## VISVESVARAYA TECHNOLOGICAL UNIVERSITY

"JnanaSangama", Belgaum -590014, Karnataka.



#### LAB REPORT On

# ANALYSIS AND DESIGN OF ALGORITHMS (23CS4PCADA)

## Submitted by

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in partial fulfillment for the award of the degree of BACHELOR OF ENGINEERING in COMPUTER SCIENCE AND ENGINEERING



B.M.S. COLLEGE OF ENGINEERING (Autonomous Institution under VTU) BENGALURU-560019

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This is to certify that the Lab work entitled "ANALYSIS AND DESIGN OF ALGORITHMS" carried out by MAKADIA RISHIT DILIPBHAI (1BM23CS177), who is bonafide student of B. M. S. College of Engineering. It is in partial fulfillment for the award of Bachelor of Engineering in Computer Science and Engineering of the Visvesvaraya Technological University, Belgaum during the year 2024-25. The Lab report has been approved as it satisfies the academic requirements in respect of Analysis and Design of Algorithms Lab - (23CS4PCADA) work prescribed for the said degree.

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#### **Course outcomes:**

CO1	Analyze time complexity of Recursive and Non-recursive algorithms using asymptotic notations.	
CO2	Apply various design techniques for the given problem.	
CO3	Apply the knowledge of complexity classes P, NP, and NP-Complete and prove certain problems are NP-Complete	
CO4	Design efficient algorithms and conduct practical experiments to solve problems.	

## Program -1(a)

Question: Write a program to obtain the Topological ordering of vertices in a given digraph.

```
#include <stdio.h>
#include <stdlib.h>
#define MAX 10
int adj[MAX][MAX], visited[MAX], result[MAX], top=-1;
void dfs_top(int n, int adj[][MAX]){
  for(int i=0; i<n; i++)
    visited[i]=0;
  for (int j=0; j<n; j++){
    if(visited[j]==0)
       dfs(j,n,adj);
  }
}
void dfs(int start, int n, int adj[][MAX]){
  visited[start]=1;
  for(int i=0; i<n; i++){
    if(adj[start][i]==1 && visited[i]==0)
       dfs(i,n,adj);
  }
  result[++top]=start;
}
int main(){
  int n;
  printf("Enter No. of Nodes: ");
  scanf("%d", &n);
```

```
printf("Enter Adjacency Matrix: \n");
for(int i=0; i<n;i++){
    for (int j=0; j<n; j++){
        scanf("%d", &adj[i][j]);
    }
}
dfs_top(n, adj);
printf("Topological Order: ");
for(int k=(n-1); k>=0; k--){
    printf("\t%d", result[k]);
}
```

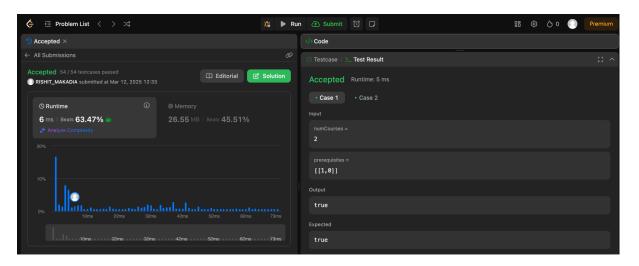
## **Output:**

## Program - 1(b)

**Question: (Leetcode) Course Schedule** 

```
#define MAX 2000
bool dfs(int course, int adjList[][MAX], int* adjSize, int* visited){
  if (visited[course]==1) // cycle detected
    return true;
  if (visited[course]==2) // already visited
    return false;
  visited[course]=1;
  for (int i = 0; i < adjSize[course]; i++) {
    if (dfs(adjList[course][i], adjList, adjSize, visited)) {
       return true;
    }
  }
  visited[course] = 2;
  return false;
}
bool canFinish(int numCourses, int** prerequisites, int prerequisitesSize, int*
prerequisitesColSize) {
  int adjL[MAX][MAX];
  int adjSize[MAX]={0};
  int visited[MAX]={0};
  for (int i=0; iirerequisitesSize; i++){
    int course = prerequisites[i][0];
    int required = prerequisites[i][1];
    adjL[required][adjSize[required]++] = course;
```

```
for(int j=0; j< numCourses; j++){
   if(visited[j] == 0 && dfs(j, adjL, adjSize, visited))
    return false;
}
return true;
}</pre>
```



## Program - 2

Question: Implement Johnson Trotter algorithm to generate permutations.

```
#include <stdio.h>
#include <stdlib.h>
#include <stdbool.h>
#define LEFT_TO_RIGHT true
#define RIGHT_TO_LEFT false
// Function to get the position of the mobile integer
int searchArr(int a[], int n, int mobile) {
  for (int i = 0; i < n; i++)
    if (a[i] == mobile)
       return i + 1;
  return -1;
}
// Function to get the largest mobile integer
int getMobile(int a[], bool dir[], int n) {
  int mobile prev = 0, mobile = 0;
  for (int i = 0; i < n; i++) {
    if (dir[a[i] - 1] == RIGHT_TO_LEFT && i != 0) {
       if (a[i] > a[i - 1] && a[i] > mobile_prev) {
         mobile = a[i];
         mobile_prev = mobile;
      }
    }
    if (dir[a[i] - 1] == LEFT_TO_RIGHT && i != n - 1) {
       if (a[i] > a[i + 1] && a[i] > mobile prev) {
          mobile = a[i];
```

```
mobile_prev = mobile;
      }
    }
  }
  return mobile;
}
// Function to print one permutation and update the array
void printOnePerm(int a[], bool dir[], int n) {
  int mobile = getMobile(a, dir, n);
  if (mobile == 0) return;
  int pos = searchArr(a, n, mobile) - 1;
  if (dir[a[pos] - 1] == RIGHT_TO_LEFT)
    // Swap with the left element
    {
      int temp = a[pos];
      a[pos] = a[pos - 1];
      a[pos - 1] = temp;
    }
  else if (dir[a[pos] - 1] == LEFT_TO_RIGHT)
    // Swap with the right element
    {
      int temp = a[pos];
      a[pos] = a[pos + 1];
      a[pos + 1] = temp;
    }
  // After swapping, change the directions of all elements greater than mobile
  for (int i = 0; i < n; i++) {
    if (a[i] > mobile) {
      dir[a[i] - 1] = !dir[a[i] - 1];
```

```
}
  }
  // Print current permutation
  for (int i = 0; i < n; i++)
    printf("%d", a[i]);
  printf(" ");
}
// Factorial function
int fact(int n) {
  int res = 1;
  for (int i = 1; i <= n; i++)
     res *= i;
  return res;
}
// Function to print all permutations using Johnson-Trotter algorithm
void printPermutation(int n) {
  int a[n];
  bool dir[n];
  // Initialize the array and direction
  for (int i = 0; i < n; i++) {
    a[i] = i + 1;
    dir[i] = RIGHT_TO_LEFT;
    printf("%d", a[i]);
  }
  printf(" ");
  // Generate and print all permutations
  for (int i = 1; i < fact(n); i++) {
     printOnePerm(a, dir, n);
  }
```

```
printf("\n");
}
int main() {
  int n;
  printf("Enter the number of elements: ");
  scanf("%d", &n);
  printPermutation(n);
  return 0;
}
```

## Program - 3 (a)

**Question:** Sort a given set of N integer elements using Merge Sort technique and compute its time taken. Run the program for different values of N and record the time taken to sort.

```
#include <stdio.h>
#include <stdlib.h>
#include <time.h>
#define MAX 100000
void merge(int a[], int low, int high, int mid);
void mergeSort(int arr[], int low, int high);
void printArray(int arr[], int no);
void merge(int a[], int low, int high, int mid)
{
  int i = low, j = mid + 1, k = 0;
  int temp[high - low + 1];
  while (i \leq mid && j \leq high)
  {
    if (a[i] <= a[j])
       temp[k++] = a[i++];
    else
       temp[k++] = a[j++];
  }
  while (i <= mid)
    temp[k++] = a[i++];
  while (j <= high)
    temp[k++] = a[j++];
  for (int i = low, k = 0; i <= high; i++, k++)
  {
```

```
a[i] = temp[k];
  }
}
void mergeSort(int arr[], int low, int high)
{
  if (low < high)
    int mid = (high + low) / 2;
    mergeSort(arr, low, mid);
    mergeSort(arr, mid + 1, high);
    merge(arr, low, high, mid);
  }
}
void printArray(int arr[], int no)
{
  for (int i = 0; i < no; i++)
  {
    printf(" %d ", arr[i]);
  }
  printf("\n");
}
void main()
{
  int N;
  printf("Enter Size of Array: ");
  scanf("%d", &N);
  int array[N];
  srand(time(NULL));
```

```
for (int i = 0; i < N; i++) {
    array[i] = rand(); // Random integers between 0 and 99
}

printf("Original Array: ");
printArray(array, N);

clock_t start_time = clock();
mergeSort(array, 0, N - 1);
clock_t end_time = clock();
double time_taken = ((double)(end_time - start_time)) / CLOCKS_PER_SEC;
printf("Sorted Array: ");
printArray(array, N);
printf("Time taken to sort: %.100f seconds\n", time_taken);
}</pre>
```

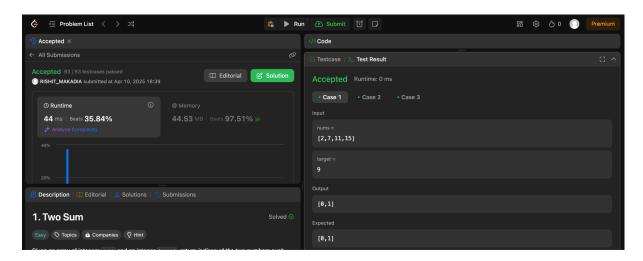
Enter Size of Array: 10
Original Array: 440077072 441668836 1424642620 1673333937 277638047 1928174645 1303025285 2055216536 1897342204 645748325
Sorted Array: 277638047 440077072 441668836 645748325 1303025285 1424642620 1673333937 1897342204 1928174645 2055216536
Time taken to sort: 0.0000070000 seconds

## Program - 3 (b)

Question: LeetCode Program related to sorting.

#### Code:

```
class Solution {
  public int[] twoSum(int[] nums, int target) {
    int[] ans = new int[2];
    for(int i=0;i<nums.length;i++){
      for(int j=(i+1) ; j< nums.length; j++){
        if ((nums[i]+nums[j]) == target){
            ans[0]=i;
            ans[1]=j;
            return ans;
        }
    }
    return ans;
}</pre>
```



## Program - 4 (a)

Question: Sort a given set of N integer elements using Quick Sort technique and compute its time taken.

```
#include <stdio.h>
#include <stdlib.h>
#include <time.h>
#define MAX 100000000
void swap(int *a, int *b){
  int temp = *a;
  *a = *b;
  *b = temp;
}
void quickSort(int arr[], int low, int high){
  if (low < high)
  {
    int par = partition(arr, low, high);
    quickSort(arr, low, par-1);
    quickSort(arr, par + 1, high);
  }
}
int partition(int a[], int low, int high){
  int pivot = a[high];
  int i=low-1;
  for (int j=low; j< high; j++){
    if (a[j]<pivot){
       i++;
      swap(&a[i], &a[j]);
    }
```

```
}
  swap(&a[i+1], &a[high]);
  return i+1;
}
void printArray(int arr[], int no){
  for (int i=0; i<no; i++)
    printf(" %d ", arr[i]);
  printf("\n");
}
void main(){
  int N;
  printf("Enter Size of Array: ");
  scanf("%d", &N);
  int array[N];
  srand(time(NULL));
  for (int i = 0; i < N; i++) {
    array[i] = rand();
  }
  printf("Original Array: ");
  printArray(array, N);
  clock_t start_time = clock();
  quickSort(array, 0, N - 1);
  clock_t end_time = clock();
  double time_taken = ((double)(end_time - start_time)) / CLOCKS_PER_SEC;
  printf("Sorted Array: ");
  printArray(array, N);
  printf("Time taken to sort: %.10f seconds\n", time_taken);
}
```

Enter Size of Array: 11

Original Array: 446077171 353601320 890133991 1110901735 702633127 142390636 862636494 669453761 842534494 2117555987 1664475425 Sorted Array: 142390636 353601320 446077171 669453761 702633127 842534494 862636494 890133991 1110901735 1664475425 2117555987 Time taken to sort: 0.0000070000 seconds

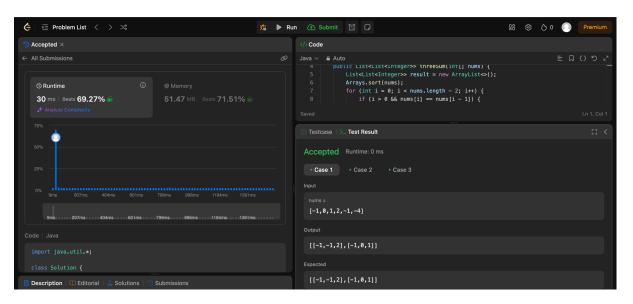
## Program - 4 (b)

Question: LeetCode Program related to sorting.

```
class Solution {
  public List<List<Integer>> threeSum(int[] nums) {
    List<List<Integer>> result = new ArrayList<>();
    Arrays.sort(nums);
    for (int i = 0; i < nums.length - 2; i++) {
       if (i > 0 \&\& nums[i] == nums[i - 1]) {
         continue;
      }
       int left = i + 1, right = nums.length - 1;
       while (left < right) {
         int sum = nums[i] + nums[left] + nums[right];
         if (sum == 0) {
           result.add(Arrays.asList(nums[i], nums[left], nums[right]));
           while (left < right && nums[left] == nums[left + 1]) {
              left++;
           }
           while (left < right && nums[right] == nums[right - 1]) {
              right--;
           }
           left++;
           right--;
         } else if (sum < 0) {
           left++;
         } else {
```

```
right--;
}

return result;
}
```



#### Program - 5

Question: Sort a given set of N integer elements using Heap Sort technique and compute its time taken.

```
#include <stdio.h>
#include <stdlib.h>
#include <time.h>
void heapify(int arr[], int n, int i) {
  int largest = i;
  int left = 2 * i + 1;
  int right = 2 * i + 2;
  // If left child is larger than root
  if (left < n && arr[left] > arr[largest])
     largest = left;
  // If right child is larger than current largest
  if (right < n && arr[right] > arr[largest])
     largest = right;
  // If largest is not root
  if (largest != i) {
     int temp = arr[i];
     arr[i] = arr[largest];
     arr[largest] = temp;
     heapify(arr, n, largest);
  }
}
void heapSort(int arr[], int n) {
  // Build heap (rearrange array)
  for (int i = n / 2 - 1; i >= 0; i--)
     heapify(arr, n, i);
```

```
// One by one extract elements from heap
  for (int i = n - 1; i > 0; i--) {
    // Move current root to end
    int temp = arr[0];
    arr[0] = arr[i];
    arr[i] = temp;
    // Call max heapify on the reduced heap
    heapify(arr, i, 0);
  }
}
int main() {
  int n;
  printf("Enter number of elements: ");
  scanf("%d", &n);
  int arr[n];
  printf("Enter %d integers:\n", n);
  for (int i = 0; i < n; i++)
    scanf("%d", &arr[i]);
  clock_t start = clock();
  heapSort(arr, n);
  clock_t end = clock();
  double time_taken = (double)(end - start) / CLOCKS_PER_SEC;
  printf("Sorted array:\n");
  for (int i = 0; i < n; i++)
    printf("%d ", arr[i]);
  printf("\n");
  printf("Time taken for Heap Sort: %.6f seconds\n", time_taken);
}
```

```
/rishitmakadia/Coding/1BM23CS177_ADA_4/"Lab_5_HeapSort
Enter number of elements: 10
Enter 10 integers:
10 14 15 22 41 9 5 34 54 11
Sorted array:
5 9 10 11 14 15 22 34 41 54
Time taken for Heap Sort: 0.000009 seconds
```

## Program - 6 (a)

Question: Implement 0/1 Knapsack problem using dynamic programming.

```
#include <stdio.h>
int max(int a, int b) {
  return (a > b) ? a : b;
}
int knapsack(int capacity, int weights[], int values[], int n) {
  int i, w;
  int dp[n+1][capacity+1];
  // Build table dp[][] in bottom-up manner
  for (i = 0; i \le n; i++) {
    for (w = 0; w \le capacity; w++) {
       if (i == 0 | | w == 0)
         dp[i][w] = 0;
       else if (weights[i-1] <= w)
         dp[i][w] = max(values[i-1] + dp[i-1][w - weights[i-1]], dp[i-1][w]);
       else
         dp[i][w] = dp[i-1][w];
    }
  }
  return dp[n][capacity];
}
int main() {
  int n, capacity;
  printf("Enter number of items: ");
  scanf("%d", &n);
  printf("Enter knapsack capacity: ");
  scanf("%d", &capacity);
```

```
int values[n], weights[n];
for (int i = 0; i < n; i++) {
    printf("Item %d - Value & Weight: ", i + 1);
    scanf("%d %d", &values[i], &weights[i]);
}
int maxValue = knapsack(capacity, weights, values, n);
printf("Maximum value in Knapsack = %d\n", maxValue);
return 0;
}</pre>
```

```
Enter number of items: 4
Enter knapsack capacity: 5
Item 1 - Value & Weight: 12 2
Item 2 - Value & Weight: 15 3
Item 3 - Value & Weight: 25 1
Item 4 - Value & Weight: 10 2
Maximum value in Knapsack = 47
```

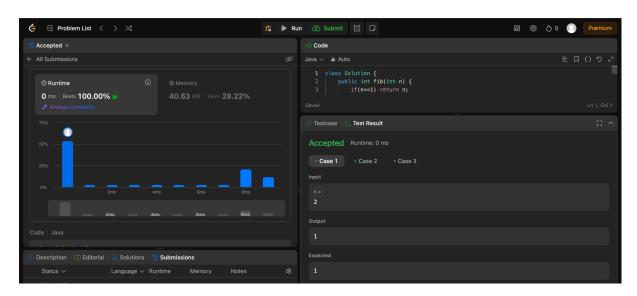
## Program - 6 (b)

Question: LeetCode Program related to Knapsack problem or Dynamic

Programming.

#### Code:

```
class Solution {
    public int fib(int n) {
        if(n<=1) return n;
        int[] dp = new int[n+1];
        dp[0]=0;
        dp[1]=1;
        for(int i =2; i<=n; i++){
              dp[i]=dp[i-1]+dp[i-2];
        }
        return dp[n];
    }
}</pre>
```



## Program - 7 (a)

Question: Implement All Pair Shortest paths problem using Floyd's algorithm.

```
#include <stdio.h>
#define INF 99 //99 for infinity
#define V 100
void printSolution(int dist[][V], int n) {
  printf("Shortest distances between every pair of vertices:\n");
  for (int i = 0; i < n; i++) {
     for (int j = 0; j < n; j++) {
       if (dist[i][j] == INF)
          printf("%4s", "INF");
       else
          printf("%4d", dist[i][j]);
     }
     printf("\n");
  }
}
void floyd(int graph[][V], int n) {
  int dist[V][V];
  for (int i = 0; i < n; i++)
    for (int j = 0; j < n; j++)
       dist[i][j] = graph[i][j];
  // Main loop
  for (int i = 0; i < n; i++) {
     for (int j = 0; j < n; j++) {
       for (int k = 0; k < n; k++) {
          if (dist[j][i] != INF && dist[i][k] != INF && dist[j][i] + dist[i][k] < dist[j][k])
            dist[j][k] = dist[j][i] + dist[i][k];
```

```
}
    }
  }
  printSolution(dist, n);
}
int main() {
  int n;
  int graph[V][V];
  printf("Enter number of vertices: ");
  scanf("%d", &n);
  printf("Enter the adjacency matrix (use 99 for INF):\n");
  for (int i = 0; i < n; i++)
    for (int j = 0; j < n; j++)
       scanf("%d", &graph[i][j]);
  floyd(graph, n);
}
```

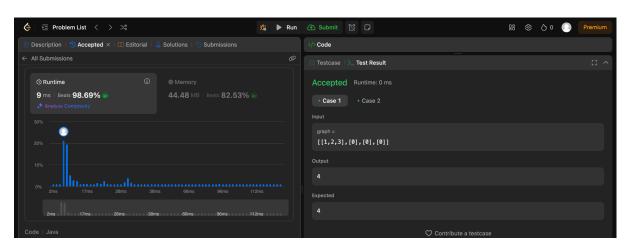
```
Enter number of vertices: 4
Enter the adjacency matrix (use 99 for INF):
      99
99 0
      99
          2
   99 0
99 99 99
Shortest distances between every pair of vertices:
               3
       1 INF
               2
 INF
       0 INF
               6
       4
 INF INF INF
               0
```

## Program - 7 (b)

**Question: Shortest Path visiting All Nodes** 

```
class Solution {
  public int shortestPathLength(int[][] graph) {
    int n = graph.length;
    if (n == 1) return 0;
    int target = (1 << n) - 1; // All nodes visited (all bits set)
    Queue<int[]> queue = new LinkedList<>();
    boolean[][] visited = new boolean[n][1 << n];</pre>
    // Initialize queue with all nodes as starting points
    for (int i = 0; i < n; i++) { // Fixed: Removed illegal character
       queue.offer(new int[]{i, 1 << i});
       visited[i][1 << i] = true;</pre>
    }
    int steps = 0;
    while (!queue.isEmpty()) {
       int size = queue.size();
       for (int i = 0; i < size; i++) {
         int[] current = queue.poll();
         int node = current[0];
         int state = current[1];
         if (state == target) {
            return steps;
         }
```

```
// Visit all neighbors
for (int neighbor : graph[node]) {
    int newState = state | (1 << neighbor);
    if (!visited[neighbor][newState]) {
        visited[neighbor][newState] = true;
        queue.offer(new int[]{neighbor, newState});
    }
    }
    steps++;
}
return -1; // Shouldn't reach here for connected graph
}</pre>
```



# Program - 8 (a)

Question: Find Minimum Cost Spanning Tree of a given undirected graph using Prim's algorithm.

```
#include <stdio.h>
int cost[10][10], vt[10], et[10][2], vis[10], n;
int sum = 0, x = 1, e = 0;
void prims() {
  int m, j, min, u, v, k;
  vt[x] = 1;
  vis[1] = 1;
  for (int s = 1; s < n; s++) {
    min = 999;
    j = x;
    while (j > 0) {
       k = vt[j];
       for (m = 1; m \le n; m++) {
         if (vis[m] == 0 \&\& cost[k][m] != 0 \&\& cost[k][m] < min) {
           min = cost[k][m];
           u = k;
           v = m;
         }
       }
      j--;
    }
    vt[++x] = v;
    e++;
    vis[v] = 1;
    sum += min;
```

```
et[e][0] = u;
    et[e][1] = v;
  }
}
void main() {
  printf("Enter No. of Vertices: ");
  scanf("%d", &n);
  printf("Enter Adjacency Matrix (Cost):\n");
  for (int i = 1; i <= n; i++) {
    for (int j = 1; j \le n; j++) {
       scanf("%d", &cost[i][j]);
      if (cost[i][j] == 0 \&\& i != j) {
         cost[i][j] = 999;
       }
    }
    vis[i] = 0;
  }
  prims();
  printf("Spanning Tree:\n");
  for (int i = 1; i <= e; i++) {
    printf("(%d, %d)\t", et[i][0], et[i][1]);
  }
  printf("\nMinimum Weight = %d\n", sum);
}
```

```
Enter No. of Vertices: 5
Enter Adjacency Matrix (Cost):
0 7 3 0 0
7 0 0 4 0
3 0 0 2 6
0 4 2 0 5
0 0 6 5 0
Spanning Tree:
(1, 3) (3, 4) (4, 2) (4, 5)
Minimum Weight = 14
```

## Program - 8 (b)

Question: Find Minimum Cost Spanning Tree of a given undirected graph using Kruskal's algorithm.

```
#include <stdio.h>
void unionn(int i, int j, int parent[]) {
  if (i < j)
     parent[j] = i;
  else
     parent[i] = j;
}
int find(int v, int parent[]) {
  while (parent[v] != v)
    v = parent[v];
  return v;
}
void kruskal(int n, int a[10][10]) {
  int count = 0, k = 0, sum = 0;
  int min, i, j, u, v, parent[10], temp[10][2];
  for (int I = 0; I < n; I++)
     parent[l] = l;
  while (count < n - 1) {
     min = 999;
     for (int i = 0; i < n; i++) {
       for (int j = 0; j < n; j++) {
         if (a[i][j] < min && a[i][j] != 0) {
            min = a[i][j];
            u = i;
            v = j;
```

```
}
      }
    }
    i = find(u, parent);
    j = find(v, parent);
    if (i != j) {
      unionn(i, j, parent);
      temp[k][0] = u;
      temp[k][1] = v;
      sum += a[u][v];
      count++;
      k++;
    }
    a[u][v] = a[v][u] = 999;
  }
  if (count == n - 1) {
    printf("Minimum Spanning Tree:\n");
    for (int m = 0; m < k; m++)
      printf("Edge (%d, %d)\n", temp[m][0], temp[m][1]);
    printf("Minimum Weight: %d\n", sum);
  } else {
    printf("Not a Spanning Tree\n");
  }
void main() {
  int n, i, j, a[10][10];
  printf("Enter No. of Vertices: ");
  scanf("%d", &n);
  printf("Enter Adjacency Matrix (Cost)\n");
```

}

```
for (i = 0; i < n; i++) {
    for (j = 0; j < n; j++)
        scanf("%d", &a[i][j]);
    }
    kruskal(n, a);
}</pre>
```

```
Enter No. of Vertices: 5
Enter Adjacency Matrix (Cost)
0 7 3 0 0
7 0 0 4 0
3 0 0 2 6
0 4 2 0 5
0 0 6 5 0
Minimum Spanning Tree:
Edge (2, 3)
Edge (0, 2)
Edge (1, 3)
Edge (3, 4)
Minimum Weight: 14
```

## Program - 9 (a)

Question: Implement Fractional Knapsack using Greedy technique.

```
#include <stdio.h>
int main() {
  int weight[50], profit[50], capacity, n, i, j;
  float pTOw[50], totalValue = 0.0, temp;
  printf("Enter the number of items: ");
  scanf("%d", &n);
  for (i = 0; i < n; i++) {
    printf("item[%d] : Weight and Profit = ", i + 1);
    scanf("%d %d", &weight[i], &profit[i]);
  }
  printf("Enter the capacity of knapsack: ");
  scanf("%d", &capacity);
  for (i = 0; i < n; i++) {
    pTOw[i] = (float)profit[i] / weight[i];
  }
  for (i = 0; i < n; i++) {
    for (j = i + 1; j < n; j++) {
       if (pTOw[i] < pTOw[j]) {</pre>
         temp = pTOw[j];
                              pTOw[j] = pTOw[i];
                                                            pTOw[i] = temp;
         temp = weight[j]; weight[j] = weight[i];
                                                            weight[i] = (int)temp;
                              profit[j] = profit[i];
                                                            profit[i] = (int)temp;
         temp = profit[j];
      }
    }
  }
  printf("\nItems included in the knapsack:\n");
  for (i = 0; i < n; i++) {
```

```
Enter the number of items: 3
item[1] : Weight and Profit = 18 25
item[2] : Weight and Profit = 15 24
item[3] : Weight and Profit = 10 15
Enter the capacity of knapsack: 20

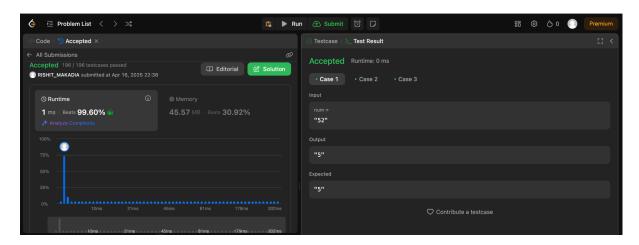
Items included in the knapsack:
100% of item 1 (Profit: 24, Weight: 15)
50.0% of item 2 (Profit: 15, Weight: 10)
Maximum profit = 31.50
```

## Program - 9 (b)

**Question: Largest Odd Number in String** 

#### Code:

```
class Solution {
  public String largestOddNumber(String num) {
    int index = num.length() - 1;
    for (int i=index ; i>=0; i--){
      if((num.charAt(i)-'0')%2==1){
         // return num; // Wrong
         return num.substring(0, i+1);
      }
      // num=num.substring(0, i-1); // Wrong
    }
    return "";
}
```



#### Program - 10

Question: From a given vertex in a weighted connected graph, find shortest paths to other vertices using Dijkstra's algorithm.

```
#include <stdio.h>
#define INF 9999
void printPath(int parent[], int j) {
  if (parent[j] == -1)
    return;
  printPath(parent, parent[j]);
  printf(" -> %d", j);
}
void dijkstra(int n, int cost[10][10], int src) {
  int dist[10], visited[10], parent[10];
  int i, j, u, min;
  // Initialize distances and visited array
  for (i = 0; i < n; i++) {
    dist[i] = cost[src][i];
    visited[i] = 0;
    if (cost[src][i] != INF && i != src)
       parent[i] = src;
    else
       parent[i] = -1;
  }
  dist[src] = 0;
                                                parent[src] = -1;
                 visited[src] = 1;
  for (i = 1; i < n; i++) {
    min = INF;
    u = -1;
    // Find the nearest unvisited vertex
```

```
for (j = 0; j < n; j++) {
       if (!visited[j] && dist[j] < min) {
         min = dist[j];
         u = j;
       }
    }
    if (u == -1) break;
    visited[u] = 1;
    // Update distances of adjacent vertices
    for (j = 0; j < n; j++) {
       if (!visited[j] && cost[u][j] != INF && dist[u] + cost[u][j] < dist[j]) {
         dist[j] = dist[u] + cost[u][j];
         parent[j] = u;
       }
    }
  }
  // Output the shortest path and cost
  printf("\nShortest paths from vertex %d:\n", src);
  for (i = 0; i < n; i++) {
    if (dist[i] != INF) {
       printf("Path to %d: %d", i, src);
       printPath(parent, i);
       printf(" | Cost: %d\n", dist[i]);
    } else {
       printf("No path to vertex %d\n", i);
    }
  }
void main() {
```

}

```
int n, i, j, src;
  int cost[10][10];
  printf("Enter number of vertices: ");
  scanf("%d", &n);
  printf("Enter adjacency matrix (0 for no edge):\n");
  for (i = 0; i < n; i++) {
    for (j = 0; j < n; j++) {
       scanf("%d", &cost[i][j]);
       if (i != j && cost[i][j] == 0)
         cost[i][j] = INF;
    }
  }
  printf("Enter source vertex (0 to %d): ", n - 1);
  scanf("%d", &src);
  dijkstra(n, cost, src);
}
```

```
Enter number of vertices: 5
Enter adjacency matrix (0 for no edge):
0 7 3 0 0
7 0 0 4 0
3 0 0 2 6
0 4 2 0 5
0 0 6 5 0
Enter source vertex (0 to 4): 0

Shortest paths from vertex 0:
Path to 0: 0 | Cost: 0
Path to 1: 0 -> 1 | Cost: 7
Path to 2: 0 -> 2 | Cost: 3
Path to 3: 0 -> 2 -> 3 | Cost: 5
Path to 4: 0 -> 2 -> 4 | Cost: 9
```

#### Program - 11

Question: Implement "N-Queens Problem" using Backtracking.

```
#include<stdio.h>
#include<stdbool.h>
#define N 4
void printSolution(int board[N][N]){
  for(int i=0; i<N;i++){
    for(int j=0; j<N;j++)
      printf("%s", board[i][j]? "Q ":". ");
    printf("\n");
  }
  printf("\n");
}
bool isSafe(int board[N][N], int row,int col){
  for (int i=0; i<col;i++)
    if(board[row][i])
       return false;
  for(int i=row, j=col; i>=0 && j>=0; i--, j--)
    if(board[i][j])
       return false;
  for(int i=row, j=col; i<=N && j>=0; i++, j--)
    if(board[i][j])
       return false;
  return true;
}
void solveNQueen(int board[N][N], int col){
  if(col == N) {
    printSolution(board);
```

```
return;
  }
  for (int i=0; i<N; i++){
    if(isSafe(board, i, col)){
      board[i][col] = 1;
      solveNQueen(board, col+1);
      board[i][col] = 0; // Backtrack
    }
  }
}
void NQueens(){
  int board[N][N] = {0}; // Initialize board with 0 (no queens)
  solveNQueen(board, 0); // Start solving the N-Queens problem from the first column
}
int main(){
  NQueens();
}
```