CIT Mid Question Solution | Session 2019-20

1) One hundred students were asked whether they had taken courses in any of the three areas, sociology, anthropology, and history. The results were:

48 had taken sociology

38 had taken anthropology

21 had taken history

18 had taken sociology and anthropology

9 had taken sociology and history

4 had taken history and anthropology

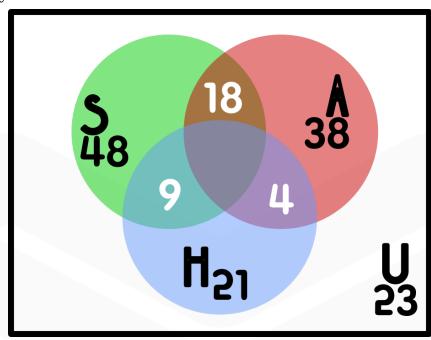
and 23 had taken no courses in any of the areas.

- (a) Draw a Venn diagram that will show the results of the survey.
- (b) Determine the number k of students who had taken classes in exactly
 - (I) one of the areas, and
 - (II) two of the areas.
- (a) Here is a Venn diagram showing the above data, Let,

S = sociology students

A = anthropology students

H = history students



(b) Students,

Here.

total students = 100

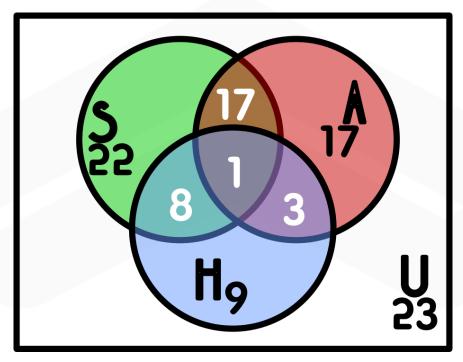
So, considering x as the students who have taken both 3 subjects,

$$48 + 21 + 38 - 18 - 9 - 4 + x = 100$$

or,
$$x = 1$$

students,

taken only sociology =
$$48 - (9 + 18 - 1) = 22$$
 taken only history = $21 - (9 + 4 - 1) = 9$ taken only anthropology = $38 - (4 + 18 - 1) = 17$



So, students taken one of these = 22 + 9 + 17 = 48And, students taken two of the areas = 8 + 3 + 17 = 28

Solution to this problems answer differs from place to place. For example, https://brainly.in/question/23019587, this website will tell you the answer, 42 and 31. Chat GPT will 45 and 31. But I followed a similar answer from the book "", page 16, chapter 1, problem 1.15 (set theory). Fell free to correct me!

2) What is proposition? Show that $(P \cap Q) \rightarrow (P \vee Q)$ is a tautology.

A proposition is a declarative sentence (that is, a sentence that declares a fact) that is either true or false, but not both (*source*, *Kenneth book*)

Let's consider a truth table for $(P \cap Q) \rightarrow (P \vee Q)$,

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P	Q	P^Q	P∨Q	$(P^{\wedge}Q) \to (P^{\vee}Q)$
T	T	Т	T	T
Т	F	F	Т	T
F	T	F	Т	T
F	F	F	F	Т

Here, for every possible values for P and Q variables, the result $(P \cap Q) \rightarrow (P \vee Q)$ is always true. So we can deduce it as a tautology.

3) Define Universal Quantification. Let Q(x) be the statement "x<2". What is the truth value of the quantification $\forall x Q(x)$, whose the domain consist of all real numbers?

Universal Quantification

In mathematical logic, a universal quantification is a type of quantifier, a logical constant which is interpreted as "given any", "for all", or "for any". It expresses that a predicate can be satisfied by every member of a domain of discourse.

Q(x) is not true for every real number x, because, for instance, Q(3) if false. That is, x = 3 is a counterexample for the statement $\forall x Q(x)$, Thus,

 $\forall x Q(x)$

is false.

source, kenneth book page 45