

Day-2  
For Nesting Concept Rules :- Time Complexity  $\Rightarrow O(n^2)$

8x5 For  $(i=0; i < n; i++) \rightarrow n+1$  times

$\downarrow$   
for  $(j=0; j < n; j++) \rightarrow n^2(n+1)$   $\Rightarrow$  memory, stack, heap.

statements  $\Rightarrow n^2n \dots n$  square

y

y;

T.C  $\Rightarrow O(n^2n)$  ..

$\Rightarrow$  Implement a 2D array & rotate the matrix 90°

C & Java  $\rightarrow$  primitive

- Python  $\rightarrow$  non-primitive

$\Rightarrow$  2x2 Matrix Rotation

$\Rightarrow$  Anti-clockwise (left):

$$\begin{bmatrix} 9 & 3 \\ 10 & 6 \end{bmatrix} \xrightarrow{\text{Ans}} \begin{bmatrix} 3 & 6 \\ 9 & 10 \end{bmatrix}$$

3x3 Matrix Rotation

$$\begin{bmatrix} 10 & 15 & 20 \\ 100 & 200 & 300 \\ 1 & 2 & 3 \end{bmatrix} \xrightarrow{\text{Ans}} \begin{bmatrix} 10 & 15 & 20 \\ 100 & 200 & 300 \\ 1 & 2 & 3 \end{bmatrix}$$

Anti-clockwise

$$\Rightarrow \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \Rightarrow \begin{bmatrix} 3 & 1 \\ 4 & 2 \end{bmatrix}$$

clock wise (right).

$$\begin{bmatrix} 20 & 300 & 3 \\ 15 & 200 & 2 \\ 10 & 100 & 1 \end{bmatrix}$$

$$\Rightarrow \text{clockwise} \begin{bmatrix} 100 & 10 \\ 200 & 15 \\ 300 & 20 \end{bmatrix}$$

$\Rightarrow \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \Rightarrow$  Transpose of Matrix

$$\text{Ans} \Rightarrow \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \quad \begin{bmatrix} 2 & 4 \\ 1 & 3 \end{bmatrix}$$

$$\xrightarrow{\text{Transpose}} \begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix} \xrightarrow{\text{reverse}} \begin{bmatrix} 3 & 1 \\ 4 & 2 \end{bmatrix}$$

$$\xrightarrow{\text{Transpose}} \begin{bmatrix} 3 & 4 \\ 6 & 8 \end{bmatrix} \xrightarrow{\text{reverse}} \begin{bmatrix} 3 & 6 \\ 4 & 8 \end{bmatrix} \xrightarrow{\text{reverse}} \begin{bmatrix} 6 & 3 \\ 8 & 4 \end{bmatrix}$$

~~②: for(i=0; i<n; i++)~~ Tested for loop

{  
for(j=0; j<~~i~~; j++)

}

statements;

};  
};

ex: i=0 then 0<0 no

i      j  
0      nothing

0<0

$\Rightarrow$  so, when i = 0 - 0 times

1 - - - 1 times

2 - - - 2 times

so 1+2+3+...+n =  $n(n+1)/2$

=  $(n^2 + n)/2$

TC = O(n square)

$0 < 1 \Rightarrow 0$  will execute

$1 < 1 \Rightarrow 1$  will stop

$0 \leq 2 \Rightarrow 0$  will execute

$1 < 2 \Rightarrow 1$  will execute

$2 < 2 \Rightarrow 2$  will stop

$0, 1$  will execute

$\Rightarrow$   
 $P = 0$        $O \in \Theta$   
 for  $i=1; P \leq n; i+1$   
 $\quad \quad \quad \downarrow$   
 $P = P+i;$   
 $\quad \quad \quad \underline{\underline{y}}$

①  $0+1$  bcs  $P=P+i$ , when  $N \neq 0$

②  $1+2+\dots+n \text{ is } 1$

③  $1+2+\dots+3=6$

$\vdots$   
 $k \quad 1+2+\dots+k$

= Not  $n$  times assuming

When will stop when  $P > n$

$P = k(k+1)/2$  bcs  $1+2+\dots+k$

$P = k^2 \geq n$

so  $n = \sqrt{n}$

$$(n = \sqrt{n})$$

Time Complexity =  $O(\sqrt{n})$

for (i=1; i<n; i\*2)

{

statements :

}

Analyse       $n=10, \log_{10} \text{base } 2$

i=1    1 time

i=2    2 times ( $1 \times 2$ )

i=3    ~~8~~  $(1 \times 2) \times 2 = 2^{\text{power } 2}$

i=4    8     $(1 \times 2) \times 2 \times 2 = 2^{\text{power } 3}$

~~i=5~~    16     $(1 \times 2) \times 2 \times 2 \times 2 = 2^{\text{power } 4}$

so, when stops  $i \geq n$

$i = 2^{\text{power } k}$

$2^{\text{power } k} \geq n$

$k = \log n \text{ base } 2$

so T.C  $\Rightarrow O(\log n \text{ base } 2)$

x = int (input ("Enter starting value:"))

y = int (input ("Enter ending value:"))

print ("The Even numbers: ")

for i in range (x, y+1):

if i%2 == 0:

print (i)

print ("The 2 power values")

for j in range (x, y+1):

if (j > (j-1)) == 0 and

j != 0:

print (j).

→ Create a <sup>dynamic</sup> array. It should contain numbers b/w 20 to 30  
extract & print all even numbers

i)  $\&$  power values.

→  $\text{for } (i=n; i>=1; i=i/2)$

statements:

y  
y

N

$n/2$

$n/2$  power 2.

$n/2$  power K

assume  $i<1$  stops right?

$n/2$  power  $K-1$

$n/2$  power  $K=1$

$n=2$  power  $\& K$

$K=\log n$  base 2

T.C  $\Rightarrow \underline{\underline{O(\log n)}}$

$\Rightarrow n=10, i=10$

$\Rightarrow n=10; 10/2=5$   $\&$  Plot

$\Rightarrow 5/2=2.5$

$n=2$

$\Rightarrow 2/2=1 \Rightarrow 1, i=1/2$

$\Rightarrow 1/2=0.5$

$\Rightarrow 0.5/2=0.25 \Rightarrow i=0.25$

## Derived Formulas

for ( $i=0; i < n; i+1$ )  $\rightarrow O(n)$

for ( $i=0, i < n; i+2$ )  $\rightarrow O(n)$

for ( $i=n; i \geq 1; i-1$ )  $\dots O(n)$

for ( $i=1; i < n; i=i \times 2$ )  $\rightarrow O(\log \text{base } 2)$

for ( $i=1; i < n; i=i \times 3$ )  $\rightarrow O(\log \text{base } 3)$

for ( $i=1; i \geq 1; i=i/2$ )  $\rightarrow O(\log \text{base } 2)$

## \*Names of TC

- ① Constant Time Complexity :  $O(1) \dots$
- ② Linear Time Complexity :  $O(n) \dots$
- ③ Logarithmic TC :  $O(\log n) \dots$
- ④ Quadratic TC :  $O(n^2)$
- ⑤ Exponential TC :  $O(2^n)$ .

$\Rightarrow$  ~~FFT~~  $i \leftarrow i/2 \rightarrow \log(n)$  base 2

- \* Parallel Concept to Time Complexity  $\rightarrow$  [Space Complexity]
- \* Array of size  $n$ , require  $O(n)$  space.
  - \* Two dimensional array of size  $n \times n = O(n^2)$  space.

Linear search  $O(1)$

Merge sort  $O(n)$

$O(n)$

DFS

$O(n)$

BFS

$\Rightarrow$  Dynamic Programming  $O(n^2)$  (or)  $O(n^{*}2)$

\* Constant Complexity  $= O(1)$

Same amount of space regardless of the I/p size  $n$   
it is called Constant Complexity:

ex:- ① Sum of array elements & linear search  
~~Ques~~ why  $O(1)$ ? why not  $O(n)$ ?

$\Rightarrow$  Space not depending on Values

\* sum of array elements using function

```
def sum(arr):
    sum = 0
    for i in arr:
        sum = sum + i
    return sum

if __name__ == "__main__":
    arr = [1, 2, 3, 4, 5]
    n = len(arr)
    ans = sum(arr)
    print("Sum of the array is", ans)
```

→ def array\_summer(arr):

```
total = 0
for item in arr:
    total += item
return total
```

```
print(array_summer([1, 2, 3, 4, 5]))
```

O/P: 16

array  $\Rightarrow$  S.C  $\Rightarrow O(n)$

sum of array  $\rightarrow$  S.C  $\Rightarrow O(1)$

linear search  $\Rightarrow O(n)$

summary  $\Rightarrow O(1)$

→ Space Complexity: - Logarithmic Complexity:-

```
#include <stdio.h>
struct {
    double x;
    int y;
    char z;
} ;
int main()
```

{ struct yes;

```
printf("%d", sizeof(yes));
return 0;
```

O/P: 16

Linear complexity  $O(n)$   
when an alg - takes space directly proportional to the

if size

or if a num

$\Rightarrow \log$  linear complexity:  $O(n \log n)$

$\Rightarrow$  log-linear complexity:  $O(n \log n)$   
when the space complexity of an alg grows proportionally  
to the if size & a logarithmic factor

Ex: Merge sort

$\Rightarrow \log(n) \Rightarrow \log$  linear Complexity

$\Rightarrow$   $n^{10}$   $\rightarrow$  nested list  $\Rightarrow$  polynomial complexity  $\Rightarrow O(n^2)$   
 $\Rightarrow$  def generate-lists-of-lists(n):  $\rightarrow$  if  $n=1$   
table-list = []  
for num in range(n):  
 row = []  
 for i in range(n):  
 row.append(i)  
 table-list.append(row)  
return table-list

print(generate\_lists\_of\_lists(10))

n-number  
n-number of o/p

0 to 10

up to 9

$\Rightarrow$  10 times

Type 1

```
char y;
int q;
double z;
double - 24
double - 24
```

char y  
int q  
double z  
double - 24  
double - 24

char  
int  
char  
int.

double  
int  
char  
int.

double  
char  
int.

y,  
16

Sum of n numbers using

Recursion

```
int add (int n);
```

```
if (n <= 0);
```

```
return 0;
```

y

```
return n + add(n-1);
```

y

$\Rightarrow O(n)$  Space Complexity

char  
double → 24

int

double → 0(1)

char  
int

double → 0(1)