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```
% This is to plot the Cramer-Rao Lower Bound of a parameter vs the  
% parameter itself and note down the my inference from the obtained plot.
```

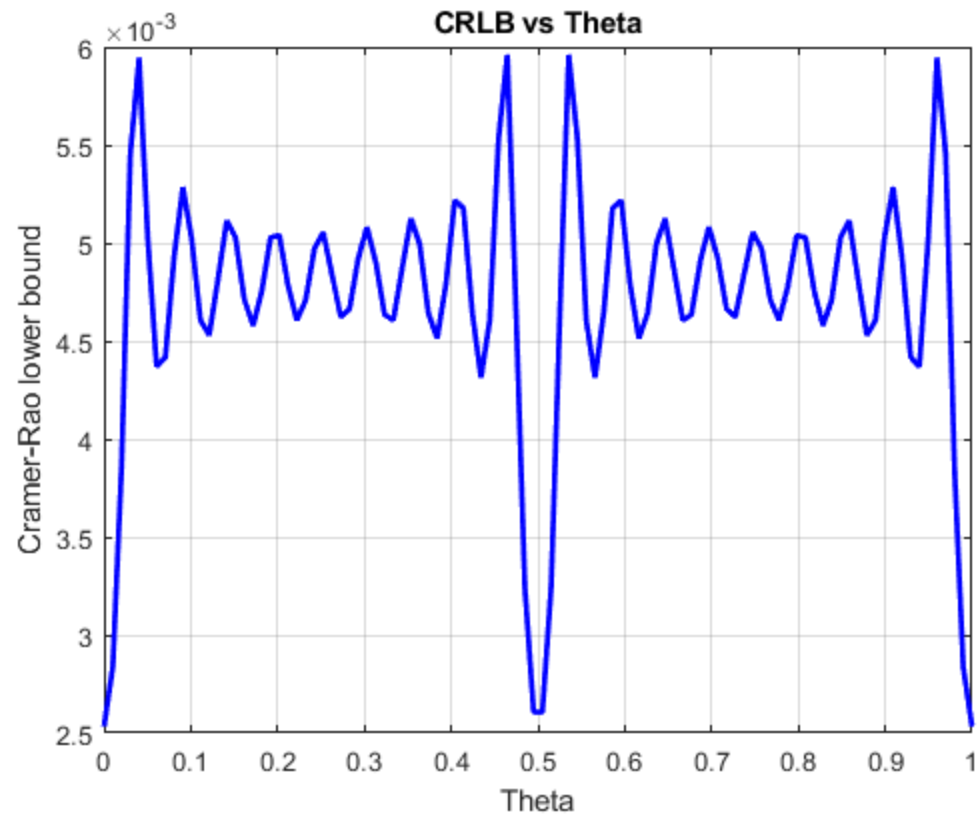
## SYSTEM SETTING

Consider a quantity  $x[n] = s[n; \theta] + w[n]$  where  $s[n; \theta]$  is any signal (AC or DC) and  $w[n]$  is an AWGN with variance  $\sigma^2$ . Let us consider that  $s[n; \theta] = A \sin(2\pi\theta n + \phi)$ . Thus,  $s[n; \theta]$  is dependent on three parameters:  $A$ ,  $\theta$  and  $\phi$ . For this example, we are trying to estimate the value of frequency, i.e.,  $\theta$  of the signal  $s$ . The CRLB for the given estimator is found out as follows:

```
% Defining the parameters  
N = 10; % Number of terms in the data set {x[n]}  
A = 1; % Assuming A is a constant  
theta_values = linspace(0, 1, 100); % Varying theta from 0 to 100  
  
variance_values = zeros(1, length(theta_values));  
  
for k = 1:length(theta_values)  
    theta = theta_values(k);  
    sum_term = 0;  
    for n = 0:N-1  
        sum_term = sum_term + (A*cos(2*pi*theta*n))^2;  
    end  
    variance = 1 / (4 * pi^2 * sum_term);  
    variance_values(k) = variance;  
end
```

## PLOTTING

```
figure  
plot(theta_values, variance_values, 'b-', 'LineWidth', 2)  
xlabel('Theta')  
ylabel('Cramer-Rao lower bound')  
title('CRLB vs Theta')  
grid on
```



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