

Assignment #3: Shrinkage and Data Reduction Methods

[Q1] The data file **mobilephone2_training.csv** is part of large European survey data for mobile phone customers. It includes the following variables:

1. dura24: the duration of remaining a customer in the past 24 months
2. age
3. Ssound: satisfaction with sound quality (1 - 10)
4. Sglob: satisfaction with overall network functioning (1 - 10)
5. Svmail: satisfaction with voicemail (1 - 10)
6. Sinfor: satisfaction with information (1 - 10)
7. Sprice: satisfaction on price (1 - 10)
8. Spromo: satisfaction on promotion (1 - 10)
9. Sadver: satisfaction with the advertisement (1 - 10)
10. Sperson: satisfaction with the salesperson (1 - 10)
11. Simage: satisfaction on company image (1 - 10)
12. Sglobal: global satisfaction (1 - 10)
13. Lintent: intention of loyalty (1 - 10)

Suppose that you are interested in predicting the duration of remaining a customer (dura24) using 12 predictors (variables 2 – 12).

- (1) Apply a series of ridge regression to the data, considering 100 candidate values of the tuning parameter λ within the interval $[10^{-5}, 1]$. Based on 10-fold cross validation, plot all MSE values against the candidate values of λ and choose the optimal λ value. Given the chosen λ value, re-run a ridge regression for the data and report its coefficient estimates. (2 points)
- (2) Apply a series of the lasso to the data, considering 100 candidate values of the tuning parameter λ within the interval $[10^{-5}, 1]$. Based on 10-fold cross validation, plot all MSE values against the candidate values of λ and choose the optimal λ value. Given the chosen λ value, re-run the lasso for the data and report its coefficient estimates. (2 points)
- (3) Apply a principal component regression to the data and choose the number of components that minimizes the cross-validated RMSE. Plot the RMSE values against the number of components. Also, describe how much variance of the predictors and the response the chosen number of components explain (2 points)
- (4) Apply a partial least squares regression to the data and choose the number of components that minimizes the cross-validated RMSE. Plot the RMSE values against the number of components. Also, describe how much variance of the predictors and the response the chosen number of components explain (2 points)

[Q2] Using the estimated solutions obtained from the above four methods, report their MSE values in the test sample (**mobilephone2_test.csv**) and conclude which method appears to perform best in terms of the test MSE values (2 points).