

Integrating Factor

$$\frac{dy}{dx} = x^5 e^x + \frac{4y}{x}$$

$$e^{-4 \ln x} \left(\frac{dy}{dx} - \frac{4y}{x} = x^5 e^x \right) x^{-4}$$

$$e^{-\frac{4}{x}} \left(\frac{dy}{dx} - \frac{4y}{x} = x^5 e^x \right)$$

$$\int \left(\frac{dy}{dx} e^{-\frac{4}{x}} - \frac{4y}{x} e^{-\frac{4}{x}} \right) = \int x^5 e^x (x^{-4})$$

$$y e^{-\frac{4}{x}} =$$

$$y x^{-4} = x e^x$$

$$y = x^5 e^x - \frac{e^x}{x^4} + \frac{C}{x^4}$$