
BASIC BIT LEVEL

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Basic Bit

Properties

What is the result of $a \wedge 0s$?

a	00001101
0s	00000000
<hr/>	
$a \wedge 0s$	00001101

The result is a

What is the result of $a \wedge 1s$?

a	00001101
1s	11111111
<hr/>	
$a \wedge 1s$	11110010

The result is $\sim a$

What is the result of $a \wedge a$?

a	00001101
0s	00000000
<hr/>	
$a \wedge 0s$	00000000

The result is 0s

What is the result of $a \wedge 0s$?

a	00001101
0s	00000000
<hr/>	
$a \wedge 0s$	00000000

The result is 0s

What is the result of $a \wedge 1s$?

a	00001101
1s	11111111
<hr/>	
$a \wedge 1s$	00001101

The result is a

What is the result of $a \vee a$?

a	00001101
a	00001101
<hr/>	
$a \vee 1s$	00001101

The result is a

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What is the result of $a \wedge a$?

a	00001101
$\sim a$	11110010
$a \wedge \sim a$	11111111

The results is 1s

Perform bitwise negation without using the \sim operator?

$$a \wedge 1s = a \wedge \sim 0$$

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Manipulation

Implement this function to return a mask of all 0s except a single 1 in bit location i

The following shows how this works with i=3

idx	7654 3 210
1	00000001
1 << 3	0000 1 000

```
public static sbyte MaskOne(int i) => (sbyte)(1 << i);
```

Implement this function to return a mask of all 1s except a single 0 in bit location i

The following shows how this works with i=3

idx	7654 3 210
1	00000001
1 << 3	0000 1 000
~(1 << 3)	1111 0 111

```
public static sbyte MaskTwo(int i) => (sbyte)(~(1 << i));
```

Implement this function to return a mask of all ones except for zeros in the i least significant bits from 0 to (i-1)

The following shows how this works with i=3

idx	76543 2 10
~0	11111111
~0 << 3	11111 0 00

```
public static sbyte MaskThree(int n) => (sbyte)(~0 << n);
```

Implement this function to return a mask of all zeroes except for ones in the n least significant bits

The following shows how this works with i=3

idx	76543 2 10
1 << 3	00001000
(1 << 3)-1	00000 1 11

```
public static sbyte MaskFour(int n) => (sbyte)((1 << n)-1);
```

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Implement this function to return a mask of all 0s except for digits i through j which

The following shows how this works with i=3, j=6

idx	7 6543 210
(1 << 6-3+1)	00010000
(1 << 6-3+1)-1	00001111
<hr/>	<hr/>
((1 << 6-3)-1)<< 3	0 1111 000

```
public static sbyte MaskFive(int i, int j) =>
    (sbyte)((1 << j-i+1) - 1) << i);
```

Implement this function to return a mask of all 1s except for digits i through j which contain 0s.

The following shows how this works with i=3, j=6

idx	7 6543 210
(1 << 6-3+1)	00010000
(1 << 6-3+1)-1	00001111
((1 << 6-3)-1)<< 3	01111000
<hr/>	<hr/>
~(((1 << 6-3)-1)<< 3)	1 0000 111

```
public static sbyte MaskSix(int i, int j)
    => (sbyte)~(((1 << j - i+1) - 1) << i);
```

Implement integer subtraction without using the – key.

We make use of the properties of twos complement

$$a - b = a + (2^n - b) = a + (b + \sim b + 1 - b) = a + \sim b + 1$$

```
public static sbyte Subtract(sbyte a, sbyte b) =>
    (sbyte)(a + ~b + 1);
```

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Getting/Setting bits

Write a function that returns true or false, reflecting whether or not the bit at index i is 1 or 0 respectively

Consider the specific case where $n = 5$ and $i=2$

idx	76543210
n	00000101
n >> 2	00000001
1	00000001
(n >> 2) & 1	00000001
((n >> 2) & 1) > 0	true

```
public bool GetBit(int n, int i) => ((n >> i) & 1) > 0;
```

Write a function set the bit at index i to 1

```
public int SetBit(int n, int i) => (1 << i) | n;
```

Write a function set the bit at index i to 0

```
public int ClearBit(int n, int i) => ~(1 << i) & n;
```

Write a function that clears all bits from msb through to i inclusive

```
public int ClearFromMsbToI(int n, int i)
{
    return ((1 << i-1) - 1) & n;
}
```

Write a function that sets all bits from msb through to i inclusive

```
public int SetFromMsbToI(int n, int i)
{
    return (~0 << i) | n;
}
```

Write a function that clears all bits from 0 through to i inclusive

```
public int ClearFromLsbToI(int n, int i)
{
    return (~0 << i+1) & n;
}
```

Write a function that sets all bits from 0 through to i inclusive

```
public int SetFromLsbToI(int n, int i)
{
    return ((1 << i+1) - 1) | n;
}
```

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Bit Based Interview Questions

Right Shift Based

Write code to find the minimum of two signed integers. You may not use Math.min or branching constructs.

Consider the case where we have two signed 8 bit integers a and b. If we take their difference (a-b) then the result can be classified as

- ◆ 0xxxxxxxx If $a \geq b$
- ◆ 1xxxxxxxx If $a < b$

If we perform a right arithmetic shift of 7 bits (size of the int -1) we get either

- ◆ 00000000 If $a \geq b$
- ◆ 11111111 If $a < b$

Now if we & the result of this shift with the original difference. $((a-b) \gg 7) \& a-b$

- ◆ 0 If $a \geq b$
- ◆ a-b If $a < b$

Now we add in b

- ◆ $0+b=b$ If $a \geq b$
- ◆ $a-b+b=a$ If $a < b$

So we have returned b if $a \geq b$ and a if $a < b$ which was the original aim

```
public sbyte Min(sbyte a, sbyte b)
{
    // Take the difference a-b. The result is one of two forms
    // a) 0xxxxxxxx if a >= b
    // b) 1xxxxxxxx if a < b
    sbyte difference = (sbyte) (a-b);

    // The result of the right shift is then one of two things
    // a) 00000000 if a >= b
    // b) 11111111 if a < b
    sbyte mask = (sbyte) (difference >> (sizeof(sbyte)*8-1));

    // Now if we & the mask and (a-b) we get one of two things
    // a) 00000000 if a >= b
    // b) a-b      if a < b
    sbyte temp = (sbyte) (mask & difference);

    // If we add b to this temp variable we get one of two things which
    // is what we wanted
    // a) 0+b=b      if a >= b
    // b) a-b+b=a    if a < b
    return (sbyte) (temp + b);
}
```

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Write code to find the maximum of two signed integers. You may not use Math.min or branching constructs.

This is the same as the previous code except for we take the complement of the shift.

```
public sbyte Max(sbyte a, sbyte b)
{
    // Take the difference a-b. The result is one of two forms
    // a) 0xxxxxxx if a >= b
    // b) 1xxxxxxx if a < b
    sbyte difference = (sbyte)(a-b);

    // The result of the complemented right shift is
    // then one of two things
    // a) 11111111 if a >= b
    // b) 00000000 if a < b
    sbyte mask = (sbyte)~(difference >> (sizeof(sbyte)*8-1));

    // Now if we & the mask and (a-b) we get one of two things
    // a) a-b      if a >= b
    // b) 0        if a < b
    sbyte temp = (sbyte)(mask & difference);

    // If we add b to this temp variable we get one of two things which
    // is what we wanted
    // a) a-b+b=a   if a >= b
    // b) 0+b=b     if a < b
    sbyte result = (sbyte)(temp + b);
    return result;
}
```


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Write code to find the absolute value of an integer without branching.

We first use our old shift right routine to form a mask. If x is positive the mask is 0s and if x is negative the mask is all 1s.

```
x=5          00000101
mask = x>>7   00000000

x=-5         11111011
mask = x>>7   11111111
```

Now if we xor the mask with x we get one of two things. If the mask is 0s then the result is just x . If the mask is negative the result is $\sim x$ because xor with 1s is the same as the complement operator.

```
x=5          00000101
mask = x>>7   00000000
mask ^ x      00000101

x=-5         11111011
mask = x>>7   11111111
mask ^ x      00000100
```

The final trick is to subtract the mask from the result of the xor. If the mask is zero then the subtraction has no effect and we return x . If the mask is 1s this represents -1 in 2s complement. In the negative case we have $x \wedge 1s$ -1 which is the same as positive x .

```
x=5          00000101
mask = x>>7   00000000
mask ^ x      00000101
(mask ^ x) - mask  00000101

x=-5         11111011
mask = x>>7   11111111
mask ^ x      00000100
(mask ^ x) - mask  00000101
```

The code is then

```
public sbyte AbsoluteValue(sbyte x)
{
    sbyte mask = (sbyte) (x >> 7);
    return (sbyte) ((mask ^ x) - mask);
}
```

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Write code to calculate the sign of an integer?

```
public sbyte GetSign(sbyte a)
    => (sbyte) (a >> ((sizeof(sbyte) * 8) - 1));

public sbyte GetSign2(sbyte a) =>
    (sbyte) (1 | (a >> ((sizeof(sbyte) * 8) - 1)));
```

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Most Significant set bit based

Write a function to check if a given unsigned integer is a power of 2

We make use of the fact the binary representation of any power of 2 is a single 1 followed by all zeros

$2^0 = 1$	00000001
$2^1 = 2$	00000010
$2^2 = 4$	00000100

Secondly we note that subtractive 1 from such a representation flips the single 1 to zero and changes all zeros following it to 1s

$2^0 - 1$	00000000
$2^1 - 1 = 1$	00000001
$2^2 - 1 = 3$	00000011

Finally we use the fact that anding the two forms gives a result of zero.]

2^0	00000001
$2^0 - 1$	00000000
$2^0 \wedge (2^0 - 1)$	00000000

2^1	00000010
$2^1 - 1$	00000001
$2^1 \wedge (2^1 - 1)$	00000000

2^2	00000100
$2^2 - 1$	00000011
$2^2 \wedge (2^2 - 1)$	00000000

The code is given as follows. Note the special case for zero which is not a power of 2

```
public bool IsPowerOfTwo(uint a)
{
    return (a != 0) && (a & (a-1)) == 0;
}
```

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Write a function to calculate the number of 1s in an integers binary representation

We can use a simple linear traversal of the integers bits counting the 1s as we go. Such as algorithm is constant time and always takes $O(\text{sizeof(int)}*8)$.

```
public int BitCount(int a)
{
    int numBits = sizeof(int) * 8;
    int bitCount = 0;

    for (int i=0; i < numBits;i++)
    {
        if ((a >> i) & 1) > 0)
            bitCount++;
    }

    return bitCount;
}
```

But actually we can do better. The following describes a clever algorithm invented by Brian Kernigan. It key idea is that if we subtract 1 from any integer then the result is that ever bit from the lsb up to a and including the least significant 1 is flipped. If we then perform an & operation we are effectively removing the least significant 1.

5	00000101
5 - 1	<u>00000100</u>
$5 \wedge (5 - 1)$	00000100

2^1	00011100
$2^1 - 1$	<u>00000001</u>
$2^1 \wedge (2^1 - 1)$	00000000

2^2	00000100
$2^2 - 1$	<u>00000011</u>
$2^2 \wedge (2^2 - 1)$	00000000

but we can go better and use Brian Kernigans algorithm. This makes use of the fact that when we subtract 1 from an integer the rightmost 1 bit and all bits following the rightmost bits are flipped. If we hence subtract 1 from a number and and the result we effectively remove the rightmost bit. If we keep doing this until the number becomes zero we count the number of 1s

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Given two integers find the number of bits you would need to change to modify x to be y?

Miscellaneous

Given a decimal fraction such as 0.46 return a string representating its binary. If the number cannot be reprinted exactly in binary in n bits throw an exception

```
private string ConvertIntegralPart(double b, int maxDigits)
{
    StringBuilder result = new StringBuilder("0.");
    if (b >= 1.0) throw new ArgumentException("Input must be a fraction");

    double frac = 0.5;

    while (b >= 0 && maxDigits-- > 0)
    {
        if (b >= frac)
        {
            result.Append("1");
            b -= frac;
        }
        else
        {
            result.Append("0");
        }

        frac /= 2;
    }

    return result.ToString();
}
```

Risk and Pricing Solutions

Given an integer find the next largest integer that has the same number of 1s in its binary representation.

```
public byte NextLargestSame1Count(byte x)
{
    int onesCount = 0;

    for (int i = 0; i < sizeof(byte) * 8; i++)
    {
        // We have found the first non-trailing zero
        if (((x >> i) & 1) == 0)
        {
            if (onesCount > 0)
            {
                // Flip first non-trailing zero to 1
                x |= (byte)(1 << i);

                // Zero locations right of flipped digit
                x &= (byte)(~1 << (i-1));

                // add back in onesCount-1 1s in lsb locations
                x |= (byte)((1 << onesCount-1)-1);

                break;
            }
        }
        else
        {
            onesCount++;
        }
    }
    return x;
}
```

Risk and Pricing Solutions

Given an integer find the next smallest integer that has the same number of 1s in its binary representation.

The key idea is that we need to swap a set bit with an unset bit. If the bit we unset is to the left (more significant) than the bit we set we have decreased the number. Consider the specific input of 62. The first step is to find the 1 that we will flip to a zero. In order to be valid the 1 bit must have a 0 bit to the right of it (less significant) We are hence looking for the first non-trailing 1. We walk from least significant bits to most significant counting zeroes on the way and stopping when we reach the first non trailing 1.

idx	76543210
x ₀	01001111
i	6

The index of the non-trailing 1 is $i = 6$, the number of zeroes is $iz = 2$ and the number of ones is $io + 1 - iz = 5$ In order to unset the first non-trailing 1 which is at index 6 we create a mask $mask1 = \sim(1 \ll i)$

idx	76543210
x ₀	01001111
mask1	10111111
x ₁ = x ₀ & mask1	00001111

Rather than look for a single bit to set to the right of i, we instead clear all bits to the right of i and insert $io - 1$ ones immediately to the right of i. First we create a mask for the zeroing $mask2 = \sim 0 \ll i$

idx	76543210
x ₁	00001111
mask2	11000000
x ₂ = x ₁ & mask2	00000000

Now we put the $io - 1$ ones immediately to the right of i. Our mask is

$$mask3 = ((1 \ll (i - 1)) - 1) \ll (i - io)$$

idx	76543210
x ₂	00000000
mask3	00111110
x ₃ = x ₂ mask3	00111110

The source code is then

Risk and Pricing Solutions

```
public byte NextSmallestSame1Count(byte x)
{
    Console.WriteLine($"{x} {Convert.ToString(x, 2).PadLeft(8, '0')}");

    int zeroCount = 0;

    for (int i = 0; i < sizeof(byte) * 8; i++)
    {
        if (((x >> i) & 1) != 0)
        {
            // If this condition is true the bit at the
            // current index is set and there exists
            // unset bits to the right of it.
            // We can do a switch
            if (zeroCount > 0)
            {
                // 1. Unset the bit at the current index.
                // To do this we form a mask of all 1s
                // except at index i where it has a zero.
                // The mask is anded with x to unset bit i
                byte mask1 = (byte)~(1 << i);
                x &= mask1;

                // 2. The index of the unset bit is i. We want to
                // clear all bits to the right of i. That is
                // we want to clear bits 0 through i-1 or
                // the leftmost i bits. We define a mask that
                // consists of i 0s in positions 0 through i-1
                // and the rest 1s. We and the mask with x to clear
                byte mask2 = (byte)(~0 << i);
                x &= mask2;

                // 4. We originally had (i+1-zeroCount) 1 digits.
                // We need to these back in location i-1
                // i-1-(i+1-zeroCount)
                int oneCount = i + 1 - zeroCount;
                byte mask3 = (byte)((1 << oneCount) - 1);

                // 5. Shift the mask into position
                mask3 = (byte)(mask3 << (i-oneCount));
                // 6. Apply the mask
                x |= mask3;
                break;
            }
        }
        else
        {
            zeroCount++;
        }
    }
    return x;
}
```


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Given an integer find the longest sequence of 1s you can form if you are allowed to flip one zero to a 1.

Risk and Pricing Solutions

Write code to swap the even and odd bits of a given integer

The first stage is to separate out the even and odd digits. We use masks . Consider the specific example

idx	76543210
x	10111101
mask odd (0xaa)	10101010
mask even (0x55)	01010101

We apply the masks

idx	76543210
x	10111101
mask _{odd}	10101010
x _{odd} = x & mask _{odd}	10101000
idx	76543210
x	10111101
mask _{even}	01010101
x _{even} = x & mask _{even}	00010101

We shift the odd bits into even positions and even bits into odd positions

idx	76543210
x _{even} = x _{even} <<< 1	00101010
x _{odd} = x _{odd} >>> 1	01010100
result = x _{even} x _{odd}	01111110

The code is then

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```
sbyte SwapEvenAndOdd(sbyte x)
{
    // 1. Define the masks
    sbyte oddMask = unchecked((sbyte)0xaa);
    sbyte evenMask = unchecked((sbyte)0b01010101);

    // 2. Separate out the even and odd bits
    sbyte xEven = (sbyte)(x & evenMask);
    sbyte xOdd = (sbyte)(x & oddMask);

    // 3. Move odd bits into even positions and
    //     even bits into odd bit. Notice the cast to int
    //     to compensate for C# having only arithmetic shift
    //     operators.
    xEven = (sbyte)(xEven << 1);
    xOdd = (sbyte)((byte)xOdd >> 1);
    return (sbyte)(xEven | xOdd);
}
```

Risk and Pricing Solutions

Integers

Write a function to add two signed bytes. Do not use the + operator?

```
public uint Add(uint a, uint b)
{
    uint carry = 0;
    uint result = 0;

    for (int bitIdx = 0; bitIdx < SizeInBits; bitIdx++)
    {
        // We deal in one binary digit at multiplicand time. By right
        // shifting multiplicand and bitIdx times we set the bit we want
        // into the least significant bit.
        uint aShifted = (a >> bitIdx);
        uint bShifted = (b >> bitIdx);

        // Now we make use of the fact that the number 1 has
        // in our unsigned representation consists of SizeInBits
        // zeros followed by multiplicand solitary one in the
        // least significant
        // position. We can hence take our shifted valued and logically
        // and them with 1 to ensure we only have the digit values in the
        // least significant locations remaining.
        uint aDigit = aShifted & 1;
        uint bDigit = bShifted & 1;

        // We have three binary digits that feed into the current digit
        // {the multiplicand digit, the multiplier digit and the carry}
        // If one or all three
        // of these are one then the digit will be one, otherwise it will be
        // zero.
        uint sumBit = (aDigit ^ bDigit) ^ carry;

        // We now shift the bit into its correct location and add it into
        // the result
        result = result | (sumBit << bitIdx);

        // Finally calculate the carry for the next digit
        carry = (aDigit & bDigit) | (aDigit & carry) | (bDigit & carry);
    }

    return result;
}
```

User your function to write unsigned subtraction?

Risk and Pricing Solutions

Write a function `Log(double x, double b)` that takes a double value and a double base and returns $\text{Log}_b x$. It should work for any valid real base.

We only have natural logarithm and logarithm base 10 in the mathematics package but we can make use of the following to calculate any base from the natural logarithm or the base 10 logarithm

$$\log_a x = \frac{\log_b x}{\log_b a}$$

Proof

Let $x = a^y$ and hence $\log_a x = y$

$$\log_b x = \log_b a^y$$

$$\log_b x = y \times \log_b a$$

$$\log_b x = \log_a x \times \log_b a$$

$$\log_a x = \frac{\log_b x}{\log_b a}$$

The C# source code is then given by

Logarithm any base

```
public double Log(double x, double b)
{
    return Math.Log(x) / Math.Log(b);
}
```

Risk and Pricing Solutions

Given an integer value calculate the number of digits d required to represent that integer in base b number system

A number n represented in a base b number system will consist of k digits if and only if $b^{k-1} \leq n < b^k$. In other words b^{k-1} is the smallest number that requires k digits. Based on these facts we can derive expressions that calculate the number of digits k required to represent n in base b .

Expression using the floor function

Taking logarithms our inequality becomes.

$$k - 1 \leq \log_b n < k.$$

From the properties of the floor function we know that $\lfloor x \rfloor = m \Leftrightarrow m \leq x < m + 1$ and hence in our case

$$\lfloor \log_b n \rfloor = k - 1$$

Expression using the ceiling function

We can achieve a similar result that uses the ceiling function by adding one to the inequality $b^{k-1} \leq n < b^k$. so we get

$$b^{k-1} < n + 1 \leq b^k \text{ and taking logarithms we get}$$

$$k - 1 < \log_b(n + 1) \leq k$$

From the properties of the ceiling function we know that $\lceil x \rceil = m \Leftrightarrow m - 1 < x \leq m$ and hence that

$$\lceil \log_b(n + 1) \rceil = k$$

Number of digits code

The following code uses the ceiling function approach. It requires a function that gives the logarithm of any base.

```
public double DigitsRequired(int x, int b)
    => Math.Ceiling(Log(x+1,b));

public double Log(double x, double b)
    => Math.Log(x) / Math.Log(b);
```

Risk and Pricing Solutions

Given a string representation of an integer N in base λ convert it to a string representation of an integer in base β . For example given the input “10” with $\lambda = 10$ and $\beta = 2$ it would return “1010”

Let $N = \pm(a_n\lambda^n + \dots + a_2\lambda^2 + a_1\lambda^1 + a_0\lambda^0)$ then we want to find the coefficients c_i such that

$$N = \pm(c_n\beta^n + \dots + c_2\beta^2 + c_1\beta^1 + c_0\beta^0)$$

We have a number N

$$N = (a_n a_{n-1} \dots a_2 a_1 a_0)_\lambda$$

That we want to convert to base β such that

$$N = (c_m c_{m-1} \dots c_2 c_1 c_0)_\beta$$

We can rewrite this as

$$N = c_0 + \beta(c_1 + \beta(c_2 + \dots + \beta(c_m)))_\beta$$

If we divide it by β then the remainder is clearly c_0 and the quotient is

$$c_1 + \beta(c_2 + \beta(c_3 + \dots + \beta(c_m)))_\beta$$

If we repeat this until the quotient is zero we can read off the value of c_0 to c_m giving us the required number in the new base $(c_m c_{m-1} \dots c_2 c_1 c_0)_\beta$

Integer change of base

```
private string ConvertIntegralPart(string input, int l, int b)
{
    var result = new StringBuilder();

    // Calculate the decimal equivalent
    var idx = 0;
    var d = input[idx].ToIntDigit();
    while(++idx < input.Length) d = (d * l) + input[idx].ToIntDigit();

    var quotient = d;
    do
    {
        var r = quotient % b;
        quotient = quotient / b;
        result.Append(r.ToChar());
    }
    while (quotient > 0);

    var chars = result.ToString().ToCharArray().Reverse().ToArray();
    return new string(chars);
}
```


Risk and Pricing Solutions

Given a string representation of a fraction N in base λ convert it to a string representation of a fraction in base β . For example given the input “0.75” with $\lambda = 10$ and $\beta = 2$ it would return “0.11”

Consider the situation where we have a fraction part $0 < x < 1$ in some base λ and we want to find the digits d_k in the representation

$$x = \sum_{k=1}^{\infty} d_k \beta^{-k} = (0.d_1 d_2 d_3 \dots)_{\beta}$$

We first note that

$$\beta x = (d_1.d_2 d_3 \dots)_{\beta}$$

So if we take our fractional part and multiply it by β then the resulting integral component is the d_1 we can similarly repeat the process to find the digits $d_2 \dots d_m$

Fractional change of base

```
private string ConvertFractionalPart(string input, int l, int b,
    int maxDigits=16)
{
    var fractionString = input.Split('.')[1];
    var result = new StringBuilder("0.");

    // Calculate the decimal Fraction
    double decimalFraction = 0.0;
    for (int i = 0; i < fractionString.Length; i++)
    {
        decimalFraction +=
            fractionString[i].ToIntDigit() * Math.Pow(l, -(i+1));
    }

    int digitIdx=0;
    while (decimalFraction > 0.0 && digitIdx++ < maxDigits)
    {
        decimalFraction = (decimalFraction * b);
        int digit = (int)decimalFraction;
        result.Append(digit.ToChar());

        decimalFraction -= digit;
    }

    return result.ToString();
}
```

Risk and Pricing Solutions

Write the simplest possible code to perform unsigned integer division?

Division is just repeated subtraction so we have

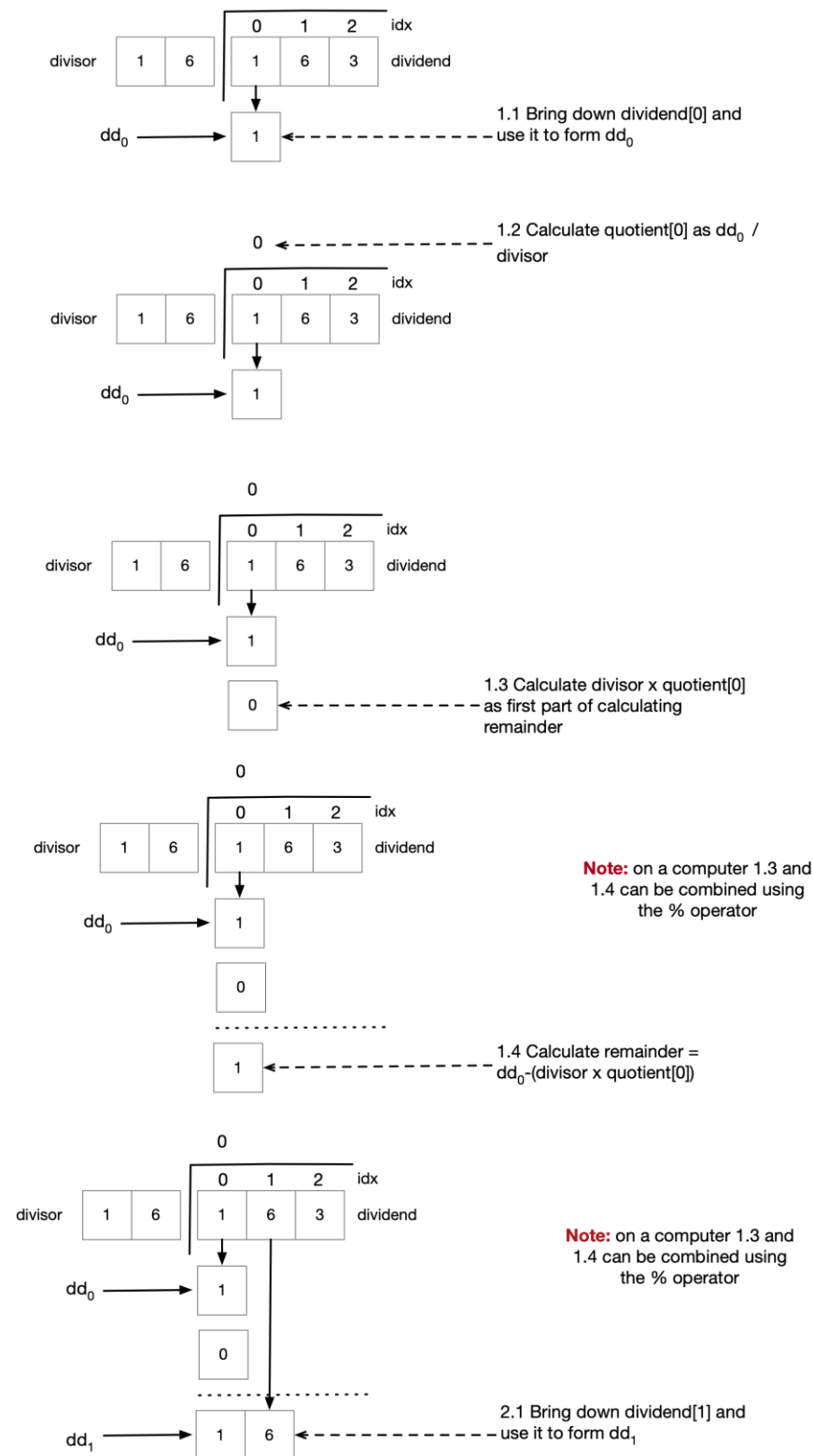
```
public (uint q, uint r) Divide(uint dividend, uint divisor)
{
    uint quotient = 0;
    uint remainder = dividend;

    while (divisor <= remainder)
    {
        remainder = remainder - divisor;
        quotient++;
    }

    return (quotient, remainder);
}
```

Risk and Pricing Solutions

Write code to perform integer division using a long division algorithm. The dividend is specified using a string. The base of the dividend and the divisor are given as simple ints?



Risk and Pricing Solutions

```
public (string quotient, string remainder) IntegerLongDivision(string
dividend, int divisor, int b = 10)
{
    StringBuilder quotient = new StringBuilder();
    int remainder = 0;
    int dd = 0;

    for (int idx = 0; idx < dividend.Length; idx++)
    {
        // idx.1 copy in next digit into temporary dividend dd
        dd = (dd * b) + dividend[idx].ToIntDigit();

        // idx.2 calculate partial quotient and set into quotient[idx]
        int partialQuotient = dd / divisor;
        quotient.Append(partialQuotient.ToChar());

        // idx.3 calculate this temporary as part of
        //calculating the remainder
        int temp = partialQuotient * divisor;

        // idx.4 Calculate the remainder
        remainder = dd % divisor;

        // the remainder will form the basis of dd[idx+1]
        dd = remainder;
    }

    return (quotient.ToString(), remainder.ToChar().ToString());
}

public static class Extensions
{
    public static int ToIntDigit(this char c)
    {
        if (char.IsNumber(c)) return (int)char.GetNumericValue(c);

        return char.ToLower(c) - 'a' + 10;
    }

    public static char ToChar(this int i)
    {
        if (i >= 0 && i < 10)
            return (char)(i + '0');

        return (char)(i + 'a' - 10);
    }
}
```

Risk and Pricing Solutions

Modify your answer from the previous section to return a floating point result rather than quotient and remainder?