

Atma Ram Sanatan Dharma College

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Data Structures

Practical File

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1. Given a list of N elements, which follows no particular arrangement, you are required to search an element x in the list. The list is stored using array data structure. If the search is successful, the output should be the index at which the element occurs, otherwise returns -1 to indicate that the element is not present in the list. Assume that the elements of the list are all distinct. Write a program to perform the desired task.

```
#include <iostream>
#define MAX_SIZE 100
using namespace std;

template <class T> int linearSearch(T *arr, int size, T el)
{
    for (int i = 0; i < size; i++)
        if (arr[i] == el)
            return i;
    return -1;
}

int main(void)
{
    int ch = 1, el, res, N, arr[MAX_SIZE];
    cout << "Enter Number of Elements: ";    cin >> N;
    cout << "Enter Array Elements: ";
    for (int i = 0; i < N; i++)
        cin >> arr[i];

    cout << "Enter Search Element: ";    cin >> el;
    res = linearSearch<int>(arr, N, el);

    if (res != -1)
        cout << "FOUND: Element found at index "<< res << endl;
    else
        cout << "NOT FOUND: Element not found in array"<< endl;

    return 0;
}
```

Output

```
Enter Number of Elements: 4
Enter Array Elements: 1 9 5 2
Enter Search Element: 5
FOUND: Element found at index 2

Enter Number of Elements: 4
Enter Array Elements: 1 9 5 2
Enter Search Element: 3
NOT FOUND: Element not found in array
```

2. Given a list of N elements, which is sorted in ascending order, you are required to search an element x in the list. The list is stored using array data structure. If the search is successful, the output should be the index at which the element occurs, otherwise returns -1 to indicate that the element is not present in the list. Assume that the elements of the list are all distinct. Write a program to perform the desired task.

```
#include <iostream>
#define MAX_SIZE 100
using namespace std;

template <class T> int binarySearch(T *arr, int left, int right, T el)
{
    if (right >= left)
    {
        int mid = (right + left) / 2;
        if (arr[mid] == el)
            return mid;
        if (arr[mid] > el)
            return binarySearch(arr, left, mid - 1, el);
        return binarySearch(arr, mid + 1, right, el);
    }
    return -1;
}

int main(void)
{
    int ch = 1, el, res, N, arr[MAX_SIZE];
    cout << "Enter Number of Elements: ";    cin >> N;

    cout << "Enter Array Elements: ";
    for (int i = 0; i < N; i++)
        cin >> arr[i];

    cout << "Enter Search Element: ";
    cin >> el;
    res = binarySearch<int>(arr, 0, N - 1, el);
    if (res != -1)
        cout << "FOUND: Element found at index "<< res << endl;
```

```

    else
        cout << "NOT FOUND: Element not found in array"<< endl;
    return 0;
}

```

Output

```

Enter Number of Elements: 4
Enter Array Elements: 1 2 3 4
Enter Search Element: 4
FOUND: Element found at index 3

Enter Number of Elements: 4
Enter Array Elements: 1 2 3 4
Enter Search Element: 5
NOT FOUND: Element not found in array

```

3. Write a program to implement singly linked list which supports the following operations:

- (i) Insert an element x at the beginning of the singly linked list
- (ii) Insert an element x at position in the singly linked list
- (iii) Remove an element from the beginning of the singly linked list
- (iv) Remove an element from position in the singly linked list.
- (v) Search for an element x in the singly linked list and return its pointer
- (vi) Concatenate two singly linked lists

```

#include <iostream>
using namespace std;

void getch();
void clrscr();

template <class T> class Node {
public:
    T info;
    Node *ptr;
};

template <class T> class SinglyLinkedList

```

```

{
    protected:
        Node<T> *head, *tail;
    public:
        // Constructor
        SinglyLinkedList()
        {
            head = tail = NULL;
        }

        // Destructor
        ~SinglyLinkedList()
        {
            if (this->isEmpty())
                return;
            Node<T> *ptr, *temp = head;
            while (temp != NULL)
            {
                ptr = temp->ptr;
                delete temp;
                temp = ptr;
            }
            head = tail = NULL;
            return;
        }

        // Checks if the list is empty - O(1)    bool isEmpty() {    return
(head == NULL || tail == NULL);
}

        // Inserts a node at the beginning - O(1)
void insertFront(T info)
{
    Node<T> *temp = new Node<T>();
    temp->info = info;
    temp->ptr = head;
    if (this->isEmpty())
        tail = temp;
    head = temp;
    cout << "Inserted " << info << " at front...";
    this->display();
    return;
}

// Inserts a node at a specified location - O(n)
void insertAtLoc(int loc, T info)
{
    if (loc == 1)

```

```

{
    this->insertFront(info);
    return;
}
Node<T> *temp = head;
for (int i = 1; temp != NULL && i < loc - 1; i++)
    temp = temp->ptr;
if (temp == NULL)
{
    cout << "Invalid location...\n";
    return;
}
if (temp == tail)
{
    this->insertBack(info);    return;
}
Node<T> *node = new Node<T>();
node->info = info;
node->ptr = temp->ptr;
temp->ptr = node;
cout << "Inserted node " << info << " at location " << loc << "...";
this->display();
return;
}

// Inserts a node at the end - O(1)
void insertBack(T info)
{
    Node<T> *temp = new Node<T>();
    temp->info = info;
    temp->ptr = NULL;
    if (this->isEmpty())
        head = tail = temp;
    else
        tail->ptr = temp;
    tail = temp;
    cout << "Inserted " << info << " at back...";
    this->display();
    return;
}

// Removes a node from the beginning - O(1)
void deleteFront()
{
    if (this->isEmpty())
    {
        cout << "\nList is empty...\n";
        return;
    }
}

```

```

    }
    Node<T> *temp = head;
    head = temp->ptr;
    delete temp;
    if (this->isEmpty())
        tail = NULL;
    cout << "\nDeleted node at front...";
    this->display();
    return;
}

// Removes a node at a specified location - O(n)
void deleteAtLoc(int loc)
{
    if (this->isEmpty())
    {
        cout << "\nList is empty...\n";
        return;
    }
    if (loc == 1)
    {
        this->deleteFront();
        return;
    }
    Node<T> *node, *temp = head;
    for (int i = 1; temp != NULL && i < loc - 1; i++)
        temp = temp->ptr;
    if (temp == NULL || temp->ptr == NULL)
    {
        cout << "Invalid location...\n";
        return;
    }
    if (temp == tail)
    {
        this->deleteBack();
        return;
    }
    node = temp->ptr->ptr;
    delete temp->ptr;
    temp->ptr = node;
    cout << "Deleted node "<< "at location " << loc << "...";
    this->display();
    return;
}

// Removes a node at the end - O(n)
void deleteBack()
{
    if (this->isEmpty())

```

```

{
    cout << "\nList is empty...\n";
    return;
}
if (head == tail)
{
    this->deleteFront();
    return;
}
else
{
    Node<T> *temp = head;
    while (temp->ptr->ptr != NULL)
        temp = temp->ptr;
    delete temp->ptr;
    temp->ptr = NULL;
    tail = temp;
}
cout << "\nDeleted node at back...";
this->display();
return;
}

// Reverses the linked list - O(n)
void reverse()
{
    if (this->isEmpty())
    {
        cout << "\nList is empty...\n";
        return;
    }
    Node<T> *temp = head, *prev = NULL,
    *next = NULL;
    tail = temp;
    while (temp != NULL)
    {
        next = temp->ptr;
        temp->ptr = prev;
        prev = temp;
        temp = next;
    }

    head = prev;
    cout << "\nList reversed...";
    this->display();
    return;
}

```



```

    // Concatenates two lists - O(n)
void concat(SinglyLinkedList<T> &list)
{
    if (!list.isEmpty() && !this->isEmpty())
    {
        Node<T> *node,
        *temp = tail,
        *temp1 = list.head;
        while (temp1 != NULL)
        {
            node = new Node<T>();
            node->info = temp1->info;
            node->ptr = NULL;
            temp->ptr = node;
            temp = temp->ptr;
            temp1 = temp1->ptr;
        }
        tail = node;
        cout << "Concatenated two lists...\n";
        this->display();
    }
    else
        cout << "\nOne of the lists is empty...\n";
    return;
}

// Overloads the + operator - O(n)
void operator+(SinglyLinkedList<T> &list)
{
    this->concat(list);
    return;
}

// Searches for an element - O(n)
Node<T> *search(T ele)
{
    if (this->isEmpty())
        return nullptr;
    Node<T> *temp = head;
    while (temp != NULL)
    {
        if (temp->info == ele)
            return temp;
        temp = temp->ptr;
    }
    return nullptr;
}

```

```

    // Calculates the number of nodes - O(n)
int count()
{
    if (this->isEmpty())
    {
        cout << "\nList is empty...\n";
        return -1;
    }
    int count = 0; Node<T> *temp;
    for (temp = head; temp != NULL;
        temp = temp->ptr, count++);
    return count;
}

// Traverses the list and prints all nodes - O(n)
void display()
{
    if (this->isEmpty())
    {
        cout << "\nList is empty...\n";
        return;
    }
    Node<T> *temp = head;
    cout << "\nList: ";
    while (temp->ptr != NULL)
    {
        cout << temp->info << " -> ";
        temp = temp->ptr;
    }
    cout << temp->info << endl;
    return;
}
};

int main(void)
{
    int choice, ele, info, loc, count;
    SinglyLinkedList<int> list, list2;
    do
    {
        cout << "\tSingly Linked List\n"
        << "===== \n"
        << "  (1) Search      (2) InsertFront\n"
        << "  (3) InsertBack  (4) InsertAtLoc\n"
        << "  (5) DeleteFront (6) DeleteBack\n"
        << "  (7) DeleteAtLoc (8) Display\n"
        << "  (9) Count       (10) Reverse\n"

```

```

<< " (11) Concat (0) Exit\n\n";
cout << "Enter Choice: ";
cin >> choice;
switch (choice)
{
    case 1:
        cout << "\nEnter Search Element: ";
        cin >> ele;
        if (list.search(ele) != nullptr)
            cout << "Element " << ele << " found...\n";
        else
            cout << "Element not found or List is Empty...\n";
        break;
    case 2:
        cout << "\nEnter Element: ";
        cin >> info;
        list.insertFront(info);
        break;
    case 3:
        cout << "\nEnter Element: ";
        cin >> info;
        list.insertBack(info);
        break;
    case 4:
        cout << "\nEnter Location: ";
        cin >> loc;
        cout << "Enter Element: ";
        cin >> info;
        list.insertAtLoc(loc, info);
        break;
    case 5:
        list.deleteFront();
        break;
    case 6:
        list.deleteBack();
        break;
    case 7:
        cout << "\nEnter Location: ";
        cin >> loc;
        list.deleteAtLoc(loc);
        break;
    case 8:
        list.display();
        break;
    case 9:
        count = list.count();
        if (count != -1)
            cout << "\nNumber of Nodes: " << count << endl;

```

```

        break;
    case 11:
        if (!list2.isEmpty())
        {
            cout << "\nList B:";
            list2.display();
        }
        cout << "\nNumber of Nodes to add in List B: ";
        cin >> count;
        if (count)
        {
            cout << "Enter Elements to List B: ";
            for (int i = 0; i < count; i++)
            {
                cin >> info;
                list2.insertBack(info);
            }
            list + list2;
        }
        break;
    case 10:
        list.reverse();
        break;
    case 0:
        default:
        break;
    }
    getch();
    clrscr();
}
while (choice != 0);
return 0;
}

void getch()
{
    cout << "\nPress any key to continue...";
    cin.ignore();
    cin.get();
    return;
}

void clrscr()
{
    #ifdef _WIN32    system("cls");
    #elif __unix__   system("clear");
    #endif    return;
}

```

Output

```

Singly Linked List
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit

```

Enter Choice: 2

Enter Element: 10
 Inserted 10 at front...
 List: 10

Press any key to continue...☐

```

Singly Linked List
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit

```

Enter Choice: 4

Enter Location: 2
 Enter Element: 20
 Inserted 20 at back...
 List: 10 -> 20

Press any key to continue...☐

```

Singly Linked List
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit

```

Enter Choice: 7

Enter Location: 2
 Deleted node at location 2...
 List: 15

Press any key to continue...☐

```

Singly Linked List
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit

```

Enter Choice: 5

Deleted node at front...
 List: 15 -> 20

Press any key to continue...☐

```

Singly Linked List
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit

```

Enter Choice: 4

Enter Location: 2
 Enter Element: 15
 Inserted node 15 at location 2...
 List: 10 -> 15 -> 20

Press any key to continue...☐

```

Singly Linked List
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit

```

Enter Choice: 1

Enter Search Element: 15
 Element 15 found...

Press any key to continue...☐

Singly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Enter Choice: 1

Enter Search Element: 10

Element not found or List is Empty...

Press any key to continue...█

Singly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Enter Choice: 11

Number of Nodes to add in List B: 3

Enter Elements to List B: 1 2 3

Inserted 1 at back...

List: 1

Inserted 2 at back...

List: 1 -> 2

Inserted 3 at back...

List: 1 -> 2 -> 3

Concatenated two lists...

List: 15 -> 1 -> 2 -> 3

Press any key to continue...█

4. Write a program to implement doubly linked list which supports the following operations:

- (i) Insert an element x at the beginning of the doubly linked list
- (ii) Insert an element x at position in the doubly linked list
- (iii) Insert an element x at the end of the doubly linked list
- (iv) Remove an element from the beginning of the doubly linked list
- (v) Remove an element from position in the doubly linked list.

- (vi) Remove an element from the end of the doubly linked list
- (vii) Search for an element x in the doubly linked list and return its pointer
- (viii) Concatenate two doubly linked lists

```
#include <iostream>
using namespace std;

void getch();
void clrscr();

template <class T> class Node {
public:
    T info;
    Node *prev;
    Node *next;
};

template <class T> class DoublyLinkedList
{
protected:
    Node<T> *head, *tail;
public:
    // Constructor
    DoublyLinkedList()
    {
        head = tail = NULL;
    }

    // Destructor
    ~DoublyLinkedList()
    {
        if (this->isEmpty())
            return;
        Node<T> *ptr;
        for (; !isEmpty();)
        {
            ptr = head->next;
            delete head;
            head = ptr;
        }
        head = tail = ptr;
        return;
    }

    // Checks if the list is empty - O(1)
    bool isEmpty()
    {

```

```

        return (head == NULL || tail == NULL);
    }

// Inserts a node at the beginning - O(1)
void insertFront(T info)
{
    Node<T> *temp = new Node<T>();
    temp->info = info;
    temp->next = head;
    temp->prev = NULL;
    if (this->isEmpty())
        tail = temp;
    else
        head->prev = temp;
    head = temp;
    cout << "Inserted " << info << " at front...";    this->
display();
    return;
}

// Inserts a node at a specified location - O(n)
void insertAtLoc(int loc, T info)
{
    if (loc == 1)
    {
        this->insertFront(info);
        return;
    }
    Node<T> *temp = head;
    for (int i = 1; temp != NULL && i < loc - 1; i++)
        temp = temp->next;
    if (temp == NULL)
    {
        cout << "Invalid location...\n";
        return;
    }
    if (temp == tail)
    {
        this->insertBack(info);
        return;
    }
    Node<T> *node = new Node<T>();
    node->info = info;
    node->next = temp->next;
    node->prev = temp;
    temp->next->prev = node;
    temp->next = node;
}

```



```

        cout << "Inserted node " << info << " at location " << loc <<
"...";
        this->display();
        return;
    }

    // Inserts a node at the end - O(1)
    void insertBack(T info)
    {
        Node<T> *temp = new Node<T>();
        temp->info = info;
        temp->next = NULL;
        temp->prev = tail;
        if (this->isEmpty())
            head = tail = temp;
        else
            tail->next = temp;
        tail = temp;
        cout << "Inserted " << info << " at back...";
        this->display();
        return;
    }

    // Removes a node from the beginning - O(1)
    void deleteFront()
    {
        if (this->isEmpty())
        {
            cout << "\nList is empty...\n";
            return;
        }
        Node<T> *temp = head;
        head = temp->next;
        if (this->isEmpty())
            tail = NULL;
        else
            head->prev = NULL;
        delete temp;

        cout << "\nDeleted node at front...";
        this->display();
        return;
    }

    // Removes a node at a specified location - O(n)
    void deleteAtLoc(int loc)
    {
        if (this->isEmpty())

```

```

{
    cout << "\nList is empty...\n";
    return;
}
i
f (loc == 1)
{
    this->deleteFront();
    return;
}
Node<T> *node, *temp = head;
for (int i = 1; temp != NULL && i < loc - 1; i++)
    temp = temp->next;
if (temp == NULL || temp->next == NULL)
{
    cout << "Invalid location...\n";
    return;
}
if (temp->next == tail)
{
    this->deleteBack();
    return;
}
node = temp->next->next;
node->prev = temp;
delete temp->next;
temp->next = node;
cout << "Deleted node "<< "at location " << loc << "...";    this-
>display();    return;
}

// Removes a node at the end - O(1)
void deleteBack()
{
    if (this->isEmpty())
    {
        cout << "\nList is empty...\n";
        return;
    }
    Node<T> *temp = tail;
    tail = temp->prev;
    if (this->isEmpty())
        head = NULL;
    else
        tail->next = NULL;
    delete temp;
    cout << "\nDeleted node at back...";
    this->display();
    return;
}

```

```

}

// Reverses the linked list - O(n)
void reverse() {
    if (this->isEmpty())
    {
        cout << "\nList is empty...\n";
        return;
    }
    Node<T> *temp = head,
    *temp1 = NULL;
    tail = temp;
    while (temp != NULL)
    {
        temp1 = temp->prev;

        temp->prev = temp->next;
        temp->next = temp1;
        temp = temp->prev;
    }
    if (temp1 != NULL)
        head = temp1->prev;
    cout << "\nList reversed...";
    this->display();
    return;
}

// Concatenates two lists - O(n)
void concat(DoublyLinkedList<T> &list)
{
    if (!list.isEmpty() && !this->isEmpty())
    {
        Node<T> *node,
        *temp = tail,
        *temp1 = list.head;
        while (temp1 != NULL)
        {
            node = new Node<T>();
            node->info = temp1->info;
            node->next = NULL;
            node->prev = temp;
            temp->next = node;
            temp = temp->next;
            temp1 = temp1->next;
        }
        tail = node;
        cout << "Concatenated two lists...\n";
        this->display();
    }
}

```

```

    }
    else
        cout << "\nOne of the lists is empty...\n";
    return;
}

// Overloads the + operator - O(n)
void operator+(DoublyLinkedList<T> &list)
{
    this->concat(list);
    return;
}

// Searches for an element - O(n)
Node<T> *search(T ele)
{
    if (this->isEmpty())
        return nullptr;
    Node<T> *temp = head;
    while (temp != NULL)
    {
        if (temp->info == ele)
            return temp;
        temp = temp->next;
    }
    return nullptr;
}

// Calculates the number of nodes - O(n)
int count() {
    if (this->isEmpty())
    {
        cout << "\nList is empty...\n";
        return -1;
    }
    int count = 0;
    Node<T> *temp;
    for (temp = head; temp != NULL;
        temp = temp->next, count++);

    return count;
}

// Traverses the list and prints all nodes - O(n)
void display() {
    if (this->isEmpty())
    {
        cout << "\nList is empty...\n";
    }
}

```

```

        return;
    }
    Node<T> *temp = head;
    cout << "\nList: ";
    while (temp->next != NULL)
    {
        cout << temp->info << " -> ";
        temp = temp->next;
    }
    cout << temp->info << endl;
    return;
}
};

int main(void) {
    int info, ele, choice, loc, count;    DoublyLinkedList<int> list, list2;
    do
    {
        cout << "\tDoubly Linked List\n"
        << "===== \n"
        << "  (1) Search      (2) InsertFront\n"
        << "  (3) InsertBack  (4) InsertAtLoc\n"
        << "  (5) DeleteFront (6) DeleteBack\n"
        << "  (7) DeleteAtLoc (8) Display\n"
        << "  (9) Count       (10) Reverse\n"
        << " (11) Concat      (0) Exit\n\n";
        cout << "Enter Choice: ";
        cin >> choice;
        switch (choice)
        {
            case 1:
                cout << "\nEnter Search Element: ";
                cin >> ele;
                if (list.search(ele) != nullptr)
                    cout << "Element " << ele << " found...\n";
                else
                    cout << "Element not found or List is Empty...\n";
                break;
            case 2:
                cout << "\nEnter Element: ";
                cin >> info;
                list.insertFront(info);
                break;
            case 3:
                cout << "\nEnter Element: ";
                cin >> info;
                list.insertBack(info);
                break;

```

```

case 4:
    cout << "\nEnter Location: ";
    cin >> loc;
    cout << "Enter Element: ";
    cin >> info;
    list.insertAtLoc(loc, info);
    break;
case 5:
    list.deleteFront();
    break;
case 6:
    list.deleteBack();
    break;
case 7:
    cout << "\nEnter Location: ";
    cin >> loc;
    list.deleteAtLoc(loc);
    break;
case 8:
    list.display();
    break;
case 9:
    count = list.count();
    if (count != -1)
        cout << "\nNumber of Nodes: " << count << endl;
    break;
case 10:
    list.reverse();
    break;
case 11:
    if (!list2.isEmpty())
    {
        cout << "\nList B:";
        list2.display();
    }
    cout << "\nNumber of Nodes to add in List B: ";
    cin >> count;
    if (count)
    {
        cout << "Enter Elements to List B: ";
        for (int i = 0; i < count; i++)
        {
            cin >> info;
            list2.insertBack(info);
        }
        list + list2;
    }
    break;

```

```

        case 0:
        default:
            break;
    }
    getch();
    clrscr();

    while (choice != 0);
    return 0;
}
}
void getch()
{
    cout << "\nPress any key to continue...";
    cin.ignore();
    cin.get();
    return;
}
void clrscr()
{
    #ifdef _WIN32    system("cls");
    #elif __unix__   system("clear");
    #endif    return;
}

```

Output

Doubly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Enter Choice: 2

Enter Element: 10

Inserted 10 at front...

List: 10

Press any key to continue...**█**

Doubly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Enter Choice: 3

Enter Element: 30

Inserted 30 at back...

List: 10 -> 30

Press any key to continue...**█**

Doubly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Enter Choice: 4

Enter Location: 2

Enter Element: 20

Inserted node 20 at location 2...

List: 10 -> 20 -> 30

Press any key to continue...**█**

Doubly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Enter Choice: 7

Enter Location: 2

Deleted node at location 2...

List: 10 -> 30

Press any key to continue...**█**

Doubly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Enter Choice: 6

Deleted node at back...

List: 10

Press any key to continue...**█**


```

Doubly Linked List
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit

```

Enter Choice: 5

Deleted node at front...
List is empty...

Press any key to continue...█

```

Doubly Linked List
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit

```

Enter Choice: 2

Enter Element: 10
Inserted 10 at front...
List: 10

Press any key to continue...█

```

Doubly Linked List
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit

```

Enter Choice: 11

Number of Nodes to add in List B: 3
Enter Elements to List B: 1 2 3
Inserted 1 at back...
List: 1
Inserted 2 at back...
List: 1 -> 2
Inserted 3 at back...
List: 1 -> 2 -> 3
Concatenated two lists...

List: 10 -> 1 -> 2 -> 3

Press any key to continue...█

5. Write a program to implement circularly linked list which supports the following operations:

- (i) Insert an element x at the front of the circularly linked list
- (ii) Insert an element x after an element y in the circularly linked list
- (iii) Insert an element x at the back of the circularly linked list
- (iv) Remove an element from the back of the circularly linked list
- (v) Remove an element from the front of the circularly linked list
- (vi) remove the element x from the circularly linked list
- (vii) Search for an element x in the circularly linked list and return its pointer
- (viii) Concatenate two circularly linked lists

```

#include <iostream>
using namespace std;

void getch();
void clrscr();

template <class T> class Node {
    public:
        T info;
        Node *prev;
        Node *next;
};

template <class T>
class CircularDoublyLinkedList
{
    protected:
        Node<T> *tail;
    public:
        // Constructor
        CircularDoublyLinkedList()
        {
            tail = NULL;
        }

        // Destructor
        ~CircularDoublyLinkedList()
        {
            if (this->isEmpty())
                return;
            Node<T> *ptr, *temp = tail->next;
            while (temp != tail)
            {
                ptr = temp;
                temp = ptr->next;
                delete ptr;
            }
            delete temp;
            tail = NULL;
            return;
        }

        // Checks if the list is empty - O(1)
        bool isEmpty() {
            return tail == NULL;
        }

        // Inserts a node at the beginning - O(1)

```

```

void insertFront(T info)
{
    Node<T> *temp = new Node<T>();
    temp->info = info;
    if (this->isEmpty())
    {
        temp->next = temp;
        temp->prev = temp;
        tail = temp;
    }

    else
    {
        temp->prev = tail;
        temp->next = tail->next;
        tail->next->prev = temp;
        tail->next = temp;
    }
    cout << "Inserted " << info << " at front...";    this->
display();
    return;
}

// Inserts a node at a specified location - O(n)
void insertAtLoc(T searchEle, T info)
{
    int loc = 0;
    if (this->isEmpty())
    {
        cout << "List Empty...\n";
        return;
    }
    int i = 0;
    Node<T> *temp = tail->next;
    do
    {
        ++i;
        if (temp->info == searchEle)
            loc = i;
        temp = temp->next;
    }
    while (temp != tail->next);

    if (loc == 0)    {
        cout << "Search Element Not Found...\n";    return;
    }
    loc++;
    if (loc == 1)

```

```

{
    this->insertFront(info);
    return;
}
int size = this->count();
if (loc > size + 1 || loc < 1)
{
    cout << "Invalid location...\n";
    return;
}
if (loc == size + 1)
{
    this->insertBack(info);
    return;
}
temp = tail->next;
for (int i = 1; temp->next != tail && i < loc - 1; i++)
    temp = temp->next;
Node<T> *node = new Node<T>();
node->info = info;
node->next = temp->next;
temp->next->prev = node;
node->prev = temp;
temp->next = node; cout << "Inserted node " << info << " at location "
<< loc << "...";
this->display();
return;
}

// Inserts a node at the end - O(1)
void insertBack(T info)
{
    Node<T> *temp = new Node<T>();
    temp->info = info;
    if (this->isEmpty())
    {
        temp->next = temp;
        temp->prev = temp;
    }
    else
    {
        temp->next = tail->next;
        temp->prev = tail;
        tail->next = temp;
        temp->next->prev = temp;
    }
    tail = temp;
    cout << "Inserted " << info << " at back...";
}

```

```

        this->display();
        return;
    }

    // Removes a node from the beginning - O(1)    void deleteFront()
    {
        if (this->isEmpty())
        {
            cout << "\nList is empty...\n";        return;        }        if (tail->next
== tail)
        {
            delete tail;        tail = NULL;
        }        else
        {
            Node<T> *temp = tail->next;        tail->next = temp->next;        temp-
>next->prev = tail;        delete temp;
        } cout << "\nDeleted node at front..."; this->display();
        return;
    }

    // Removes a node at a specified location - O(n)    void deleteAtLoc(T ele)
    {
        int loc = 0;
        if (this->isEmpty())
        {
            cout << "List Empty...\n";        return;
        }        int i = 0;
        Node<T> *temp = tail->next;        do        {            ++i;            if (temp-
>info == ele)                loc = i;            temp = temp->next;
        } while (temp != tail->next);

        if (loc == 0)        {            cout << "Search Element Not
Found...\n";            return;
        }        int size = this->count();        if (loc > size || loc < 1)
        {            cout << "Invalid location...\n";            return;        }
        if (loc == size)
        {
            this->deleteBack();            return;        }        temp = tail->next;        for
(int i = 1; temp->next != tail && i < loc; i++)            temp = temp->next; temp-
>prev->next = temp->next;
        temp->next->prev = temp->prev; delete temp; cout << "Deleted node
"
        << "at location " << loc << "...";        this->display();        return;
    }

    // Removes a node at the end - O(1)    void deleteBack()    {
        if (this->isEmpty())
        {
            cout << "\nList is empty...\n";            return;        }
        if (tail->next == tail)
        {
            delete tail;            tail = NULL;        }        else
        {

```

```

        Node<T> *temp = tail;        tail = temp->prev;        temp->next->prev
= tail;        tail->next = temp->next;        delete temp;        }        cout <<
"\nDeleted node at back...";        this->display();        return;
    }

    // Reverses the linked list - O(n)    void reverse()    {
        if (this->isEmpty())
        {
            cout << "\nList is empty...\n";            return;
        }
        Node<T> *temp = tail->next,
                *headRef = tail->next,                *temp1 =
NULL;        do        {            temp1 = temp->prev;            temp->prev = temp-
>next;            temp->next = temp1;            temp = temp->prev;        } while (temp !=
headRef);        tail = headRef;        cout << "\nList reversed...";        this-
>display();        return;
    }

    // Concatenates two lists - O(n)    void concat(CircularDoublyLinkedList<T>
&list)
    {
        if (!list.isEmpty() && !this->isEmpty())
        {
            tail->next->prev = list.tail;            Node<T> *temp = tail-
>next;            tail->next = list.tail->next;            list.tail->next =
temp;            tail = list.tail;            cout << "Concatenated two
lists...\n";            this->display();
        }        else        cout << "\nOne of the lists is
empty...\n";        return;
    }

    // Overloads the + operator - O(n)    void
operator+(CircularDoublyLinkedList<T> &list)
    {
        this->concat(list);        return;
    }

    // Searches for an element - O(n)
    Node<T> *search(T ele)
    {
        if (this->isEmpty())            return nullptr;            Node<T> *temp = tail-
>next;        do        {            if (temp->info == ele)            return
temp;            temp = temp->next;
        } while (temp != tail->next);        return nullptr;
    }

    // Calculates the number of nodes - O(n)    int count()    {
        if (this->isEmpty())
        {
            cout << "\nList is empty...\n";            return -1;        }        int
count = 0;        Node<T> *temp = tail->next;        do        {            temp = temp-
>next;            count++;
        } while (temp != tail->next);        return count;
    }

```

```

    }

    // Traverses the list and prints all nodes - O(n)    void display()    {
        if (this->isEmpty())
        {
            cout << "\nList is empty...\n";            return;
        }
        Node<T> *temp = tail->next;            cout << "\nList: ";            while (temp !=
tail)
        {
            cout << temp->info << " -> ";            temp = temp->next;
        }            cout << temp->info << endl;            return;
    }
}; int main(void) {
    int info, ele, choice, loc, count;    CircularDoublyLinkedList<int> list,
list2;    do    {        cout << "\tCircular Doubly Linked List\n"            <<
"===== \n"                <<
"    (1) Search        (2) InsertFront\n"
            << "    (3) InsertBack    (4) InsertAtLoc\n"
            << "    (5) DeleteFront    (6) DeleteBack\n"
            << "    (7) DeleteAtLoc    (8) Display\n"
            << "    (9) Count        (10) Reverse\n"                << "    (11)
Concat        (0) Exit\n\n";        cout << "Enter Choice: ";        cin >>
choice;        switch (choice)
        {            case 1:
                cout << "\nEnter Search Element: ";                cin >> ele;                if
(list.search(ele) != nullptr)                cout << "Element " << ele << "
found...\n";                else                cout << "Element not found or List is
Empty...\n";                break;            case 2:
                cout << "\nEnter Element: ";                cin >>
info;                list.insertFront(info);                break;            case 3:
                cout << "\nEnter Element: ";                cin >>
info;                list.insertBack(info);                break;            case 4:
                cout << "\nEnter After: ";                cin >> ele;                cout << "Enter
Element: ";                cin >> info;                list.insertAtLoc(ele,
info);                break;            case
5:                list.deleteFront();                break;            case
6:                list.deleteBack();                break;            case 7:
                cout << "\nEnter Element: ";                cin >>
ele;                list.deleteAtLoc(ele);                break;            case 8:
                list.display();
                break;            case 9:
                count = list.count();                if (count != -1)                cout << "\nNumber
of Nodes: " << count << endl;                break;            case
10:                list.reverse();                break;            case 11:                if
(!list2.isEmpty())
                {                    cout << "\nList B: ";                    list2.display();

```

```

    }        cout << "\nNumber of Nodes to add in List B: ";        cin >>
count;        if (count)        {        cout << "Enter Elements to List B:
";        for (int i = 0; i < count; i++)
        {        cin >> info;        list2.insertBack(info);
        }        list + list2;        }        break;        case
0:        default:        break;        }        getch();        clrscr();        } while
(choice != 0);        return 0;
} void getch() {
    cout << "\nPress any key to
continue...";    cin.ignore();    cin.get();    return;
} void clrscr()
{
#ifdef _WIN32    system("cls"); #elif __unix__    system("clear");
#endif    return; }

```

Output

Circular Doubly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Enter Choice: 4

Insert After: 10

Enter Element: 20

Inserted node 20 at location 2...

List: 10 -> 20 -> 30

Press any key to continue...

Circular Doubly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Enter Choice: 2

Enter Element: 10

Inserted 10 at front...

List: 10

Press any key to continue...

Circular Doubly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Enter Choice: 7

Enter Element: 20

Deleted node at location 2...

List: 10 -> 30

Press any key to continue...

Circular Doubly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Enter Choice: 3

Enter Element: 30

Inserted 30 at back...

List: 10 -> 30

Press any key to continue...

Circular Doubly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Enter Choice: 6

Deleted node at back...

List: 10

Press any key to continue...

Circular Doubly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Enter Choice: 5

Deleted node at front...

List is empty...

Press any key to continue...

Circular Doubly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Enter Choice: 2

Enter Element: 10

Inserted 10 at front...

List: 10

Press any key to continue...

Circular Doubly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Circular Doubly Linked List

```
=====
(1) Search      (2) InsertFront
(3) InsertBack  (4) InsertAtLoc
(5) DeleteFront (6) DeleteBack
(7) DeleteAtLoc (8) Display
(9) Count       (10) Reverse
(11) Concat     (0) Exit
```

Enter Choice: 1

Enter Search Element: 10

Element 10 found...

Press any key to continue...

Enter Choice: 11

Number of Nodes to add in List B: 3

Enter Elements to List B: 1 2 3

Inserted 1 at back...

List: 1

Inserted 2 at back...

List: 1 -> 2

Inserted 3 at back...

List: 1 -> 2 -> 3

Concatenated two lists...

List: 10 -> 1 -> 2 -> 3

Press any key to continue...

6. Implement a stack using Array representation

```
#include <iostream>
using namespace std;

#define n 100

class Stack{
    int *arr;
    int top;

public:
    Stack(){
        arr = new int[n];
        top = -1;
    }

    void Push(int data){
        if(top==n-1)
            cout<<"Stack Overflow"<<endl;

        top++;
        arr[top]=data;
    }
    void Pop(){
        if(top== -1)
            cout<<"Stack Underflow"<<endl;
        top--;
    }
    void Top(){
        cout<<arr[top]<<endl;
    }
    bool isEmpty(){
        return top== -1;
    }
    int isFull(){
        return top==n-1;
    }
};

int main(){

    Stack s;
    s.Push(1);
    s.Push(2);
    s.Push(3);
    s.Push(4);
    s.Push(5);
```

```

    s.Top();

    s.Pop();

    s.Top();

    cout<<s.isFull()<<endl;

    s.Pop();
    s.Pop();
    s.Pop();
    s.Pop();

    cout<<s.isEmpty()<<endl;
}

```

Output:

```

5
4
0
1

```

7. Implement a stack using Linked representation

```

#include <iostream>
using namespace std;

class Node{
public:
    int val;
    Node * next;

    Node(){
        val = 0 ;
        next = NULL;
    }

    Node(int data){
        val = data;
        next = NULL;
    }
};

class LL{
public:
    Node * head;

```

```

LL(){
    head = NULL;
}

void Push(int);

void Display();

void Pop();
};

void LL::Push(int data){
    Node *temp = new Node(data);
    if(head == NULL){
        head = temp;
        return;
    }
    Node *cur = head;
    while(cur->next!=NULL){
        cur = cur->next;
    }
    cur->next = temp;
}

void LL::Pop(){
    if(head == NULL){
        cout<<"Stack Underflow\n";
        return;
    }
    Node * cur = head;
    Node *temp = cur->next;
    while(temp->next!=NULL){
        temp = temp->next;
    }
    cur->next = NULL;
    free(temp);
}

void LL::Display()
{
    Node* temp = head;
    if (head == NULL) {
        cout << "List empty" << endl;
        return;
    }
}

```

```

        while (temp != NULL) {
            cout << temp->val << " -> ";
            temp = temp->next;
        }cout<<"NULL\n";
    }

int main(){
    LL l;
    l.Push(11);
    l.Push(22);
    l.Push(33);
    l.Push(44);
    l.Push(55);

    l.Display();

    l.Pop();

    l.Display();
}

```

Output:

```

11 -> 22 -> 33 -> 44 -> 55 -> NULL
11 -> NULL

```

8. Implement Queue using Circular Array representation

```

#include <iostream>
using namespace std;
#define SIZE 5
int A[SIZE];
int front = -1;
int rear = -1;

// Function to check if queue is empty or not
bool isempty()
{
    if (front == -1 && rear == -1)
        return true;
    else
        return false;
}

// function to enter elements in queue
void enqueue(int value)
{
    // queue is full

```

```

    if ((rear + 1) % SIZE == front)
        cout << "Queue is full \n";
    else
    {
        // first element inserted
        if (front == -1)
            front = 0;
        // insert element at rear
        rear = (rear + 1) % SIZE;
        A[rear] = value;
    }
}

// function to delete/remove element from queue
void dequeue()
{
    if (isempty())
        cout << "Queue is empty\n";
    else
    {
        // only one element
        if (front == rear)
            front = rear = -1;
        else
            front = (front + 1) % SIZE;
    }
}

// function to show the element at front
void showfront()
{
    if (isempty())
        cout << "Queue is empty\n";
    else
        cout << "element at front is:" << A[front];
}

// function to display queue
void displayQueue()
{
    if (isempty())
        cout << "Queue is empty\n";
    else
    {
        int i;
        if (front <= rear)
        {
            for (i = front; i <= rear; i++)
                cout << A[i] << " ";
        }
    }
}

```

```

        else
        {
            i = front;
            while (i < SIZE)
            {
                cout << A[i] << " ";
                i++;
            }
            i = 0;
            while (i <= rear)
            {
                cout << A[i] << " ";
                i++;
            }
        }
    }
}

// Main Function
int main()
{
    int choice, flag = 1, value;
    while (flag == 1)
    {
        cout << "\n1.enqueue 2.dequeue 3.showfront 4.displayQueue 5.exit\n";
        cin >> choice;
        switch (choice)
        {
            case 1:
                cout << "Enter Value:\n";
                cin >> value;
                enqueue(value);
                break;
            case 2:
                dequeue();
                break;
            case 3:
                showfront();
                break;
            case 4:
                displayQueue();
                break;
            case 5:
                flag = 0;
                break;
        }
    }
}

```



```
    return 0;  
}
```

Output :

```
1.enqueue 2.dequeue 3.showfront 4.displayQueue 5.exit  
1  
Enter Value:  
1  
  
1.enqueue 2.dequeue 3.showfront 4.displayQueue 5.exit  
1  
Enter Value:  
4  
  
1.enqueue 2.dequeue 3.showfront 4.displayQueue 5.exit  
1  
Enter Value:  
6  
  
1.enqueue 2.dequeue 3.showfront 4.displayQueue 5.exit  
2  
  
1.enqueue 2.dequeue 3.showfront 4.displayQueue 5.exit  
3  
element at front is:4  
1.enqueue 2.dequeue 3.showfront 4.displayQueue 5.exit  
4  
4 6  
1.enqueue 2.dequeue 3.showfront 4.displayQueue 5.exit  
5
```

9. Implement Queue using Circular linked list representation

```
// circularSinglyLinkedList.hpp  
#include <iostream>  
  
using namespace std;  
template <class T>  
class Node  
{  
public:  
    T info;  
    Node *ptr;  
};  
template <class T>  
class CircularSinglyLinkedList  
{  
public:  
    Node<T> *tail;
```

```

// Constructor
CircularSinglyLinkedList()
{
    tail = NULL;
}

// Destructor
~CircularSinglyLinkedList()
{
    if (this->isEmpty())
        return;
    Node<T> *ptr, *temp = tail->ptr;
    while (temp != tail)
    {
        ptr = temp;
        temp = ptr->ptr;
        delete ptr;
    }
    delete temp;
    tail = NULL;
    return;
}

// Checks if the list is empty - O(1)    bool isEmpty() {    return tail
== NULL;
}

// Inserts a node at the beginning - O(1)    void insertFront(T info)
{
    Node<T> *temp = new Node<T>();
    temp->info = info;
    if (this->isEmpty())
    {
        temp->ptr = temp;
        tail = temp;
    }
    else
    {
        temp->ptr = tail->ptr;
        tail->ptr = temp;
    }
    return;
}

// Inserts a node at a specified location - O(n)    void insertAtLoc(int loc, T
info)
{
    if (loc == 1)

```

```

{
    this->insertFront(info);
    return;
}
int size = this->count();
if (loc > size + 1 || loc < 1)
{
    cout << "Invalid location...\n";
    return;
}
if (loc == size + 1)
{
    this->insertBack(info);
    return;
}
Node<T> *temp = tail->ptr;
for (int i = 1; temp->ptr != tail && i < loc - 1; i++)
    temp = temp->ptr;
Node<T> *node = new Node<T>();
node->info = info;
node->ptr = temp->ptr;
temp->ptr = node;
return;
}

// Inserts a node at the end - O(1)    void insertBack(T info)
{
    Node<T> *temp = new Node<T>();
    temp->info = info;
    if (this->isEmpty())
        temp->ptr = temp;
    else
    {
        temp->ptr = tail->ptr;
        tail->ptr = temp;
    }
    tail = temp;
    return;
}

// Removes a node from the beginning - O(1)    void deleteFront()
{
    if (this->isEmpty())
    {
        cout << "\nList is empty...\n";
        return;
    }
    else if (tail->ptr == tail)

```

```

{
    delete tail;
    tail = NULL;
}
else
{
    Node<T> *temp;
    temp = tail->ptr->ptr;
    delete tail->ptr;
    tail->ptr = temp;
}
return;
}
}

// Removes a node at a specified location - O(n)    void deleteAtLoc(int loc)
{
    if (this->isEmpty())
    {
        cout << "\nList is empty...\n";
        return;
    }
    int size = this->count();
    if (loc > size || loc < 1)
    {
        cout << "Invalid location...\n";
        return;
    }
    if (loc == size)
    {
        this->deleteBack();
        return;
    }
    Node<T> *node, *temp = tail->ptr;
    for (int i = 1; temp->ptr != tail && i < loc - 1; i++)
        temp = temp->ptr;
    node = temp->ptr->ptr;
    delete temp->ptr;
    temp->ptr = node;
    return;
}

// Removes a node at the end - O(n)    void deleteBack()
{
    if (this->isEmpty())
    {
        cout << "\nList is empty...\n";
        return;
    }
}

```

```

        else if (tail->ptr == tail)
        {
            delete tail;
            tail = NULL;
        }
        else
        {
            Node<T> *temp = tail->ptr;
            while (temp->ptr != tail)
                temp = temp->ptr;
            temp->ptr = tail->ptr;
            delete tail;
            tail = temp;
        }
        return;
    }

// Traverses the list and prints all nodes - O(n)    void display()    {
if (this->isEmpty())
{
    cout << "\nList is empty...\n";
    return;
}
Node<T> *temp = tail->ptr;
while (temp != tail)
{
    cout << temp->info << " -> ";
    temp = temp->ptr;
}
cout << temp->info << endl;
return;
}
}
;

// main.cpp
#include "circularSinglyLinkedList.hpp"

using namespace std;
void getch();
void clrscr();
template <class T>
class Queue
{
protected:
    Node<T> *front, *rear;
    CircularSinglyLinkedList<T> list;

```

```

public:
    Queue()
    {
        this->front = this->list.tail;
        this->rear = this->list.tail;
    }
    bool enqueue(T ele)
    {
        this->list.insertBack(ele);
        this->front = this->list.tail->ptr;
        this->rear = this->list.tail;
        return true;
    }

    T dequeue()
    {
        if (this->isEmpty())
        {
            cout << "ERROR: Queue Empty\n";
            return (T)(NULL);
        }
        T temp = this->front->info;
        this->list.deleteFront();
        if (this->isEmpty())
            this->front = this->list.tail;
        else
            this->front = this->list.tail->ptr;
        this->rear = this->list.tail;
        return temp;
    }

    T frontEl()
    {
        if (this->isEmpty())
        {
            cout << "Queue Empty";
            return (T)(NULL);
        }
        return this->front->info;
    }
    bool isEmpty()
    {
        return this->list.isEmpty();
    }
    void clear()
    {
        while (!this->isEmpty())
            this->dequeue();
    }

```

```

    }
    void display()
    {
        if (this->isEmpty())
        {
            cout << "Queue Empty";
            return;
        }
        this->list.display();
        return;
    }
};

int main(void)
{
    int el, res, choice;
    Queue<int> q;
    do
    {
        cout << "\tCircular Queue - CSLList\n"
              << "===== \n"
              << "  (1) Enqueue  (2) Dequeue\n"
              << "  (3) Front    (4) Clear\n"
              << "  (5) Display  (0) Exit\n\n";
        cout << "Enter Choice: ";
        cin >> choice;
        switch (choice)
        {
            case 1:
                cout << "\nEnter Element: ";
                cin >> el;
                res = q.enqueue(el);
                if (res)
                {
                    cout << "\nEnqueued " << el << "... \n";
                    cout << "Queue: ";
                    q.display();
                }
                break;
            case 2:
                res = q.dequeue();
                if (res)
                {
                    cout << "\nDequeued " << res << "... \n";
                    cout << "Queue: ";
                    q.display();
                }
                break;
            case 3:

```

```

        cout << "\nFront Element: " << q.frontEl() << endl;
        break;
    case 4:
        q.clear();
        break;
    case 5:
        cout << "\nQueue: ";
        q.display();
    default:
        break;
    }
    getch();
    clrscr();
} while (choice != 0);
return 0;
}

void getch()
{
    cout << "\nPress any key to continue...";
    cin.ignore();
    cin.get();
    return;
}

void clrscr()
{
#ifdef _WIN32 system("cls");
#elif __unix__ system("clear");
#endif return;
}

```

Output:


```

Circular Queue - CSLList
=====
(1) Enqueue (2) Dequeue
(3) Front (4) Clear
(5) Display (0) Exit

Enter Choice: 1

Enter Element: 2

Enqueued 2 ...
Queue: 1 → 2

Press any key to continue ...

Circular Queue - CSLList
=====
(1) Enqueue (2) Dequeue
(3) Front (4) Clear
(5) Display (0) Exit

Enter Choice: 1

Enter Element: 2

Enqueued 3 ...
Queue: 1 → 2 → 3

Press any key to continue ...

Circular Queue - CSLList
=====
(1) Enqueue (2) Dequeue
(3) Front (4) Clear
(5) Display (0) Exit

Enter Choice: 1

Enter Element: 1

Enqueued 1 ...
Queue: 1

Press any key to continue ...

Circular Queue - CSLList
=====
(1) Enqueue (2) Dequeue
(3) Front (4) Clear
(5) Display (0) Exit

Enter Choice: 2

Dequeued 1 ...
Queue: 2 → 3

Press any key to continue ...

```

```
        Circular Queue - CSLList
=====
(1) Enqueue  (2) Dequeue
(3) Front    (4) Clear
(5) Display  (0) Exit
```

Enter Choice: 3

Front Element: 2

Press any key to continue ...

```
        Circular Queue - CSLList
=====
(1) Enqueue  (2) Dequeue
(3) Front    (4) Clear
(5) Display  (0) Exit
```

Enter Choice: 2

Dequeued 2 ...

Queue: 3

Press any key to continue ...

```
        Circular Queue - CSLList
=====
(1) Enqueue  (2) Dequeue
(3) Front    (4) Clear
(5) Display  (0) Exit
```

Enter Choice: 2

Enqueued 90 ...

Queue: 90

Press any key to continue ...

```
        Circular Queue - CSLList
=====
(1) Enqueue  (2) Dequeue
(3) Front    (4) Clear
(5) Display  (0) Exit
```

Enter Choice: 2

Dequeued 90 ...

Queue: Queue Empty

Press any key to continue ...

10. Implement Double-ended Queues using Linked list representation

```
// doublyLinkedList.hpp
#include <iostream>

using namespace std;
void getch();
void clrscr();
template <class T>
class Node
{
public:
    T info;
    Node *prev;
    Node *next;
};
template <class T>
class DoublyLinkedList
{
public:
    Node<T> *head, *tail;

    // Constructor
    DoublyLinkedList()
    {
        head = tail = NULL;
    }

    // Destructor
    ~DoublyLinkedList()
    {
        if (this->isEmpty())
            return;
        Node<T> *ptr;
        for (; !isEmpty();)
        {
            ptr = head->next;
            delete head;
            head = ptr;
        }
        head = tail = ptr;
        return;
    }
}
```

```

    // Checks if the list is empty - O(1)    bool isEmpty()    {    return
(head == NULL || tail == NULL);
}

// Inserts a node at the beginning - O(1)    void insertFront(T info)
{
    Node<T> *temp = new Node<T>();
    temp->info = info;
    temp->next = head;
    temp->prev = NULL;
    if (this->isEmpty())
        tail = temp;
    else
        head->prev = temp;
    head = temp;
    return;
}

// Inserts a node at the end - O(1)    void insertBack(T info)
{
    Node<T> *temp = new Node<T>();
    temp->info = info;
    temp->next = NULL;
    temp->prev = tail;
    if (this->isEmpty())
        head = tail = temp;
    else
        tail->next = temp;
    tail = temp;
    return;
}

// Removes a node from the beginning - O(1)    void deleteFront()    {
if (this->isEmpty())
{
    cout << "\nList is empty...\n";
    return;
}
Node<T> *temp = head;
head = temp->next;
if (this->isEmpty())
    tail = NULL;
else
    head->prev = NULL;
delete temp;
return;
}

```

```

// Removes a node at the end - O(1)    void deleteBack()
{
    if (this->isEmpty())
    {
        cout << "\nList is empty...\n";
        return;
    }
    Node<T> *temp = tail;
    tail = temp->prev;
    if (this->isEmpty())
        head = NULL;
    else
        tail->next = NULL;
    delete temp;
    return;
}

// Traverses the list and prints all nodes - O(n)    void display()    {
if (this->isEmpty())
{
    cout << "\nList is empty...\n";
    return;
}
Node<T> *temp = head;
while (temp->next != NULL)
{
    cout << temp->info << " -> ";
    temp = temp->next;
}
cout << temp->info << endl;
return;
}
}
;

// main.cpp
#include "doublyLinkedList.hpp"
using namespace std;
void getch();
void clrscr();
template <class T>
class DoublyEndedQueue
{
protected:
    Node<T> *front, *rear;
    DoublyLinkedList<T> list;

public:

```

```

DoublyEndedQueue()
{
    this->front = this->list.head;
    this->rear = this->list.tail;
}
void enqueueFront(T ele)
{
    this->list.insertFront(ele);
    this->front = this->list.head;
    this->rear = this->list.tail;
}
void enqueueRear(T ele)
{
    this->list.insertBack(ele);
    this->front = this->list.head;
    this->rear = this->list.tail;
}

T dequeueFront()
{
    if (this->isEmpty())
    {
        cout << "ERROR: Queue Empty\n";
        return (T)(NULL);
    }
    T temp = this->front->info;
    this->list.deleteFront();
    this->front = this->list.head;
    this->rear = this->list.tail;
    return temp;
}

T dequeueRear()
{
    if (this->isEmpty())
    {
        cout << "ERROR: Queue Empty\n";
        return (T)(NULL);
    }
    T temp = this->rear->info;
    this->list.deleteBack();
    this->front = this->list.head;
    this->rear = this->list.tail;
    return temp;
}

T frontEl()
{

```

```

        if (this->isEmpty())
        {
            cout << "Queue Empty";
            return (T)(NULL);
        }
        return this->front->info;
    }
    bool isEmpty()
    {
        return this->list.isEmpty();
    }
    void clear()
    {
        while (!this->isEmpty())
            this->dequeue();
    }
    void display()
    {
        if (this->isEmpty())
        {
            cout << "Queue Empty";
            return;
        }
        this->list.display();
        return;
    }
};

int main(void)
{
    int el, res, choice;
    DoublyEndedQueue<int> q;
    do
    {
        cout << "\tDoubly Ended Queue - Deque\n"
              << "===== \n"
              << "  (1) EnqueueBack   (2) DequeueRear\n"
              << "  (3) EnqueueFront  (4) DequeueFront\n"
              << "  (5) Front         (6) Display\n"
              << "  (0) Exit\n\n";
        cout << "Enter Choice: ";
        cin >> choice;
        switch (choice)
        {
            case 1:
                cout << "\nEnter Element: ";
                cin >> el;
                q.enqueueRear(el);
                cout << "\nEnqueued " << el << " at rear...\n";

```

```

        cout << "Queue: ";
        q.display();
        break;
    case 2:
        res = q.dequeueRear();
        if (res)
        {
            cout << "\nDequeued " << res << " from rear...\n";
            cout << "Queue: ";
            q.display();
        }
        break;
    case 3:
        cout << "\nEnter Element: ";
        cin >> el;
        q.enqueueFront(el);
        cout << "\nEnqueued " << el << " at front...\n";
        cout << "Queue: ";
        q.display();
        break;
    case 4:
        res = q.dequeueFront();
        if (res)
        {
            cout << "\nDequeued " << res << " from front...\n";
            cout << "Queue: ";
            q.display();
        }
        break;
    case 5:
        cout << "\nFront Element: " << q.frontEl() << endl;
        break;
    case 6:
        cout << "\nQueue: ";
        q.display();
    default:
        break;
    }
    getch();
    clrscr();
} while (choice != 0);
return 0;
}

void getch()
{
    cout << "\nPress any key to continue...";
    cin.ignore();
    cin.get();
}

```



```
        return;
    }
    void clrscr()
    {
#ifdef _WIN32 system("cls");
#elif __unix__ system("clear");
#endif return;
    }
```

Output:

```

Doubly Ended Queue - Deque
=====
(1) EnqueueBack  (2) DequeueRear
(3) EnqueueFront (4) DequeueFront
(5) Front        (6) Display
(0) Exit

```

Enter Choice: 1

Enter Element: 10

Enqueued 10 at rear...

Queue: 10

Press any key to continue...█

```

Doubly Ended Queue - Deque
=====
(1) EnqueueBack  (2) DequeueRear
(3) EnqueueFront (4) DequeueFront
(5) Front        (6) Display
(0) Exit

```

Enter Choice: 3

Enter Element: 20

Enqueued 20 at front...

Queue: 20 -> 10

Press any key to continue...█

```

Doubly Ended Queue - Deque
=====
(1) EnqueueBack  (2) DequeueRear
(3) EnqueueFront (4) DequeueFront
(5) Front        (6) Display
(0) Exit

```

Enter Choice: 2

Dequeued 10 from rear...

Queue: 20

Press any key to continue...█

```

Doubly Ended Queue - Deque
=====
(1) EnqueueBack  (2) DequeueRear
(3) EnqueueFront (4) DequeueFront
(5) Front        (6) Display
(0) Exit

```

Enter Choice: 4

Dequeued 20 from front...

Queue: Queue Empty

Press any key to continue...█

11. Write a program to implement Binary Search Tree which supports the following operations:

- (i) Insert an element x
- (ii) Delete an element x

- (iii) Search for an element x in the BST and change its value to y and then place the node with value y at its appropriate position in the BST
- (iv) Display the elements of the BST in preorder, inorder, and postorder traversal
- (v) Display the elements of the BST in level-by-level traversal
- (vi) Display the height of the BST

```
#include <iostream>
#define MAX_SIZE 100
using namespace std;
template <class T>
class Stack
{
protected:
    int tos, size;
    T arr[MAX_SIZE];

public:
    Stack(int size = 30)
    {
        this->tos = -1;
        this->size = size;
    }
    bool push(T ele)
    {
        if (this->tos >= (this->size - 1))
        {
            cerr << "ERROR: Stack Overflow\n";
            return false;
        }
        this->arr[++(this->tos)] = ele;
        return true;
    }

    T pop()
    {
        if (this->isEmpty())
        {
            cout << "ERROR: Stack Underflow\n";
            return (T)(NULL);
        }
        return this->arr[(this->tos)--];
    }

    T top()
    {
```

```

        if (this->isEmpty())
        {
            cout << "Stack Empty";
            return (T)(NULL);
        }
        return this->arr[this->tos];
    }
    bool isEmpty()
    {
        return this->tos == -1;
    }
    void clear()
    {
        while (!this->isEmpty())
            this->pop();
    }
};

// queue.hpp
#include <iostream>
#define MAX_SIZE 100

using namespace std;
template <class T>
class Queue
{
protected:
    T arr[MAX_SIZE];
    int front, rear, size;

public:
    Queue(int size = 100)
    {
        this->front = -1;
        this->rear = -1;
        this->size = size;
    }
    bool enqueue(T ele)
    {
        if (this->rear >= (this->size - 1))
        {
            cerr << "ERROR: Queue Filled\n";
            return false;
        }
        else if (this->isEmpty())
        {
            this->rear++;
            this->front++;
        }
    }
};

```

```

        this->arr[this->front] = ele;
    }
    else
        this->arr[++(this->rear)] = ele;
    return true;
}

T dequeue()
{
    if (this->front >= this->size)
    {
        cout << "ERROR: Queue Finished\n";
        return (T)(NULL);
    }
    else if (this->isEmpty())
    {
        cout << "ERROR: Queue Empty\n";
        return (T)(NULL);
    }
    else if (this->front == this->rear)
    {
        T temp = this->arr[this->front];
        this->clear();
        return temp;
    }
    return this->arr[(this->front)++];
}

T frontEl()
{
    if (this->isEmpty())
    {
        cout << "Queue Empty";
        return (T)(NULL);
    }
    return this->arr[this->front];
}

bool isEmpty()
{
    return this->front == -1;
}

void clear()
{
    this->front = this->rear = -1;
}

void display()
{
    if (this->isEmpty())

```

```

        {
            cout << "Queue Empty";
            return;
        }
        int i;
        for (i = this->front; i < this->rear; i++)
            cout << this->arr[i] << " <- ";
        cout << this->arr[i] << endl;
        return;
    }
};

```

```

// main.cpp
#include "stack.hpp"
#include "queue.hpp"
void getch();
void clrscr();
template <class T>
class Node
{
public:
    T data;
    Node *left, *right;
    Node()
    {
        left = nullptr;
        right = nullptr;
    }
};

class BinarySearchTree
{
public:
    Node<int> *root;
    Stack<Node<int> *> stack;
    Queue<Node<int> *> queue;
    int countLeaf, countNonLeaf;

    BinarySearchTree()
    {
        root = nullptr;
    }
    void insert(int data, Node<int> *current)
    {
        Node<int> *temp;
        if (root == nullptr)
        {
            root = new Node<int>;

```

```

        root->data = data;
        root->left = root->right = nullptr;
    }
    else
    {
        if ((data < current->data) &&
            (current->left == nullptr))
        {
            temp = new Node<int>;
            temp->data = data;
            temp->left = temp->right = nullptr;
            current->left = temp;
        }
        else if ((data >= current->data) &&
                 (current->right == nullptr))
        {
            temp = new Node<int>;
            temp->data = data;
            temp->left = temp->right = nullptr;
            current->right = temp;
        }
        else
        {
            if (data < current->data)
                insert(data, current->left);
            else
                insert(data, current->right);
        }
    }
}

bool search(Node<int> *node, int key)
{
    if (node == nullptr)
        return false;
    if (node->data == key)
        return true;
    bool left = search(node->left, key);
    if (left)
        return true;
    bool right = search(node->right, key);
    return right;
}

void inOrderRecursive(Node<int> *root)
{
    if (root != nullptr)
    {
        inOrderRecursive(root->left);
        cout << root->data << " ";
    }
}

```

```

        inOrderRecursive(root->right);
    }
}

void preOrderRecursive(Node<int> *root)
{
    if (root != nullptr)
    {
        cout << root->data << " ";
        preOrderRecursive(root->left);
        preOrderRecursive(root->right);
    }
}

void postOrderRecursive(Node<int> *root)
{
    if (root != nullptr)
    {
        postOrderRecursive(root->left);
        postOrderRecursive(root->right);
        cout << root->data << " ";
    }
}

void inOrderIterative()
{
    Node<int> *current = root;
    while (current != nullptr || stack.isEmpty() == false)
    {
        while (current != nullptr)
        {
            stack.push(current);
            current = current->left;
        }
        current = stack.pop();
        cout << current->data << " ";
        current = current->right;
    }
}

void preOrderIterative()
{
    Node<int> *node, *temp = root;
    if (temp == nullptr)
        return;
    stack.push(temp);
    while (!stack.isEmpty())
    {
        node = stack.pop();
        cout << node->data << " ";
        if (node->right)
            stack.push(node->right);
    }
}

```



```

        if (node->left)
            stack.push(node->left);
    }
}

void postOrderIterative()
{
    Node<int> *temp = root;
    if (temp == nullptr)
        return;
    do
    {
        while (temp)
        {
            if (temp->right)
                stack.push(temp->right);
            stack.push(temp);
            temp = temp->left;
        }
        temp = stack.pop();
        if (temp->right && !stack.isEmpty() && stack.top() == temp->right)
        {
            stack.pop();
            stack.push(temp);
            temp = temp->right;
        }
        else
        {
            cout << temp->data << " ";
            temp = nullptr;
        }
    } while (!stack.isEmpty());
}

void levelByLevelTraversal()
{
    Node<int> *current = root;
    if (current == nullptr)
        return;
    queue.enqueue(current);
    while (!queue.isEmpty())
    {
        current = queue.dequeue();
        cout << current->data << " ";
        if (current->left)
            queue.enqueue(current->left);
        if (current->right)
            queue.enqueue(current->right);
    }
    cout << endl;
}

```

```

}
void mirror(Node<int> *current)
{
    if (current == nullptr)
        return;
    else
    {
        mirror(current->left);
        mirror(current->right);

        Node<int> *temp = current->left;

        current->left = current->right;
        current->right = temp;
    }
}
int height(Node<int> *current)
{
    if (current == nullptr)
        return 0;
    else
    {
        int leftHeight = height(current->left);
        int rightHeight = height(current->right);
        if (leftHeight > rightHeight)
            return (leftHeight + 1);
        else
            return (rightHeight + 1);
    }
}
void countNodes(Node<int> *current)
{
    if (current == nullptr)
        return;
    if (current->left != nullptr || current->right != nullptr)
        countNonLeaf++;
    if (current->left == nullptr && current->right == nullptr)
        countLeaf++;
    countNodes(current->left);
    countNodes(current->right);
}
void deleteByMerging(Node<int> *temp, int key)
{
    Node<int> *prev = nullptr;

    while (temp != nullptr)
    {
        if (temp->data == key)

```

```

        break;
    prev = temp;
    if (temp->data < key)
        temp = temp->right;
    else
        temp = temp->left;
}
if (temp != nullptr && temp->data == key)
{
    if (temp == root)
        mergeHelper(root);
    else if (prev->left == temp)
        mergeHelper(prev->left);
    else
        mergeHelper(prev->right);
}
else if (root != nullptr)
    cout << "\nNode Not Found...";
return;
}

void mergeHelper(Node<int> *&node)
{
    Node<int> *temp = node;
    if (node == nullptr)
        return;

    // no right child - single child    if (node->right ==
    nullptr)        node = node->left;

    // no left child - single child    else if (node->left ==
    nullptr)        node = node->right;

    // node has both children    else
    {
        // find in-order predecessor    temp = node->left;    while
        (temp->right != nullptr)    temp = temp->right;    // merge subtree to
        predecessor    temp->right = node->right;    temp = node;    node =
        node->left;
    }

    // delete the node    delete temp;    return;
}

void deleteByCopying(Node<int> *temp, int key)
{
    Node<int> *prev = nullptr;
    while (temp != nullptr && temp->data != key)
    {
        prev = temp;
    }

```

```

        if (temp->data < key)
            temp = temp->right;
        else
            temp = temp->left;
    }
    if (temp != nullptr && temp->data == key)
    {
        if (temp == root)
            copyHelper(root);
        else if (prev->left == temp)
            copyHelper(prev->left);
        else
            copyHelper(prev->right);
    }
    else if (root != nullptr)
        cout << "\nNode Not Found...";
    return;
}
void copyHelper(Node<int> *&node)
{
    Node<int> *prev, *temp = node;

    // no right child - single child    if (node->right ==
    nullptr)        node = node->left;

    // no left child - single child    else if (node->left ==
    nullptr)        node = node->right;

    // node has both children    else    {        prev = node;
    // find the in-order predecessor    temp = node->left;        while
    (temp->right != nullptr)
    {
        prev = temp;
        temp = temp->right;
    }
    // copy the predecessor key    node->data = temp->data;    //
    handle dangling subtrees    if (prev == node)        prev->left = temp-
    >left;    else
        prev->right = temp->left;
    }

    // delete the node    delete temp;    return;
}
void searchAndReplace(int key, int newKey)
{
    if (search(root, key))
    {
        deleteByMerging(root, key);
        insert(newKey, root);
    }
}

```

```

    }
    else
    {
        cout << "Node Not Found...";
    }
}
}
;
int main(void)
{
    BinarySearchTree tree;
    int choice, data, data2;
    do
    {
        cout << "          MENU          \n"
              << "===== \n"
              << "(1) Insertion \n"
              << "(2) Searching a node \n"
              << "(3) Display its preorder, postorder and inorder traversals.
(recursive) \n"
              << "(4) Display its preorder, postorder and inorder traversals.
(Iterative) \n"
              << "(5) Display level-by-level traversal. (BFS) \n"
              << "(6) Create a mirror image of tree \n"
              << "(7) Count the non-leaf, leaf and total number of nodes \n"
              << "(8) Search for an element x in the BST and change its value
to y \n"
              << "      and then place the node with value y at its appropriate
position \n"
              << "(9) Display height of tree \n"
              << "(10) Perform deletion by merging \n"
              << "(11) Perform deletion by copying \n"
              << "(0) Exit \n \n";
        cout << "Enter Choice: ";
        cin >> choice;
        switch (choice)
        {
            case 1:
                cout << "\nEnter Node Data: ";
                cin >> data;
                tree.insert(data, tree.root);
                break;
            case 2:
                cout << "\nEnter Search Data: ";
                cin >> data;
                cout << "Search Result: ";
                if (tree.search(tree.root, data))
                    cout << "Found";

```

```

        else
            cout << "Not Found";
        cout << endl;
        break;
    case 3:
        cout << endl;
        cout << "In-Order Recursive Traversal: ";
        tree.inOrderRecursive(tree.root);
        cout << endl;
        cout << "Pre-Order Recursive Traversal: ";
        tree.preOrderRecursive(tree.root);
        cout << endl;
        cout << "Post-Order Recursive Traversal: ";
        tree.postOrderRecursive(tree.root);
        cout << endl;
        break;
    case 4:
        cout << endl;
        cout << "In-Order Iterative Traversal: ";
        tree.inOrderIterative();
        cout << endl;
        cout << "Pre-Order Iterative Traversal: ";
        tree.preOrderIterative();
        cout << endl;
        cout << "Post-Order Iterative Traversal: ";
        tree.postOrderIterative();
        cout << endl;
        break;
    case 5:
        cout << endl;
        cout << "Level-by-level Traversal: \n";
        tree.levelByLevelTraversal();
        break;
    case 6:
        cout << endl;
        tree.mirror(tree.root);
        cout << "Tree converted to its Mirror Tree..."
            << endl;
        break;
    case 7:
        tree.countLeaf = tree.countNonLeaf = 0;
        tree.countNodes(tree.root);
        cout << endl;
        cout << "Leaf Nodes: " << tree.countLeaf << endl;
        cout << "Non-Leaf Nodes: " << tree.countNonLeaf << endl;
        cout << "Total Nodes: " << tree.countNonLeaf + tree.countLeaf <<
endl;
        break;

```

```

        case 8:
            cout << "\nEnter Search Data: ";
            cin >> data;
            cout << "Enter Replacement: ";
            cin >> data2;
            tree.searchAndReplace(data, data2);
            break;
        case 9:
            cout << endl;
            cout << "Height of Tree: "
                 << tree.height(tree.root)
                 << endl;
            break;
        case 10:
            cout << "\nEnter Node to Delete: ";
            cin >> data;
            tree.deleteByMerging(tree.root, data);
            break;
        case 11:
            cout << "\nEnter Node to Delete: ";
            cin >> data;
            tree.deleteByCopying(tree.root, data);
            break;
        case 0:
        default:
            break;
    }
    getch();
    clrscr();
} while (choice != 0);
return 0;
}

void getch()
{
    cout << "\nPress any key to continue...";
    cin.ignore();
    cin.get();
    return;
}

void clrscr()
{
#ifdef _WIN32 system("cls");
#elif __unix__ system("clear");
#endif return;
}

```

Output :

MENU

=====

- (1) Insertion
- (2) Searching a node
- (3) Display its preorder, postorder and inorder traversals. (recursive)
- (4) Display its preorder, postorder and inorder traversals. (iterative)
- (5) Display level-by-level traversal. (BFS)
- (6) Create a mirror image of tree
- (7) Count the non-leaf, leaf and total number of nodes
- (8) Search for an element x in the BST and change its value to y and then place the node with value y at its appropriate position
- (9) Display height of tree
- (10) Perform deletion by merging
- (11) Perform deletion by copying
- (0) Exit

Enter Choice: 1

Enter Node Data: 10

Press any key to continue...

MENU

=====

- (1) Insertion
- (2) Searching a node
- (3) Display its preorder, postorder and inorder traversals. (recursive)
- (4) Display its preorder, postorder and inorder traversals. (iterative)
- (5) Display level-by-level traversal. (BFS)
- (6) Create a mirror image of tree
- (7) Count the non-leaf, leaf and total number of nodes
- (8) Search for an element x in the BST and change its value to y and then place the node with value y at its appropriate position
- (9) Display height of tree
- (10) Perform deletion by merging
- (11) Perform deletion by copying
- (0) Exit

Enter Choice: 1

Enter Node Data: 5

Press any key to continue...

MENU

=====

- (1) Insertion
- (2) Searching a node
- (3) Display its preorder, postorder and inorder traversals. (recursive)
- (4) Display its preorder, postorder and inorder traversals. (iterative)
- (5) Display level-by-level traversal. (BFS)
- (6) Create a mirror image of tree
- (7) Count the non-leaf, leaf and total number of nodes
- (8) Search for an element x in the BST and change its value to y and then place the node with value y at its appropriate position
- (9) Display height of tree
- (10) Perform deletion by merging
- (11) Perform deletion by copying
- (0) Exit

Enter Choice: 1

Enter Node Data: 14

Press any key to continue...

MENU

=====

- (1) Insertion
- (2) Searching a node
- (3) Display its preorder, postorder and inorder traversals. (recursive)
- (4) Display its preorder, postorder and inorder traversals. (iterative)
- (5) Display level-by-level traversal. (BFS)
- (6) Create a mirror image of tree
- (7) Count the non-leaf, leaf and total number of nodes
- (8) Search for an element x in the BST and change its value to y and then place the node with value y at its appropriate position
- (9) Display height of tree
- (10) Perform deletion by merging
- (11) Perform deletion by copying
- (0) Exit

Enter Choice: 1

Enter Node Data: 0

Press any key to continue...

MENU

=====

- (1) Insertion
- (2) Searching a node
- (3) Display its preorder, postorder and inorder traversals. (recursive)
- (4) Display its preorder, postorder and inorder traversals. (iterative)
- (5) Display level-by-level traversal. (BFS)
- (6) Create a mirror image of tree
- (7) Count the non-leaf, leaf and total number of nodes
- (8) Search for an element x in the BST and change its value to y and then place the node with value y at its appropriate position
- (9) Display height of tree
- (10) Perform deletion by merging
- (11) Perform deletion by copying
- (0) Exit

Enter Choice: 1

Enter Node Data: 6

Press any key to continue...

MENU

=====

- (1) Insertion
- (2) Searching a node
- (3) Display its preorder, postorder and inorder traversals. (recursive)
- (4) Display its preorder, postorder and inorder traversals. (iterative)
- (5) Display level-by-level traversal. (BFS)
- (6) Create a mirror image of tree
- (7) Count the non-leaf, leaf and total number of nodes
- (8) Search for an element x in the BST and change its value to y and then place the node with value y at its appropriate position
- (9) Display height of tree

- (10) Perform deletion by merging
- (11) Perform deletion by copying
- (0) Exit

Enter Choice: 1

Enter Node Data: 10

Press any key to continue...

MENU

=====

- (1) Insertion
- (2) Searching a node
- (3) Display its preorder, postorder and inorder traversals. (recursive)
- (4) Display its preorder, postorder and inorder traversals. (iterative)
- (5) Display level-by-level traversal. (BFS)
- (6) Create a mirror image of tree
- (7) Count the non-leaf, leaf and total number of nodes
- (8) Search for an element x in the BST and change its value to y
and then place the node with value y at its appropriate position
- (9) Display height of tree
- (10) Perform deletion by merging
- (11) Perform deletion by copying
- (0) Exit

Enter Choice: 1

Enter Node Data: 14

Press any key to continue...

MENU

=====

- (1) Insertion
- (2) Searching a node
- (3) Display its preorder, postorder and inorder traversals. (recursive)
- (4) Display its preorder, postorder and inorder traversals. (iterative)
- (5) Display level-by-level traversal. (BFS)
- (6) Create a mirror image of tree

- (7) Count the non-leaf, leaf and total number of nodes
- (8) Search for an element x in the BST and change its value to y and then place the node with value y at its appropriate position
- (9) Display height of tree
- (10) Perform deletion by merging
- (11) Perform deletion by copying
- (0) Exit

Enter Choice: 2

Enter Search Data: 14

Search Result: Found

Press any key to continue...

MENU

=====

- (1) Insertion
- (2) Searching a node
- (3) Display its preorder, postorder and inorder traversals. (recursive)
- (4) Display its preorder, postorder and inorder traversals. (iterative)
- (5) Display level-by-level traversal. (BFS)
- (6) Create a mirror image of tree
- (7) Count the non-leaf, leaf and total number of nodes
- (8) Search for an element x in the BST and change its value to y and then place the node with value y at its appropriate position
- (9) Display height of tree
- (10) Perform deletion by merging
- (11) Perform deletion by copying
- (0) Exit

Enter Choice: 2

Enter Search Data: 2

Search Result: Not Found

Press any key to continue...

MENU

=====

- (1) Insertion
- (2) Searching a node
- (3) Display its preorder, postorder and inorder traversals. (recursive)
- (4) Display its preorder, postorder and inorder traversals. (iterative)
- (5) Display level-by-level traversal. (BFS)
- (6) Create a mirror image of tree
- (7) Count the non-leaf, leaf and total number of nodes
- (8) Search for an element x in the BST and change its value to y and then place the node with value y at its appropriate position
- (9) Display height of tree
- (10) Perform deletion by merging
- (11) Perform deletion by copying
- (0) Exit

Enter Choice: 3

In-Order Recursive Traversal: 0 5 6 10 10 14 14

Pre-Order Recursive Traversal: 10 5 0 6 14 10 14

Post-Order Recursive Traversal: 0 6 5 10 14 14 10

Press any key to continue...

MENU

=====

- (1) Insertion
- (2) Searching a node
- (3) Display its preorder, postorder and inorder traversals. (recursive)
- (4) Display its preorder, postorder and inorder traversals. (iterative)
- (5) Display level-by-level traversal. (BFS)
- (6) Create a mirror image of tree
- (7) Count the non-leaf, leaf and total number of nodes
- (8) Search for an element x in the BST and change its value to y and then place the node with value y at its appropriate position
- (9) Display height of tree
- (10) Perform deletion by merging
- (11) Perform deletion by copying
- (0) Exit

Enter Choice: 4

In-Order Iterative Traversal: 0 5 6 10 10 14 14

Pre-Order Iterative Traversal: 10 5 0 6 14 10 14

Post-Order Iterative Traversal: 0 6 5 10 14 14 10

Press any key to continue...

MENU

=====

- (1) Insertion
- (2) Searching a node
- (3) Display its preorder, postorder and inorder traversals. (recursive)
- (4) Display its preorder, postorder and inorder traversals. (iterative)
- (5) Display level-by-level traversal. (BFS)
- (6) Create a mirror image of tree
- (7) Count the non-leaf, leaf and total number of nodes
- (8) Search for an element x in the BST and change its value to y and then place the node with value y at its appropriate position
- (9) Display height of tree
- (10) Perform deletion by merging
- (11) Perform deletion by copying
- (0) Exit

Enter Choice: 5

Level-by-level Traversal:

10 5 14 0 6 10 14

Press any key to continue...

MENU

=====

- (1) Insertion
- (2) Searching a node
- (3) Display its preorder, postorder and inorder traversals. (recursive)
- (4) Display its preorder, postorder and inorder traversals. (iterative)
- (5) Display level-by-level traversal. (BFS)
- (6) Create a mirror image of tree
- (7) Count the non-leaf, leaf and total number of nodes
- (8) Search for an element x in the BST and change its value to y and then place the node with value y at its appropriate position
- (9) Display height of tree

- (10) Perform deletion by merging
- (11) Perform deletion by copying
- (0) Exit

Enter Choice: 7

Leaf Nodes: 4

Non-Leaf Nodes: 3

Total Nodes: 7

Press any key to continue...

MENU

=====

- (1) Insertion
- (2) Searching a node
- (3) Display its preorder, postorder and inorder traversals. (recursive)
- (4) Display its preorder, postorder and inorder traversals. (iterative)
- (5) Display level-by-level traversal. (BFS)
- (6) Create a mirror image of tree
- (7) Count the non-leaf, leaf and total number of nodes
- (8) Search for an element x in the BST and change its value to y and then place the node with value y at its appropriate position
- (9) Display height of tree
- (10) Perform deletion by merging
- (11) Perform deletion by copying
- (0) Exit

Enter Choice: 0

Press any key to continue...

12. Write a program, using templates, to sort a list of n elements. Give user the option to perform sorting using Insertion sort, Bubble sort or Selection sort.

```
#include <iostream>
#define MAX_SIZE 100
using namespace std;
```

```

void getch();
void clrscr();
template <class T>
void swapElements(T &a, T &b)
{
    T t = a;
    a = b;
    b = t;
}
template <class T>
T *bubbleSort(T *arr, int size)
{
    for (int i = 0; i < size - 1; i++)
        for (int j = 0; j < size - i - 1; j++)
            if (arr[j] > arr[j + 1])
                swapElements<T>(arr[j], arr[j + 1]);
    return arr;
}
template <class T>
T *insertionSort(T *arr, int size)
{
    T key;
    int i, j;
    for (i = 1; i < size; i++)
    {
        key = arr[i];
        j = i - 1;
        while (j >= 0 && arr[j] > key)
        {
            arr[j + 1] = arr[j--];
        }
        arr[j + 1] = key;
    }
    return arr;
}
template <class T>
T *selectionSort(T *arr, int size)
{
    int min;
    for (int i = 0; i < size - 1; i++)
    {
        min = i;
        for (int j = i + 1; j < size; j++)
            if (arr[j] < arr[min])
                min = j;
        swapElements<T>(arr[min], arr[i]);
    }
    return arr;
}

```



```

}
template <class T>
void display(T *arr, int size)
{
    for (int i = 0; i < size; i++)
        cout << arr[i] << " ";
}
int main(void)
{
    int ch = 1, size, arr[MAX_SIZE];
    cout << "Enter Number of Elements: ";
    cin >> size;

    cout << "Enter Array Elements: ";
    for (int i = 0; i < size; i++)
        cin >> arr[i];
    clrscr();
    do
    {
        cout << "\t\tMenu\n===== \n"
             << " (1) Bubble Sort      (2) Insertion Sort\n"
             << " (3) Selection Sort   (0) Exit\n\n";
        cout << "Enter Choice: ";
        cin >> ch;
        switch (ch)
        {
            case 1:
                cout << endl;
                cout << "Original Array: ";
                display<int>(arr, size);
                cout << endl;
                cout << "Bubble Sort: ";
                display<int>(bubbleSort<int>(arr, size), size);
                cout << endl;
                break;
            case 2:
                cout << endl;
                cout << "Original Array: ";
                display<int>(arr, size);
                cout << endl;
                cout << "Insertion Sort: ";
                display<int>(insertionSort<int>(arr, size), size);
                cout << endl;
                break;
            case 3:
                cout << endl;
                cout << "Original Array: ";
                display<int>(arr, size);

```

```

        cout << endl;
        cout << "Selection Sort: ";
        display<int>(selectionSort<int>(arr, size), size);
        cout << endl;
        break;
    default:
        break;
    }
    getch();
    clrscr();
} while (ch != 0);
return 0;
}

void getch()
{
    cout << "\nPress any key to continue...";
    cin.ignore();
    cin.get();
    return;
}

void clrscr()
{
#ifdef _WIN32 system("cls");
#elif __unix__ system("clear");
#endif return;
}

```

Output:

Enter Number of Elements: 5
Enter Array Elements: 1 9 8 2 3

```
Menu
=====
(1) Bubble Sort      (2) Insertion Sort
(3) Selection Sort   (0) Exit
```

Enter Choice: 1

Original Array: 1 9 8 2 3
Bubble Sort: 1 2 3 8 9

Press any key to continue...

Enter Number of Elements: 5
Enter Array Elements: 1 9 8 2 3

```
Menu
=====
(1) Bubble Sort      (2) Insertion Sort
(3) Selection Sort   (0) Exit
```

Enter Choice: 2

Original Array: 1 9 8 2 3
Insertion Sort: 1 2 8 2 3

Press any key to continue...

Enter Number of Elements: 5
Enter Array Elements: 1 9 8 2 3

```
Menu
=====
(1) Bubble Sort      (2) Insertion Sort
(3) Selection Sort   (0) Exit
```

Enter Choice: 3

Original Array: 1 9 8 2 3
Selection Sort: 1 2 3 8 9

Press any key to continue...

13. Write a program to implement:

(a) Diagonal Matrix using one-dimensional array

```
#include <climits>
#include <iostream>
#define MAX_SIZE 10

using namespace std;
```

```

void getch();
void clrscr();
class DiagonalMatrix
{
public:
    int *arr;
    int size;
    int nrows;
    int ncols;

    DiagonalMatrix(int rows = MAX_SIZE, int cols = MAX_SIZE)
    {
        if (rows != cols)
            cerr << "ERROR: Invalid Dimensions" << endl;
        else
        {
            size = rows;
            nrows = ncols = rows;
            arr = new int[size];
            for (int i = 0; i < size; i++)
                arr[i] = 0;
        }
    }

    ~DiagonalMatrix()
    {
        delete[] arr;
    }

    void store(int data, int row, int col)
    {
        if (row != col || row >= nrows || col >= ncols)
            cerr << "ERROR: Invalid Location" << endl;
        else
            arr[row] = data;
    }

    int retrieve(int row, int col)
    {
        if (row >= nrows || col >= ncols)
            return INT_MIN;
        if (row != col)
            return 0;
        else
            return arr[row];
    }

    void display()
    {
        for (int i = 0; i < nrows; i++)
        {

```

```

        for (int j = 0; j < ncols; j++)
            if (i == j)
                cout << arr[i] << " ";
            else
                cout << 0 << " ";
        cout << endl;
    }
}
};

int main(void)
{
    int rows, cols, data, choice = 1;
    cout << "Enter Number of Rows: ";
    cin >> rows;
    cout << "Enter Number of Columns: ";
    cin >> cols;
    clrscr();

    DiagonalMatrix matrix(rows, cols);
    do
    {
        cout << "          MENU          \n"
              << "===== \n"
              << "(1) Display\n"
              << "(2) Store\n"
              << "(3) Retrieve\n"
              << "(0) Exit\n\n";
        cout << "Enter Choice: ";
        cin >> choice;

        switch (choice)
        {
            case 1:
                cout << "\nMatrix:\n";
                matrix.display();
                break;
            case 2:
                cout << "Enter Data: ";
                cin >> data;
                cout << "Enter Position: ";
                cin >> rows >> cols;
                matrix.store(data, rows, cols);
                break;
            case 3:
                cout << "Enter Position: ";
                cin >> rows >> cols;
                data = matrix.retrieve(rows, cols);
                if (data != INT_MIN)

```

```

        cout << "Retrieved " << data << endl;
    else
        cerr << "ERROR: Invalid Location" << endl;
        break;
    case 0:
    default:
        break;
    }
    getch();
    clrscr();

} while (choice != 0);
return 0;
}

void getch()
{
    cout << "\nPress any key to continue...";
    cin.ignore();
    cin.get();
    return;
}

void clrscr()
{
#ifdef _WIN32 system("cls");
#elif __unix__ system("clear");
#endif return;
}

```

Output:

Enter Number of Rows: 3

Enter Number of Columns: 3

MENU

=====

(1) Display (2) Store

(3) Retrieve

(0) Exit

Enter Choice: 2

Enter Data: 8

Enter Position: 0 1

ERROR: Invalid Location

Press any key to continue...

MENU

=====

- (1) Display
- (2) Store
- (3) Retrieve
- (0) Exit

Enter Choice: 2

Enter Data: 5

Enter Position: 1 1

Press any key to continue...

MENU

=====

- (1) Display (2) Store (3) Retrieve
- (0) Exit

Enter Choice: 1

Matrix:

0 0 0

0 5 0

0 0 0

Press any key to continue...

MENU

=====

- (1) Display
- (2) Store (3) Retrieve
- (0) Exit

Enter Choice: 2

Enter Data: 4

Enter Position: 2 2

Press any key to continue..

MENU

=====

(1) Display (2) Store (3) Retrieve
(0) Exit

Enter Choice: 3

Enter Position: 2 2

Retrieved 4

Press any key to continue...

MENU

=====

(1) Display (2)
Store (3) Retrieve
(0) Exit

Enter Choice: 3

Enter Position: 0 2

Retrieved 0

Press any key to continue...

MENU

=====

(1) Display (2)
Store (3) Retrieve
(0) Exit

Enter Choice: 3

Enter Position: 5 5

ERROR: Invalid Location

Press any key to continue...

(b) Lower Triangular Matrix using one-dimensional array

```
#include <climits>
#include <iostream>
#define MAX_SIZE 10

using namespace std;
void getch();
void clrscr();
class LowerTriangularMatrix
{
public:
    int *arr;
    int size;
    int nrows;
    int ncols;

    LowerTriangularMatrix(int rows = MAX_SIZE, int cols = MAX_SIZE)
    {
        if (rows != cols)
            cerr << "ERROR: Invalid Dimensions" << endl;
        else
        {
            size = rows * (rows + 1) / 2;
            nrows = ncols = rows;
            arr = new int[size];
            for (int i = 0; i < size; i++)
                arr[i] = 0;
        }
    }

    ~LowerTriangularMatrix()
    {
        delete[] arr;
    }

    void store(int data, int row, int col)
    {
        if (col > row || row >= nrows || col >= ncols)
            cerr << "ERROR: Invalid Location" << endl;
        else
            arr[row * (row + 1) / 2 + col] = data;
    }

    int retrieve(int row, int col)
    {
        if (row >= nrows || col >= ncols)
            return INT_MIN;
        if (col > row)
            return 0;
    }
}
```

```

        else
            return arr[row * (row + 1) / 2 + col];
    }
    void display()
    {
        for (int i = 0; i < nrows; i++)
        {
            for (int j = 0; j < ncols; j++)
                if (i >= j)
                    cout << arr[i * (i + 1) / 2 + j] << " ";
                else
                    cout << 0 << " ";
            cout << endl;
        }
    }
};

int main(void)
{
    int rows, cols, data, choice = 1;
    cout << "Enter Number of Rows: ";
    cin >> rows;
    cout << "Enter Number of Columns: ";
    cin >> cols;
    clrscr();

    LowerTriangularMatrix matrix(rows, cols);
    do
    {
        cout << "          MENU          \n"
              << "===== \n"
              << "(1) Display\n"
              << "(2) Store\n"
              << "(3) Retrieve\n"
              << "(0) Exit\n\n";
        cout << "Enter Choice: ";
        cin >> choice;

        switch (choice)
        {
            case 1:
                cout << "\nMatrix:\n";
                matrix.display();
                break;
            case 2:
                cout << "Enter Data: ";
                cin >> data;
                cout << "Enter Position: ";
                cin >> rows >> cols;

```

```

        matrix.store(data, rows, cols);
        break;
    case 3:
        cout << "Enter Position: ";
        cin >> rows >> cols;
        data = matrix.retrieve(rows, cols);
        if (data != INT_MIN)
            cout << "Retrieved " << data << endl;
        else
            cerr << "ERROR: Invalid Location" << endl;
        break;
    case 0:
    default:
        break;
    }
    getch();
    clrscr();

} while (choice != 0);
return 0;
}

void getch()
{
    cout << "\nPress any key to continue...";
    cin.ignore();
    cin.get();
    return;
}

void clrscr()
{
#ifdef _WIN32 system("cls");
#elif __unix__ system("clear");
#endif return;
}

```

Output:

Enter Number of Rows: 3

Enter Number of Columns: 3

MENU

=====

(1) Display (2) Store
(3) Retrieve

(0) Exit

Enter Choice: 2

Enter Data: 4

Enter Position: 1 0

Press any key to continue...

MENU

=====

(1) Display

(2) Store

(3) Retrieve

(0) Exit

Enter Choice: 1

Matrix:

0 0 0

4 0 0

0 0 0

Press any key to continue...

MENU

=====

(1) Display

(2) Store

(3) Retrieve

(0) Exit

Enter Choice: 2

Enter Data: 2

Enter Position: 0 1

ERROR: Invalid Location

Press any key to continue...

MENU

=====

(1) Display
(2) Store
(3) Retrieve
(0) Exit
Enter Choice: 2

Enter Data: 8

Enter Position: 2 1

Press any key to continue...

MENU

=====

(1) Display
(2) Store (3)
Retrieve
(0) Exit

Enter Choice: 1

Matrix:

0 0 0

4 0 0

0 8 0

Press any key to continue...

MENU

=====

(1) Display (2) Store
(3) Retrieve
(0) Exit

Enter Choice: 3

Enter Position: 1 0

Retrieved 4

Press any key to continue...

(c) Upper Triangular Matrix using one-dimensional array

```
#include <climits>
#include <iostream>
#define MAX_SIZE 10

using namespace std;
void getch();
void clrscr();
class UpperTriangularMatrix
{
public:
    int *arr;
    int size;
    int nrows;
    int ncols;

    UpperTriangularMatrix(int rows = MAX_SIZE, int cols = MAX_SIZE)
    {
        if (rows != cols)
            cerr << "ERROR: Invalid Dimensions" << endl;
        else
        {
            size = cols * (cols + 1) / 2;
            nrows = ncols = rows;
            arr = new int[size];
            for (int i = 0; i < size; i++)
                arr[i] = 0;
        }
    }

    ~UpperTriangularMatrix()
    {
        delete[] arr;
    }

    void store(int data, int row, int col)
    {
        if (row > col || row >= nrows || col >= ncols)
            cerr << "ERROR: Invalid Location" << endl;
        else
            arr[col * (col + 1) / 2 + row] = data;
    }

    int retrieve(int row, int col)
    {
        if (row >= nrows || col >= ncols)
            return INT_MIN;
        if (row > col)
            return 0;
        else
```

```

        return arr[col * (col + 1) / 2 + row];
    }
    void display()
    {
        for (int i = 0; i < nrows; i++)
        {
            for (int j = 0; j < ncols; j++)
                if (j >= i)
                    cout << arr[j * (j + 1) / 2 + i] << " ";
                else
                    cout << 0 << " ";
            cout << endl;
        }
    }
};

int main(void)
{
    int rows, cols, data, choice = 1;
    cout << "Enter Number of Rows: ";
    cin >> rows;
    cout << "Enter Number of Columns: ";
    cin >> cols;
    clrscr();

    UpperTriangularMatrix matrix(rows, cols);
    do
    {
        cout << "          MENU          \n"
              << "===== \n"
              << "(1) Display\n"
              << "(2) Store\n"
              << "(3) Retrieve\n"
              << "(0) Exit\n\n";
        cout << "Enter Choice: ";
        cin >> choice;

        switch (choice)
        {
            case 1:
                cout << "\nMatrix:\n";
                matrix.display();
                break;
            case 2:
                cout << "Enter Data: ";
                cin >> data;
                cout << "Enter Position: ";
                cin >> rows >> cols;
                matrix.store(data, rows, cols);

```

```

        break;
    case 3:
        cout << "Enter Position: ";
        cin >> rows >> cols;
        data = matrix.retrieve(rows, cols);
        if (data != INT_MIN)
            cout << "Retrieved " << data << endl;
        else
            cerr << "ERROR: Invalid Location" << endl;
        break;
    case 0:
    default:
        break;
    }
    getch();
    clrscr();

} while (choice != 0);
return 0;
}

void getch()
{
    cout << "\nPress any key to continue...";
    cin.ignore();
    cin.get();
    return;
}

void clrscr()
{
#ifdef _WIN32 system("cls");
#elif __unix__ system("clear");
#endif return;
}

```

Output:

Enter Number of Rows: 3

Enter Number of Columns: 3

MENU

=====

(1) Display (2) Store

(3) Retrieve

(0) Exit

Enter Choice: 2

Enter Data: 3

Enter Position: 0 2

Press any key to continue...

MENU

=====

(1) Display (2)
Store (3) Retrieve
(0) Exit

Enter Choice: 2

Enter Data: 5

Enter Position: 1 1

Press any key to continue...

MENU

=====

(1) Display
(2) Store
(3) Retrieve
(0) Exit

Enter Choice: 1

Matrix:

0 0 3

0 5 0

0 0 0

Press any key to continue...

MENU

=====

(1) Display (2) Store
(3) Retrieve

(0) Exit
Enter Choice: 2
Enter Data: 7
Enter Position: 2 0
ERROR: Invalid Location
Press any key to continue...

MENU
=====

- (1) Display
- (2) Store
- (3) Retrieve (0) Exit

Enter Choice: 3
Enter Position: 0 2
Retrieved 3

Press any key to continue...

MENU
=====

- (1) Display (2) Store
- (3) Retrieve
- (0) Exit

Enter Choice: 3
Enter Position: 1 1
Retrieved 5

Press any key to continue...

(d) Symmetric Matrix using one-dimensional array

```
#include <climits>
#include <iostream>
#define MAX_SIZE 10
```

```

using namespace std;
void getch();
void clrscr();
class SymmetricMatrix
{
public:
    int *arr;
    int size;
    int nrows;
    int ncols;

    SymmetricMatrix(int rows = MAX_SIZE, int cols = MAX_SIZE)
    {
        if (rows != cols)
            cerr << "ERROR: Invalid Dimensions" << endl;
        else
        {
            size = rows * (rows + 1) / 2;
            nrows = ncols = rows;
            arr = new int[size];
            for (int i = 0; i < size; i++)
                arr[i] = 0;
        }
    }

    ~SymmetricMatrix()
    {
        delete[] arr;
    }

    void store(int data, int row, int col)
    {
        if (row >= nrows || col >= ncols)
            cerr << "ERROR: Invalid Location" << endl;
        else if (col > row)
            arr[col * (col + 1) / 2 + row] = data;
        else
            arr[row * (row + 1) / 2 + col] = data;
    }

    int retrieve(int row, int col)
    {
        if (row >= nrows || col >= ncols)
            return INT_MIN;
        if (col > row)
            return arr[col * (col + 1) / 2 + row];
        else
            return arr[row * (row + 1) / 2 + col];
    }
}

```

```

void display()
{
    for (int i = 0; i < nrows; i++)
    {
        for (int j = 0; j < ncols; j++)
            if (i > j)
                cout << arr[i * (i + 1) / 2 + j] << " ";
            else
                cout << arr[j * (j + 1) / 2 + i] << " ";
        cout << endl;
    }
}

};

int main(void)
{
    int rows, cols, data, choice = 1;
    cout << "Enter Number of Rows: ";
    cin >> rows;
    cout << "Enter Number of Columns: ";
    cin >> cols;
    clrscr();

    SymmetricMatrix matrix(rows, cols);
    do
    {
        cout << "          MENU          \n"
              << "===== \n"
              << "(1) Display\n"
              << "(2) Store\n"
              << "(3) Retrieve\n"
              << "(0) Exit\n\n";
        cout << "Enter Choice: ";
        cin >> choice;

        switch (choice)
        {
            case 1:
                cout << "\nMatrix:\n";
                matrix.display();
                break;
            case 2:
                cout << "Enter Data: ";
                cin >> data;
                cout << "Enter Position: ";
                cin >> rows >> cols;
                matrix.store(data, rows, cols);
                break;
            case 3:

```

```

        cout << "Enter Position: ";
        cin >> rows >> cols;
        data = matrix.retrieve(rows, cols);
        if (data != INT_MIN)
            cout << "Retrieved " << data << endl;
        else
            cerr << "ERROR: Invalid Location" << endl;
        break;
    case 0:
    default:
        break;
    }
    getch();
    clrscr();

} while (choice != 0);

return 0;
}

void getch()
{
    cout << "\nPress any key to continue...";
    cin.ignore();
    cin.get();
    return;
}

void clrscr()
{
#ifdef _WIN32 system("cls");
#elif __unix__ system("clear");
#endif return;
}

```

Output:

Enter Number of Rows: 3

Enter Number of Columns: 3

MENU

=====

- (1) Display
- (2) Store
- (3) Retrieve
- (0) Exit

Enter Choice: 2

Enter Data: 8

Enter Position: 1 2

Press any key to continue...

MENU

=====

- (1) Display
- (2) Store
- (3) Retrieve
- (0) Exit

Enter Choice: 1

Matrix:

0 0 0

0 0 8

0 8 0

Press any key to continue...

MENU

=====

- (1) Display (2) Store
- (3) Retrieve
- (0) Exit

Enter Choice: 2

Enter Data: 9

Enter Position: 0 2

Press any key to continue...

MENU

=====

(1) Display (2)
Store (3) Retrieve
(0) Exit

Enter Choice: 1

Matrix:

0 0 9

0 0 8

9 8 0

Press any key to continue...

MENU

=====

(1) Display (2) Store
(3) Retrieve

(0) Exit

Enter Choice: 2

Enter Data: 5

Enter Position: 0 0

Press any key to continue...

MENU

=====

(1) Display
(2) Store
(3) Retrieve
(0) Exit

Enter Choice: 1

Matrix:

5 0 9

0 0 8

9 8 0

Press any key to continue...

MENU

=====

(1) Display (2) Store
(3) Retrieve
(0) Exit

Enter Choice: 3

Enter Position: 2 0

Retrieved 9

Press any key to continue...

14. Write a program to implement AVL Tree.

```
#include <iostream>

using namespace std;
void getch();
void clrscr();
int max(int, int);
template <class T>
class Node
{
public:
    T data;
    int height;
    int balanceFactor;
    Node *left, *right, *parent;
    Node()
    {
        left = nullptr;
        right = nullptr;
        parent = nullptr;
        height = 1;
        balanceFactor = 0;
    }
};

class AVLTree
{
public:
```



```

Node<int> *root;

AVLTree()
{
    root = nullptr;
}

int getBalanceFactor(Node<int> *node)
{
    if (node == nullptr)
        return 0;
    return height(node->right) - height(node->left);
}

Node<int> *rightRotate(Node<int> *y)
{
    Node<int> *x = y->left;
    y->left = x->right;
    if (x->right != nullptr)
        x->right->parent = y;
    x->parent = y->parent;
    if (y->parent == nullptr)
        root = x;
    else if (y == y->parent->right)
        y->parent->right = x;
    else
        y->parent->left = x;
    x->right = y;
    y->parent = x;
    y->height = 1 + max(height(y->left), height(y->right));
    x->height = 1 + max(height(x->left), height(x->right));
    x->balanceFactor = getBalanceFactor(x);
    y->balanceFactor = getBalanceFactor(y);
    return x;
}

Node<int> *leftRotate(Node<int> *x)
{
    Node<int> *y = x->right;
    x->right = y->left;
    if (y->left != nullptr)
        y->left->parent = x;
    y->parent = x->parent;

    if (x->parent == nullptr)
        root = y;
    else if (x == x->parent->left)
        x->parent->left = y;
    else

```

```

        x->parent->right = y;
    y->left = x;
    x->parent = y;
    y->height = 1 + max(height(y->left), height(y->right));
    x->height = 1 + max(height(x->left), height(x->right));
    x->balanceFactor = getBalanceFactor(x);
    y->balanceFactor = getBalanceFactor(y);
    return y;
}

Node<int> *insert(int data, Node<int> *current)
{
    Node<int> *temp;
    if (current == nullptr)
    {
        temp = new Node<int>;
        temp->data = data;
        return temp;
    }
    if (data < current->data)
    {
        current->left = insert(data, current->left);
        current->left->parent = current;
    }
    else
    {
        current->right = insert(data, current->right);
        current->right->parent = current;
    }
    current->height = 1 + max(height(current->left), height(current->right));
    current->balanceFactor = getBalanceFactor(current);

    if (current->balanceFactor < -1 && data < current->left->data)
        return rightRotate(current);
    if (current->balanceFactor > 1 && data > current->right->data)
        return leftRotate(current);

    if (current->balanceFactor < -1 && data > current->left->data)
    {
        current->left = leftRotate(current->left);
        return rightRotate(current);
    }
    if (current->balanceFactor > 1 && data < current->right->data)
    {
        current->right = rightRotate(current->right);
        return leftRotate(current);
    }
}

```

```

        return current;
    }
    bool search(Node<int> *node, int key)
    {
        if (node == nullptr)
            return false;
        if (node->data == key)
            return true;
        bool left = search(node->left, key);
        if (left)
            return true;
        bool right = search(node->right, key);
        return right;
    }
    void inOrderRecursive(Node<int> *root)
    {
        if (root != nullptr)
        {
            inOrderRecursive(root->left);
            cout << root->data << " (" << root->balanceFactor << ") ";
            inOrderRecursive(root->right);
        }
    }
    void preOrderRecursive(Node<int> *root)
    {
        if (root != nullptr)
        {
            cout << root->data << " (" << root->balanceFactor << ") ";
            preOrderRecursive(root->left);
            preOrderRecursive(root->right);
        }
    }
    void postOrderRecursive(Node<int> *root)
    {
        if (root != nullptr)
        {
            postOrderRecursive(root->left);
            postOrderRecursive(root->right);
            cout << root->data << " (" << root->balanceFactor << ") ";
        }
    }
    int height(Node<int> *current)
    {
        if (current == nullptr)
            return 0;
        else
        {
            int leftHeight = height(current->left);

```

```

        int rightHeight = height(current->right);
        if (leftHeight > rightHeight)
            return (leftHeight + 1);
        else
            return (rightHeight + 1);
    }
}

Node<int> *deleteByCopying(Node<int> *current, int key)
{
    if (key < current->data)
        current->left = deleteByCopying(current->left, key);
    else if (key > current->data)
        current->right = deleteByCopying(current->right, key);
    else
    {
        // node with only one child or no child        if ((current->left
== nullptr) ||
        (current->right == nullptr))
        {
            Node<int> *temp = current->left ? current->left : current-
>right;

            if (temp == nullptr)
            {
                temp = current;
                current = nullptr;
            }
            else
                *current = *temp;
            delete temp;
        }
        else
        {
            // copy inorder predecessor        Node<int> *temp = current-
>left;
            while (temp->right != nullptr)        temp = temp-
>right;
            current->data = temp->data;        current->right =
temp-
deleteByCopying(current->right,
>data);
        }
    }
    if (current == nullptr)
        return current;
    current->height = 1 + max(height(current->left), height(current-
>right));
    current->balanceFactor = getBalanceFactor(current);
}

```

```

        // R(0) and R(-1)    if (current->balanceFactor < -1
&&        getBalanceFactor(current->left) <= 0)        return
rightRotate(current);
        // R(+1)    if (current->balanceFactor < -1
&&        getBalanceFactor(current->left) > 0)
        {
            current->left = leftRotate(current->left);
            return rightRotate(current);
        }

        // L(0) and L(+1)    if (current->balanceFactor > 1
&&        getBalanceFactor(current->right) >= 0)        return
leftRotate(current);
        // L(-1)    if (current->balanceFactor > 1
&&        getBalanceFactor(current->right) < 0)
        {
            current->right = rightRotate(current->right);
            return leftRotate(current);
        }
        return current;
    }
};
int main(void)
{
    AVLTree tree;
    int choice, data, data2;
    do
    {
        cout << "          MENU          \n"
              << "===== \n"
              << "(1) Insert a Node\n"
              << "(2) Search a Node\n"
              << "(3) Display Traversals\n"
              << "(4) Delete a Node\n"
              << "(0) Exit\n\n";
        cout << "Enter Choice: ";
        cin >> choice;

        switch (choice)
        {
            case 1:
                cout << "\nEnter Node Data: ";
                cin >> data;
                tree.root = tree.insert(data, tree.root);
                break;
            case 2:
                cout << "\nEnter Search Data: ";
                cin >> data;

```

```

        cout << "Search Result: ";
        if (tree.search(tree.root, data))
            cout << "Found";
        else
            cout << "Not Found";
        cout << endl;
        break;
    case 3:
        cout << endl;
        cout << "In-Order Recursive Traversal: ";
        tree.inOrderRecursive(tree.root);
        cout << endl;
        cout << "Pre-Order Recursive Traversal: ";
        tree.preOrderRecursive(tree.root);
        cout << endl;
        cout << "Post-Order Recursive Traversal: ";
        tree.postOrderRecursive(tree.root);
        cout << endl;
        break;
    case 4:
        cout << "\nEnter Node to Delete: ";
        cin >> data;
        tree.root = tree.deleteByCopying(tree.root, data);
        break;
    case 0:
    default:
        break;
    }
    getch();
    clrscr();
} while (choice != 0);
return 0;
}

int max(int a, int b)
{
    return (a > b) ? a : b;
}

void getch()
{
    cout << "\nPress any key to continue...";
    cin.ignore();
    cin.get();
    return;
}

void clrscr()
{
#ifdef _WIN32 system("cls");
#elif __unix__ system("clear");

```

```
#endif return;  
}
```

Output:

MENU

=====

- (1) Insert a Node
- (2) Search a Node
- (3) Display Traversals
- (4) Delete a Node
- (0) Exit

Enter Choice: 1

Enter Node Data: 10

Press any key to continue...

MENU

=====

- (1) Insert a Node (2) Search a Node (3) Display Traversals
- (4) Delete a Node
- (0) Exit

Enter Choice: 3

In-Order Recursive Traversal: 10 (0)

Pre-Order Recursive Traversal: 10 (0)

Post-Order Recursive Traversal: 10 (0)

Press any key to continue...

MENU

=====

- (1) Insert a Node (2) Search a Node (3) Display Traversals
- (4) Delete a Node
- (0) Exit

Enter Choice: 1

Enter Node Data: 20

Press any key to continue...

MENU

=====

- (1) Insert a Node
- (2) Search a Node
- (3) Display Traversals
- (4) Delete a Node
- (0) Exit

Enter Choice: 3

In-Order Recursive Traversal: 10 (1) 20 (0)

Pre-Order Recursive Traversal: 10 (1) 20 (0)

Post-Order Recursive Traversal: 20 (0) 10 (1)

Press any key to continue...

MENU

=====

- (1) Insert a Node (2) Search a Node (3) Display Traversals
- (4) Delete a Node

- (0) Exit

Enter Choice: 1

Enter Node Data: 30

Press any key to continue...

MENU

=====

- (1) Insert a Node
- (2) Search a Node
- (3) Display Traversals
- (4) Delete a Node
- (0) Exit

Enter Choice: 3

In-Order Recursive Traversal: 10 (0) 20 (0) 30 (0)

Pre-Order Recursive Traversal: 20 (0) 10 (0) 30 (0)

Post-Order Recursive Traversal: 10 (0) 30 (0) 20 (0)

Press any key to continue...

MENU

=====

- (1) Insert a Node
- (2) Search a Node
- (3) Display Traversals
- (4) Delete a Node
- (0) Exit

Enter Choice: 1

Enter Node Data: 40

Press any key to continue...

MENU

=====

- (1) Insert a Node (2) Search a Node (3) Display Traversals
- (4) Delete a Node
- (0) Exit

Enter Choice: 3

In-Order Recursive Traversal: 10 (0) 20 (1) 30 (1) 40 (0)

Pre-Order Recursive Traversal: 20 (1) 10 (0) 30 (1) 40 (0)

Post-Order Recursive Traversal: 10 (0) 40 (0) 30 (1) 20 (1)

Press any key to continue...

MENU

=====

- (1) Insert a Node
- (2) Search a Node
- (3) Display Traversals
- (4) Delete a Node
- (0) Exit

Enter Choice: 1

Enter Node Data: 50

Press any key to continue...

MENU

=====

- (1) Insert a Node (2) Search a Node (3) Display Traversals
- (4) Delete a Node
- (0) Exit

Enter Choice: 3

In-Order Recursive Traversal: 10 (0) 20 (1) 30 (0) 40 (0) 50 (0)

Pre-Order Recursive Traversal: 20 (1) 10 (0) 40 (0) 30 (0) 50 (0) Post-Order Recursive Traversal:
10 (0) 30 (0) 50 (0) 40 (0) 20 (1)

Press any key to continue..

MENU

=====

- (1) Insert a Node (2) Search a Node (3) Display Traversals
- (4) Delete a Node
- (0) Exit

Enter Choice: 1

Enter Node Data: 25

Press any key to continue...

MENU

=====

- (1) Insert a Node (2) Search a Node (3) Display Traversals
- (4) Delete a Node
- (0) Exit

Enter Choice: 3

In-Order Recursive Traversal: 10 (0) 20 (0) 25 (0) 30 (0) 40 (1) 50 (0)

Pre-Order Recursive Traversal: 30 (0) 20 (0) 10 (0) 25 (0) 40 (1) 50 (0)

Post-Order Recursive Traversal: 10 (0) 25 (0) 20 (0) 50 (0) 40 (1) 30 (0)

Press any key to continue...

MENU

=====

- (1) Insert a Node (2) Search a Node (3) Display Traversals
- (4) Delete a Node
- (0) Exit

Enter Choice: 1

Enter Node Data: 5

Press any key to continue..

MENU

=====

- (1) Insert a Node (2) Search a Node (3) Display Traversals
- (4) Delete a Node

(0) Exit

Enter Choice: 3

In-Order Recursive Traversal: 5 (0) 10 (-1) 20 (-1) 25 (0) 30 (-
1) 40 (1) 50 (0)

Pre-Order Recursive Traversal: 30 (-1) 20 (-1) 10 (-
1) 5 (0) 25 (0) 40 (1) 50 (0)

Post-Order Recursive Traversal: 5 (0) 10 (-1) 25 (0) 20 (-
1) 50 (0) 40 (1) 30 (-1)

Press any key to continue..

MENU

=====

(1) Insert a Node (2) Search a
Node (3) Display Traversals
(4) Delete a Node
(0) Exit

Enter Choice: 1

Enter Node Data: 1

Press any key to continue...

MENU

=====

(1) Insert a Node (2) Search a Node (3) Display Traversals
(4) Delete a Node
(0) Exit

Enter Choice: 3

In-Order Recursive Traversal: 1 (0) 5 (0) 10 (0) 20 (-1) 25 (0) 30 (-

1) 40 (1) 50 (0)

Pre-Order Recursive Traversal: 30 (-1) 20 (-

1) 5 (0) 1 (0) 10 (0) 25 (0) 40 (1) 50 (0)

Post-Order Recursive Traversal: 1 (0) 10 (0) 5 (0) 25 (0) 20 (-

1) 50 (0) 40 (1) 30 (-1)

Press any key to continue...

15. Write a program to implement a priority queue using heap data structure.

```
#include <iostream>
#define MAX_SIZE 20
using namespace std;
void getch();
void clrscr();
class Heap
{
public:
    int *heap;
    int heapSize;

    Heap(int *&A, int n)
    {
        heap = A;
        heapSize = n;
    }
    int parent(int i)
    {
        return (i - 1) / 2;
    }
    int left(int i)
    {
        return 2 * i + 1;
    }
    int right(int i)
    {
        return 2 * i + 2;
    }
    void maxHeapify(int *&A, int n, int i)
    {
        int temp;
        int largest;
        int l = left(i);
        int r = right(i);
        if (l < n && A[l] > A[i])
        {
            largest = l;
        }
        else
        {
            largest = i;
        }
        if (r < n && A[r] > A[largest])
        {
            largest = r;
        }
        if (largest != i)
```

```

        {
            temp = A[i];
            A[i] = A[largest];
            A[largest] = temp;
            maxHeapify(A, n, largest);
        }
    }
    void buildMaxHeap()
    {
        for (int i = heapSize / 2; i >= 0; i--)
            maxHeapify(heap, heapSize, i);
    }
};

class MaxPriorityQueue
{
public:
    Heap *heap;

    MaxPriorityQueue(int A[], int n)
    {
        heap = new Heap(A, n);
        heap->buildMaxHeap();
    }

    ~MaxPriorityQueue()
    {
        delete heap;
    }

    int size()
    {
        return heap->heapSize;
    }

    void display()
    {
        if (heap->heapSize == 0)
        {
            cerr << "ERROR: Heap Empty";
            return;
        }
        for (int i = 0; i < heap->heapSize; i++)
            cout << heap->heap[i] << " ";
    }

    void heapIncreaseKey(int i, int key)
    {
        int temp;
        if (key < heap->heap[i])
        {

```

```

        cerr << "ERROR: New Key is smaller than Existing Key";
        return;
    }
    heap->heap[i] = key;
    while (i > 0 && heap->heap[heap->parent(i)] < heap->heap[i])
    {
        temp = heap->heap[heap->parent(i)];
        heap->heap[heap->parent(i)] = heap->heap[i];
        heap->heap[i] = temp;
        i = heap->parent(i);
    }
}

void maxHeapInsert(int key)
{
    heap->heapSize++;
    heap->heap[heap->heapSize - 1] = INT8_MIN;
    heapIncreaseKey(heap->heapSize - 1, key);
}

int heapMaximum()
{
    if (heap->heapSize == 0)
    {
        cerr << "ERROR: Heap Empty";
        return -1;
    }
    return heap->heap[0];
}

int heapExtractMax()
{
    if (heap->heapSize < 0)
    {
        cerr << "ERROR: Heap Underflow";
        return -1;
    }
    else if (heap->heapSize == 0)
    {
        cerr << "ERROR: Heap Empty";
        return -1;
    }
    int max = heap->heap[0];
    heap->heap[0] = heap->heap[heap->heapSize];
    heap->maxHeapify(heap->heap, --heap->heapSize, 0);
    return max;
}

};

int main(void)
{
    int idx, key;

```



```

int n, choice = 1, A[MAX_SIZE] = {INT8_MAX};
cout << "Initial Data\n=====\n";
cout << "Enter Number of Nodes: ";
cin >> n;
cout << "Enter Keys of the Nodes: ";
for (int i = 0; i < n; i++)
    cin >> A[i];
clrscr();

MaxPriorityQueue queue(A, n);
do
{
    cout << "\t\t Max Priority Queue\n"
         << "=====\n"
         << " (1) HeapIncreaseKey (2) MaxHeapInsert\n"
         << " (3) HeapMaximum (4) HeapExtractMax\n"
         << " (5) Display (0) Exit\n\n";
    cout << "Enter Choice: ";
    cin >> choice;
    cout << endl;
    switch (choice)
    {
        case 1:
            cout << endl;
            cout << "Enter Position: ";
            cin >> idx;
            cout << "Enter New Key: ";
            cin >> key;
            queue.heapIncreaseKey(idx - 1, key);
            cout << endl;
            break;
        case 2:
            cout << endl;
            cout << "Enter Key: ";
            cin >> key;
            queue.maxHeapInsert(key);
            break;
        case 3:
            cout << endl;
            key = queue.heapMaximum();
            if (key != -1)
                cout << "Heap Maximum: " << key << endl;
            break;
        case 4:
            cout << endl;
            key = queue.heapExtractMax();
            if (key != -1)
            {

```

```

        cout << "After Heap Extract Max: ";
        queue.display();
        cout << endl;
    }
    break;
case 5:
    cout << endl;
    queue.display();
    cout << endl;
    break;
case 0:
default:
    break;
}
getch();
clrscr();
} while (choice != 0);
return 0;
}

void getch()
{
    cout << "\nPress any key to continue...";
    cin.ignore();
    cin.get();
    return;
}

void clrscr()
{
#ifdef _WIN32 system("cls");
#elif __unix__ system("clear");
#endif return;
}

#include <iostream>
#define MAX_SIZE 20
using namespace std;
void getch();
void clrscr();
class Heap
{
public:
    int *heap;
    int heapSize;

    Heap(int *&A, int n)
    {
        heap = A;
        heapSize = n;
    }
}

```

```

int parent(int i)
{
    return (i - 1) / 2;
}
int left(int i)
{
    return 2 * i + 1;
}
int right(int i)
{
    return 2 * i + 2;
}
void maxHeapify(int *&A, int n, int i)
{
    int temp;
    int largest;
    int l = left(i);
    int r = right(i);
    if (l < n && A[l] > A[i])
    {
        largest = l;
    }
    else
    {
        largest = i;
    }
    if (r < n && A[r] > A[largest])
    {
        largest = r;
    }
    if (largest != i)
    {
        temp = A[i];
        A[i] = A[largest];
        A[largest] = temp;
        maxHeapify(A, n, largest);
    }
}
void buildMaxHeap()
{
    for (int i = heapSize / 2; i >= 0; i--)
        maxHeapify(heap, heapSize, i);
}
};
class MaxPriorityQueue
{
public:
    Heap *heap;

```

```

MaxPriorityQueue(int A[], int n)
{
    heap = new Heap(A, n);
    heap->buildMaxHeap();
}

~MaxPriorityQueue()
{
    delete heap;
}

int size()
{
    return heap->heapSize;
}

void display()
{
    if (heap->heapSize == 0)
    {
        cerr << "ERROR: Heap Empty";
        return;
    }
    for (int i = 0; i < heap->heapSize; i++)
        cout << heap->heap[i] << " ";
}

void heapIncreaseKey(int i, int key)
{
    int temp;
    if (key < heap->heap[i])
    {
        cerr << "ERROR: New Key is smaller than Existing Key";
        return;
    }
    heap->heap[i] = key;
    while (i > 0 && heap->heap[heap->parent(i)] < heap->heap[i])
    {
        temp = heap->heap[heap->parent(i)];
        heap->heap[heap->parent(i)] = heap->heap[i];
        heap->heap[i] = temp;
        i = heap->parent(i);
    }
}

void maxHeapInsert(int key)
{
    heap->heapSize++;
    heap->heap[heap->heapSize - 1] = INT8_MIN;
    heapIncreaseKey(heap->heapSize - 1, key);
}

```

```

}
int heapMaximum()
{
    if (heap->heapSize == 0)
    {
        cerr << "ERROR: Heap Empty";
        return -1;
    }
    return heap->heap[0];
}
int heapExtractMax()
{
    if (heap->heapSize < 0)
    {
        cerr << "ERROR: Heap Underflow";
        return -1;
    }
    else if (heap->heapSize == 0)
    {
        cerr << "ERROR: Heap Empty";
        return -1;
    }
    int max = heap->heap[0];
    heap->heap[0] = heap->heap[heap->heapSize];
    heap->maxHeapify(heap->heap, --heap->heapSize, 0);
    return max;
}
};
int main(void)
{
    int idx, key;
    int n, choice = 1, A[MAX_SIZE] = {INT8_MAX};
    cout << "Initial Data\n=====\n";
    cout << "Enter Number of Nodes: ";
    cin >> n;
    cout << "Enter Keys of the Nodes: ";
    for (int i = 0; i < n; i++)
        cin >> A[i];
    clrscr();

    MaxPriorityQueue queue(A, n);
    do
    {
        cout << "\t\t Max Priority Queue\n"
              << "=====\n"
              << "  (1) HeapIncreaseKey  (2) MaxHeapInsert\n"
              << "  (3) HeapMaximum      (4) HeapExtractMax\n"
              << "  (5) Display          (0) Exit\n\n";
    }

```

```

cout << "Enter Choice: ";
cin >> choice;
cout << endl;
switch (choice)
{
case 1:
    cout << endl;
    cout << "Enter Position: ";
    cin >> idx;
    cout << "Enter New Key: ";
    cin >> key;
    queue.heapIncreaseKey(idx - 1, key);
    cout << endl;
    break;
case 2:
    cout << endl;
    cout << "Enter Key: ";
    cin >> key;
    queue.maxHeapInsert(key);
    break;
case 3:
    cout << endl;
    key = queue.heapMaximum();
    if (key != -1)
        cout << "Heap Maximum: " << key << endl;
    break;
case 4:
    cout << endl;
    key = queue.heapExtractMax();
    if (key != -1)
    {
        cout << "After Heap Extract Max: ";
        queue.display();
        cout << endl;
    }
    break;
case 5:
    cout << endl;
    queue.display();
    cout << endl;
    break;
case 0:
default:
    break;
}
getch();
clrscr();
} while (choice != 0);

```

```

        return 0;
    }
    void getch()
    {
        cout << "\nPress any key to continue...";
        cin.ignore();
        cin.get();
        return;
    }
    void clrscr()
    {
#ifdef _WIN32 system("cls");
#elif __unix__ system("clear");
#endif return;
    }

```

Output:

Initial Data

=====

Enter Number of Nodes: 10

Enter Keys of the Nodes: 14 8 10 4 7 9 3 2 1 6

Max Priority Queue

=====

- (1) HeapIncreaseKey (2) MaxHeapInsert
 (3) HeapMaximum (4) HeapExtractMax
 (5) Display (0) Exit

Enter Choice: 5

14 8 10 4 7 9 3 2 1 6

Press any key to continue...

Max Priority Queue

=====

- (1) HeapIncreaseKey (2) MaxHeapInsert
 (3) HeapMaximum (4) HeapExtractMax

(5) Display (0) Exit

Enter Choice: 1

Enter Position: 10

Enter New Key: 26

Press any key to continue...

Max Priority Queue =====

(1) HeapIncreaseKey (2) MaxHeapInsert
(3) HeapMaximum (4) HeapExtractMax
(5) Display (0) Exit

Enter Choice: 5

26 14 10 4 8 9 3 2 1 7

Press any key to continue...

Max Priority Queue

=====

(1) HeapIncreaseKey (2) MaxHeapInsert
(3) HeapMaximum (4) HeapExtractMax
(5) Display (0) Exit

Enter Choice: 2

Enter Key: 40

Press any key to continue...

Max Priority Queue

=====

(1) HeapIncreaseKey (2) MaxHeapInsert
(3) HeapMaximum (4) HeapExtractMax
(5) Display (0) Exit

Enter Choice: 5

40 26 10 4 14 9 3 2 1 7 8

Press any key to continue...

Max Priority Queue

=====

(1) HeapIncreaseKey (2) MaxHeapInsert
(3) HeapMaximum (4) HeapExtractMax
(5) Display (0) Exit

Enter Choice: 3

Heap Maximum: 40

Press any key to continue...

Max Priority Queue =====

(1) HeapIncreaseKey (2) MaxHeapInsert
(3) HeapMaximum (4) HeapExtractMax
(5) Display (0) Exit

Enter Choice: 4

After Heap Extract Max: 26 14 10 4 8 9 3 2 1 7

Press any key to continue...

16. Write a program to evaluate a prefix/postfix expression using stacks.

```
// stack.hpp
#include <iostream>
#define MAX_SIZE 100

using namespace std;
template <class T>
class Stack
{
protected:
    int tos, size;
    T arr[MAX_SIZE];

public:
    Stack(int size = 30)
    {
        this->tos = -1;
        this->size = size;
    }
    bool push(T ele)
    {
        if (this->tos >= (this->size - 1))
        {
            cerr << "ERROR: Stack Overflow\n";
            return false;
        }
        this->arr[++(this->tos)] = ele;
        return true;
    }

    T pop()
    {
        if (this->isEmpty())
        {
            cout << "ERROR: Stack Underflow\n";
            return (T)(NULL);
        }
        return this->arr[(this->tos)--];
    }

    T top()
    {
        if (this->isEmpty())
        {
            cout << "Stack Empty";
            return (T)(NULL);
        }
        return this->arr[this->tos];
    }
};
```

```

    }
    bool isEmpty()
    {
        return this->tos == -1;
    }
    void clear()
    {
        while (!this->isEmpty())
            this->pop();
    }
};

// main.cpp
#include "stack.hpp"
#include <cstring> #include <string>
#include <cstdlib>
#define MAX_STRLEN 256
class PostfixEvaluator
{
protected:
    Stack<int> stack;

public:
    int evaluate(string &str)
    {
        int val1, val2, temp;
        int size = str.length();
        for (int i = 0; i < size; ++i)
        {
            if (str[i] == ' ')
                continue;
            else if (isdigit(str[i]))
            {
                temp = 0;
                while (isdigit(str[i]))
                    temp = temp * 10 + (int)(str[i++] - '0');
                i--;
                this->stack.push(temp);
            }
            else
            {
                val1 = this->stack.pop();
                val2 = this->stack.pop();
                switch (str[i])
                {
                    case '+':
                        this->stack.push(val2 + val1);
                        break;

```

```

        case '-':
            this->stack.push(val2 - val1);
            break;
        case '*':
            this->stack.push(val2 * val1);
            break;
        case '/':
            this->stack.push(val2 / val1);
            break;
        case '%':
            this->stack.push(val2 % val1);
            break;
    }
}
}
return this->stack.pop();
}
};

class PrefixEvaluator
{
private:
    void swap(char &x, char &y)
    {
        char temp = x;
        x = y;
        y = temp;
    }

protected:
    Stack<int> stack;

public:
    int evaluate(string &str)
    {
        string strTemp;
        int val1, val2, temp;
        int size = str.length();
        // parse expression in a reverse fashion    for (int i = size - 1; i
        >= 0; i--)
        {
            if (str[i] == ' ')
                continue;
            else if (isdigit(str[i]))
            {
                strTemp = "";
                while (isdigit(str[i]))
                    strTemp.append(string(1, str[i--]));
                i++;
            }
        }
    }
};

```

```

        for (int i = 0; i < strTemp.length() / 2; i++)
            swap(strTemp[i], strTemp[strTemp.length() - i - 1]);
        temp = atoi(strTemp.c_str());
        this->stack.push(temp);
    }
    else
    {
        val1 = this->stack.pop();
        val2 = this->stack.pop();
        switch (str[i])
        {
            case '+':
                this->stack.push(val1 + val2);
                break;
            case '-':
                this->stack.push(val1 - val2);
                break;
            case '*':
                this->stack.push(val1 * val2);
                break;
            case '/':
                this->stack.push(val1 / val2);
                break;
            case '%':
                this->stack.push(val1 % val2);
                break;
        }
    }
}

return this->stack.pop();
}

};

int main(void)
{
    string str;
    PrefixEvaluator preEval;
    PostfixEvaluator postEval;
    cout << "Enter Prefix Expression: ";
    getline(cin, str);
    cout << "Value of Expression: " << preEval.evaluate(str) << endl;
    cout << endl;
    cout << "Enter Postfix Expression: ";
    getline(cin, str);
    cout << "Value of Expression: " << postEval.evaluate(str) << endl;
    return 0;
}

// stack.hpp
#include <iostream>

```

```

#define MAX_SIZE 100

using namespace std;
template <class T>
class Stack
{
protected:
    int tos, size;
    T arr[MAX_SIZE];

public:
    Stack(int size = 30)
    {
        this->tos = -1;
        this->size = size;
    }
    bool push(T ele)
    {
        if (this->tos >= (this->size - 1))
        {
            cerr << "ERROR: Stack Overflow\n";
            return false;
        }
        this->arr[++(this->tos)] = ele;
        return true;
    }

    T pop()
    {
        if (this->isEmpty())
        {
            cout << "ERROR: Stack Underflow\n";
            return (T)(NULL);
        }
        return this->arr[(this->tos)--];
    }

    T top()
    {
        if (this->isEmpty())
        {
            cout << "Stack Empty";
            return (T)(NULL);
        }
        return this->arr[this->tos];
    }
    bool isEmpty()
    {

```

```

        return this->tos == -1;
    }
    void clear()
    {
        while (!this->isEmpty())
            this->pop();
    }
};

// main.cpp
#include "stack.hpp"
#include <cstring> #include <string>
#include <cstdlib>
#define MAX_STRLEN 256
class PostfixEvaluator
{
protected:
    Stack<int> stack;

public:
    int evaluate(string &str)
    {
        int val1, val2, temp;
        int size = str.length();
        for (int i = 0; i < size; ++i)
        {
            if (str[i] == ' ')
                continue;
            else if (isdigit(str[i]))
            {
                temp = 0;
                while (isdigit(str[i]))
                    temp = temp * 10 + (int)(str[i++] - '0');
                i--;
                this->stack.push(temp);
            }
            else
            {
                val1 = this->stack.pop();
                val2 = this->stack.pop();
                switch (str[i])
                {
                    case '+':
                        this->stack.push(val2 + val1);
                        break;
                    case '-':
                        this->stack.push(val2 - val1);
                        break;
                }
            }
        }
    }
};

```

```

        case '*':
            this->stack.push(val2 * val1);
            break;
        case '/':
            this->stack.push(val2 / val1);
            break;
        case '%':
            this->stack.push(val2 % val1);
            break;
    }
}
}
return this->stack.pop();
}
};

class PrefixEvaluator
{
private:
    void swap(char &x, char &y)
    {
        char temp = x;
        x = y;
        y = temp;
    }

protected:
    Stack<int> stack;

public:
    int evaluate(string &str)
    {
        string strTemp;
        int val1, val2, temp;
        int size = str.length();
        // parse expression in a reverse fashion    for (int i = size - 1; i
>= 0; i--)
        {
            if (str[i] == ' ')
                continue;
            else if (isdigit(str[i]))
            {
                strTemp = "";
                while (isdigit(str[i]))
                    strTemp.append(string(1, str[i--]));
                i++;
                for (int i = 0; i < strTemp.length() / 2; i++)
                    swap(strTemp[i], strTemp[strTemp.length() - i - 1]);
                temp = atoi(strTemp.c_str());
            }
        }
    }
};

```



```

        this->stack.push(temp);
    }
    else
    {
        val1 = this->stack.pop();
        val2 = this->stack.pop();
        switch (str[i])
        {
            case '+':
                this->stack.push(val1 + val2);
                break;
            case '-':
                this->stack.push(val1 - val2);
                break;
            case '*':
                this->stack.push(val1 * val2);
                break;
            case '/':
                this->stack.push(val1 / val2);
                break;
            case '%':
                this->stack.push(val1 % val2);
                break;
        }
    }
}

return this->stack.pop();
}

};

int main(void)
{
    string str;
    PrefixEvaluator preEval;
    PostfixEvaluator postEval;
    cout << "Enter Prefix Expression: ";
    getline(cin, str);
    cout << "Value of Expression: " << preEval.evaluate(str) << endl;
    cout << endl;
    cout << "Enter Postfix Expression: ";
    getline(cin, str);
    cout << "Value of Expression: " << postEval.evaluate(str) << endl;
    return 0;
}

```

Output:

Enter Prefix Expression: - * 5 + 6 2 / 12 4
Value of Expression: 37

Enter Postfix Expression: 5 6 2 + * 12 4 / -
Value of Expression: 37