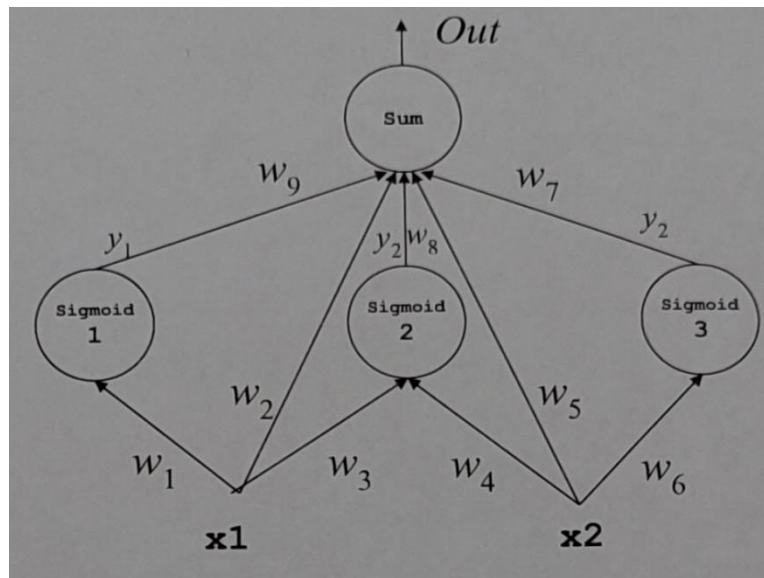


## IS53002B: Coursework Assignment



Initial weights = [  $\Delta w_1 = 0.2$ ,  $\Delta w_2 = 0.1$ ,  $\Delta w_3 = 0.2$ ,  $\Delta w_4 = -0.1$ ,  $\Delta w_5 = -0.2$ ,  $\Delta w_6 = 0.1$ ,  $\Delta w_7 = -0.1$ ,  $\Delta w_8 = 0.2$ ,  $\Delta w_9 = -0.2$  ],  $n=0.2$

Here sigmoid is:  $f(x) = \frac{1}{1+e^{-x}}$

Case 1:  $x_1=0$ ,  $x_2=1$ ,  $y=1$

$$\text{OutY1} = \text{Sigmoid}[(W_1 \cdot x_1)] = \text{Sigmoid}[(0.2 \cdot 0)] = 0.5$$

$$\text{OutY2} = \text{Sigmoid}[(W_3 \cdot x_1) + (W_4 \cdot x_2)] = \text{Sigmoid}[(0.2 \cdot 0) + (-0.1 \cdot 1)] = 0.4750$$

$$\text{OutY3} = \text{Sigmoid}[(W_6 \cdot x_2)] = \text{Sigmoid}[(0.1 \cdot 1)] = 0.5250$$

$$\begin{aligned} \text{Out} &= (w_9 \cdot \text{OutY1}) + (w_2 \cdot x_1) + (w_8 \cdot \text{OutY2}) + (w_5 \cdot x_2) + (w_7 \cdot \text{OutY3}) \\ &= (-0.2 \cdot 0.5) + (1 \cdot 0) + (0.2 \cdot 0.4750) + (-0.2 \cdot 1) + (-0.1 \cdot 0.5250) = -0.2575 \end{aligned}$$

$$\text{beta\_out} = (y - \text{Out}) = (1 - (-0.2575)) = 1.2575$$

$$\Delta w_{9\_Out} = (n \cdot \text{beta\_out} \cdot \text{OutY1}) = (0.2 \cdot 1.2575 \cdot 0.5) = 0.1257$$

$$\Delta w_{2\_Out} = (n \cdot \text{beta\_out} \cdot x_1) = (0.2 \cdot 1.2575 \cdot 0) = 0$$

$$\Delta w_{8\_Out} = (n \cdot \text{beta\_out} \cdot \text{OutY2}) = (0.2 \cdot 1.2575 \cdot 0.4750) = 0.1195$$

$$\Delta w_{5\_Out} = (n \cdot \text{beta\_out} \cdot x_2) = (0.2 \cdot 1.2575 \cdot 1) = 0.2515$$

$$\Delta w_{7\_Out} = (n \cdot \text{beta\_out} \cdot \text{OutY3}) = (0.2 \cdot 1.2575 \cdot 0.5250) = 0.1320$$

$$\begin{aligned} \text{beta\_Y1} &= \text{OutY1} \cdot (1 - \text{OutY1}) \cdot [(\text{beta\_out} \cdot w_9)] = \\ &= 0.5 \cdot (1 - 0.5) \cdot (1.2575 \cdot -0.2) = -0.0629 \end{aligned}$$

$$\begin{aligned} \text{beta\_Y2} &= \text{OutY2} \cdot (1 - \text{OutY2}) \cdot [(\text{beta\_out} \cdot w_8)] = \\ &= 0.4750 \cdot (1 - 0.4750) \cdot (1.2575 \cdot 0.2) = 0.0627 \end{aligned}$$

$$\begin{aligned}\text{beta\_Y3} &= \text{OutY3} * (1 - \text{OutY3}) * [(\text{beta\_out} * w_7)] = \\ 0.5250 * (1 - 0.5250) * (1.2575 * -0.1) &= -0.0314\end{aligned}$$


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$$\begin{aligned}\text{delta\_w1\_Y1} &= (n * \text{beta\_Y1} * x_1) = (0.2 * -0.0629 * 0) = 0 \\ \text{delta\_w3\_Y2} &= (n * \text{beta\_Y2} * x_1) = (0.2 * 0.0627 * 0) = 0 \\ \text{delta\_w4\_Y2} &= (n * \text{beta\_Y2} * x_2) = (0.2 * 0.0627 * 1) = 0.0125 \\ \text{delta\_w6\_Y5} &= (n * \text{beta\_Y3} * x_2) = (0.2 * -0.0314 * 1) = -0.0063\end{aligned}$$


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$$\begin{aligned}\text{delta\_w1} &= \text{delta\_w1} + \text{delta\_w1\_Y1} = 0.2 + 0 = 0.2 \\ \text{delta\_w2} &= \text{delta\_w2} + \text{delta\_w2\_Out} = 0.1 + 0 = 0.1 \\ \text{delta\_w3} &= \text{delta\_w3} + \text{delta\_w3\_Y2} = 0.2 + 0 = 0.2 \\ \text{delta\_w4} &= \text{delta\_w4} + \text{delta\_w4\_Y2} = -0.1 + 0.0125 = -0.0875 \\ \text{delta\_w5} &= \text{delta\_w5} + \text{delta\_w5\_Out} = -0.2 + 0.2515 = 0.0515 \\ \text{delta\_w6} &= \text{delta\_w6} + \text{delta\_w6\_Y5} = 0.1 + (-0.0063) = 0.0937 \\ \text{delta\_w7} &= \text{delta\_w7} + \text{delta\_w7\_Out} = -0.1 + 0.1320 = 0.032 \\ \text{delta\_w8} &= \text{delta\_w8} + \text{delta\_w8\_Out} = 0.2 + 0.1195 = 0.3195 \\ \text{delta\_w9} &= \text{delta\_w9} + \text{delta\_w9\_Out} = -0.2 + 0.1257 = -0.0743\end{aligned}$$

$$\begin{aligned}\text{new weights are} &= [\text{delta\_w1} = 0.2000, \text{delta\_w2} = 0.1000, \text{delta\_w3} = 0.2000, \text{delta\_w4} = - \\ 0.0875, \text{delta\_w5} &= 0.0515, \text{delta\_w6} = 0.0937, \text{delta\_w7} = 0.0320, \text{delta\_w8} = 0.3195, \\ \text{delta\_w9} &= -0.0743], n=0.2\end{aligned}$$

Case 2:  $x_1=1, x_2=0, y=0$

$$\begin{aligned}\text{OutY1} &= \text{Sigmoid}[(W_1 * x_1)] = \text{Sigmoid}[(0.2 * 1)] = 0.5498 \\ \text{OutY2} &= \text{Sigmoid}[(W_3 * x_1) + (W_4 * x_2)] = \text{Sigmoid}[(0.2 * 1) + (-0.0875 * 0)] = 0.5498 \\ \text{OutY3} &= \text{Sigmoid}[(W_6 * x_2)] = \text{Sigmoid}[(0.0937 * 0)] = 0.5 \\ \text{Out} &= (w_9 * \text{OutY1}) + (w_2 * x_1) + (w_8 * \text{OutY2}) + (w_5 * x_2) + (w_7 * \text{OutY3}) = \\ (-0.0743 * 0.5498) &+ (0.1 * 1) + (0.3195 * 0.5498) + (0.0515 * 0) + (0.0320 * 0.5) = 0.2508\end{aligned}$$


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$$\text{beta\_out} = (y - \text{Out}) = 0 - 0.2508 = -0.2508$$


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$$\begin{aligned}\text{delta\_w9\_Out} &= (n * \text{beta\_out} * \text{OutY1}) = (0.2 * -0.2508 * 0.5498) = -0.0276 \\ \text{delta\_w2\_Out} &= (n * \text{beta\_out} * x_1) = (0.2 * -0.2508 * 1) = -0.0502 \\ \text{delta\_w8\_Out} &= (n * \text{beta\_out} * \text{OutY2}) = (0.2 * -0.2508 * 0.5498) = -0.0276 \\ \text{delta\_w5\_Out} &= (n * \text{beta\_out} * x_2) = (0.2 * -0.2508 * 0) = 0 \\ \text{delta\_w7\_Out} &= (n * \text{beta\_out} * \text{OutY3}) = (0.2 * -0.2508 * 0.5) = -0.0251\end{aligned}$$


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$$\begin{aligned}\text{beta\_Y1} &= \text{OutY1} * (1 - \text{OutY1}) * [(\text{beta\_out} * w_9)] = \\ 0.5498 * (1 - 0.5498) * (-0.2508 * -0.0743) &= 0.0046 \\ \text{beta\_Y2} &= \text{OutY2} * (1 - \text{OutY2}) * [(\text{beta\_out} * w_8)] = \\ 0.5498 * (1 - 0.5498) * (-0.2508 * 0.3195) &= -0.0198 \\ \text{beta\_Y3} &= \text{OutY3} * (1 - \text{OutY3}) * [(\text{beta\_out} * w_7)] =\end{aligned}$$


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$$0.5*(1-0.5)*(-0.2508*0.0320) = -0.0020$$

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$$\text{delta\_w1\_Y1} = (n*\text{beta\_Y1}*x1) = (0.2*0.0046*1) = 0.0009$$

$$\text{delta\_w3\_Y2} = (n*\text{beta\_Y2}*x1) = (0.2*-0.0198*1) = -0.0040$$

$$\text{delta\_w4\_Y2} = (n*\text{beta\_Y2}*x2) = (0.2*-0.0198*0) = 0$$

$$\text{delta\_w6\_Y5} = (n*\text{beta\_Y3}*x2) = (0.2*-0.0020*0) = 0$$

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$$\text{delta\_w1} = \text{delta\_w1} + \text{delta\_w1\_Y1} = 0.2 + 0.0009 = 0.2009$$

$$\text{delta\_w2} = \text{delta\_w2} + \text{delta\_w2\_Out} = 0.1 + (-0.0502) = 0.0498$$

$$\text{delta\_w3} = \text{delta\_w3} + \text{delta\_w3\_Y2} = 0.2 + (-0.0040) = 0.196$$

$$\text{delta\_w4} = \text{delta\_w4} + \text{delta\_w4\_Y2} = -0.0875 + 0 = -0.0875$$

$$\text{delta\_w5} = \text{delta\_w5} + \text{delta\_w5\_Out} = 0.0515 + 0 = 0.0515$$

$$\text{delta\_w6} = \text{delta\_w6} + \text{delta\_w6\_Y5} = 0.0937 + 0 = 0.0937$$

$$\text{delta\_w7} = \text{delta\_w7} + \text{delta\_w7\_Out} = 0.0320 + (-0.0251) = 0.0069$$

$$\text{delta\_w8} = \text{delta\_w8} + \text{delta\_w8\_Out} = 0.3195 + (-0.0276) = 0.2919$$

$$\text{delta\_w9} = \text{delta\_w9} + \text{delta\_w9\_Out} = -0.0743 + (-0.0276) = -0.1018$$

final weights are:

$$w1=0.2009 \quad w2=0.0498 \quad w3=0.1960 \quad w4=-0.0875 \quad w5=0.0515 \quad w6=0.0937$$

$$w7=0.0069 \quad w8=0.2919 \quad w9=-0.1018$$