

Name: _____

ID : _____

CSE 130, Fall 2014: Midterm Examination

Nov 6th, 2014

- Do **not** start the exam until you are told to.
- This is a open-book, open-notes exam, but with no computational devices allowed (such as calculators/cellphones/laptops).
- Do **not** look at anyone else's exam. Do **not** talk to anyone but an exam proctor during the exam.
- Write your answers in the space provided.
- Wherever it gives a line limit for your answer, write no more than the specified number of lines. *The rest will be ignored.*
- Work out your solution in blank space or scratch paper, and only put your answer in the answer blank given.
- In all exercises, you are allowed to use the "@" operator.
- Good luck!

| | | |
|-------|-----------|--|
| 1. | 20 Points | |
| 2. | 20 Points | |
| 3. | 10 Points | |
| 4. | 10 Points | |
| TOTAL | 60 Points | |

1. [20 points] Consider the following data type for representing arithmetic expressions with constants, variables and binary operators:

```
type expr =  
  | Const of int  
  | Var of string  
  | Op of string * expr * expr;;
```

For example:

- `Op ("+", Var "a", Const 4)` represents `a+4`
 - `Op ("+", Var "a", Op ("-", Var "b", Const 4))` represents `a+(b-4)`
- a. [10 points] You will write a function `rename_var : expr -> string -> string -> expr` which renames variables. In particular, given an expression `e`, and two variable names `n1` and `n2`, `(rename_var e n1 n2)` returns a new expression in which all occurrences of variable `n1` have been replaced with variable `n2`. For example:

```
# rename_var (Op ("+", Var "a", Const 4)) "a" "b";;  
- : expr = Op ("+", Var "b", Const 4)  
  
# rename_var (Op ("+", Var "a", Const 4)) "b" "c";;  
- : expr = Op ("+", Var "a", Const 4)  
  
# rename_var (Op ("+", Op ("*", Var "x", Var "y"), Op ("-", Var "x", Var "z"))) "x" "y";;  
- : expr = Op ("+", Op ("*", Var "y", Var "y"), Op ("-", Var "y", Var "z"))
```

Fill in the code below for `rename_var`:

```
let rec rename_var e n1 n2 =
```

```
-----  
  
-----  
  
-----  
  
-----  
  
-----  
  
-----
```

- b. [10 points] You will write a function `to_str : expr -> string` which takes an expression and returns a string representation of that expression. For example:

```
# to_str (Op ("+", Var "a", Const 4));  
- : string = "a+4"  
  
# to_str (Op ("+", Const 10, Op ("+", Const 10, Var "b")));  
- : string = "10+(10+b)"  
  
# to_str (Op ("+", Op ("*", Var "x", Var "y"), Op ("-", Var "x", Var "z")));  
- : string = "(x*y)+(x-z)"
```

Carefully note the behavior of parentheses: parentheses are added around binary expressions, *except* if the expression is at the top-level, in which case no parentheses are added. In particular, the nested expressions above, like “10+b” and “x*y”, have parentheses around them, but “a+4” does *not* have parentheses, because the expression is at the top-level.

Fill in the code for `to_str` below. You will want to make use of the built-in OCaml function `string_of_int : int -> string` which converts an integer to its string representation, and the `^` operator which concatenates two strings.

```
let to_str e =
```

```
  let rec str_helper e top_level =
```

```
    -----  
    -----  
    -----  
    -----  
    -----  
    -----  
    -----  
    -----
```

```
  in
```

```
    str_helper e true;;
```

Scratch space to work out your answers:

2. [20 points] You will use `fold_left` to write a function `average_if : (int -> bool) -> int list -> int`. Given a “tester” function `f` and a list `l` of integers, `average_if f l` returns the average of all integers in `l` for which `f` returns true, or 0 if `f` returns false for all integers in `l`. For example:

```
# let even x = x mod 2 = 0;;
val even : int -> bool = <fun>

# average_if even [1;2;3;4;5];; (* returns average of 2,4 -> 3*)
- : int = 3

# average_if even [1;2;3;4;5;6;7;8];; (* returns average of 2,4,6,8 -> 5 *)
- : int = 5

# average_if even [1;3;5;7];; (* no even numbers -> 0 *)
- : int = 0
```

Fill in the implementation of `average_if` below. Recall that the type of `fold_left` is:

`fold_left: ('a -> 'b -> 'a) -> 'a -> 'b list -> 'a`

Hint: The accumulator is a pair.

```
let average_if f l =
```

```
  let folding_fn _____ =
    _____
    _____
    _____
    _____
    _____
```

```
  let base = _____ in
```

```
  let _____ = List.fold_left folding_fn base l in
```

```
  _____
  _____
```

Scratch space to work out your answers:

3. [10 points]

- a. [5 points] You will use `map` and `fold_left` to write a function `length_2 : int list list -> int`, which takes a list of lists of integers, and returns the total number of integers in all the lists. For example:

```
# length_2 [[1;2;3];[4;6]];;
- : int = 5

# length_2 [[1;2;3];[4;6];[9;10]];;
- : int = 7

# length_2 [[];[];[]];;
- : int = 0
```

Recall that the type of `fold` and `map` are:

```
fold_left: ('a -> 'b -> 'a) -> 'a -> 'b list -> 'a
map:      ('a -> 'b) -> 'a list -> 'b list
```

You can also use the `length` function, which has type `'a list -> int`.
Fill in the implementation of `length_2` below.

```
let length_2 l =
```

```
    List.fold_left (+) _____ (List.map _____ )
```

- b. [5 points] You will now use `map`, `fold_left` and `length_2` to write a function `length_3 : int list list list -> int`, which takes a list of lists of lists of integers (wow!), and returns the total number of integers in all the lists. For example:

```
# length_3 [[[1;2;3]],[[4;6];[7;8]]];;
- : int = 7

# length_3 [[[1;2;3]],[[4;6];[7;8];[10;11]]];;
- : int = 9
```

Fill in the implementation of `length_3` below.

```
let length_3 l =
```

```
    List.fold_left (+) _____ (List.map _____ )
```

4. [10 points] For each expression below, write down the returned value (not the type).

```
let f1 = List.map (fun x->2*x);;
```

```
f1 [1;2;3;4];;
```

```
let f2 = List.fold_left (fun x y -> (y+2)::x) [];;
```

```
f2 [3;5;7;9];;
```

```
let f3 = List.fold_left (fun x y -> x@[3*y]) [];;
```

```
f3 [1;3;6];;
```

```
(* This is going to get harder now... *)
```

```
let f = List.fold_left (fun x y -> y x);;
```

```
f 1 [(+) 1; (-) 2];;
```

```
f "abc" [ (^) "zzz"; (^) "yyy" ];;
```

```
(* Ok, this one is insanely hard!!! *)
```

```
f [1;2;3] [f1;f2;f3];;
```
