

Ques 3 $\{x_1 = [1, 1]^T \text{ and } y_1 = 1\}$ and $\{x_2 = [1, -1]^T, y_2 = -1\}$

perception error f^0 $e = (\hat{y} - y)^2$ $\hat{y} = \text{predicted value}$
 $= \omega^T x$

for point x_1 ; $x_1 = 1$
 $x_2 = 1$ then $\hat{y} = \omega_1 + \omega_2 = \omega_1 x_1 + \omega_2 x_2$

$$\begin{aligned} \text{then } e_1 &= (\omega_1 + \omega_2 - 1)^2 \\ &= \omega_1^2 + (\omega_2 - 1)^2 + 2(\omega_1)(\omega_2 - 1) \\ &= \omega_1^2 + \omega_2^2 + 1 + 2\omega_1\omega_2 - 2\omega_1 - 2\omega_2 \end{aligned}$$

for point x_2
 $x_1 = 1$

$$\begin{aligned} x_2 &= -1 \quad \text{then } \hat{y} = \omega_1 - \omega_2 \\ e_2 &= (\omega_1 - \omega_2 + 1)^2 = (\omega_1 - (\omega_2 - 1))^2 \\ &= \omega_1^2 + (\omega_2 - 1)^2 - 2(\omega_1)(\omega_2 - 1) \\ &= \omega_1^2 + \omega_2^2 + 1 - 2\omega_2 - 2\omega_1\omega_2 + 2\omega_1 \end{aligned}$$

mean error f^n

$$f(\omega_1, \omega_2) = \frac{e_1 + e_2}{2}$$

$$f(\omega_1, \omega_2) = \omega_1^2 + \omega_2^2 + 1 - 2\omega_2$$

- 1) surface will be look like convex / bowl parabol
3 D (facing upward) & its local/global
minima will be on first quadrant

i) along with ω_1 & ω_2 it will form hyperbola in $f(z)$ direction

ii) center point Minima point $z = (0, 1)$
 ie $[\omega_1 = 0]$
 $\omega_2 = 1$

b) Given error f^p

$$e = (y - \hat{y})^2$$

$$= (\omega_1 + \omega_2 - 1)^2 = \omega_1^2 + \omega_2^2 + 1 + 2\omega_1\omega_2 - 2\omega_1 - 2\omega_2$$

then
$$H = \begin{bmatrix} \frac{\partial^2 e}{\partial \omega_1^2} & \frac{\partial^2 e}{\partial \omega_1 \partial \omega_2} \\ \frac{\partial^2 e}{\partial \omega_2 \partial \omega_1} & \frac{\partial^2 e}{\partial \omega_2^2} \end{bmatrix}$$

$$\frac{\partial e}{\partial \omega_1} = 2\omega_1 + 2\omega_2 - 2 \quad \left| \begin{array}{l} \frac{\partial e}{\partial \omega_1} = 2\omega_1 + 2\omega_2 - 2 \\ \frac{\partial^2 e}{\partial \omega_2} = 0 \end{array} \right.$$

$$\frac{\partial^2 e}{\partial \omega_1^2} = 2 + 2 = 4$$

$$\frac{\partial e}{\partial \omega_2} = 2\omega_2 + 2\omega_1 - 2 \quad \frac{\partial^2 e}{\partial \omega_2^2} = 4$$

$$\frac{\partial e}{\partial \omega_2} = 0$$

$$H = \begin{bmatrix} 4 & 0 \\ 0 & 4 \end{bmatrix}$$

$$\lambda - 4 = 0$$

$$\boxed{\lambda = 4}$$

eigen value \neq constant