

CS-5340/6340, Written Assignment #2
DUE: Thursday, September 19, 2019 by 11:59pm
Submit your assignment on CANVAS in pdf format
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1. (20 pts) For each sentence below, indicate whether the main verb appears in an intransitive construction, a transitive construction, or a ditransitive construction. Only give the answer transitive if the usage is not ditransitive

(a) She solved the puzzle in two minutes.

Answer: transitive construction.

(b) Tom has read ten books by Stephen King.

Answer: ditransitive construction.

(c) Lee cooked Mary a steak for her birthday.

Answer: ditransitive construction.

(d) The boy dreamt about summer camp.

Answer: ditransitive construction

(e) The rabbit hopped up the stairs to its favorite room.

Answer: intransitive construction

(f) Jim sneezes often during allergy season.

Answer: intransitive construction.

(g) Susan lent her brother some money for his tuition.

Answer: ditransitive construction.

(h) Pat learned to ski by trial and error.

Answer: intransitive construction.

(i) A bird flew into the building.

Answer: intransitive construction.

(j) The reporter investigated the story thoroughly and carefully.

Answer: transitive construction.

2. (40 pts) Use the following tables of probabilities to answer this question. Note that these numbers are completely fictional and not necessarily realistic!

a) $P(\text{California} = \text{NOUN})$

$$\begin{aligned} \text{Answer: } & P(\text{California} \mid \text{NOUN}) * P(\text{NOUN} \mid \phi) \\ &= 0.04 * 0.75 \\ &= 0.03 \end{aligned}$$

b) $P(\text{California} = \text{VERB})$

$$\begin{aligned} \text{Answer: } & P(\text{California} \mid \text{VERB}) * P(\text{VERB} \mid \phi) \\ &= 0.008 * 0.25 \\ &= 0.002 \end{aligned}$$

c) $P(\text{seals} = \text{NOUN})$

$$\begin{aligned} \text{Answer : } & P(\text{seals} \mid \text{NOUN}) * \max(P(\text{NOUN} \mid \text{NOUN}) * \text{Score}(\text{NOUN}, \text{California}), \\ & P(\text{NOUN} \mid \text{VERB}) * \text{Score}(\text{VERB}, \text{California})) \\ &= 0.05 * \max(0.30 * 0.03, 0.55 * 0.002) \\ &= 0.05 * \max(0.009, 0.0011) \\ &= 0.05 * 0.009 \\ &= 4.5\text{E-}4 \end{aligned}$$

d) $P(\text{seals} = \text{VERB})$

$$\begin{aligned} \text{Answer: } & P(\text{seals} \mid \text{VERB}) * \max(P(\text{VERB} \mid \text{NOUN}) * \text{Score}(\text{NOUN}, \text{California}), P(\text{VERB} \\ & \mid \text{VERB}) * \text{Score}(\text{VERB}, \text{California})) \\ &= 0.02 * \max(0.015, 0.0007) \\ &= 0.02 * 0.015 \\ &= 0.0003 \end{aligned}$$

Using the same network, compute the forward probabilities α word (tag) indicated below. You should assume that $w_0 = \phi$, $w_1 = \text{California}$, $w_2 = \text{seals}$, $w_3 = \text{report}$, and $w_4 = \Omega$. Show all your work!

e) $\alpha w_1(\text{NOUN})$

Answer: $P(\text{California} \mid \text{NOUN}) * P(\text{NOUN} \mid \phi)$
 $= 0.04 * 0.75$
 $= 0.03$

f) $\alpha w_1(\text{VERB})$

Answer: $P(\text{California} \mid \text{VERB}) * P(\text{VERB} \mid \phi)$
 $= 0.008 * 0.25$
 $= 0.002$

g) $\alpha w_2(\text{NOUN})$

Answer: $\alpha w_1(N) * P(N \mid N) * P(\text{seals} \mid N) + \alpha w_1(V) * P(N \mid V) * P(\text{seals} \mid N)$
 $= 0.03 * 0.30 * 0.05 + 0.002 * 0.55 * 0.05$
 $= 5.05E-4$

h) $\alpha w_2(\text{VERB})$

Answer: $\alpha w_1(N) * P(V \mid N) * P(\text{seals} \mid V) + \alpha w_1(V) * P(V \mid V) * P(\text{seals} \mid V)$
 $= 0.03 * 0.50 * 0.02 + 0.002 * 0.35 * 0.02$
 $= 3.55E-4$

Using the previous forward probabilities, normalize them to estimate $O(o_i/t_k \mid o_0 \dots o_i)$ for the following cases. Show all your work!

i) $P(w_2/\text{NOUN} \mid w_0 \dots w_2)$

Answer : $\alpha w_2(\text{NOUN}) / \alpha w_2(\text{NOUN}) + \alpha w_2(\text{VERB})$
 $= 5.05E-4 / (5.05E-4 + 3.55E-4)$
 $= 0.5872$

j) $P(w_2/\text{VERB} \mid w_0 \dots w_2)$

Answer: $\alpha w_2(\text{VERB}) / \alpha w_2(\text{NOUN}) + \alpha w_2(\text{VERB})$
 $= 3.55E-4 / (5.05E-4 + 3.55E-4)$
 $= 0.4128$

Using the same network, compute the backward probabilities α word (tag) indicated below. You should assume that $w_0 = \phi$, $w_1 = \text{California}$, $w_2 = \text{seals}$, $w_3 = \text{report}$, and $w_4 = \Omega$. Show all your work!

k) $\beta w_3(\text{NOUN})$

$$\begin{aligned}\textbf{Answer: } & P(\text{report} \mid N) * P(\Omega \mid N) \\ & = 0.07 * 0.20 \\ & = 0.014\end{aligned}$$

l) $\beta w_3(\text{VERB})$

$$\begin{aligned}\textbf{Answer: } & P(\text{report} \mid V) * P(\Omega \mid V) \\ & = 0.06 * 0.10 \\ & = 0.006\end{aligned}$$

m) $\beta w_2(\text{NOUN})$

$$\begin{aligned}\textbf{Answer: } & \beta w_3(N) * P(N \mid N) * P(\text{seals} \mid N) + \beta w_3(V) * P(N \mid V) * P(\text{seals} \mid N) \\ & = 0.014 * 0.30 * 0.05 + 0.006 * 0.55 * 0.05 \\ & = 3.75\text{E-}4\end{aligned}$$

n) $\beta w_2(\text{VERB})$

$$\begin{aligned}\textbf{Answer: } & \beta w_3(N) * P(V \mid N) * P(\text{seals} \mid V) + \beta w_3(V) * P(V \mid V) * P(\text{seals} \mid V) \\ & = 0.014 * 0.50 * 0.02 + 0.006 * 0.35 * 0.02 \\ & = 1.82\text{E-}4\end{aligned}$$

Using the previous forward probabilities, normalize them to estimate $O(o_i/t_k \mid o_0 \dots o_i)$ for the following cases. Show all your work!

o) $P(w_2/\text{NOUN} \mid w_2 \dots w_4)$

$$\begin{aligned}\textbf{Answer: } & \beta w_2(\text{NOUN}) / \beta w_2(\text{NOUN}) + \beta w_2(\text{VERB}) \\ & = 3.75\text{E-}4 / (3.75\text{E-}4 + 1.82\text{E-}4) \\ & = 0.6732\end{aligned}$$

p) $P(w_2/\text{VERB} \mid w_2 \dots w_4)$

$$\begin{aligned}\textbf{Answer: } & \beta w_2(\text{VERB}) / \beta w_2(\text{NOUN}) + \beta w_2(\text{VERB}) \\ & = 1.82\text{E-}4 / (3.75\text{E-}4 + 1.82\text{E-}4) \\ & = 0.3267\end{aligned}$$

Using the previous forward and backward probabilities, normalize them together to estimate $P(o_i/t_k \mid o_0 \dots o_i)$ for the following cases. Show all your work!

q) $P(w_2/\text{NOUN} \mid w_0 \dots w_4)$

Answer: $(\alpha w_2(\text{NOUN}) * \beta w_2(\text{NOUN})) / (\alpha w_2(\text{NOUN}) * \beta w_2(\text{NOUN}) + (\alpha w_2(\text{VERB}) * \beta w_2(\text{VERB})))$
 $= (5.05\text{E-}4 * 3.75\text{E-}4) / (5.05\text{E-}4 * 3.75\text{E-}4 + (3.55\text{E-}4 * 1.82\text{E-}4))$
 $= 1.0000$

r) $P(w_2/\text{VERB} \mid w_0 \dots w_4)$

Answer: $(\alpha w_2(\text{VERB}) * \beta w_2(\text{VERB})) / (\alpha w_2(\text{NOUN}) * \beta w_2(\text{NOUN}) + (\alpha w_2(\text{VERB}) * \beta w_2(\text{VERB})))$
 $= (3.55\text{E-}4 * 1.82\text{E-}4) / (5.05\text{E-}4 * 3.75\text{E-}4 + (3.55\text{E-}4 * 1.82\text{E-}4))$
 $= 1.0000$

3) Consider the following four Verb Phrase (VP) grammars:

Answers:

- a) adv = NONE
- b) verb = G1
- c) verb verb = NONE
- d) adv verb adv = G1, G2, G3
- e) adv adv adv verb = G1, G2
- f) verb adv adv adv = G1, G3, G4
- g) adv adv verb adv verb: NONE
- h) adv adv verb adv adv adv = G1, G2, G3, G4

4.

a)

Grammar Rules without frequency:

Parse tree A

$S \rightarrow NP VP$

NP -> noun
VP -> verb NP1 NP2 PP
NP1 -> noun
NP2 -> art noun
PP -> prev NP3
NP3 -> noun

Parse tree B

S -> NP VP
NP -> noun
VP -> verb NP1 NP2
NP1 -> noun
NP2 -> art noun PP
PP -> prep NP3
NP3 -> noun

Parse tree C

S -> NP VP
NP -> noun
VP -> verb NP1 PP
NP1 -> art noun
PP -> prep NP2
NP2 -> noun

Parse tree D

S -> NP VP
NP -> noun
VP -> verb NP1 PP
NP1 -> art noun
PP -> prep NP2
NP2 -> noun

Grammar Rules

S -> NP VP
NP -> noun
VP -> verb NP1 NP2 PP
NP1 -> noun
NP2 -> art noun
PP -> prep NP3

Total Frequency

- 4 times
- 4 times
- 1 time
- 2 times
- 1 time
- 2 times

NP3 -> noun	- 2 times
VP -> verb NP1 NP2	- 1 time
NP2 -> art noun PP	- 1 time
VP -> verb NP1 PP	- 2 times
NP1 -> art noun	- 2 times
PP -> prep NP2	- 2 times
NP2 -> noun	- 2 times

b)

Answer:

i. John bought a car with cash **on Friday**,

Answer : VP

ii. John bought a car with cash **with his brother**

Answer: NP3

iii. John bought a car with cash **from his savings account**

Answer: NP3

iv. John bought a car with cash **with excitement**

Answer: NP1