

BJT Small-Signal Analysis

Semiconductor Devices and Circuits

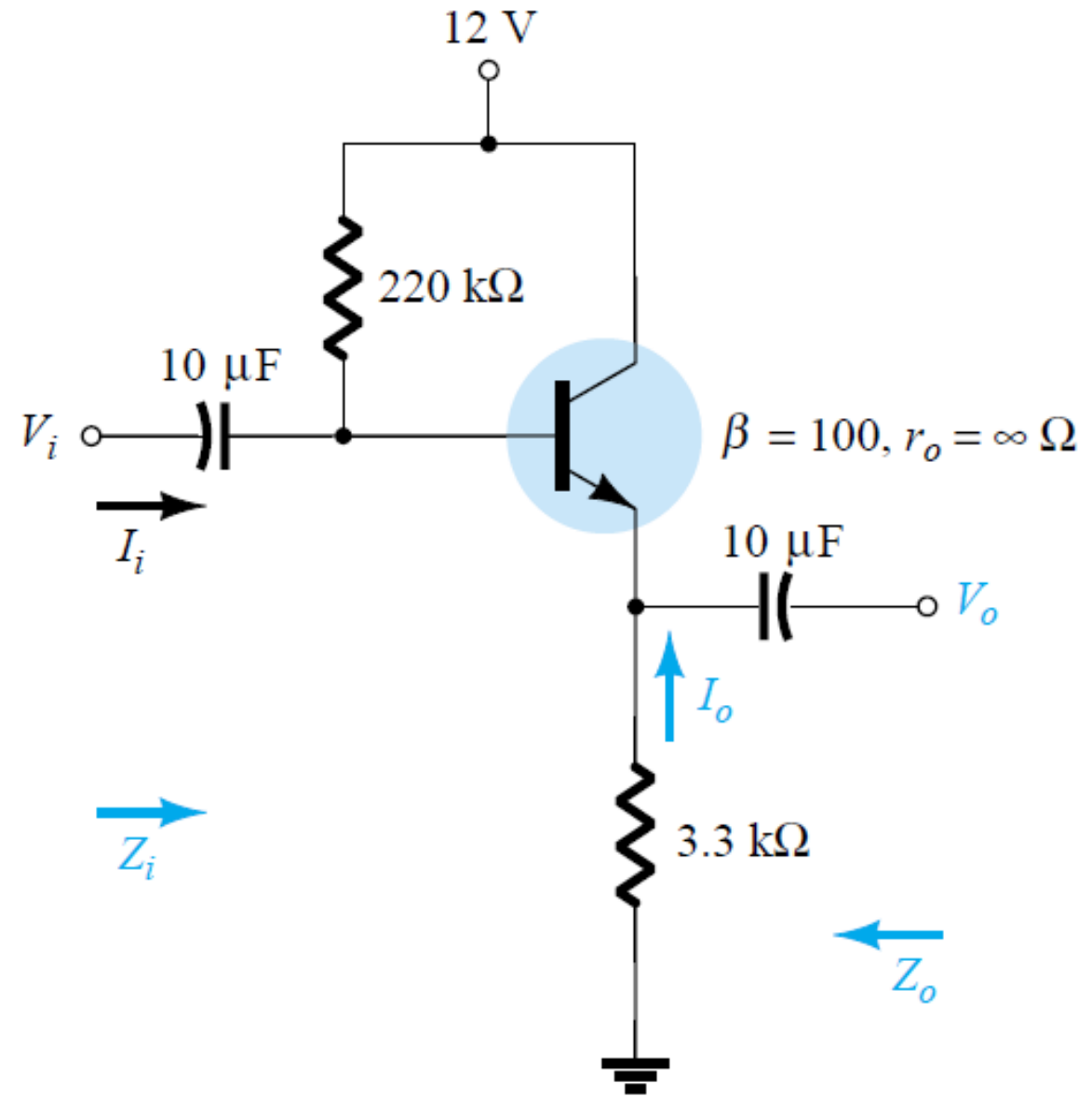
(ECE 181302)

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Example

- Determine:

- (a) r_e .
- (b) Z_i .
- (c) Z_o .
- (d) A_v .
- (e) A_i .



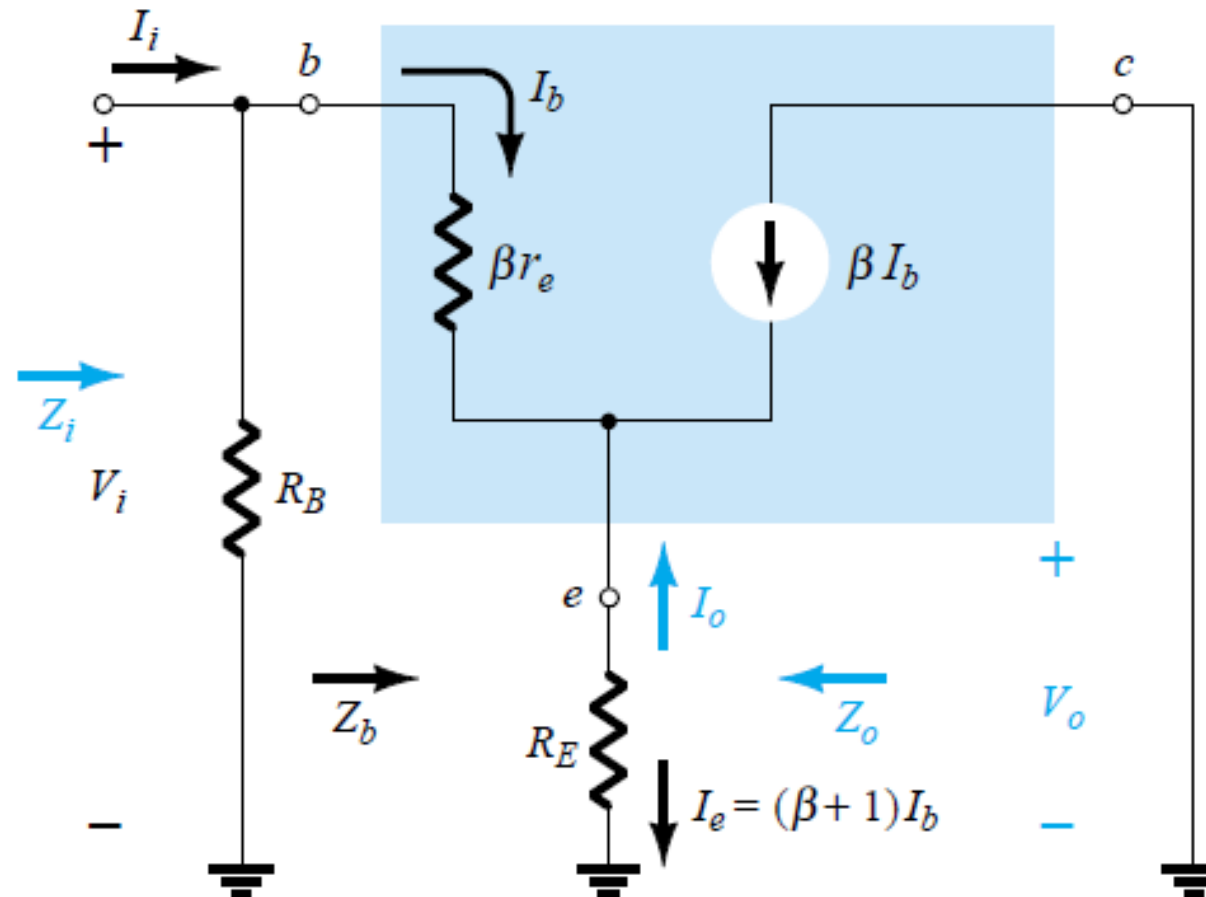
- To find r_e do the dc analysis:

$$\begin{aligned} \text{(a) } I_B &= \frac{V_{CC} - V_{BE}}{R_B + (\beta + 1)R_E} \\ &= \frac{12 \text{ V} - 0.7 \text{ V}}{220 \text{ k}\Omega + (101)3.3 \text{ k}\Omega} = 20.42 \text{ }\mu\text{A} \end{aligned}$$

$$\begin{aligned} I_E &= (\beta + 1)I_B \\ &= (101)(20.42 \text{ }\mu\text{A}) = 2.062 \text{ mA} \end{aligned}$$

$$r_e = \frac{26 \text{ mV}}{I_E} = \frac{26 \text{ mV}}{2.062 \text{ mA}} = \mathbf{12.61 \text{ }\Omega}$$

- Do the ac analysis:
- Substituting the r_e equivalent circuit into the ac equivalent network



- Applying Kirchhoff's voltage law to the input side:

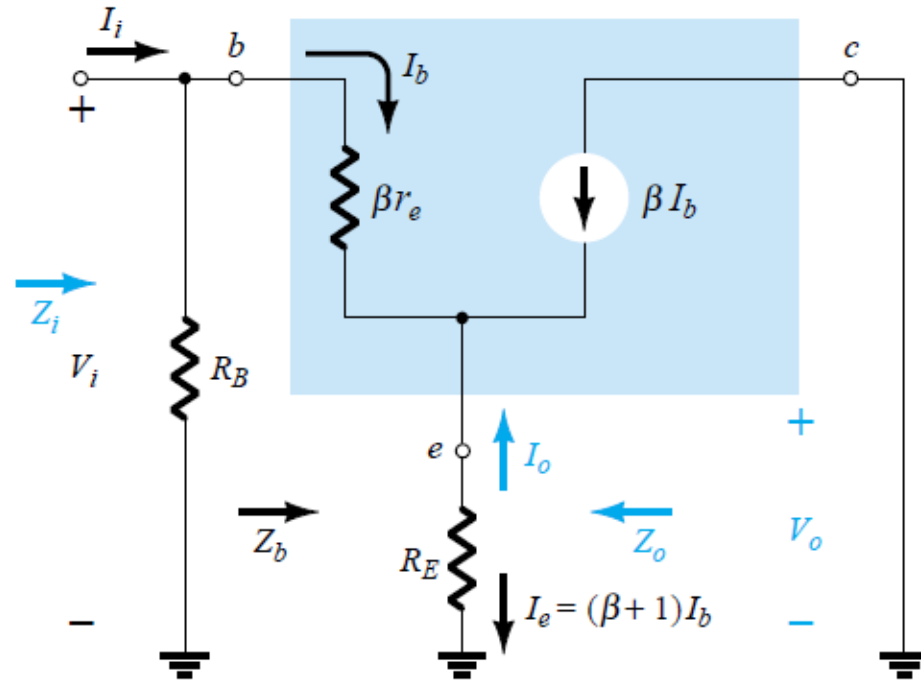
$$V_i = I_b \beta r_e + I_e R_E$$

or
$$V_i = I_b \beta r_e + (\beta + 1) I_b R_E$$

and the input impedance looking into the network to the right of R_B is

$$\begin{aligned} Z_b &= \frac{V_i}{I_b} = \beta r_e + (\beta + 1) R_E \\ &= (100)(12.61 \, \Omega) + (101)(3.3 \, \text{k}\Omega) \\ &= 1.261 \, \text{k}\Omega + 333.3 \, \text{k}\Omega \\ &= 334.56 \, \text{k}\Omega \cong \beta R_E \\ Z_i &= R_B \parallel Z_b = 220 \, \text{k}\Omega \parallel 334.56 \, \text{k}\Omega \\ &= \mathbf{132.72 \, \text{k}\Omega} \end{aligned}$$

- To find Z_o ;



$$I_b = \frac{V_i}{Z_b}$$

and

$$I_e = (\beta + 1)I_b = (\beta + 1) \frac{V_i}{Z_b}$$

Substituting for Z_b gives

$$I_e = \frac{(\beta + 1)V_i}{\beta r_e + (\beta + 1)R_E}$$

or

$$I_e = \frac{V_i}{[\beta r_e / (\beta + 1)] + R_E}$$

but

$$(\beta + 1) \cong \beta$$

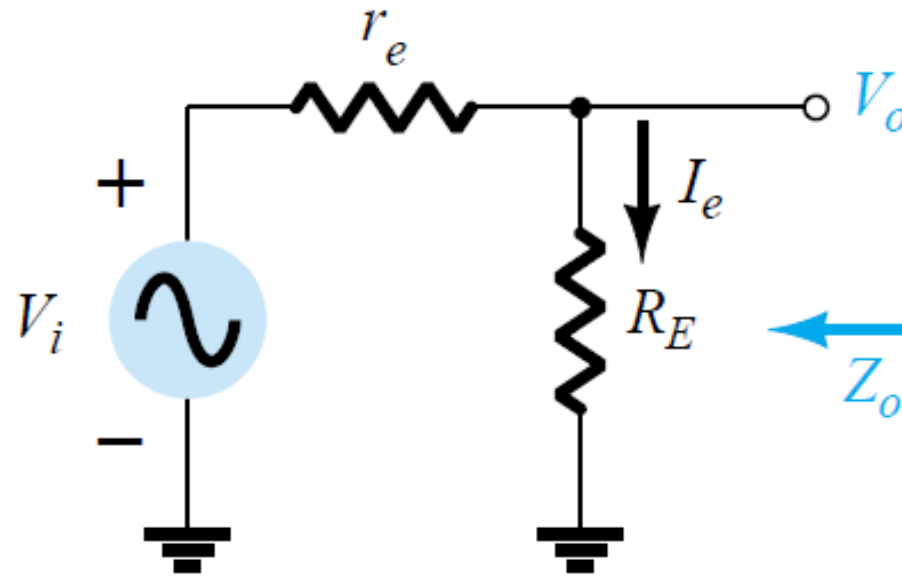
and

$$\frac{\beta r_e}{\beta + 1} \cong \frac{\beta r_e}{\beta} = r_e$$

so that

$$I_e \cong \frac{V_i}{r_e + R_E}$$

- To determine Z_o , V_i is set to zero:



$$Z_o = R_E \parallel r_e$$

$$\begin{aligned} \text{(c) } Z_o &= R_E \parallel r_e = 3.3 \text{ k}\Omega \parallel 12.61 \text{ }\Omega \\ &= \mathbf{12.56 \text{ }\Omega} \cong r_e \end{aligned}$$

- Voltage gain and current gain:

$$V_o = \frac{R_E V_i}{R_E + r_e}$$

$$A_v = \frac{V_o}{V_i} = \frac{R_E}{R_E + r_e}$$

$$\begin{aligned} \text{(d)} \quad A_v &= \frac{V_o}{V_i} = \frac{R_E}{R_E + r_e} = \frac{3.3 \text{ k}\Omega}{3.3 \text{ k}\Omega + 12.61 \text{ }\Omega} \\ &= \mathbf{0.996} \cong 1 \end{aligned}$$

- Current gain:

$$I_b = \frac{R_B I_i}{R_B + Z_b}$$

or
$$\frac{I_b}{I_i} = \frac{R_B}{R_B + Z_b}$$

and
$$I_o = -I_e = -(\beta + 1)I_b$$

or
$$\frac{I_o}{I_b} = -(\beta + 1)$$

so that
$$A_i = \frac{I_o}{I_i} = \frac{I_o}{I_b} \frac{I_b}{I_i}$$

$$= -(\beta + 1) \frac{R_B}{R_B + Z_b}$$

and since
$$(\beta + 1) \cong \beta,$$

$$A_i \cong -\frac{\beta R_B}{R_B + Z_b}$$

or

$$A_i = -A_v \frac{Z_i}{R_E}$$

$$(e) \quad A_i \cong -\frac{\beta R_B}{R_B + Z_b} = -\frac{(100)(220 \text{ k}\Omega)}{220 \text{ k}\Omega + 334.56 \text{ k}\Omega} = -39.67$$



References:

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