systemic failures, unless each intersectional group comprises a single individual.

5 Model-Sharing Experiments

255 Having found that data-sharing appears to exacerbate outcome homogenization, especially for small datasets, we now turn to model-sharing. Specifically, we test how sharing pretrained models, or foundation models [Bommasani et al., 2021], affects outcome homogenization. Bommasani et al. [2021] define foundation models as "models trained on broad data (generally using self-supervision 258 at scale) that can be adapted to a wide range of downstream tasks". These models have had a sweeping 259 impact on the AI research community, most notably in NLP, and are increasingly central to deploying 260 ML at both startups (e.g., Hugging Face, Anthropic, Inflection) and established technology companies 261 (e.g., Google, Microsoft, Meta). Sharing is endemic to foundation models: to justify their immense 262 resource requirements, the models must be used repeatedly for these costs to amortize favorably. In 263 the extreme, if an entire domain like NLP comes to build almost all downstream systems on one or 264 a few foundation models, then any biases or idiosyncrasies of these models that pervasively manifest 265 266 downstream could potentially yield unprecedented systemic failures and outcome homogenization [Bommasani et al., 2021, Fishman and Hancox-Li, 2022]. We see initial evidence for such algorithmic 267 monoculture: BERT was downloaded 10 million times in the past month alone and GPT-3 enables 268 hundreds of deployed apps.⁵ Consequently, we believe it is especially timely to understand if, and 269 to what extent, outcomes get homogenized as these models become entrenched as infrastructure.

5.1 Experiments

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Data. To test how foundation models influence homogenization, we run experiments for both vision and language data.⁶ On the vision side, we work with the **CelebA** dataset [Liu et al., 2015] of celebrity faces paired with annotations for facial attributes. For each face image, given the associated attributes, we define two tasks (**Earrings, Necklace**) that involve predicting whether the individual is wearing the specific apparel item. Attribute prediction in CelebA has been studied previously in work on fairness and robustness [Sagawa* et al., 2020, Khani and Liang, 2021, Wang et al., 2021]. On the language side, we use four standard English text classification datasets following Gururangan et al. [2019]: **IMDB** [Maas et al., 2011], **AGNews** [Zhang et al., 2015], **Yahoo** [Chang et al., 2008], and **HateSpeech18** [de Gibert et al., 2018].

Individuals and Groups. Since the vision tasks are all based on CelebA, we have individual-level information. However, since the language tasks involve entirely different data (e.g., movie reviews vs. news articles), there is no (shared) individual-level information. At the group-level, for vision we use annotations for *hair color* and for whether the individual has a *beard*, whereas for language we automatically group inputs by *binary gender*.

Experimental Design. To test if model-sharing influences outcome homogenization, we contrast setting with differing degrees of model-sharing. In the vision experiments, we produce task-specific models for each task by either (i) training from **scratch** on CelebA data, (ii) linearly **probing** by fitting a linear classifier on frozen CLIP [Radford et al., 2021] features, or (iii) **finetuning** CLIP. To ensure meaningful comparisons, the models trained from scratch shared the same ViT architecture [Dosovitskiy et al., 2021] used in CLIP but with weights initialized randomly.

In the language experiments, we further hone in on the specific *adaptation method* used to adapt the foundation model (specifically RoBERTa-base [Liu et al., 2019]) to each task. We consider (i) linear **probing**, (ii) **finetuning**, and (iii) **BitFiT** [Ben Zaken et al., 2022], which is a recent *lightweight finetuning* method in NLP that involves freezing all the RoBERTa weights except the bias parameters which are updated as in finetuning. Consequently, BitFit is an intermediary between probing and finetuning, which has been shown to achieve similar accuracy as finetuning while updating very few of the pretrained parameters. For both vision and for language, all models are trained for the same number of epochs and we repeat each experiment for 5 random seeds per adaptation method.

Hypotheses. Much like data-sharing, model-sharing is graded and is not binary: different downstream systems can share varying degrees of underlying models. By design, our experimental design

⁵https://huggingface.co/bert-base-uncased as of May 2022.

⁶Full reproducibility details for vision are in §B.2; for language are in §B.3.

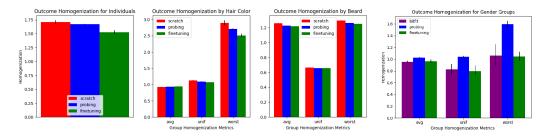


Figure 2: Results for model-sharing experiments showing homogenization as a function of training method for vision (**left three**) and language (**rightmost**).

Vision: scratch is the most homogeneous, then **probing**, then **finetuning**.

Language: probing is the most homogeneous; finetuning and BitFit are similarly homogeneous.

suggests a continuum in sharing: first, downstream system either can share a foundation model or not (**scratch**). Second, among methods that involve foundation models, all methods initialize the weights using the pretrained weights but differ in which parameters remain the same *after* adaptation is completed: **finetuning** changes all the parameters, **BitFit** only changes the bias parameters, and **probing** changes none of the parameters. As a result, overall, we can rank methods from most to least sharing as (i) **probing**, (ii) **BitFit**, (iii) **finetuning**, (iv) **scratch**, which leads us to predict the degree of homogenization will also follow this ranking under our component-sharing hypothesis.

Results. In Figure 2 (**left**), across all vision settings, we surprisingly find that **scratch** is the most homogeneous, i.e., more homogeneous than either approach involving shared foundation models. This is the opposite of what we hypothesized: we posit that this may indicate model sharing is not the key explanatory variable for outcome homogenization here, but instead it is a more complex form of data sharing. Specifically, we conjecture that since the **scratch** models are only trained on **CelebA** data, whereas the others also are trained on the much larger WebImageText via the CLIP foundation model, this may mean that the models based on CLIP are effectively regularized from learning idiosyncrasies of **CelebA** that the **scratch** models acquire. This may more generally suggest that a more correct hypothesis around data sharing should factor in the relationship (e.g., distribution shift) between the training data and the evaluation data for each model. Additionally, we find **probing** is consistently more homogeneous than **finetuning**, which aligns with our hypothesis. Finally, akin to the census results (§4), we once again find that outcome homogenization is significantly higher for individuals than for groups (comparing to H_{avg} and H_{unif}).

In Figure 2 (**right**), across all language settings, we find the ordering of homogenization matches what our hypothesis predicts. Specifically, we find **BitFit** and **finetuning** achieve similar levels of homogeneity, even though **BitFit** updates 0.08% of the parameters full finetuning does (i.e., the number of shared parameters for BitFit is more like probing than finetuning), suggesting the number of shared parameters is not the right lens for understanding model sharing. More broadly, these results do suggest parametersharing effects may contribute to outcome homogenization within the foundation model regime, but comparisons between foundation models and no foundation models may be more complex to explain.

5.2 Correlations between Metrics

Since we introduce several metrics, we measure the correlations between our metrics. Further, we measure correlations with accuracy (specifically, the expected rate of systemic failure) to test if homogenization is disentangled from accuracy. Since outcome homogenization is related to fairness, we also measure the correlation between our metrics and a standard group fairness metric. Fairness metrics are generally defined for a single model h, whereas we study entire systems $\{h^i\}_{i=1}^k$. We extend the fairness definition used by Khani et al. [2019] as the variance in the systemic failure rates across groups.

$$\operatorname{Fairness}_{G}(h^{1},...,h^{k}) \triangleq \operatorname{Var}_{g} \left[\prod_{i} \operatorname{fail}_{g}(h^{i}) \right]$$
 (6)

Results. In Table 1, we report the pairwise correlation between metric pairs, based on the models we trained in $\S 5.1$. These correlations are for 45 systems (3 methods \times 3 groupings \times 5 random seeds) of 2 models for vision and 15 systems of 4 models for language. For vision, our metrics are highly correlated

Table 1: The correlation between our metrics and other metrics. Correlations are (Pearson R^2 , Spearman ρ) with * indicating significance at p = 0.05 and *italics* indicating p = 0.001.

H _{avg}	$H_{ m unif}$	Vision $H_{\mathbf{worst}}$	Accuracy	Fairness	H _{avg}	$H_{ m unif}$	Language $H_{\mathbf{worst}}$	Accuracy	Fairness
$\begin{array}{c c} H_{avg} & - \\ H_{unif} & (0.87, 0.93) \\ H_{worst} & (0.0, 0.96) \end{array}$	(0.87, 0.93) - (0.0, 0.96)	(0.0, 0.96) (0.0, 0.96)	(0.0, 0.09*) (0.0, -0.02) (0.05, 0.1*)	(0.0, 0.74)	(0.22, -0.47) (0.11, 0.56)	(0.22, -0.47) - (0.63, -0.53)	(0.11, 0.56) (0.63, -0.53)	(0.06*, -0.22*) (0.0, 0.19*) (0.02, 0.13)	(0.02, 0.09) (0.0, -0.01) (0.13, 0.47)

with each other, whereas for language, H_{unif} patterns quite differently (columns 1-3, 6-8). This is to be expected in that the vision groups (e.g., hair colors) all share similar frequencies, whereas the female group is significantly rarer in the language datasets. For both language and vision, we find that our metrics are generally not correlated, or perhaps weakly correlated, with accuracy as we intended (columns 4, 9). With respect to fairness, our worst-case metric H_{worst} is strongly correlated for both modalities, but for the other two metrics we see no linear correlations and only monotone correlations for the vision experiments (columns 5, 10). This is in line with our broader expectations that fairness and outcome homogenization are indeed related (especially for the worst-performing group), but that given they are distinct theoretical constructs, they should not always be correlated [Campbell and Fiske, 1959].

5.3 Discussion

Based on our experimental findings for both data-sharing and model-sharing, we provide considerable evidence that sharing in various forms does contribute to homogenization. However, we also provide nuance with our findings, indicating that the simple notion of sharing will need to be refined to properly capture the full effects observed in terms of homogenization. This is particularly relevant when the findings in §4 and §5 are contrasted with each other, given model-sharing in the foundation model regime also implies immense data-sharing in the form of the pretraining data (as mediated by the pretrained initialization). We emphasize that the regimes we study are considerably different: low-dimensional tabular data with simple model families in the data-sharing experiments vs. high-dimensional images/text with large and deep neural networks in the model-sharing, so it is not surprising the results do not fully coincide. Most broadly, we believe a more complete explanation will require factoring in the nature of the various data distributions and the associated distribution shifts (e.g., between pretraining and adaptation) at play. What we believe is clear, however, is that our findings provide an empirical basis to build on our conceptual arguments that sharing in ML can increase homogenization, and that this motivates exploration into whether these effects manifest in deployed high-stakes systems like those used for algorithmic hiring.

Societal Considerations and Challenges

To situate our work in a broader social context, we identify and discuss core challenges in **diagnosing**, **measuring**, and **rectifying** outcome homogenization.

Diagnosis. To diagnose homogenization as a byproduct of monoculture requires knowing which companies rely on the same vendor, dataset, or foundation model. How specific algorithmic systems are constructed is often so opaque that determining the responsibility of a shared component for outcome homogenization is nigh impossible. However, if a high outcome homogenization score was measured across deployments, the measurement itself could justify a request for increased transparency and access. We believe this could be a useful practical mechanism for balancing tensions in auditing to provide conditional access to auditors.

Measurement. Measuring homogenization only requires black box access to algorithmic systems, which is often achievable in practice [see Buolamwini and Gebru, 2018, Raji and Buolamwini, 2019, Metaxa et al., 2021]. However, identifying individual-level effects requires observing outcomes for the same individual across deployments. Due to privacy constraints, correlating individuals across datasets from different companies might be challenging or impossible. Such constraints incentivize the study of homogenization for groups as a more accessible concept, as in §3.2.

Rectification. Even once outcome homogenization is identified, organizations deploying systems responsible for homogeneous outcomes may not be incentivized to reduce it. When outcome homogenization does not align with each organization's interests (e.g., maximizing accuracy), it may be necessary to introduce regulation, policy, or other compliance mechanisms to encourage

organizations to alter their outcomes. Navigating this trade-off is further complicated if the harms of homogeneous outcomes take time to observe or accrue. More optimistically, Kleinberg and Raghavan [2021] show that in some instances, there may not be a trade-off between policies optimal for each organization and those that diversify outcomes for societal benefit.

7 Limitations and Conclusion

We have introduced, formalized, and measured outcome homogenization as a systemic harm that may arise from practices of sharing in ML. Our work has an important limitation: our measure cannot accommodate every setting and may be brittle given that systemic failures are often rare. Furthermore, direct optimization of our measure may not lead to desirable outcomes, potentially contributing to ethics-washing. The interpretation of our measure must be **contextual**: the implications and severity of homogeneous outcomes must be situated in a broader societal context.

Outcome homogenization is essential to comprehensively characterizing algorithmic harm at scale, especially given the trend towards algorithmic monoculture. Without scrutiny, the harms of homogenization may become insidiously entrenched. Consequently, we believe further study and early intervention is necessary to mitigate and prevent such harms in society.

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640 Checklist

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The checklist follows the references. Please read the checklist guidelines carefully for information on how to answer these questions. For each question, change the default **[TODO]** to **[Yes]**, **[No]**, or **[N/A]**. You are strongly encouraged to include a **justification to your answer**, either by referencing the appropriate section of your paper or providing a brief inline description. For example:

- Did you include the license to the code and datasets? [Yes] See Section ??.
- Did you include the license to the code and datasets? [No] The code and the data are proprietary.
- Did you include the license to the code and datasets? [N/A]

Please do not modify the questions and only use the provided macros for your answers. Note that the Checklist section does not count towards the page limit. In your paper, please delete this instructions block and only keep the Checklist section heading above along with the questions/answers below.

- 1. For all authors...
 - (a) Do the main claims made in the abstract and introduction accurately reflect the paper's contributions and scope? [Yes]
 - (b) Did you describe the limitations of your work? [Yes]
 - (c) Did you discuss any potential negative societal impacts of your work? [Yes]
 - (d) Have you read the ethics review guidelines and ensured that your paper conforms to them? [Yes]
- 2. If you are including theoretical results...
 - (a) Did you state the full set of assumptions of all theoretical results? [N/A]
 - (b) Did you include complete proofs of all theoretical results? [N/A]
- 3. If you ran experiments...
 - (a) Did you include the code, data, and instructions needed to reproduce the main experimental results (either in the supplemental material or as a URL)? [Yes]
 - (b) Did you specify all the training details (e.g., data splits, hyperparameters, how they were chosen)? [Yes]
 - (c) Did you report error bars (e.g., with respect to the random seed after running experiments multiple times)? [Yes]
 - (d) Did you include the total amount of compute and the type of resources used (e.g., type of GPUs, internal cluster, or cloud provider)? [Yes]
- 4. If you are using existing assets (e.g., code, data, models) or curating/releasing new assets...
 - (a) If your work uses existing assets, did you cite the creators? [Yes]
 - (b) Did you mention the license of the assets? [Yes]
 - (c) Did you include any new assets either in the supplemental material or as a URL? [N/A]
 - (d) Did you discuss whether and how consent was obtained from people whose data you're using/curating? [Yes]

677 678	(e) Did you discuss whether the data you are using/curating contains personally identifiable information or offensive content? [Yes]
679	5. If you used crowdsourcing or conducted research with human subjects
000	(a) Did you include the full text of instructions given to participants and screenshots, if
680 681	applicable? [N/A]
682 683	(b) Did you describe any potential participant risks, with links to Institutional Review Board (IRB) approvals, if applicable? $[N/A]$
684 685	(c) Did you include the estimated hourly wage paid to participants and the total amount spent on participant compensation? [N/A]

Homogenization Metrics 686

Group Homogenization Metrics 687

In §3.2, we introduced our group level homogenization metrics. Specifically, we note the design 688 decision of how to weight groups and the three weightings we consider: average, uniform, and worst. 689 Here, we provide the full mathematical definition of these metrics. For convenience, let the frequency 690 of group g in a specific dataset D^i by denoted as $p^i(g)$ and the joint probability of the group across 691 all datasets be denoted as $p(g) \triangleq \prod_{i=1}^{k} p^{i}(g)$.

$$H_{\text{avg}}(h^{1},...,h^{k}) \triangleq \frac{\frac{1}{\sum_{g \in \mathcal{G}} p(g)} \sum_{g \in \mathcal{G}} p(g) \text{err}_{g}(h^{1}) \times \cdots \times \text{err}_{g}(h^{k})}{\text{err}(h^{1}) \times \cdots \times \text{err}(h^{k})}$$

$$H_{\text{unif}}(h^{1},...,h^{k}) \triangleq \frac{\frac{1}{|\mathcal{G}|} \sum_{g \in \mathcal{G}} \text{err}_{g}(h^{1}) \times \cdots \times \text{err}_{g}(h^{k})}{\text{err}(h^{1}) \times \cdots \times \text{err}(h^{k})}$$

$$H_{\text{worst}}(h^{1},...,h^{k}) \triangleq \frac{\max_{g \in \mathcal{G}} \text{err}_{g}(h^{1}) \times \cdots \times \text{err}_{g}(h^{k})}{\text{err}(h^{1}) \times \cdots \times \text{err}(h^{k})}$$
(9)

$$H_{\mathbf{unif}}(h^1, \dots, h^k) \triangleq \frac{\frac{1}{|\mathcal{G}|} \sum_{g \in \mathcal{G}} \mathbf{err}_g(h^1) \times \dots \times \mathbf{err}_g(h^k)}{\mathbf{err}(h^1) \times \dots \times \mathbf{err}(h^k)}$$
(8)

$$H_{\mathbf{worst}}(h^1, \dots, h^k) \triangleq \frac{\max_{g \in \mathcal{G}} \mathtt{err}_g(h^1) \times \dots \times \mathtt{err}_g(h^k)}{\mathtt{err}(h^1) \times \dots \times \mathtt{err}(h^k)}$$
(9)

Relating Individual and Group Homogenization

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In §4, we demonstrate empirically that outcomes can be more homogeneous for individuals than for 694 racial groups. Here we provide two scenarios that demonstrate circumstances where individual-level 695 outcome homogenization is greater than, and is less than, group-level outcome homogenization. (Of 696 course, they can also be equal.) In both settings, we will have two applications and two groups, where 697 each group is comprised of two individuals. As a result, $H_{avg} = H_{unif}$, so we can compare either to 698 699

In both settings, we will say Alice and Angelique are members of Group 1 and Bob and Bernardo 700 are members of Group 2. 701

Scenario 1. Let Alice and Bob be misclassified in Application 1 but not 2, and Angelique and Bernardo 702 be misclassified in Application 2 but not 1. No one is misclassified by both models, hence the number 703 of observed systemic failures is 0 at the individual level, hence $H^{\text{individual}} = 0$. However, since there is a 704 failure within Group 1 for both applications (and for Group 2 as well), the number of observed systemic 705 failures is nonzero at the group level, hence $H_{\rm avg}=H_{\rm unif}>0$. Thus, in this scenario, we have seen that individual-level outcome homogenization can be less than group-level outcome homogenization. 706 707

Scenario 2. Let Alice and Bob be misclassified in both applications, and Angelique and Bernardo 708 be misclassified in neither application. At the individual level, there are 2 systemic failures, so the 709 be misclassified in neither application. At the individual level, there are 2 systemic failures, so the observed rate of systemic failure is $\frac{2}{4} = 0.5$. The overall error rate for each application is 0.5, so the expected rate of systemic failure is $0.5 \times 0.5 = 0.25$. Therefore, $H^{\text{individual}} = \frac{0.5}{0.25} = 2$. At the group level, the observed rate of systemic failures is 0.25 for both groups. The overall error rate for each application is still 0.5, so the expected rate of systemic failure is still $0.5 \times 0.5 = 0.25$. Therefore, $H_{\text{avg}} = H_{\text{worst}} = \frac{\frac{1}{2}(0.25 + 0.25)}{0.25} = 1$. Thus, in this scenario, we have seen that individual-level outcome homogenization can be greater than group-level outcome homogenization. 710 711 712 713 714 715

A.3 Generalizing Individual-Level Metric

In §3.3, we note that our individual-level framing assumes that every individual j produces inputs 717 x_i^i for every company i. The formalism in the main paper already permits these inputs to be different 718 across companies for the same individual (e.g., Bob may submit different resumes when applying 719 to Microsoft and Google). However, the formalism does not support two further general concepts: 720 (i) multiple inputs per company and (ii) no inputs for some company (e.g., Bob does not apply to 721 Amazon). To accommodate the former, we note that the notion of failure can be modified depending 722 on how the outcomes for the multiple inputs should be aggregated (e.g., a failure of a search engine may be determined by some fraction of search queries producing poor results for the user).

To address the latter concern, we introduce notation c_j to indicate the subset of companies that individual j interacts with, i.e., $c_j \subseteq \{1,...,k\}$. That is, any companies $i \in \{1,...,k\}$ that are not in c_j are those that individual j does not interact with. Accordingly, we definite $H^{\text{individual}}$ as:

$$H^{\text{individual}}(h^{1},...,h^{k}) \triangleq \frac{\mathbb{E}\left[\prod_{i \in c_{j}} I^{i}(x_{j}^{i})\right]}{\mathbb{E}\left[\prod_{i \in c_{j}} \text{fail}(h^{i})\right]}$$
(10)

Notably, when $\forall j, c_j = [k]$, the denominator simplifies to $\prod_{i \in [k]} \mathtt{fail}(h^i)$, which matches Equation 3.

729 A.4 Alternative Metrics

In §3, we introduce the metrics we use to quantify outcome homogenization. Of course, much like the many mathematical expressions that have been used to measure bias and fairness, there are many ways to reasonably measure homogenization. Fundamentally, given the underlying construct of outcome homogenization is largely new, we begin by recognizing our understanding of the concept is incomplete and likely will require study in real systems to truly identify the precise desiderata for a measure.

In the interim, it is difficult to assess if the metric has *structural fidelity* [Loevinger, 1957], i.e., does the metric's structure faithfully captures outcome homogenization? Further, it is unclear if the metric has sufficient predictive validity to predict long-term outcomes (e.g., longitudinal harms arising from outcome homogenization) or how useful it is for testing specific scientific and social hypotheses [Jacobs and Wallach, 2021]. Ultimately, we believe the key test for the metric will be its *consequential validity* [Messick, 1987]: will the metric yield positive social impact as it "both reflects structure in the world and imposes structure upon the world" [Hand, 2016].

To facilitate understanding, we transparently discuss other metrics we considered and why they may
be preferable in some circumstances. Ultimately, we worked with the metrics we describe in the paper
as we found them to be the simplest and preferred their probabilistic interpretations, but we include
reasons to prefer alternative as we describe them.

746 A.4.1 Alternative Metrics in the Binary Setting

Covariance and Pointwise Mutual Information. When k=2, i.e., there are two companies, we note that our metric bears a very close resemblance to the *covariance* between the (indicator) random variables I^1 and I^2 . In particular, the covariance is the difference of the quantities that define the ratio for our homogenization metric. Similarly, our metric is the *pointwise mutual information* (PMI) evaluated at (1,1) up to the \log .

$$H^{\text{individual}}(h^1, h^2) = \frac{\underset{j}{\mathbb{E}}[I^1 I^2]}{\underset{j}{\mathbb{E}}[I^2]} \tag{11}$$

$$\operatorname{Cov}(I^{1}, I^{2}) = \underset{j}{\mathbb{E}} \left[I^{1} I^{2} \right] - \underset{j}{\mathbb{E}} \left[I^{1} \right] \underset{j}{\mathbb{E}} \left[I^{2} \right]$$
(12)

$$PMI(I^{1}=1,I^{2}=1) = \log \left(\frac{\mathbb{E}\left[I^{1}I^{2}\right]}{\mathbb{E}\left[I^{1}\right]\mathbb{E}\left[I^{2}\right]} \right) = \log \left(H^{\mathbf{individual}}(h^{1},h^{2})\right)$$
(13)

With respect to the covariance, we prefer that our metric is more naturally comparable across settings where the failure rates of social systems vary, whereas the covariance is more directly tied to the absolute scale of the failure rates. With respect to the pointwise mutual information, we note that we are simply looking at the behavior of the social system in a special case where all models fail (which is one of the 2^k possible outcomes an individual could receive overall), whereas the overall PMI considers all of them and is invariant to symmetries that are significant in our setting. Further, both are traditionally studied in the binary setting, whereas we study behavior in settings where k > 2.

Pearson Correlation. Building on the relationship with the covariance, we note that our metric therefore also resembles the *Pearson correlation*.

$$H^{\text{individual}}(h^1, h^2) = \frac{\mathbb{E}\left[I^1 I^2\right]}{\mathbb{E}\left[I^1\right] \mathbb{E}\left[I^2\right]}$$

$$\operatorname{Corr}(I^1, I^2) = \frac{\mathbb{E}\left[I^1 I^2\right] - \mathbb{E}\left[I^1\right] \mathbb{E}\left[I^2\right]}{\sqrt{\left(\mathbb{E}\left[I^1\right] \left(1 - \mathbb{E}\left[I^1\right]\right)\right) \left(\mathbb{E}\left[I^2\right] \left(1 - \mathbb{E}\left[I^2\right]\right)\right)}}$$

$$\tag{15}$$

$$\operatorname{Corr}(I^{1}, I^{2}) = \frac{\mathbb{E}\left[I^{1}I^{2}\right] - \mathbb{E}\left[I^{1}\right]\mathbb{E}\left[I^{2}\right]}{\sqrt{\left(\mathbb{E}\left[I^{1}\right]\left(1 - \mathbb{E}\left[I^{1}\right]\right)\right)\left(\mathbb{E}\left[I^{2}\right]\left(1 - \mathbb{E}\left[I^{2}\right]\right)\right)}}$$
(15)

In particular, when dealing with accurate models that are homogeneous (i.e., $\mathbb{E}\left[I^{1}I^{2}\right]>>$ 761 $\mathbb{E}[I^1]\mathbb{E}[I^2]$), the Pearson correlation coefficient approximates our metric up to the square root in 762 the denominator. Arguments can be made in favor and against this square root (and more generally 763 a k-th root for k > 2); for simplicity we favor our metric that does not introduce such normalization but 764 acknowledge this normalization may prove to be more favorable as the metric is further stress-tested. 765

Alternative Metrics beyond the Binary Setting

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As we note in Footnote 2, our formalism and metrics are designed to be general, meaning that they can 767 accommodate settings where the models h^i correspond to different tasks or scenarios. (We make use of 768 this generality in our experiments (§5) for vision and, especially, language.) To permit this generality, 769 we (reductively) binarize outcomes as either failures or not in our use of the indicator functions I^i . 770 In particular, for arbitrarily different tasks, the outcome spaces and their consequences on individuals 771 may not be (easily) related. 772

In some settings, specifically those where the tasks that constitute the social system are sufficiently 773 similar, we may instead prefer a more graded loss in the place of the binary notion of failures. For 774 each deployment by company i, denote the associated loss function as \mathcal{L}^i such that $\mathcal{L}^i(h^i(x_i^i), y_i^i) = \ell_i^i$ 775 is the loss experienced by individual j when interacting with model h^i . In these settings, where the loss achieved across different applications is comparable, we can consider additional measures for homogenization in terms of this loss.

$$H^{\text{individual}}(h^1,...,h^k) = \frac{\mathbb{E}_j^{\left[\prod_i \ell_j^i\right]}}{\prod_i \left[\mathbb{E}_j \ell_j^i\right]}$$
(16)

$$\operatorname{MinExp}(h^{1},...,h^{k}) = \frac{\mathbb{E}\left[\min_{i} \ell_{j}^{i}\right]}{\min_{i} \left[\mathbb{E} \ell_{j}^{i}\right]}$$

$$\operatorname{ExpExp}(h^{1},...,h^{k}) = \frac{\mathbb{E}\left[\min_{i} \ell_{j}^{i}\right]}{\mathbb{E}\left[\mathbb{E} \ell_{j}^{i}\right]}$$

$$(17)$$

$$\operatorname{ExpExp}(h^{1},...,h^{k}) = \frac{\mathbb{E}\left[\min_{i} \ell_{j}^{i}\right]}{\mathbb{E}\left[\mathbb{E}\left[\ell_{j}^{i}\right]\right]}$$
(18)

(19)

In words, the MinExp definition is the ratio of the average best-case loss for individuals with the loss of the best model h^{best} and the ExpExp definition is the same but the denominator is the average loss of the models rather than the best loss. These definitions bear close resemblance to the MaxMin and lexicographic (leximax and leximin) fairness definitions studied in the fairness literature [Dubins and Spanier, 1961, Henzinger et al., 2022]; the group-weighted analogue that use the worst group weighting recovers the MaxMin definition in the denominator. (Note that the naming conventions are reversed since we define metrics in terms of loss whereas work in fairness and equitable allocations generally defines metrics in terms of utility.)

When the loss is the 0-1 classification loss, the MinExp definition and $H^{individual}$ are very similar: 787 the numerators are the same (as the product of indicator variables is the same as their minimum) and 788 the denominators are precisely $z = \frac{\prod_{i=1}^{k} \mathtt{fail}(h^{i})}{\mathtt{fail}(h^{\text{best}})}$ factors of each other (i.e., the failure rate of all of the models except the best one). Consequently, the MinExp yields values in the range [0,1] whereas 789 790

 $H^{ ext{individual}}$ is in $[0,\infty)$. Independent behavior across models in $H^{ ext{individual}}$ is guaranteed to be 1 and maximal systemic failure in MinExp is guaranteed to be 1; symmetrically, independent behavior in MinExp is z (which is non-constant) and maximal systemic failure in $H^{ ext{individual}}$ is $\frac{1}{z}$.

More broadly, the indicator variables we use in the main paper can be seen as a special case when using 794 the 0-1 classification loss whereas arbitrary loss functions can be mapped to indicators by thresholding 795 the loss (which does not require the loss to comparable, as different thresholds can be applied for 796 different deployments). As a result, both $H^{individual}$ and MinExp have clear merits; we believe MinExp 797 may especially be a more natural definition where individuals have *choices* on which model h^i to 798 interact with of the k possible models. In these settings (e.g., picking which voice assistant to use, 799 or more generally consumer products), the losses will naturally be comparable and it may suffice for 800 the individual to have one good option, which is more smoothly encoded by the minimum of the loss 801 rather than the product of the indicators. 802

We encourage future work to explore whether the MinExp or $H^{\text{individual}}$ is preferable: in many settings we expect they will be strongly correlated given they are scalings of each other that depend not on the correlated nature of errors but the overall error rates, but they may be some settings where they diverge and one is clearly preferable to the other. Currently, we recommend work to also consider MinExp when the losses are comparable, but to default to $H^{\text{individual}}$ since this is not required and $H^{\text{individual}}$ has a simple probabilistic interpretation.

809 B Reproducibility

All of the code required to train the models, group inputs for group-based metrics, measure homogenization, and generate visualizations will be released upon acceptance. Additionally, to facilitate accessibility we will release a simple tool to compute our homogenization metrics. We provide further experimental details below.

814 B.1 Census Experiments

B.1.1 Data

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We work with the ACS PUMS data introduced by Ding et al. [2021], which contains US Census survey data for 3.6 million individuals. Ding et al. [2021] introduce the dataset to facilitate research into algorithmic fairness and the measurement of harms associated with algorithmic systems. For each individual in the Census, 286 features are recorded (e.g., self-reported race and sex, occupation, average hours worked per week, marital status, healthcare status). Ding et al. [2021] construct several classification tasks using this data, where each task uses some of an individual's features as inputs and one of their features as the label for the prediction task (e.g., predicting if an individual's income exceeds \$50000). Of these tasks, we work with three in particular: **ACSEmployment** (predict if an individual is employed), ACSIncomePovertyRatio (predict an individual's income normalized by the poverty threshold), and ACSHealthInsurance (predict if an individual has health insurance). Following Ding et al. [2021], we split the data 80/20 for train/test. We access this data through their folktables package. We use the data for all of the US (they provided state-level data as well) from 2018, which is the primary data they analyze in their paper. We select these tasks because Ding et al. [2021] do not impose any filtering constraints in selecting data for these tasks, meaning all three tasks are posed for the same underlying individuals. See Ding et al. [2021] for more details. License information is provided at https://github.com/zykls/folktables#license-and-terms-of-use and our use of the dataset adheres to these terms of service. The data clearly can be personally identifying given it has census records for particular individuals, but there is no offensive content.

B.1.2 Models

Following Ding et al. [2021], we train logistic regression models using sk-learn [Pedregosa et al., 2011] with default hyperparameters. As a sanity check, we compared average model performance and saw it matched/exceeded what is reported in Ding et al. [2021]. For each setting (**fixed**, **disjoint**) and amount of training data, we trained 25 models across 5 random subsamples of training and 5 random seeds for model run per subsample, for each of the three tasks. In aggregate, all of the models we

⁷https://github.com/zykls/folktables

trained took approximately 10 hours across 5 NVIDIA Titan Xp GPUs (or 50 hours on 1 NVIDIA Titan Xp GPU), with additional experiments/debugging that is unreported in the paper taking approximately an additional 400 NVIDIA Titan Xp GPU hours.

BA3 B.1.3 Groupings

We consider racial groups, which are already provided in the dataset based on the self-identified category individuals chose in providing their information to the US Census. The specific racial categories used are: White alone, Black/African American alone, American Indian alone, Alaska Native alone, American Indian and Alaska Native, Asian alone, Native Hawaiian and Other Pacific Islander alone, other unspecified race, two or more races.

849 **B.2 Vision Experiments**

850 **B.2.1 Data**

851 We work with the **CelebA** dataset [Liu et al., 2015], which is a widely used dataset of celebrity faces paired with annotations for facial attributes. For each face image, given the associated attributes, 852 we define two tasks (Earrings, Necklace) that involve predicting whether the individual is wearing the specific apparel item. Attribute prediction in CelebA has been studied previously in work on fairness and robustness [Sagawa* et al., 2020, Khani and Liang, 2021, Wang et al., 2021]. Given 855 recent documentation of significant issues with computer vision datasets [e.g., Birhane and Prabhu, 856 2021, Birhane et al., 2021, we emphasize that we use the dataset solely for analytic reasons to study 857 homogenization. Further, given works like GenderShades [Buolamwini and Gebru, 2018] that highlight 858 the harms of face recognition, we emphasize that we do not use the dataset for face recognition, but 859 instead consider apparel prediction tasks where each apparel item/accessory is clearly observable in the 860 face image. In addition to Earrings and Necklace, the dataset also contains attributes for Eyeglasses 861 and **Neckties**. We initially included these tasks, but observed no individual was misclassified for 862 863 all four tasks since these two tasks were very easy and models rarely produced any errors (e.g., the error rate for **Eveglasses** was generally less than 1%). To be able to present non-trivial results for 864 individual-level outcome homogenization, we therefore removed these tasks from consideration so 865 that a nonzero number of systemic failures could be observed. We downloaded the CelebA data from 866 https://mmlab.ie.cuhk.edu.hk/projects/CelebA.html. We resized images to 224-by-224, 867 and then apply the same augmentations as in CLIP [Radford et al., 2021], before feeding the image into 868 the ViT-B/16 (which is what Radford et al. [2021] do as well). License information is provided here: 869 https://mmlab.ie.cuhk.edu.hk/projects/CelebA.html. Our use of the dataset is consistent with the requirements for non-commercial research use. The data clearly can be personally identifying 871 given it has face images for particular individuals, but there is no offensive content. 872

B.2.2 Models

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Following Radford et al. [2021], we either use their released 150M parameter ViT-B/16 CLIP model (the 875 largest publicly available CLIP model at the time of writing) or a randomly initialized model with the same architecture. We used code from the official CLIP repository at https://github.com/opena 876 i/CLIP. Since Radford et al. [2021] modify the standard Vision Transformer [Dosovitskiy et al., 2021], 877 we use their modified version for our *scratch* models. As a sanity check of our implementation, we con-878 firmed that our average finetuning accuracy were comparable to prior work (Sagawa* et al. [2020] paper 879 considers the task of predicting Blonde hair, with an ImageNet pretrained ResNet-50, they get 94.8% and 880 we get 95.9% in this particular task, i.e., when we also do the task of predicting Blonde hair with the same 881 ImageNet pretrained ResNet-50). Further, on the **Wearing Earrings** task, we also confirmed that the 882 CLIP pretrained ViT-B/16 did better than a ResNet-50 (both ImageNet pretrained and CLIP pretrained). 883 For each setting (scratch, probing, finetuning), we trained 5 model runs with different seeds, for each 884 885 of the tasks. The final learning rates we used were 0.003 (training from scratch), 0.01 (linear probing), 0.000003 (fine-tuning), and they were selected by grid searching the learning rates on the **Earrings** task 886 and we sanity checked that choosing a higher or lower learning rate led to lower accuracy. We also train 887 each approach for 10 epochs to ensure similar computational resources are provided to each approach. In 888 aggregate, all of the models we trained took approximately 1000 hours on one NVIDIA Titan Xp GPU.

B.2.3 Groupings

We consider groups based on hair color. The dataset provides five hair-related annotations of Black, Brown, Blonde, Grey, and Bald. Since the Bald category was quite small, we collapsed the category with all examples that lacked a hair annotation (e.g., the hair color is obscured due to a hat) into an "Other" category to yield five total categories. In addition, we measure outcome homogenization for individuals based on whether they have a *beard*. While the **CelebA** dataset also contains annotations for race and gender, we chose to not look at these groups given we were concerned that the gender/race was being inferred by an annotator (crowdworker) from the face rather than being self-identified [Liu et al., 2015].

898 B.3 Language Experiments

899 B.3.1 Data

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We use the **IMDB**, **AGNews**, **Yahoo**, and **HateSpeech18** datasets. For **IMDB**, we were unable to find formal license information. The data may contain some PII, but it is unlikely there is significant offensive content. For **AGNews**, we were unable to find formal license information but found information indicating it should be used non-commercially, which we adhere to see. The data may contain some PII, but it is unlikely there is significant offensive content. For **Yahoo**, we were unable to find formal license information. The data may contain some PII, especially given its nature, but it is unlikely there is significant offensive content. For **HateSpeech18**, we adhere to the license provided here: https://github.com/Vicomtech/hate-speech-dataset#license. The data likely contains some PII given it is from forums, and certainly contains offensive content. We access this data through Hugging Face Datasets [Lhoest et al., 2021]. The associated papers describe how the data was collected or scraped. We tokenize the data using the RoBERTa [Liu et al., 2019] tokenizer provided in Hugging Face Transformers [Wolf et al., 2020].

2 B.3.2 Models

For all models we produced, we adapt RoBERTa-base [Liu et al., 2019] using the weights provided 913 through Hugging Face Transformers [Wolf et al., 2020]. For all models, we use the default hyperparame-914 ters in the Trainer provide in the Transformer library, with the only change being a fairly standard setting 915 of the learning rate to 2e-5. As a sanity check of our implementation, we confirmed that our accuracy 916 matches those provided in standard scripts/tutorials provided in Transformers and are quite similar 917 to other works that work with these standard datasets [e.g., Gururangan et al., 2019]. For each setting 918 (probing, finetuning, BitFit), we trained 5 model runs with different seeds, for each of the four tasks. In aggregate, all of the models we discuss in the paper took approximately 36 hours across 5 NVIDIA Titan Xp GPUs (or 180 hours on 1 NVIDIA Titan Xp GPU), with additional experiments/debugging 921 that is unreported in the paper taking approximately an additional 2000 NVIDIA Titan Xp GPU hours. 922

B.3.3 Groupings

consider Since we four deployments that are largely unre-924 lated other, there annotations individuals 925 to each are no of or groups available that apply across all four datasets. Conse-926 quently, group inputs (binary) gender, this we by as group-927 datasets.10 Specifically, applies the four ing across for 928 identify each input whether the contains more ref-929 we input female like erences to the gender (e.g., uses of words 930 gender, "she"), the male reference to explic-931 or no an itly gendered We acknowledge this term is made. that 932 treats gender a binary part of an unfortunate trend as as 933 in **NLP** works involving gender using binaries [Cao and 934

⁸See http://groups.di.unipi.it/~gulli/AG_corpus_of_news_articles.html.

⁹https://huggingface.co/datasets

¹⁰We also considered grouping by *names*, given recent works showing systemic behavior in NLP models for names [Shwartz et al., 2020, Romanov et al., 2019], and by *race*, using names that are strongly statistically associated [Tzioumis, 2018, Garg et al., 2018]. However, we found few systemic failures that we traced to the underlying groups: very few names appear in every dataset (often because the fictional movie characters and actors in **IDMB** are not discussed in the rest).

Daumé III, 20201. We peer-reviewed use the list gen-935 [2018] der terms from Garg et al. and in accordance with 936 recommendations Mimno [2021]. the Antoniak and In of 937 genthe that same number male and female event the of 938 der mentioned (possibly for both) in interms are zero an 939 put. we grouped the input in a third "Other" category. While 940 941 we did not extensively test. we did observe that the findsmall sensitive perturbations (i.e., 942 ings were not to randeletions words from lists dom of each list) of the we 943 used. 944 Following Antoniak Mimno [2021], provide the lists and we exact be-945 low. 946

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Male words = {"he", "son", "his", "him", "father", "man", "boy", "himself", "male", "brother", "sons", 948 "fathers", "men", "boys", "males", "brothers", "uncle", "uncles", "nephew", "nephews"}
Female words = {"she", "daughter", "hers", "her", "mother", "woman", "girl", "herself", "female", "sis-949 950 ter", "daughters", "mothers", "women", "girls", "femen", "sisters", "aunt", "aunts", "niece", "nieces"} 951

Additional Experiments \mathbf{C} 952

Summary. In §4, we report results on the ACS PUMS dataset. Here, we supplement those findings to 953 clarify whether the findings generalize across model families and to other datasets. Qualitatively, across 954 these additional evaluations, we do find the findings transfer: (i) the **fixed** partition of the data, where 955 there is strictly greater data-sharing, reliably yields greater homogenization and (ii) when group-level 956 data is available, individual-level homogenization exceeds group-level homogenization in magnitude. 957

Datasets. In §4, we report results on the ACS PUMS dataset. Here, we replicate the experiments performed in that section, but vary the dataset to clarify if the qualitative trends generalize to other datasets. Recall that the structure of the data we deal with is fairly unusual: we are interested in datasets where each input is associated with multiple outcomes (i.e., the traditional multi-task learning setting) as we will share the training data across the models for each task. However, because of our interests in social outcomes, we would further like each input to be meaningfully associated with a person (e.g., arbitrary multi-task learning datasets could be used but are unideal if they don't additionally have this human-centric structure).

To identify additional relevant datasets, we survey datasets for multi-task learning, datasets for fairness 966 in ML (which are generally human-centric as desired), and work at the intersection of fairness and 967 multi-task ML. Of these, we looked at Zhang and Yang [2017] for multi-task learning as well as 968 https://paperswithcode.com/task/multi-task-learning, which provided a list of 51 969 datasets. We also looked at the 15 fairness datasets surveyed by Le Quy et al. [2022]. Finally, Wang 970 et al. [2021] initiated the study of multi-task fairness, considering four datasets. 971

From all of these, we arrived at four datasets with the structure we wanted: CelebA, UCI Adult, LSAC 972 [Wightman et al., 1998], and GC [German Contracts; Dua and Graff, 2017]. All of these datasets 973 have the desired structure: each input x_i^j is directly associated with an individual j and corresponds to multiple outcomes $y_i^1, ..., y_i^k$. Of them, we report results for **CelebA** in §5.1, and we use the **ACS PUMS** 975 dataset of Ding et al. [2021] that was explicitly designed to supersede the similar US Census-based 976 UCI Adult. Hence, we turn our attention to GC and LSAC. 977

The GC dataset contains information on 1000 German contracts, including credit history, credit 978 amount, and the corresponding credit risk for that individual [Dua and Graff, 2017]. Following Wang 979 et al. [2021], the two prediction tasks we consider are (i) predicting if the individual receives a good 980 or bad loan and (ii) predicting whether their credit amount exceeds 2000.¹¹ We additionally featurize 981 in the same way as Wang et al. [2021], using 16 attributes as features. The data is accessed through the UCI Machine Learning Repository¹² and we use an 80/20 train-test split like Wang et al. [2021]. All other experimental conditions match what we describe for the data-sharing experiments in §4 with 984 further details given in §B.1.

¹¹We filter any individuals where only one of the outcomes is reported.

¹²https://archive.ics.uci.edu/ml/datasets/statlog+(german+credit+data)

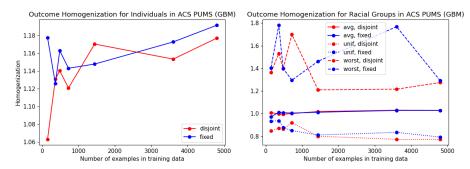


Figure 3: Results for data-sharing experiments on **ACS PUMS** with gradient boosted classifiers showing homogenization (y) as a function of training dataset size (x). Training across tasks on the same data (**fixed**) yields more homogeneous outcomes than on non-identical but identically distributed data (**disjoint**), especially for small datasets.

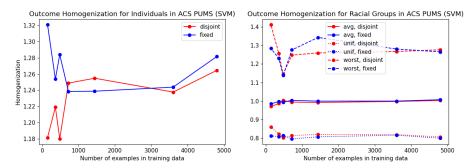


Figure 4: Results for data-sharing experiments on **ACS PUMS** with support vector machines showing homogenization (y) as a function of training dataset size (x). Training across tasks on the same data (**fixed**) yields more homogeneous outcomes than on non-identical but identically distributed data (**disjoint**), especially for small datasets.

The **LSAC** dataset was generated by the Law School Admission Council in the United States [Wightman et al., 1998]. This dataset contains information on 21,790 law students such as their entrance exam scores (LSAT) and their undergrad grade-point average (GPA) collected prior to law school. From this, the two prediction tasks we consider are predicting (i) whether they pass the bar exam and (ii) whether their law school GPA exceeds the mean, directly following Wang et al. [2021]. The data is accessed through the tempeh package with the default train-test split. All other experimental conditions match what we describe for the data-sharing experiments in §4 with further details given in §B.1.

Model Families. In §4, we report results using logistic regression as the model family. Here, we replicate the experiments performed in that section, but vary the model family to clarify the influence of the model family in the homogenization of outcomes. Specifically, we consider three additional model families: gradient boosted decision tree classifiers (GBM), ¹⁵ support vector machines, and neural networks. All of these models are implemented using sk-learn [Pedregosa et al., 2011] with default parameters.

Results and Analysis. We report additional results for **ACS PUMS** in Figures 3–5, for **LSAC** in Figures 6–8, and for **GC** in Figures 9–12. Across these figures, we first establish that our core findings are upheld: (i) homogenization is reliably greater when there is more homogenized (**fixed**) than less (**disjoint**) across datasets and model families and (ii) homogenization is reliably greater when contrasting individual-level measures with the appropriate racial group-level measures. ¹⁶ However, we do note the absolute scale of homogenization is quite different across the datasets: we note that this is

¹³We filter any students where only one of the outcomes is reported.

¹⁴https://github.com/microsoft/tempeh

¹⁵Also considered by Ding et al. [2021] in their work with **ACS PUMS**.

¹⁶**ACS PUMS** is the only dataset where we have race metadata.

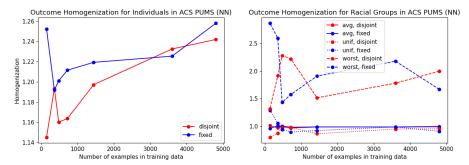


Figure 5: Results for data-sharing experiments on **ACS PUMS** with neural network classifiers showing homogenization (y) as a function of training dataset size (x). Training across tasks on the same data (**fixed**) yields more homogeneous outcomes than on non-identical but identically distributed data (**disjoint**), especially for small datasets.

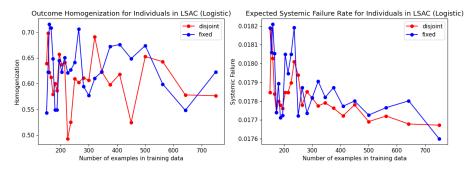


Figure 6: Results for data-sharing experiments on **LSAC** with logistic regression classifiers showing homogenization (**left**) and expected systemic failure rate $(\prod_{i \in [k]} \mathtt{fail}(h^i); \mathbf{right})$, which is the denominator in homogenization, as a function of training dataset size (x).

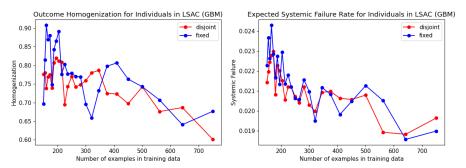


Figure 7: Results for data-sharing experiments on **LSAC** with gradient boosted classifiers showing homogenization (**left**) and expected systemic failure rate $(\prod_{i \in [k]} \mathtt{fail}(h^i); \mathbf{right})$, which is the denominator in homogenization, as a function of training dataset size (x).

not surprising given the datasets are quite different, as are the relationship between the prediction tasks within a dataset. Therefore, we highlight that our hypotheses make predictions about relative change (i.e., sharing increases homogenization), but the underlying homogenization and absolute quantities will also depend significantly on the structure of the data and relationship between prediction tasks.

Further, for the **LSAC** and **GC** datasets, we visualize how the expected systemic failure rate (i.e., the product of the error rates of the models, which is the denominator in our homogenization metric) changes as a function of data scale. What we find is for both datasets, even one we have sufficient samples that the systemic failure rates in both the **disjoint** and **fixed** settings are identical (i.e., variance

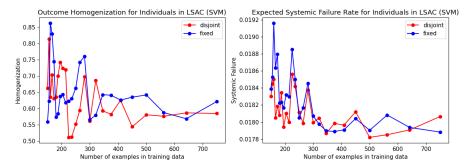


Figure 8: Results for data-sharing experiments on **LSAC** with support vector machines showing homogenization (**left**) and expected systemic failure rate $(\prod_{i \in [k]} \mathtt{fail}(h^i); \mathbf{right})$, which is the denominator in homogenization, as a function of training dataset size (x).

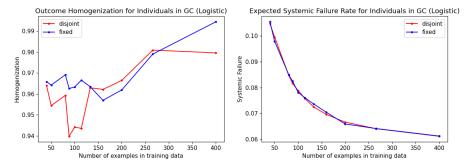


Figure 9: Results for data-sharing experiments on GC with logistic regression showing homogenization (left) and expected systemic failure rate $(\prod_{i \in [k]} \mathtt{fail}(h^i); \mathtt{right})$, which is the denominator in homogenization, as a function of training dataset size (x).

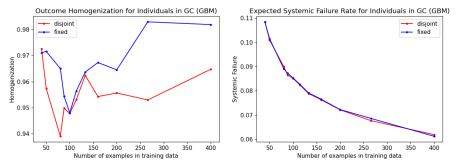


Figure 10: Results for data-sharing experiments on **GC** with gradient boosted classifiers showing homogenization (**left**) and expected systemic failure rate $(\prod_{i \in [k]} \mathtt{fail}(h^i); \mathbf{right})$, which is the denominator in homogenization, as a function of training dataset size (x).

due to finite sample effects in error rates becomes minimal), we see higher homogenization. This demonstrates an important point: as the data grows, the expected systemic failure rate converges (as expected) to the same value for the **disjoint** and **fixed** partitions. That is, if one pays attention only to the accuracies for each task, these systems are the same. But even at this state, we see sizable discrepancies in outcome homogenization (i.e., the *observed* systemic failure rates remain different) with the **fixed** partition displaying greater homogenization. This drives home the point that data-sharing here has no effect on the accuracies of the resultant models, but that it does yield

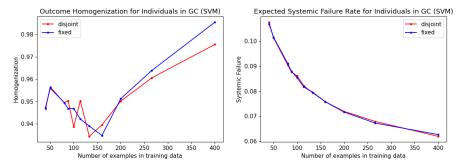


Figure 11: Results for data-sharing experiments on **GC** with support vector machines showing homogenization (**left**) and expected systemic failure rate $(\prod_{i \in [k]} \mathtt{fail}(h^i); \mathbf{right})$, which is the denominator in homogenization, as a function of training dataset size (x).

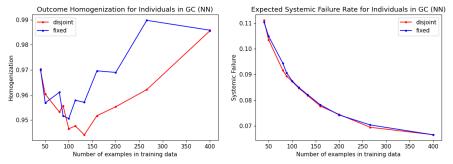


Figure 12: Results for data-sharing experiments on \mathbf{GC} with neural network classifiers showing homogenization (**left**) and expected systemic failure rate $(\prod_{i \in [k]} \mathtt{fail}(h^i); \mathbf{right})$, which is the denominator in homogenization, as a function of training dataset size (x).

greater homogenization. This demonstration is reminscent of work that demonstrates¹⁷ the existence of models of (near) equal accuracy but that are simpler [Semenova et al., 2022] or more fair [Marx et al., 2020]. Here we observe a Rashomon effect [Breiman, 2001] at the level of social systems: both systems achieve the same accuracies, but one (**disjoint**) is more homogeneous than the other (**fixed**).

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¹⁷Generally these works show the existence of such models is theoretically guaranteed. We encourage future work to provide similar guarantees for the systems we describe, beyond our initial empirical demonstrations