

Additional Task for week 1 & 2

Study of all sorting algorithms.

Q1) Classification of sorting Algorithms

→ Sorting algorithms are categorized on the following basis :-

1) By number of comparisons.

→ Comparison-based sorting algorithms check the elements of the list by key comparison operation & need atleast $O(n \log n)$ comparisons for most inputs.

→ Best case behaviour is $O(n \log n)$ and worst-case is $O(n^2)$

Eg: Counting sort, bucket sort, radix sort, etc.

2) By Number of Swaps.

→ Sorting algorithms are categorized by the no. of swaps.

3) By memory usage.

→ Some sorting algorithms are 'in place' and they need $O(1)$ or $O(\log N)$ memory to create auxillary locations for sorting data temporarily.

4) By recursion.

→ Sorting algorithms are either recursive (quicksort) or non-recursive (selection sort) and there are some algorithms that use both.

5) By stability.

→ Sorting algorithm is stable if 2 elements with equal

values appear in the same order in o/p as it was in i/p. The stability of a sorting algorithm can be checked with how it treats equal elements.

→ Stable algorithms preserve the relative order of equal elements, while unstable algorithms - don't.

6) By adaptability.

→ In a few sorting algorithms, the complexity changes based on pre-sorted input, i.e. pre-sorted array of the input affects the running time. The algorithms that take this adaptability into account are called adaptive algorithms.

Eg → Bubble, Insertion, Quick → Adaptive.

7) Internal Sorting

→ Sorting algorithms that use main memory exclusively during the sort are called internal sorting algorithms.

Eg → Bubble, Insertion, Quick

8) External Sorting

→ Sorting algorithms that use external memory, during the sorting, come under this category.

→ They are comparatively slower than internal sorting algorithms.

Eg → Merge sort algorithm.

Q2) Performance of Sorting Algorithms

1) Worst Case Analysis (Usually Done)

- In the worst case analysis, we calculate the upper bound running of an algorithm. we must know the case that causes maximum number of operations to be executed.
- For linear search, the worst case happens when the element to be searched is not present in the array. when x is not present, the search function compares it with all elements of `arr[]` one by one.
∴ worst case complexity of linear search would be $O(n)$.

2) Average Case Analysis.

- In average case analysis, we take all possible inputs and calculate computing time for all of the inputs. Sum all the calculated values & divide the sum by total number of inputs. we must know the distribution of cases.

3) Best case Analysis.

- In the best-case analysis, we calculate lower bound on running time of an algorithm, we must know the case that causes min. no. of operations to be executed.
- In the linear search problem, the best case occurs when x is present at the first location. The no. of operations in the best case is constant. So, the time complexity in the best case would be $O(1)$.

- Mostly, we use worst case analysis - practical. Average case is not easy to determine and best case is bogus.