

Q2 1

Bayes Theorem

$$P(A/B) = \frac{P(B/A) \cdot P(A)}{P(B)}$$

So, classification prob. given by

$$P(C_i/x) = \frac{P(x/C_i) P(C_i)}{P(x)}$$

$$= \frac{P(x/C_i) P(C_i)}{\sum_{j=1}^J P(x/C_j) P(C_j)}$$

for using Gaussian likelihood (Gaussian (Normal) Distribution)

$$P(x/C_i) = \frac{1}{\sqrt{2\pi} \sigma_i} e^{-\frac{1}{2} \left( \frac{x - \mu_i}{\sigma_i} \right)^2}$$

$$\hat{\mu}_i = \frac{1}{N_i} \sum_{k=1}^N x_k \quad ; \quad \hat{\sigma}_i^2 = \frac{1}{N_i} \sum_{k=1}^N (x_k - \mu_i)^2$$

$$P(C_j) = \frac{N_j}{\sum_{k=1}^N N_k} \quad \left( \frac{0.5 + 0.1 + 0.2 + 0.4 + 0.3 + 0.2 + 0.2 + 0.1 + 0.35 + 0.25}{10} \right)$$

$$\hat{\mu}_1 = 0.26 \quad , \quad \hat{\mu}_2 = 0.8625 \quad \left( \frac{0.9 + 0.8 + 0.75 + 1.0}{4} \right)$$

$$\hat{\sigma}_1^2 = 0.0149 \quad \hat{\sigma}_2^2 = 0.0092$$

$$P(C_1) = 0.714 \quad P(C_2) = 0.28$$

$$P(C_1/0.6) = 0.6305$$

$$\text{MLE of class } p_1 = \frac{\# \text{ occurrence of } p_1}{\text{Total } \# \text{ of occurrence of } p_1 \text{ \& } p_2} = \frac{10}{14}$$

$$\text{MLE of class } p_2 = \cancel{\# \text{ of } p_2} - \text{MLE of } p_1 = 1 - \frac{10}{14}$$

$$= \frac{4}{14}$$

Q 2 (b)

$X = (\text{goal, football, golf, defence, offence, wicket, office, Strategy})$

$$x_{\text{politics}} = \begin{bmatrix} 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 0 & 0 & 1 & 1 \\ 1 & 0 & 0 & 1 & 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 & 1 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 1 & 0 & 0 & 1 \end{bmatrix} \left[ \begin{array}{l} P(\frac{\text{goal}}{\text{Politics}}) = 2/6 \\ P(\frac{\text{football}}{\text{Politics}}) = 1/6 \\ P(\frac{\text{golf}}{\text{Politics}}) = 1/6 \\ P(\frac{\text{defence}}{\text{Politics}}) = 5/6 \\ P(\frac{\text{offence}}{\text{Politics}}) = 5/6 \\ P(\frac{\text{wicket}}{\text{Politics}}) = 1/6 \\ P(\frac{\text{office}}{\text{Politics}}) = 4/6 = 2/3 \\ P(\frac{\text{Strategy}}{\text{Politics}}) = 5/6 \end{array} \right]$$

$$x_{\text{Sport}} = \begin{bmatrix} 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 \end{bmatrix} \left[ \begin{array}{l} P(\text{goal}) = 4/6 \\ P(\text{football}) = 4/6 \\ P(\text{golf}) = 1/6 \\ P(\text{defence}) = 4/6 \\ P(\text{offence}) = 1/6 \\ P(\text{wicket}) = 1/6 \\ P(\text{office}) = 0 \\ P(\text{Strategy}) = 1/6 \end{array} \right]$$

$$X = [1 \ 0 \ 0 \ 1 \ 1 \ 1 \ 0]$$

$$P(a/b) = \frac{P(b/a) P(a)}{P(b)}$$

$$P(X/\text{politics}) = \frac{\frac{1}{2} \left( \frac{2}{6} \times \frac{5}{6} \times \frac{5}{6} \times \frac{5}{6} \times \frac{5}{6} \times \frac{1}{6} \times \frac{4}{6} \times \frac{1}{6} \right) + \frac{1}{2} \left( \frac{4}{6} \times \frac{2}{6} \times \frac{5}{6} \times \frac{4}{6} \times \frac{1}{6} \times \frac{1}{6} \right)}{\frac{1}{2} \left( \frac{2}{6} \times \frac{5}{6} \times \frac{5}{6} \times \frac{5}{6} \times \frac{1}{6} \times \frac{4}{6} \times \frac{1}{6} \right) + \frac{1}{2} \left( \frac{4}{6} \times \frac{2}{6} \times \frac{5}{6} \times \frac{4}{6} \times \frac{1}{6} \times \frac{1}{6} \right)} \times \frac{1}{6}$$

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$$P(x/\text{politics}) = 2$$