

```
public static int numberOfWaysToMakeChange(int sum, int[] denoms) {
   int n = denoms.length;
   //return solveRecursion(denoms,n,sum);
   int[][] dp = new int[n + 1][sum + 1];
   for (int rows[] : dp) {
        Arrays.fill(rows, val: -1);
   }
   return solveMemo(denoms, n, sum, dp);
}
```

```
/*
    Take and not take approach

Function has → (Array,size,sum)
    if taken → (array,n,sum - array[n-1]) //reduce the sum
    it not taken → (array,n-1,sum) //reduce the size

*/

2 usages
static int solveRecursion(int[] arr, int n, int sum) {

    //if we reach sum = 0 then we got one value
    if (sum = 0) return 1;

    if (sum < 0) return 0;

    int take = solveRecursion(arr, n, sum: sum - arr[n - 1]);
    int notTake = solveRecursion(arr, n: n - 1, sum);

    return take + notTake;</pre>
```

```
//recursion and memo
/*
    2 states are changing here on is sum and size
    */
3 usages
static int solveMemo(int[] arr, int n, int sum, int[][] dp) {
    //base cases

    //if we reach sum = 0 then we got one value
    if (sum = 0) return 1;

    if (sum < 0) return 0;

    if (n < 0) return 0;

    if (dp[n][sum] ≠ -1) return dp[n][sum];

int take = solveMemo(arr, n, sum: sum - arr[n - 1], dp);
    int notTake = solveMemo(arr, n: n - 1, sum, dp);

    dp[n][sum] = take + notTake;

return dp[n][sum];</pre>
```