Name:	
ID:	

CSE 130, Spring 2013: Midterm Examination May 9th, 2013

- Do **not** start the exam until you are told to.
- This is a open-book, open-notes exam, but with no computational devices allowed (such as calculators/cellphones/laptops).
- Do **not** look at anyone else's exam. Do **not** talk to anyone but an exam proctor during the exam.
- Write your answers in the space provided.
- Wherever it gives a line limit for your answer, write no more than the specified number of lines. The rest will be ignored.
- Work out your solution in blank space or scratch paper, and only put your answer in the answer blank given.
- \bullet In all exercises, you are allowed to use the "@" operator.
- Good luck!

1.	20 Points	
2.	30 Points	
3.	15 Points	
TOTAL	65 Points	

1.	20 point	s l Let's	warm	up	with	two	small	folds.
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a.	[10 points]	Use fold_	left to imp	element le	ngth :	'a list	->	int,	which	takes a	a list	and	returns
	its length. For	vour refere	ence, the typ	e of fold	left is	given bel	ow:						

Fill in the implementation of length below using fold_left:

let length 1 =

b. [10 points]

Use fold_left to implement remove: 'a list -> 'a -> 'a list, which takes a list and an element, and returns a new list in which all occurrences of the given element have been removed. The elements in the returned list should be in the same order as in the original list. Do not use List.rev.

Fill in the implementation of remove below using fold_left:

let	remove	1	x	=

- 2. [30 points] In this question you will write several functions that will allow us to use OCaml lists to represent arrays that support indexing and functional updates. Each time an index is passed in, you can assume the index is greater or equal to 0.
 - a. [10 points] Indexing. First, you will write a function ith: 'a list \rightarrow int \rightarrow 'a \rightarrow 'a, which returns the i^{th} element of a list. In particular, given a list 1, an integer index i greater or equal to 0, and a "default" value d, then (ith 1 i d) returns the ith element of the list 1, or d if this element does not exists. For example:

```
# ith ["a";"b";"c";"d"] 0 "";;
   - : string = "a"
   # ith ["a";"b";"c";"d"] 1 "";;
   - : string = "b"
   # ith ["a";"b";"c";"d"] 2 "";;
   - : string = "c"
   # ith ["a";"b";"c";"d"] 3 "";;
   - : string = "d"
   # ith ["a";"b";"c";"d"] 4 "";;
   - : string = ""
Fill in the implementation of ith below:
```

let rec ith 1 i	d =
match 1 with	
[] ->	
h::t ->	

b. [10 points] Update. Next write a function update: 'a list -> int -> 'a -> 'a list, which updates the i^{th} element of a list. Since we are doing functional programming, the update function does not actually update the list, it returns a new list in which the i^{th} element has been replaced. More specifically, given a list 1, an integer index i greater or equal to 0, and a new value n, then (update 1 i n) returns a new list which is equal to 1, except that the ith element of the returned list is equal to n. If the ith element does not exist, update returns a list equal to 1. For example:

<pre># update ["a";"b";"c";"d"] 0 "ZZZ";; - : string list = ["ZZZ"; "b"; "c"; "d"]</pre>
<pre># update ["a";"b";"c";"d"] 1 "ZZZ";; - : string list = ["a"; "ZZZ"; "c"; "d"]</pre>
<pre># update ["a";"b";"c";"d"] 2 "ZZZ";; - : string list = ["a"; "b"; "ZZZ"; "d"]</pre>
<pre># update ["a";"b";"c";"d"] 3 "ZZZ";; - : string list = ["a"; "b"; "c"; "ZZZ"]</pre>
<pre># update ["a";"b";"c";"d"] 4 "ZZZ";; - : string list = ["a"; "b"; "c"; "d"]</pre>
Fill in the implementation of update below:
<pre>let rec update l i n =</pre>
match 1 with
[] ->
h::t ->

c. [10 points] Functional Update, Revisited. Next you will write a new version of update, namely a function update2 : 'a list -> int -> 'a -> 'a -> 'a list, which updates the ith element of a list, but also extends the list with a number of default values if the ith element does not exist. In particular, given a list 1, an integer index i greater or equal to 0, a new value n, and a "default" value d, then (update 1 i n d) returns a new list which is equal to 1, except that the ith element of the returned list is equal to n. If the ith element does not exist, update2 returns a list in which enough default values d are added to the returned list so that the ith element exists. For example:

```
# update2 ["a";"b";"c";"d"] 0 "ZZZ" "";;
- : string list = ["ZZZ"; "b"; "c"; "d"]
# update2 ["a";"b";"c";"d"] 1 "ZZZ" "";;
- : string list = ["a"; "ZZZ"; "c"; "d"]
# update2 ["a";"b";"c";"d"] 2 "ZZZ" "";;
- : string list = ["a"; "b"; "ZZZ"; "d"]
# update2 ["a";"b";"c";"d"] 3 "ZZZ" "";;
- : string list = ["a"; "b"; "c"; "ZZZ"]
# update2 ["a";"b";"c";"d"] 4 "ZZZ" "";;
- : string list = ["a"; "b"; "c"; "d"; "ZZZ"]
# update2 ["a";"b";"c";"d"] 5 "ZZZ" "";;
- : string list = ["a"; "b"; "c"; "d"; ""; "ZZZ"]
# update2 ["a";"b";"c";"d"] 6 "ZZZ" "";;
- : string list = ["a"; "b"; "c"; "d"; ""; ""; "ZZZ"]
# update2 ["a";"b";"c";"d"] 7 "ZZZ" "";;
- : string list = ["a"; "b"; "c"; "d"; ""; ""; "ZZZ"]
```

let rec update2 1 i n d =

Fill in the implementation of update2 below (hint: In my solution the h::t case of update and update2 are exactly the same. The only difference between update and update2 is in the base case):

match 1 with

| [] -> ______
| h::t -> ______

3. [15 points] In this problem you will write a function categorize: ('a -> int) -> 'a list -> 'a list list, which will categorize the elements of a list into different bins. Bins are numbered starting at 0. The first parameter to categorize is a function f, which given an element returns what bin to place that element in. The second parameter to categorize is the list 1 of elements to categorize. Then (categorize f 1) returns a list r such that the ith element of r is a list of all elements from 1 for which f returned i. The length of the list r is one more than the maximum value returned by f when called on the elements of 1. For example:

Note a few things:

- the elements in each bin appear in the same order as they did in the original list
- in the first call to categorize four bins are returned, numbered 0, 1, 2 and 3, because in this call f returns a maximum of 3.
- in the second call to categorize three bins are returned, because in this call f returns a maximum of 2

Fill in the implementation of categorize below (hint: you may want to use some of the functions you wrote in the previous problem):