

Assignment 2

Find global minimum point and value for function $f(x,y) = x^2 + y^2 + 10$

→ Do manual calculations for 2 iterations

step 1: $x = -1$ $y = +1$ $\eta = 0.1$ $\text{epochs} = 2$

step 2: $\text{iter} = 1$

step 3: $\frac{\partial f}{\partial x} = 2x = -2$

$$\frac{\partial f}{\partial y} = 2y = 2$$

step 4: $\Delta x = -\eta \frac{\partial f}{\partial x} = -0.1(-2) = 0.2$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -0.1(2) = -0.2$$

steps: $x = x + \Delta x = -1 + 0.2 = -0.8$

$$y = y + \Delta y = 1 - 0.2 = 0.8$$

step 6: $\text{iter} = \text{iter} + 1 = 1 + 1 = 2$

step 7: if ($\text{iter} > \text{epochs}$)
goto step 8

else

goto step 3

step 3: $\frac{\partial f}{\partial x} = 2x = 2(-0.8) = -1.6$

$$\frac{\partial f}{\partial y} = 2y = 2(0.8) = 1.6$$

step 4: $\Delta x = -\eta \frac{\partial f}{\partial x}$

$$= -(0.1)(-1.6) = 0.16$$

$$\Delta y = -\eta \frac{\partial f}{\partial y}$$

$$= -(0.1)(1.6) = -0.16$$

step 5: $x = x + \Delta x$

$$= -0.8 + 0.16 \Rightarrow -0.64$$

$$y = y + \Delta y$$

$$= 0.8 - 0.16 \Rightarrow 0.64$$

step 6: $itr = itr + 1 = 2 + 1 = 3$

step 7: if ($itr > epochs$)

$$3 > 2$$

goto step 8

else : goto step 3

step 8: $x = -0.64$

$$y = 0.64$$

$$f(x, y) = x^2 + y^2 + 10$$

$$= (-0.64)^2 + (0.64)^2 + 10$$

$$= 0.4 + 0.4 + 10$$

$$= 10.8$$