

Algorithmics	Student information	Date	Number of session
	UO: 284185	1/3/2022	3
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## Activity 1. Tromino Times.

N	T TROMINO
4096	94
8192	341
16384	1295

These are the values I obtained from a reliable time until a heap overflow.

### 1. What should be the time complexity of the algorithm?

As the problem is solved by division (we divide the board in 4 quadrants), we must apply one of these formulas:

- $O(n^k)$                       if  $a < b^k$
- $O(n^k * \log n)$             if  $a = b^k$
- $O(n^{\log_b a})$                 if  $a > b^k$

$a = 4$  as we do four recursive calls. The number of sub problems (number of quadrants we divide the board) is 4.

$b = 2$  because each time we make a recursive call we divide by 2 the size of the board.

$k = 0$  because excluding recursive calls, the complexity of the method is  $O(1)$ .

Then, as  $4 > 2^0$  ( $a > b^k$ ), we have a complexity of  $O(n^{\log_2 4}) = O(n^2)$ .

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**2. Check if the time obtained in the previous section does or does not meet the theoretical complexity of the algorithm.**

According to the following results, we can conclude that the values obtained meet the theoretical complexity of the algorithm:

We know that  $t_2 = ( f(n_2) / f(n_1) ) \times t_1$ , being  $f(n) = n^2$

Taking this values:

$n_1 = 4096$     $t_1 = 94$

$n_2 = 8192$     $t_2 = 341$

$$t_2 = ( 8192^2 / 4096^2 ) \times 94 = 376 \approx 341$$

Taking this values:

$n_1 = 8192$     $t_1 = 341$

$n_2 = 16384$     $t_2 = 1295$

$$t_2 = ( 16384^2 / 8192^2 ) \times 341 = 1364 \approx 1295$$