

# Partition Problem

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## 1 PARTITION PROBLEM

### 1.1 PROBLEM STATEMENT

There are  $N$  packets, each with one or more candies. There are  $K$  students among which the packets have to be distributed. (Assume  $K \leq N$  for all cases). The parameters  $N$  and  $K$  have to be provided by the user at run-time. Each student gets only one packet. The number of candies in various packets are  $(x_1, x_2, x_3, \dots, x_k)$ , where  $x_i$  denotes the number of candies in the  $i$ th packet. Find the number of triplets  $(x_1, x_2, x_3)$  possible such that sum of the candies  $(x_1 + x_2 + x_3)$  is even.

Divide the packets into two parts ( $p_1$  and  $p_2$ ) such that the difference  $(|p_1 - p_2|)$  is minimum, where  $p_1$  and  $p_2$  are the total number of candies in part 1 and part 2 respectively.

### 1.2 ABSTRACT

This problem was originally designed for Dynamic Programming. However, it has been solved as a deterministic problem as it is trivial.

### 1.3 SPECIFICATION AND ASSUMPTIONS

**Tool Specifications:**

Language used: Java

Platform: Ubuntu 12.04

Additional tools used: none

Eclipse Version: Version: 3.7.2

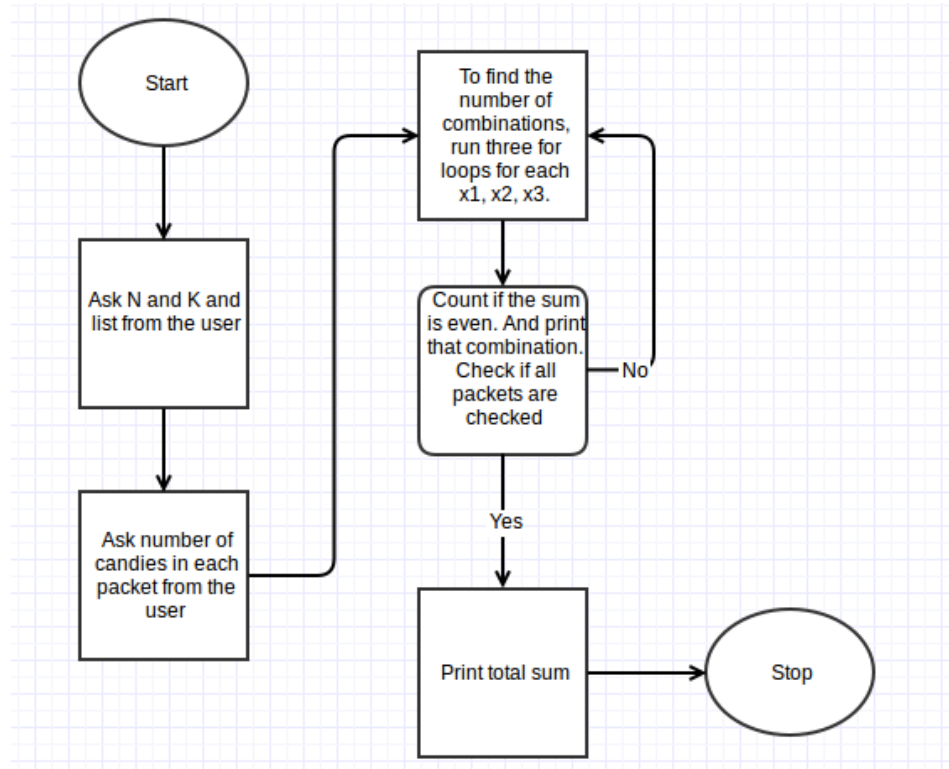
### Assumptions

Input is taken one at a time

The list of  $x_1$  to  $x_n$  is separated by commas

Prints each combination of triplet whose sum is even on terminal

### 1.4 FLOW CHART



### 1.5 LOGIC IMPLEMENTATION

**Following are the two main steps to solve this problem:**

1. Calculate sum of the array. If sum is odd, there can not be two subsets with equal sum, so return false.
2. If sum of array elements is even, calculate  $\text{sum}/2$  and find a subset of array with sum equal to  $\text{sum}/2$ .

The first step is simple. The second step is crucial, it can be solved either using recursion or Dynamic Programming.

## 1.6 EXECUTION DIRECTIVE

### **Compiling:**

javac dp.java

### **Running:**

java dp

## 1.7 OUTPUT OF THE PROGRAM

Part A

Enter N

10

Enter K

4

Enter x0

10

Enter x1

20

Enter x2

30

Enter x3

3

Enter x4

3

Enter x5

3

Enter x6

3

Enter x7

3

Enter x8

3

Enter x9

2

The total number of possible triplets such that the sum is even is 64

Part B

The students get packets containing the following number of candies:

0

2 1

3 2

3 3  
3 4  
3 5  
3 6  
3 7  
10 8  
20 9  
30

Part C  
Partition problem  
true  
5 = 2+3  
5 = 2+3  
5 = 2+3  
5 = 2+3  
5 = 2+3  
5 = 2+3

## 1.8 RESULT

Solved the trivial partition problem.

- Recognized when dynamic programming is a plausible approach. E.g., recursive formulation, repeated subproblems, Global opt depends on opt subsolution, but not details thereof.