

**B.M.S. COLLEGE OF ENGINEERING BENGALURU**  
Autonomous Institute, Affiliated to VTU



Lab Record

**Machine Learning**

*Submitted in partial fulfillment for the 6<sup>th</sup> Semester Laboratory*

Bachelor of Technology in  
Computer Science and Engineering

*Submitted by:*

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**B.M.S. COLLEGE OF ENGINEERING**  
**DEPARTMENT OF COMPUTER SCIENCE AND**  
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***CERTIFICATE***

This is to certify that the Machine Learning (20CS6PCMAL) laboratory has been carried out by **RITHESH M RAO (1BM20CS126)** during the 6<sup>th</sup> Semester Mar-July-2023.

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Lab Program	Unit #	Program Details
1	1	Implement and demonstrate the FIND-S algorithm for finding the most specific hypothesis based on a given set of training data samples.
2	1	For a given set of training data examples stored in a .CSV file, implement and demonstrate the Candidate-Elimination algorithm to output a description of the set of all hypotheses consistent with the training examples.
3	1	Write a program to demonstrate the working of the decision tree based ID3 algorithm. Use an appropriate data set for building the decision tree and apply this knowledge to classify a new sample.
4	3	Write a program to implement the naïve Bayesian classifier for a sample training data set stored as a .CSV file. Compute the accuracy of the classifier, considering few test data sets
5	3	Write a program to construct a Bayesian network considering training data. Use this model to make predictions.
6	3	Apply k-Means algorithm to cluster a set of data stored in a .CSV file.
7	3	Apply EM algorithm to cluster a set of data stored in a .CSV file. Compare the results of k-Means algorithm and EM algorithm.
8	4	Write a program to implement k-Nearest Neighbour algorithm to classify the iris data set. Print both correct and wrong predictions.
9	4	Implement the Linear Regression algorithm in order to fit data points. Select appropriate data set for your experiment and draw graphs.
10	4	Implement the non-parametric Locally Weighted Regression algorithm in order to fit data points. Select appropriate data set for your experiment and draw graphs.

## Program 1: Implement and demonstrate the FIND-S algorithm for finding the most specific hypothesis based on a given set of training data samples.

```
In [ ]: # Interactive

len_x = int(input('enter no. of samples: '))
x = []
attrib = input('enter attributes: ').split()
n_attrib = len(attrib)
for i in range(len_x):
    X = input(f'enter sample {i}: ').split()
    x.append(X)
y = []
for i in range(len_x):
    Y = input(f'output for sample {i} (true/false): ')
    Y = Y.lower()
    y.append(True if Y == 'true' else False)
```

```
In [4]: # Read from csv

import pandas as pd
import numpy as np

data = pd.read_csv("data.csv")
print(data)
x = np.array(data)[:, :-1]
y = np.array(data)[:, -1]
len_x = len(x)
print(x)
print(y)

      temp   time is_holiday  result
0   hot  afternoon      yes    True
1   hot    morning       no   False
2  cold  afternoon      yes    True
[['hot' 'afternoon' 'yes']
 ['hot' 'morning' 'no']
 ['cold' 'afternoon' 'yes']]
[True False True]
```

```
In [7]: def findsAlgo(x, y, len_x):
    h = x[0] # initial generalization

    for i in range(1, len_x):
        if not y[i]:
            continue

        for j, attrib in enumerate(x[i]):
            if h[j] != attrib:
                h[j] = '?'

    return h
```

```
In [8]: findsAlgo(x, y, len_x)
Out[8]: array(['?', 'afternoon', 'yes'], dtype=object)
```

## ALGORITHM:

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FIND S Algorithm.

1. Initialize 'h' to the most Specific hypothesis
2. For each positive training instance 'x'  
For each attribute constraint  $a_i \leq h$   
if the constraint  $a_i$  is satisfied by 'x'  
nothing  
else  
Replace  $a_i$  in 'h' by the next more  
general constraint that is replaced by 'x'
3. Output hypothesis 'h'

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**Program 2:** For a given set of training data examples stored in a .CSV file, implement and demonstrate the Candidate-Elimination algorithm to output a description of the set of all hypotheses consistent with the training examples.

```
In [1]: import numpy as np
import pandas as pd

In [2]: data = pd.read_csv('../input/enjoysport/enjoysport.csv')
X = data.to_numpy()[:, :-1]
y = data.to_numpy()[:, -1]

In [3]: def candidateElimination(X, y):
    n_attrib = len(X[0])
    specific_h = ['0' for _ in range(n_attrib)]
    general_h = ['?' for _ in range(n_attrib)] for _ in range(n_attrib)]

    print('===== Iteration 0 =====')
    print(f'Specific Boundary: {specific_h}')
    print(f'General Boundary: {general_h}')
    print()

    specific_h = X[0].copy()

    for i, x in enumerate(X):
        print(f'===== Iteration {i + 1} =====')
        print(f'Instance {i + 1}: {x} \t Target: {y[i]}')

        if y[i] == 'yes':
            for j in range(n_attrib):
                if x[j] != specific_h[j]:
                    specific_h[j] = '?'
                    general_h[j][j] = '?'
        else:
            for j in range(n_attrib):
                if x[j] != specific_h[j]:
                    general_h[j][j] = specific_h[j]
                else:
                    general_h[j][j] = '?'

        print(f'Specific Boundary: {specific_h}')
        print(f'General Boundary: {general_h}')
        print()

    general_h = [h for h in general_h if h != ['?' for _ in range(n_attrib)]]

    print('===== Result =====')
    print(f'Specific Boundary: {specific_h}')
    print(f'General Boundary: {general_h}')
    print()

    return list(specific_h), list(general_h)
```

In [4]: candidateElimination(X, y)

```
===== Iteration 0 =====
Specific Boundary: ['0', '0', '0', '0', '0', '0']
General Boundary: [[ '?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?']]

===== Iteration 1 =====
Instance 1: ['sunny' 'warm' 'normal' 'strong' 'warm' 'same'] Target: yes
Specific Boundary: ['sunny' 'warm' 'normal' 'strong' 'warm' 'same']
General Boundary: [[ '?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?']]

===== Iteration 2 =====
Instance 2: ['sunny' 'warm' 'high' 'strong' 'warm' 'same'] Target: yes
Specific Boundary: ['sunny' 'warm' '?' 'strong' 'warm' 'same']
General Boundary: [[ '?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?']]

===== Iteration 3 =====
Instance 3: ['rainy' 'cold' 'high' 'strong' 'warm' 'change'] Target: no
Specific Boundary: ['sunny' 'warm' '?' 'strong' 'warm' 'same']
General Boundary: [[['sunny', '?', '?', '?', '?', '?'], ['?', 'warm', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', 'same']]]

===== Iteration 4 =====
Instance 4: ['sunny' 'warm' 'high' 'strong' 'cool' 'change'] Target: yes
Specific Boundary: ['sunny' 'warm' '?' 'strong' '?' '?']
General Boundary: [[['sunny', '?', '?', '?', '?', '?'], ['?', 'warm', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?']]]

===== Result =====
Specific Boundary: ['sunny' 'warm' '?' 'strong' '?' '?']
General Boundary: [[['sunny', '?', '?', '?', '?', '?'], ['?', 'warm', '?', '?', '?', '?']]]
```

Out[4]: ([['sunny', 'warm', '?', 'strong', '?', '?'],  
[['sunny', '?', '?', '?', '?', '?'], ['?', 'warm', '?', '?', '?', '?']]])

## ALGORITHM:

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### CANDIDATE-ELIMINATION Learning Algorithm

- Initialize  $G$  to the set of maximally general hypotheses in  $H$ .
- Initialize  $S$  to the set of maximally specific hypotheses in  $H$ .

For each training example  $d$ , do

- Remove from  $G$  any hypothesis inconsistent with  $d$ .
- Remove For each hypothesis  $g$  in  $S$  that is not consistent with  $d$ .
  - Remove  $g$  from  $S$
  - Add to  $S$  all minimal generalization  $h$  of  $g$  such that
    - $h$  is consistent with  $d$ , and some member of  $G$  is more general than  $h$ .
  - Remove from  $S$  any hypothesis that is more general than another hypothesis in  $S$ .
- If  $d$  is a negative example
  - Remove from  $S$  any hypothesis inconsistent with  $d$
  - For each hypothesis  $g$  in  $G$  that is not consistent with  $d$ 
    - Remove  $g$  from  $G$
    - Add to  $G$  all minimal specializations  $h$  of  $g$  such that
      - $h$  is consistent with  $d$ , and some member of  $S$  is more specific than  $h$

- Remove from  $G$  any hypothesis that is less general than another hypothesis

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**Program 3:** Write a program to demonstrate the working of the decision tree based ID3 algorithm. Use an appropriate data set for building the decision tree and apply this knowledge to classify a new sample.

```
In [62]: import numpy as np
import pandas as pd
eps = np.finfo(float).eps
from numpy import log2 as log

In [63]: df = pd.read_csv('../input/playtennis/playtennis.csv')
df
```

```
Out[63]:
```

	outlook	temperature	humidity	wind	play
0	sunny	hot	high	weak	no
1	sunny	hot	high	strong	no
2	overcast	hot	high	weak	yes
3	rain	mild	high	weak	yes
4	rain	cool	normal	weak	yes
5	rain	cool	normal	strong	no
6	overcast	cool	normal	strong	yes
7	sunny	mild	high	weak	no
8	sunny	cool	normal	weak	yes
9	rain	mild	normal	weak	yes
10	sunny	mild	normal	strong	yes
11	overcast	mild	high	strong	yes
12	overcast	hot	normal	weak	yes
13	rain	mild	high	strong	no

```
In [64]: def find_entropy(df):
    Class = df.keys()[-1]
    entropy = 0
    values = df[Class].unique()
    for value in values:
        fraction = df[Class].value_counts()[value]/len(df[Class])
        entropy += -fraction*np.log2(fraction)
    return entropy

def find_entropy_attribute(df,attribute):
    Class = df.keys()[-1]
    target_variables = df[Class].unique()
    variables = df[attribute].unique()
    entropy2 = 0
    for variable in variables:
        entropy = 0
        for target_variable in target_variables:
            num = len(df[attribute][df[attribute]==variable][df[Class] ==target_variable])
            den = len(df[attribute][df[attribute]==variable])
            if num > 0:
                entropy += -num/den * np.log2(num/den)
        entropy2 += -len(df[attribute])/len(df)*entropy
    return entropy2
```

```

        fraction = num/(den+eps)
        entropy += -fraction*log(fraction+eps)
    fraction2 = den/len(df)
    entropy2 += -fraction2*entropy
    return abs(entropy2)

def find_winner(df):
    Entropy_att = []
    IG = []
    for key in df.keys()[:-1]:
        IG.append(find_entropy(df)-find_entropy_attribute(df,key))
    return df.keys()[:-1][np.argmax(IG)]

def get_subtable(df, node,value):
    return df[df[node] == value].reset_index(drop=True)

def buildTree(df,tree=None):
    Class = df.keys()[-1]
    node = find_winner(df)
    attValue = np.unique(df[node])
    if tree is None:
        tree={}
        tree[node] = {}
    for value in attValue:
        subtable = get_subtable(df,node,value)
        c1Value,counts = np.unique(subtable['play'],return_counts=True)

        if len(counts)==1:
            tree[node][value] = c1Value[0]
        else:
            tree[node][value] = buildTree(subtable)

    return tree

```

In [65]: t = buildTree(df)  
t

Out[65]: {'outlook': {'overcast': 'yes',
 'rain': {'wind': {'strong': 'no', 'weak': 'yes'}},
 'sunny': {'humidity': {'high': 'no', 'normal': 'yes'}}}}

In [ ]:

## ALGORITHM:

### ID3 Algorithm.

ID3 (Examples, Target-attribute, Attributes)

- Create a Root node for the tree
- If all examples are positive, Returns the single-node tree Root, with label = +
- If all examples are negative, Returns the single-node tree Root, with label = -
- If attributes is empty. Returns the single-node tree Root, with label = most common value of Target attribute in Examples
- Otherwise Begins
  - $A \leftarrow$  the attribute from Attributes that best\* classifies Examples
  - The decision attribute for Root  $\leftarrow A$
  - For each possible value,  $v_i$ , of  $A$ .
    - Add a new tree branch below Root, corresponding to the test  $A = v_i$
    - Let Examples  $v_i$ , be the subset of Examples that have value  $v_i$  for  $A$ .
    - If Examples  $v_i$ , is empty
      - Then below this new branch add a leaf node with label = most common value of Target-attribute in Examples
      - Else below this new branch add the Subtree
- ID3 (Examples  $v_i$ , Target-attribute, Attributes -  $\{A\}$ ))
- End
- Return Root.

**Program 4:** Write a program to implement the naïve Bayesian classifier for a sample training data set stored as a .CSV file. Compute the accuracy of the classifier, considering few test data sets.

```
In [1]: import csv
import random
import math

In [2]: def load_csv(filename):
    lines = csv.reader(open(filename, "r"));
    dataset = list(lines)
    for i in range(len(dataset)):
        dataset[i] = [float(x) for x in dataset[i]]
    return dataset

def split_dataset(dataset, splitratio):
    trainsize = int(len(dataset) * splitratio);
    trainset = []
    copy = list(dataset);
    while len(trainset) < trainsize:
        index = random.randrange(len(copy));
        trainset.append(copy.pop(index))
    return [trainset, copy]

def separate_by_class(dataset):
    separated = {}
    for i in range(len(dataset)):
        vector = dataset[i]
        if (vector[-1] not in separated):
            separated[vector[-1]] = []
        separated[vector[-1]].append(vector)
    return separated

def mean(numbers):
    return sum(numbers)/float(len(numbers))

def std_dev(numbers):
    avg = mean(numbers)
    variance = sum([pow(x-avg,2) for x in numbers])/float(len(numbers)-1)
    return math.sqrt(variance)

def summarize(dataset):
    summaries = [(mean(attribute), std_dev(attribute)) for attribute in zip(*dataset)];
    del summaries[-1]
    return summaries

def summarize_by_class(dataset):
    separated = separate_by_class(dataset);
    summaries = {}
    for classvalue, instances in separated.items():
        summaries[classvalue] = summarize(instances)
    return summaries

def calculate_probability(x, mean, stdev):
    exponent = math.exp(-(math.pow(x-mean,2)/(2*math.pow(stdev,2))))
    return (1 / (math.sqrt(2*math.pi) * stdev)) * exponent

def calculate_class_probabilities(summaries, inputvector):
    probabilities = {}
```

```

for classvalue, classsummaries in summaries.items():
    probabilities[classvalue] = 1
for i in range(len(classsummaries)):
    mean, stdev = classsummaries[i]
    x = inputvector[i]
    probabilities[classvalue] *= calculate_probability(x, mean, stdev)
return probabilities

def predict(summaries, inputvector):
    probabilities = calculate_class_probabilities(summaries, inputvector)
    bestLabel, bestProb = None, -1
    for classvalue, probability in probabilities.items():
        if bestLabel is None or probability > bestProb:
            bestProb = probability
            bestLabel = classvalue
    return bestLabel

def get_predictions(summaries, testset):
    predictions = []
    for i in range(len(testset)):
        result = predict(summaries, testset[i])
        predictions.append(result)
    return predictions

def get_accuracy(testset, predictions):
    correct = 0
    for i in range(len(testset)):
        if testset[i][-1] == predictions[i]:
            correct += 1
    return (correct/float(len(testset))) * 100.0

```

```

In [3]: splitratio = 0.67
dataset = load_csv('../input/pima-indians-diabetes.csv')
trainingset, testset = split_dataset(dataset, splitratio)

print(f'Split {len(dataset)} rows into train={len(trainingset)} and test={len(testset)} rows')

summaries = summarize_by_class(trainingset)
predictions = get_predictions(summaries, testset)
accuracy = get_accuracy(testset, predictions)

print(f'Accuracy of the classifier is :{accuracy}%')

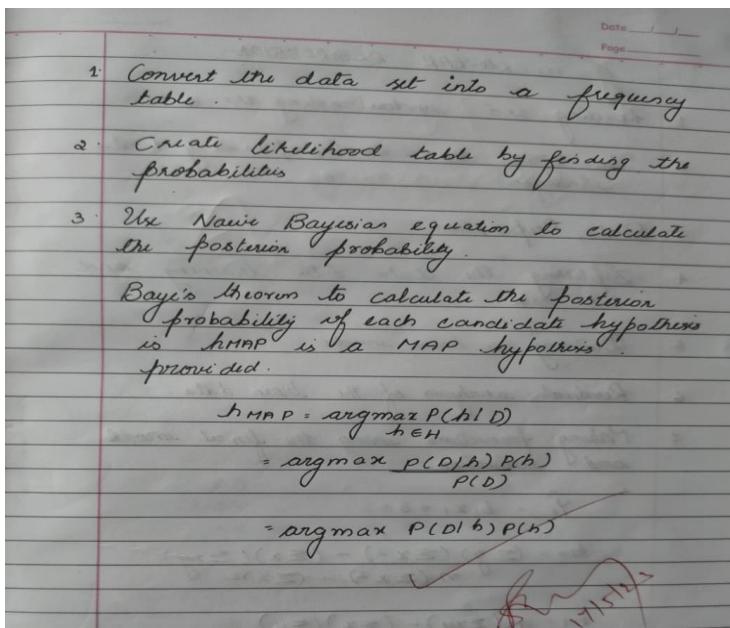
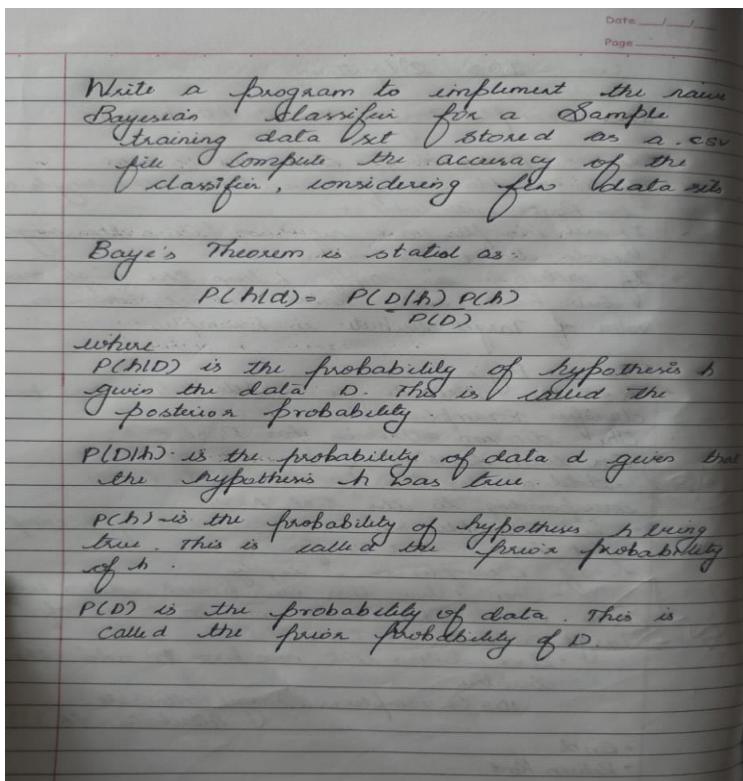
Split 768 rows into train=514 and test=254 rows
Accuracy of the classifier is :64.96062992125984%

```

In [ ]:

---

## ALGORITHM:



## Program 5: Write a program to construct a Bayesian network considering training data. Use this model to make predictions.

```
In [1]: import numpy as np
import pandas as pd
import csv
!pip install pgmpy
from pgmpy.estimators import MaximumLikelihoodEstimator
from pgmpy.models import BayesianModel
from pgmpy.inference import VariableElimination

Collecting pgmpy
  Downloading pgmpy-0.1.14-py3-none-any.whl (331 kB)
|██████████| 331 kB 3.0 MB/s
Requirement already satisfied: pandas in /opt/conda/lib/python3.7/site-packages (from pgmpy) (1.2.3)
Requirement already satisfied: scikit-learn in /opt/conda/lib/python3.7/site-packages (from pgmpy) (0.24.1)
Requirement already satisfied: scipy in /opt/conda/lib/python3.7/site-packages (from pgmpy) (1.5.4)
Requirement already satisfied: torch in /opt/conda/lib/python3.7/site-packages (from pgmpy) (1.7.0)
Requirement already satisfied: tqdm in /opt/conda/lib/python3.7/site-packages (from pgmpy) (4.59.0)
Requirement already satisfied: joblib in /opt/conda/lib/python3.7/site-packages (from pgmpy) (1.0.1)
Requirement already satisfied: pyparsing in /opt/conda/lib/python3.7/site-packages (from pgmpy) (2.4.7)
Requirement already satisfied: statsmodels in /opt/conda/lib/python3.7/site-packages (from pgmpy) (0.12.2)
Requirement already satisfied: networkx in /opt/conda/lib/python3.7/site-packages (from pgmpy) (2.5)
Requirement already satisfied: numpy in /opt/conda/lib/python3.7/site-packages (from pgmpy) (1.19.5)
Requirement already satisfied: decorator>=4.3.0 in /opt/conda/lib/python3.7/site-packages (from networkx->pgmpy) (4.4.2)
Requirement already satisfied: python-dateutil>=2.7.3 in /opt/conda/lib/python3.7/site-packages (from pandas->pgmpy) (2.8.1)
Requirement already satisfied: pytz>=2017.3 in /opt/conda/lib/python3.7/site-packages (from pandas->pgmpy) (2021.1)
Requirement already satisfied: six>=1.5 in /opt/conda/lib/python3.7/site-packages (from python-dateutil>=2.7.3->pandas->pgmpy) (1.15.0)
Requirement already satisfied: threadpoolctl>=2.0.0 in /opt/conda/lib/python3.7/site-packages (from scikit-learn->pgmpy) (2.1.0)
Requirement already satisfied: patsy>=0.5 in /opt/conda/lib/python3.7/site-packages (from statsmodels->pgmpy) (0.5.1)
Requirement already satisfied: future in /opt/conda/lib/python3.7/site-packages (from torch->pgmpy) (0.18.2)
Requirement already satisfied: typing_extensions in /opt/conda/lib/python3.7/site-packages (from torch->pgmpy) (3.7.4.3)
Requirement already satisfied: dataclasses in /opt/conda/lib/python3.7/site-packages (from torch->pgmpy) (0.6)
Installing collected packages: pgmpy
Successfully installed pgmpy-0.1.14

In [2]: heartDisease = pd.read_csv('../input/heartdisease/heart.csv')
heartDisease = heartDisease.replace('?',np.nan)

print('Sample instances from the dataset are given below')
print(heartDisease.head())
print('\n Attributes and datatypes')
print(heartDisease.dtypes)

Sample instances from the dataset are given below
   age  sex  cp  trestbps  chol  fbs  restecg  thalach  exang  oldpeak  slope \
0    63     1     1    145    233     1      2     150      0     2.3      3
1    67     1     4    160    286     0      2     108      1     1.5      2
2    67     1     4    120    229     0      2     129      1     2.6      2
3    37     1     3    130    250     0      0     187      0     3.5      3
4    41     0     2    130    204     0      2     172      0     1.4      1
```

```
      ca thal  heartdisease
0  0     6          0
1  3     3          2
2  2     7          1
3  0     3          0
4  0     3          0
```

```
Attributes and datatypes
age           int64
sex           int64
cp            int64
trestbps     int64
chol          int64
fbs           int64
restecg       int64
thalach       int64
exang         int64
oldpeak      float64
slope         int64
ca            object
thal          object
heartdisease int64
dtype: object
```

```
In [3]: model = BayesianModel([('age','heartdisease'),('sex','heartdisease'),('exang','heartdisease'),('cp','heartdisease'),
('heartdisease','restecg'),('heartdisease','chol')])
```

```
In [4]: print('\nLearning CPD using Maximum likelihood estimators')
model.fit(heartDisease,estimator=MaximumLikelihoodEstimator)

print('\nInferencing with Bayesian Network:')
HeartDiseasetest_infer = VariableElimination(model)
```

Learning CPD using Maximum likelihood estimators

Inferencing with Bayesian Network:

```
In [5]: print('\n1. Probability of HeartDisease given evidence = restecg :')
q1=HeartDiseasetest_infer.query(variables=['heartdisease'],evidence={'restecg':1})
print(q1)

print('\n2. Probability of HeartDisease given evidence = cp :')
q2=HeartDiseasetest_infer.query(variables=['heartdisease'],evidence={'cp':2})
print(q2)

Finding Elimination Order: :  0% | 0/5 [00:00<?, ?it/s]
  0% | 0/5 [00:00<?, ?it/s]
Finding Elimination Order: : 100%|██████████| 5/5 [00:00<00:00, 480.98it/s]

Eliminating: age:  0% | 0/5 [00:00<?, ?it/s]
Eliminating: sex:  0% | 0/5 [00:00<?, ?it/s]
Eliminating: chol: 0% | 0/5 [00:00<?, ?it/s]
Eliminating: exang: 100%|██████████| 5/5 [00:00<00:00, 92.85it/s]
```

```
1. Probability of HeartDisease given evidence = restecg :
+-----+-----+
| heartdisease | phi(heartdisease) |
+=====+=====
| heartdisease(0) | 0.1012 |
+-----+-----+
| heartdisease(1) | 0.0000 |
+-----+-----+
| heartdisease(2) | 0.2392 |
+-----+-----+
| heartdisease(3) | 0.2015 |
+-----+-----+
| heartdisease(4) | 0.4581 |
+-----+-----+  
2. Probability of HeartDisease given evidence = cp :  
Finding Elimination Order: : 0% | 0/5 [00:00<?, ?it/s]  
0% | 0/5 [00:00<?, ?it/s]  
Eliminating: age: 0% | 0/5 [00:00<?, ?it/s]  
Eliminating: sex: 0% | 0/5 [00:00<?, ?it/s]  
Eliminating: chol: 0% | 0/5 [00:00<?, ?it/s]  
Eliminating: exang: 0% | 0/5 [00:00<?, ?it/s]  
Eliminating: restecg: 100% | 5/5 [00:00<00:00, 227.41it/s]  
+-----+-----+
| heartdisease | phi(heartdisease) |
+=====+=====
| heartdisease(0) | 0.3610 |
+-----+-----+
| heartdisease(1) | 0.2159 |
+-----+-----+
| heartdisease(2) | 0.1373 |
+-----+-----+
| heartdisease(3) | 0.1537 |
+-----+-----+
| heartdisease(4) | 0.1321 |
+-----+-----+
```

In [ ]:

## ALGORITHM:

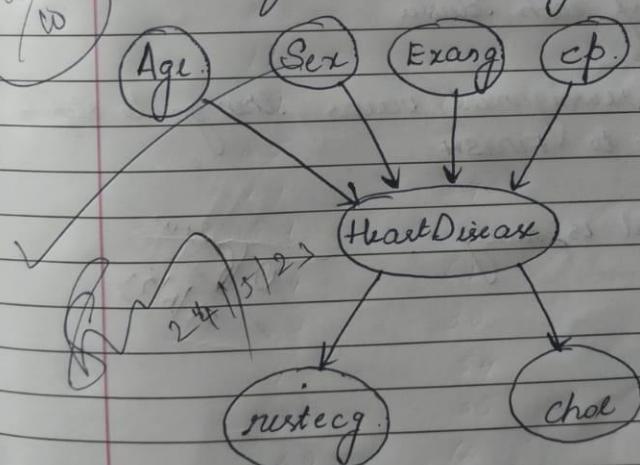
Bayesian Belief Network

A Bayesian Network is a directed acyclic graph in which each edge corresponds to a conditional dependency, and each node corresponds to a unique random variable.

It consists of 2 Major types: a directed acyclic graph and a set of conditional probability distributions

- The directed acyclic graph is a set of random variables represented by nodes.
- The conditional probability distribution of a node is defined for every possible outcome of the preceding causal node.

NP/10



$$P(\text{Heartdisease} | \text{restecg}=1) =$$

## Program 6: Apply k-Means algorithm to cluster a set of data stored in a .CSV file.

```
In [1]: from sklearn import datasets
import matplotlib.pyplot as plt
import pandas as pd
from sklearn.cluster import KMeans
from sklearn.metrics import accuracy_score, confusion_matrix
```

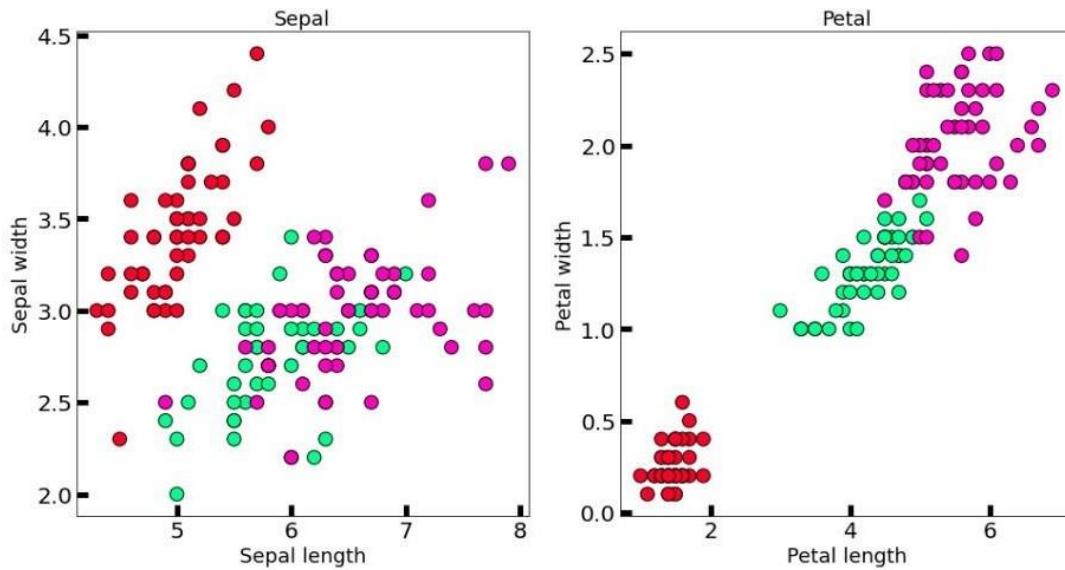
### Dataset

```
In [2]: iris = datasets.load_iris()
iris
```

```
Out[2]: {'data': array([[5.1, 3.5, 1.4, 0.2],
[4.9, 3. , 1.4, 0.2],
[4.7, 3.2, 1.3, 0.2],
[4.6, 3.1, 1.5, 0.2],
[5. , 3.6, 1.4, 0.2],
[5.4, 3.9, 1.7, 0.4],
[4.6, 3.4, 1.4, 0.3],
[5. , 3.4, 1.5, 0.2],
[4.4, 2.9, 1.4, 0.2],
[4.9, 3.1, 1.5, 0.1],
[5.4, 3.7, 1.5, 0.2],
[4.8, 3.4, 1.6, 0.2],
[4.8, 3. , 1.4, 0.1],
[4.3, 3. , 1.1, 0.1],
[5.8, 4. , 1.2, 0.2],
[5.7, 4.4, 1.5, 0.4],
[5.4, 3.9, 1.3, 0.4],
[5.1, 3.5, 1.4, 0.3],
[5.7, 3.8, 1.7, 0.3],
[5.1, 3.8, 1.5, 0.3],
[5.4, 3.4, 1.7, 0.2],
[5.1, 3.7, 1.5, 0.4],
[4.6, 3.6, 1. , 0.2],
[5.1, 3.3, 1.7, 0.5],
[4.8, 3.4, 1.9, 0.2],
[5. , 3. , 1.6, 0.2],
[5. , 3.4, 1.6, 0.4],
[5.2, 3.5, 1.5, 0.2],
[5.2, 3.4, 1.4, 0.2],
[4.7, 3.2, 1.6, 0.2],
[4.8, 3.1, 1.6, 0.2],
[5.4, 3.4, 1.5, 0.4],
[5.2, 4.1, 1.5, 0.1],
[5.5, 4.2, 1.4, 0.2],
[4.9, 3.1, 1.5, 0.2],
[5. , 3.2, 1.2, 0.2],
[5.5, 3.5, 1.3, 0.2],
[4.9, 3.6, 1.4, 0.1],
[4.4, 3. , 1.3, 0.2],
[5.1, 3.4, 1.5, 0.2],
```

```
In [3]: sepal_X = iris.data[:, :2]
petal_X = iris.data[:, 2:]
y = iris.target
categories = len(iris.target_names)

fig, axes = plt.subplots(1, 2, figsize=(16,8))
axes[0].scatter(sepal_X[:, 0], sepal_X[:, 1], c=y, cmap='gist_rainbow', edgecolor='k', s=150)
axes[1].scatter(petal_X[:, 0], petal_X[:, 1], c=y, cmap='gist_rainbow', edgecolor='k', s=150)
axes[0].set_xlabel('Sepal length', fontsize=18)
axes[0].set_ylabel('Sepal width', fontsize=18)
axes[1].set_xlabel('Petal length', fontsize=18)
axes[1].set_ylabel('Petal width', fontsize=18)
axes[0].tick_params(direction='in', length=10, width=5, colors='k', labelsize=20)
axes[1].tick_params(direction='in', length=10, width=5, colors='k', labelsize=20)
axes[0].set_title('Sepal', fontsize=18)
axes[1].set_title('Petal', fontsize=18)
plt.show()
```



## Model

```
In [4]: model_sepals = KMeans(n_clusters=3)
model_sepals.fit(sepal_X)
model_petal = KMeans(n_clusters=3)
model_petal.fit(petal_X)

Out[4]: KMeans(n_clusters=3)
```

## Analysis

```
In [5]: def plot_centers(sepal_centers, petal_centers):
    plt.scatter([point[0] for point in sepal_centers], [point[1] for point in sepal_centers])
    plt.title('Sepal KMeans Centers')
    plt.show()
```

```

plt.title( f'Actual KMeans Centers' )
plt.show()

def plot_actualvpredicted(X, y, predicted, part):
    fig, axes = plt.subplots(1, 2, figsize=(16,8))
    axes[0].scatter(X[:, 0], X[:, 1], c=y, cmap='gist_rainbow', edgecolor='k', s=150)
    axes[1].scatter(X[:, 0], X[:, 1], c=predicted, cmap='jet', edgecolor='k', s=150)
    axes[0].set_xlabel(f'{part} length', fontsize=18)
    axes[0].set_ylabel(f'{part} width', fontsize=18)
    axes[1].set_xlabel(f'{part} length', fontsize=18)
    axes[1].set_ylabel(f'{part} width', fontsize=18)
    axes[0].tick_params(direction='in', length=10, width=5, colors='k', labelsize=20)
    axes[1].tick_params(direction='in', length=10, width=5, colors='k', labelsize=20)
    axes[0].set_title('Actual', fontsize=18)
    axes[1].set_title('Predicted', fontsize=18)
    plt.show()

def plot_confusion(accuracy, confusion, part):
    print(f'{part} Accuracy: {accuracy}')

    fig, ax = plt.subplots()
    im = ax.imshow(confusion)

    ax.set_xticks(range(categories))
    ax.set_yticks(range(categories))
    ax.set_xticklabels(iris.target_names)
    ax.set_yticklabels(iris.target_names)

    plt.setp(ax.get_xticklabels(), rotation=45, ha="right",
             rotation_mode="anchor")

    for i in range(categories):
        for j in range(categories):
            text = ax.text(j, i, confusion[i, j],
                           ha="center", va="center", color="w")

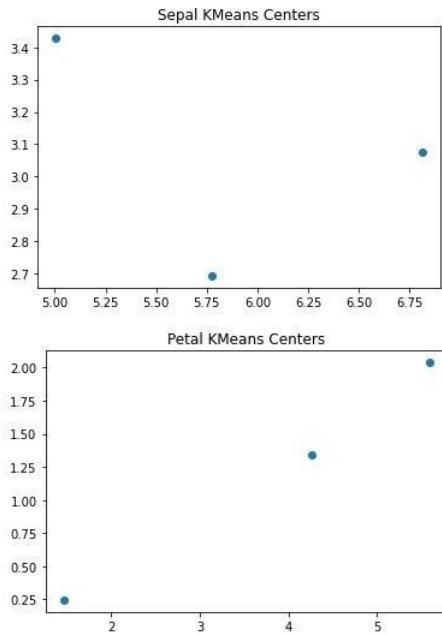
    ax.set_title(f'{part} Confusion Matrix (Actual / Predicted)')
    fig.tight_layout()
    plt.show()

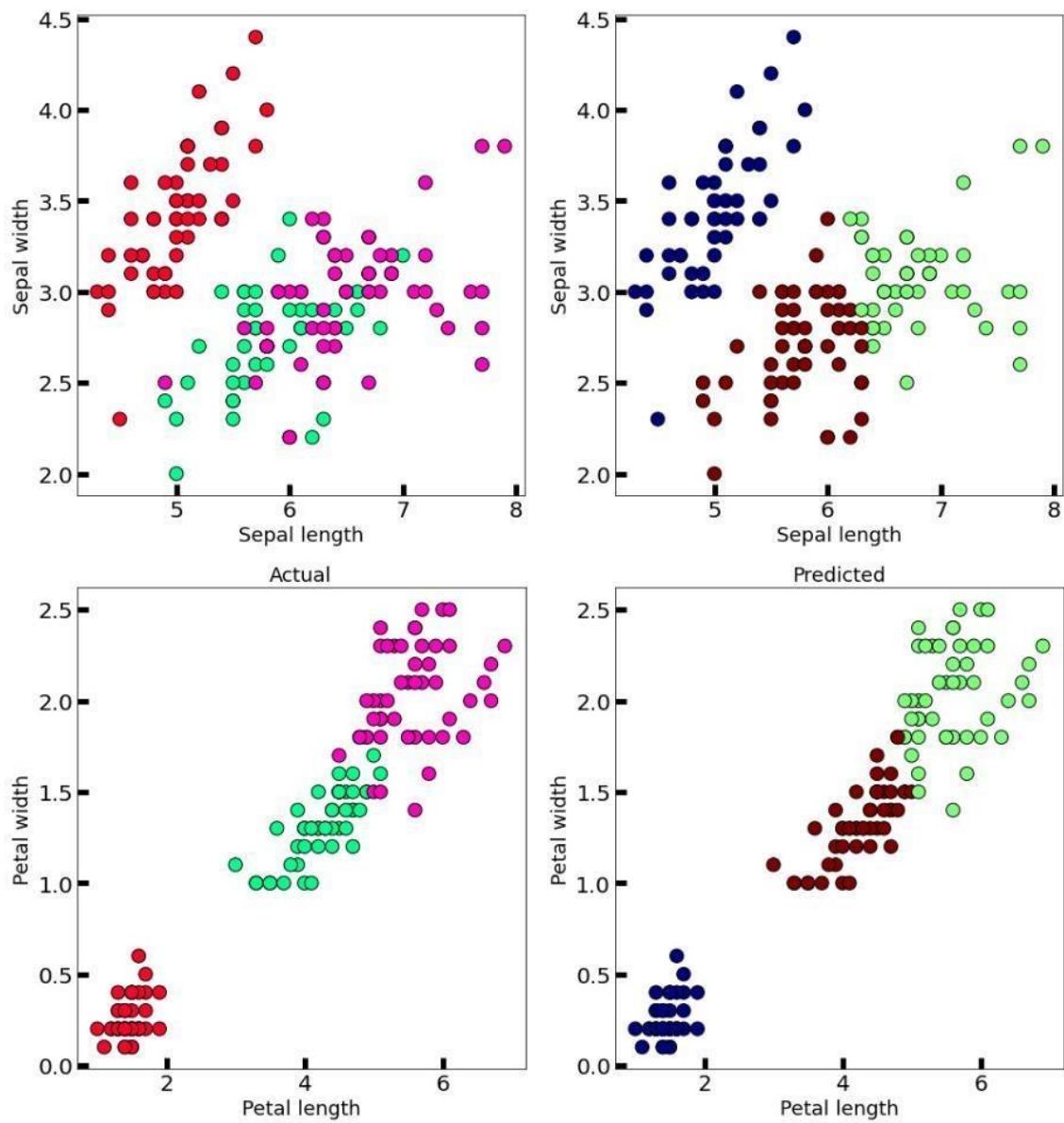
```

```

In [6]: sepal_centers = model_sepal.cluster_centers_
petal_centers = model_petal.cluster_centers_
plot_centers(sepal_centers, petal_centers)

```



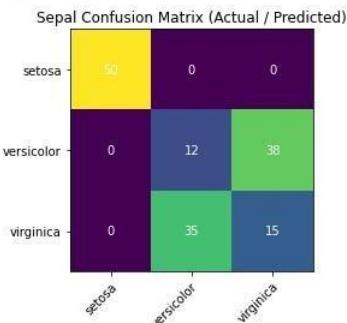


```
In [9]: sepal_accuracy = accuracy_score(y, sepal_labels)
petal_accuracy = accuracy_score(y, petal_labels)
```

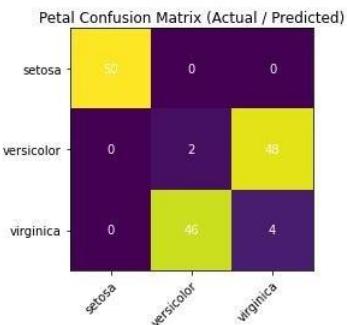
```
sepal_confusion = confusion_matrix(y, sepal_labels)
petal_confusion = confusion_matrix(y, petal_labels)
```

```
In [10]: plot_confusion(sepal_accuracy, sepal_confusion, 'Sepal')
plot_confusion(petal_accuracy, petal_confusion, 'Petal')
```

Sepal Accuracy: 0.5133333333333333



Petal Accuracy: 0.3733333333333335



## ALGORITHM:

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### K-Means Algorithm.

- ① Select the number  $k$  to divide the number of clusters
- ② Select random  $k$  points or centroids.
- ③ Assign each data point to their closest centroid, which will form the predefined  $k$  clusters.
- ④ Calculate the variance and place a new centroid of each cluster.
- ⑤ Repeat the third step, which means reassign each datapoint to the new closest centroid of each cluster.
- ⑥ If any reassignment occurs, then go to step 4  
else go to FINISH
- ⑦ The model is ready

0/12 new  
x b/23

## Program 7: Apply EM algorithm to cluster a set of data stored in a .CSV file. Compare the results of k-Means algorithm and EM algorithm.

```
In [1]: import matplotlib.pyplot as plt
import pandas as pd
from sklearn.mixture import GaussianMixture
from sklearn.metrics import accuracy_score, confusion_matrix
```

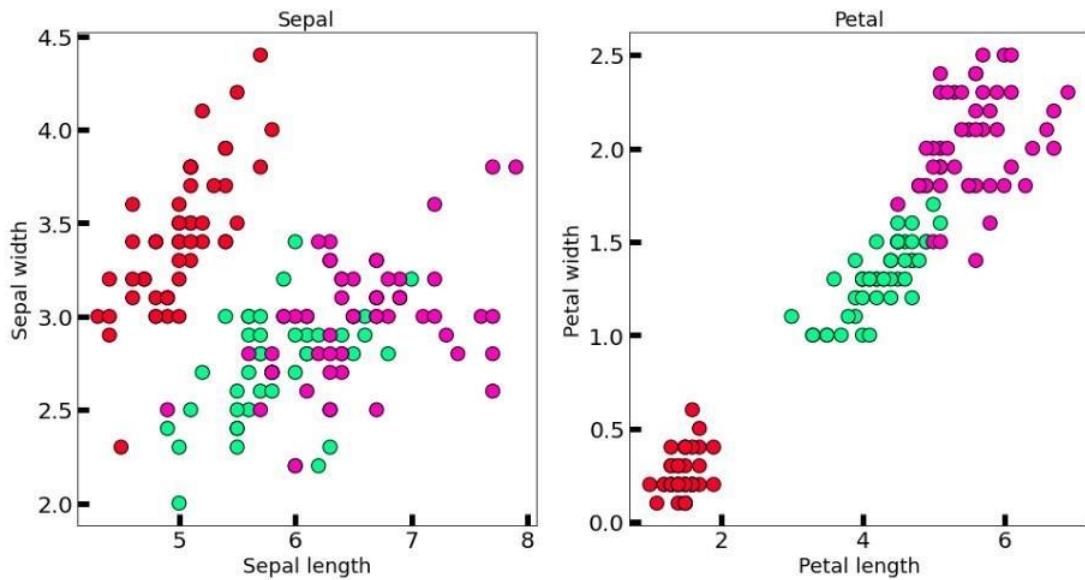
### Data

```
In [2]: data = pd.read_csv('../input/iris/Iris.csv')
data.head()
```

	<b>Id</b>	<b>SepalLengthCm</b>	<b>SepalWidthCm</b>	<b>PetalLengthCm</b>	<b>PetalWidthCm</b>	<b>Species</b>
<b>0</b>	1	5.1	3.5	1.4	0.2	Iris-setosa
<b>1</b>	2	4.9	3.0	1.4	0.2	Iris-setosa
<b>2</b>	3	4.7	3.2	1.3	0.2	Iris-setosa
<b>3</b>	4	4.6	3.1	1.5	0.2	Iris-setosa
<b>4</b>	5	5.0	3.6	1.4	0.2	Iris-setosa

```
In [3]: sepal_X = data[['SepalLengthCm', 'SepalWidthCm']]
petal_X = data[['PetalLengthCm', 'PetalWidthCm']]
y = data['Species'].astype("category").cat.codes
num_cat = y.nunique()
categories = data['Species'].astype("category").cat.categories
```

```
In [4]: fig, axes = plt.subplots(1, 2, figsize=(16,8))
axes[0].scatter(sepal_X.SepalLengthCm, sepal_X.SepalWidthCm, c=y, cmap='gist_rainbow', edgecolor='k', s=150)
axes[1].scatter(petal_X.PetalLengthCm, petal_X.PetalWidthCm, c=y, cmap='gist_rainbow', edgecolor='k', s=150)
axes[0].set_xlabel('Sepal length', fontsize=18)
axes[0].set_ylabel('Sepal width', fontsize=18)
axes[1].set_xlabel('Petal length', fontsize=18)
axes[1].set_ylabel('Petal width', fontsize=18)
axes[0].tick_params(direction='in', length=10, width=5, colors='k', labelsize=20)
axes[1].tick_params(direction='in', length=10, width=5, colors='k', labelsize=20)
axes[0].set_title('Sepal', fontsize=18)
axes[1].set_title('Petal', fontsize=18)
plt.show()
```



## Model

```
In [5]: model_sepals = GaussianMixture(n_components=3)
sepals_labels = model_sepals.fit_predict(sepals_X)
model_petal = GaussianMixture(n_components=3)
petals_labels = model_petal.fit_predict(petals_X)
```

## Analysis

```
In [6]: def plot_actualvpredicted(X, y, predicted, part):
    fig, axes = plt.subplots(1, 2, figsize=(16,8))
    axes[0].scatter(X[f'{part}LengthCm'], X[f'{part}WidthCm'], c=y, cmap='gist_rainbow', edgecolor='k', s=150)
    axes[1].scatter(X[f'{part}LengthCm'], X[f'{part}WidthCm'], c=predicted, cmap='jet', edgecolor='k', s=150)
    axes[0].set_xlabel(f'{part} length', fontsize=18)
    axes[0].set_ylabel(f'{part} width', fontsize=18)
    axes[1].set_xlabel(f'{part} length', fontsize=18)
    axes[1].set_ylabel(f'{part} width', fontsize=18)
    axes[0].tick_params(direction='in', length=10, width=5, colors='k', labelsize=20)
    axes[1].tick_params(direction='in', length=10, width=5, colors='k', labelsize=20)
    axes[0].set_title('Actual', fontsize=18)
    axes[1].set_title('Predicted', fontsize=18)
    plt.show()
```

```

def plot_confusion(accuracy, confusion, part):
    print(f'{part} Accuracy: {accuracy}')

    fig, ax = plt.subplots()
    im = ax.imshow(confusion)

    ax.set_xticks(range(num_cat))
    ax.set_yticks(range(num_cat))
    ax.set_xticklabels(categories)
    ax.set_yticklabels(categories)

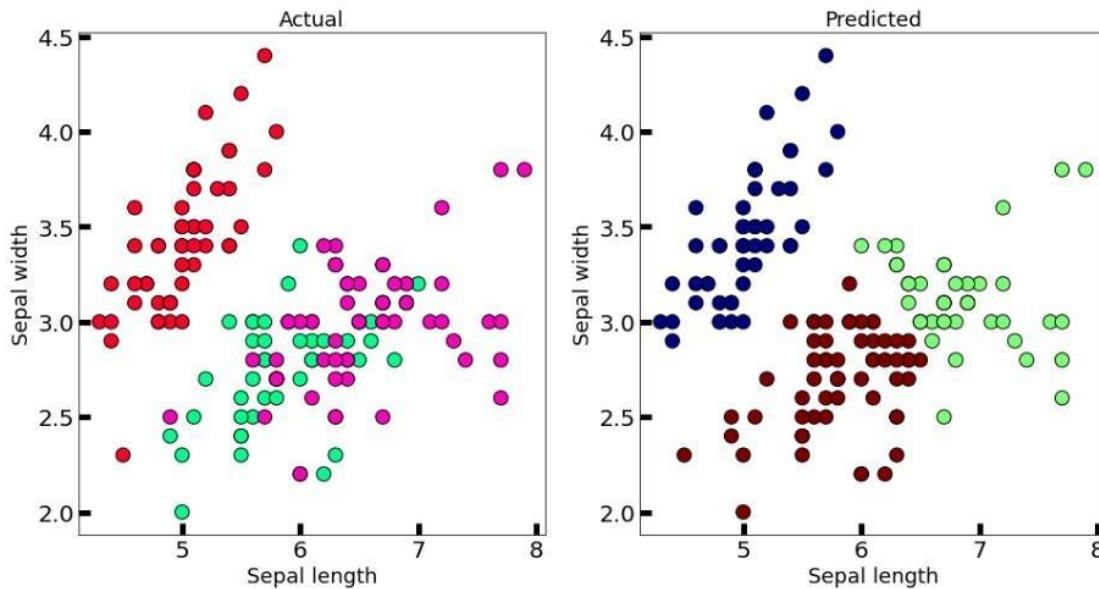
    plt.setp(ax.get_xticklabels(), rotation=45, ha="right",
             rotation_mode="anchor")

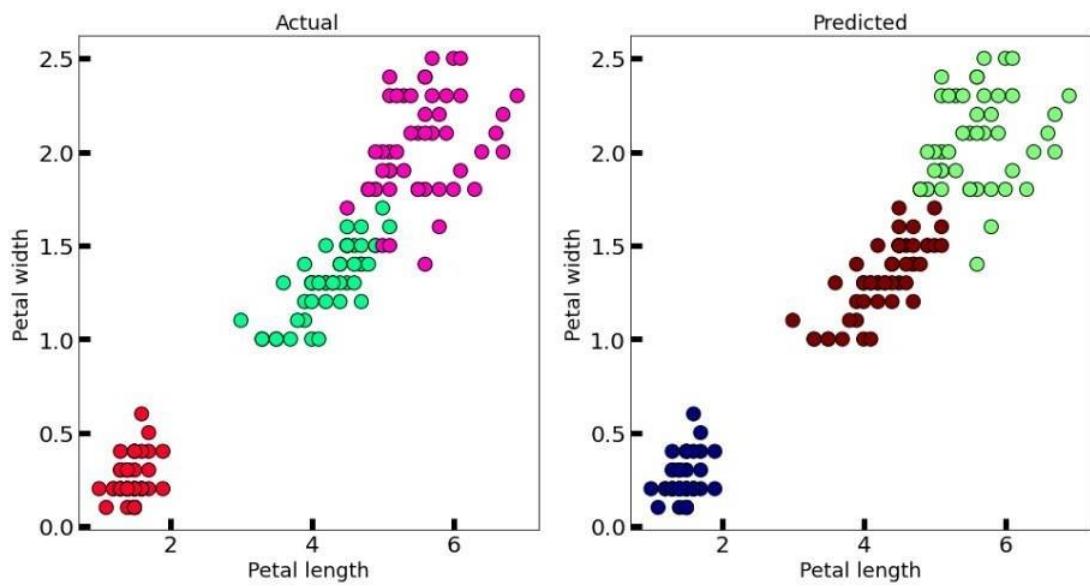
    for i in range(num_cat):
        for j in range(num_cat):
            text = ax.text(j, i, confusion[i, j],
                           ha="center", va="center", color="w")

    ax.set_title(f'{part} Confusion Matrix (Actual / Predicted)')
    fig.tight_layout()
    plt.show()

```

In [7]: `plot_actualvpredicted(sepal_X, y, sepal_labels, 'Sepal')`  
`plot_actualvpredicted(petal_X, y, petal_labels, 'Petal')`



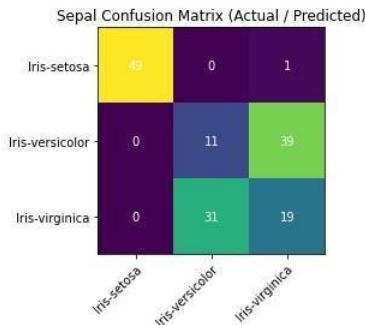


```
In [8]: sepal_accuracy = accuracy_score(y, sepal_labels)
petal_accuracy = accuracy_score(y, petal_labels)

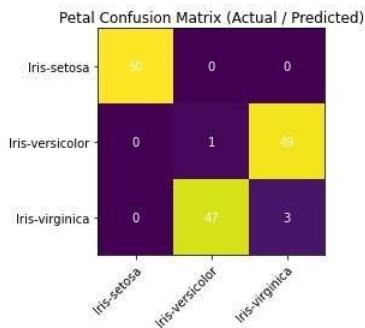
sepal_confusion = confusion_matrix(y, sepal_labels)
petal_confusion = confusion_matrix(y, petal_labels)
```

```
In [9]: plot_confusion(sepal_accuracy, sepal_confusion, 'Sepal')
plot_confusion(petal_accuracy, petal_confusion, 'Petal')
```

Sepal Accuracy: 0.5266666666666666



Petal Accuracy: 0.36



## Comparison with K-Means

When we compare the results of the GaussianMixture model (uses EM algorithm) with that of [K-Means clustering](#) we observe that both give almost equal accuracies:

- K-Means: 0.5133333333333333 (Sepal) & 0.3733333333333335 (Petal)
- GaussianMixture: 0.5333333333333333 (Sepal) & 0.02 (Petal)

GaussianMixture performs slightly better when classified based on the Sepal length & width. Likewise K-Means performs slightly better when classified based on the Petal length & width.

```
In [ ]:
```

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### EM Algorithm

- ① The very first step is to initialize the parameter values. Further, the system is provided with incomplete observed data with the assumption that data is obtained from a specific Model.
- ② This step is known as Expectation or E-step, which is used to estimate or guess the values of the missing or incomplete data using the observed data. Further, E-step primarily updates the variables.
- ③ This step is known as Maximization or M-step, where we use complete data obtained from the 2nd step to update the parameter values. Further, M-step primarily updates the hypothesis.
- ④ The last step is to check if the values of latent variables are converging or not. If it gets yes then stop the process. Else repeat the process from step 2 until the convergence occurs.

**Program 8:** Write a program to implement k-Nearest Neighbour algorithm to classify the iris data set. Print both correct and wrong predictions.

```
In [1]: import matplotlib.pyplot as plt
import numpy as np
import pandas as pd
from sklearn.neighbors import KNeighborsClassifier
from sklearn.metrics import accuracy_score, confusion_matrix, classification_report
from sklearn.model_selection import train_test_split
```

## Data

```
In [2]: data = pd.read_csv('../input/iris/Iris.csv')
```

```
In [3]: data.head()
```

```
Out[3]:
```

	<b>Id</b>	<b>SepalLengthCm</b>	<b>SepalWidthCm</b>	<b>PetalLengthCm</b>	<b>PetalWidthCm</b>	<b>Species</b>
<b>0</b>	1	5.1	3.5	1.4	0.2	Iris-setosa
<b>1</b>	2	4.9	3.0	1.4	0.2	Iris-setosa
<b>2</b>	3	4.7	3.2	1.3	0.2	Iris-setosa
<b>3</b>	4	4.6	3.1	1.5	0.2	Iris-setosa
<b>4</b>	5	5.0	3.6	1.4	0.2	Iris-setosa

```
In [4]: data.describe()
```

```
Out[4]:
```

	<b>Id</b>	<b>SepalLengthCm</b>	<b>SepalWidthCm</b>	<b>PetalLengthCm</b>	<b>PetalWidthCm</b>
<b>count</b>	150.000000	150.000000	150.000000	150.000000	150.000000
<b>mean</b>	75.500000	5.843333	3.054000	3.758667	1.198667
<b>std</b>	43.445368	0.828066	0.433594	1.764420	0.763161
<b>min</b>	1.000000	4.300000	2.000000	1.000000	0.100000
<b>25%</b>	38.250000	5.100000	2.800000	1.600000	0.300000
<b>50%</b>	75.500000	5.800000	3.000000	4.350000	1.300000
<b>75%</b>	112.750000	6.400000	3.300000	5.100000	1.800000
<b>max</b>	150.000000	7.900000	4.400000	6.900000	2.500000

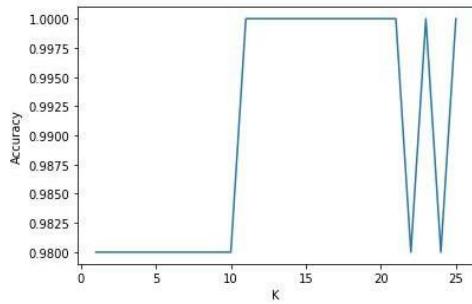
```
In [5]: X = data[['SepalLengthCm', 'SepalWidthCm', 'PetalLengthCm', 'PetalWidthCm']]
sepal_X = data[['SepalLengthCm', 'SepalWidthCm']]
petal_X = data[['PetalLengthCm', 'PetalWidthCm']]
y = data['Species'].astype("category").cat.codes
num_cat = y.unique()
categories = data['Species'].astype("category").cat.categories
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.33, random_state=42)
```

## Model

```
In [6]: scores = []
scores_list = []
for k in range(1, 26):
    knn = KNeighborsClassifier(n_neighbors=k)
    knn.fit(X_train, y_train)
    y_pred = knn.predict(X_test)
    scores[k] = accuracy_score(y_test, y_pred)
    scores_list.append(scores[k])
```

## Analysis

```
In [7]: plt.plot(range(1, 26), scores_list)
plt.xlabel('K')
plt.ylabel('Accuracy')
plt.show()
```



```
In [8]: knn = KNeighborsClassifier(n_neighbors=5)
knn.fit(X_train, y_train)
y_pred = knn.predict(X_test)
print("Confusion Matrix")
print(confusion_matrix(y_test, y_pred))
print(f"Correct Predictions: {accuracy_score(y_test, y_pred)}")
print(f"Wrong Predictions: {1 - accuracy_score(y_test, y_pred)}")
print("Accuracy Metrics:")
print(classification_report(y_test, y_pred))
```

```
Confusion Matrix
[[19  0  0]
 [ 0 15  0]
 [ 0  1 15]]
Correct Predictions: 0.98
Wrong Predictions: 0.02000000000000018
Accuracy Metrics:
      precision    recall  f1-score   support
          0       1.00     1.00     1.00      19
          1       0.94     1.00     0.97      15
          2       1.00     0.94     0.97      16

   accuracy                           0.98
  macro avg       0.98     0.98     0.98      50
weighted avg       0.98     0.98     0.98      50
```

```
In [ ]:
```

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### K-Nearest Neighbour Algorithm.

Step 1: Select the number of the neighbours

Step 2: Calculate the Euclidean distance of K number of Neighbours.

Step 3: Take the k nearest neighbors as per the calculated Euclidean distance.

Step 4: Among these k neighbors, count the number of the data points in each category.

Step 5: Assign the new data points to that category for which the number of the neighbor is maximum.

Step 6: Our model is ready.

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## Program 9: Implement the Linear Regression algorithm in order to fit data points. Select appropriate data set for your experiment and draw graphs.

```
In [1]: import matplotlib.pyplot as plt
import numpy as np
import pandas as pd
from sklearn.model_selection import train_test_split
from sklearn.linear_model import LinearRegression
from sklearn.metrics import mean_squared_error
```

### Data

```
In [2]: df = pd.read_csv('../input/housesalesprediction/kc_house_data.csv')
```

```
In [3]: df.head()
```

```
Out[3]:
```

	id	date	price	bedrooms	bathrooms	sqft_living	sqft_lot	floors	waterfront	view	...	grade	sqft_above
0	7129300520	20141013T000000	221900.0	3	1.00	1180	5650	1.0	0	0	...	7	1180
1	6414100192	20141209T000000	538000.0	3	2.25	2570	7242	2.0	0	0	...	7	2170
2	5631500400	20150225T000000	180000.0	2	1.00	770	10000	1.0	0	0	...	6	770
3	2487200875	20141209T000000	604000.0	4	3.00	1960	5000	1.0	0	0	...	7	1050
4	1954400510	20150218T000000	510000.0	3	2.00	1680	8080	1.0	0	0	...	8	1680

5 rows × 21 columns

```
In [4]: X = np.array(df['sqft_living']).reshape(-1, 1)
y = df['price']
```

```
In [5]: X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.33, random_state=42)
```

### Model

```
In [6]: model = LinearRegression()
model.fit(X_train, y_train)
# model.fit(X, y)
```

```
Out[6]: LinearRegression()
```

### Analysis

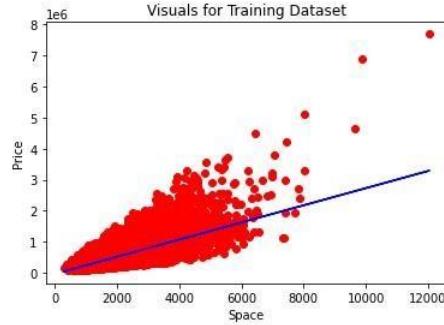
```
In [7]: y_pred = model.predict(X_test)
print(f"Mean Squared Error: {mean_squared_error(y_pred, y_test)}")
```

Mean Squared Error: 76715223988.35832

```
In [8]: #Visualizing the training Test Results
plt.scatter(X_train, y_train, color='red')
```

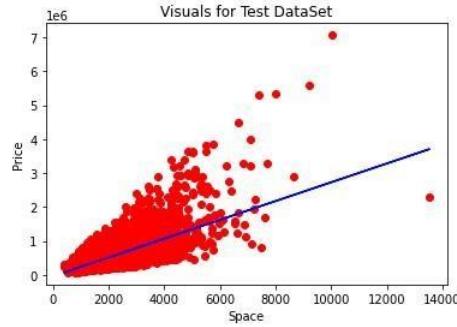
```
In [8]:
```

```
#Visualizing the training Test Results
plt.scatter(X_train, y_train, color= 'red')
plt.plot(X_train, model.predict(X_train), color = 'blue')
plt.title ("Visuals for Training DataSet")
plt.xlabel("Space")
plt.ylabel("Price")
plt.show()
```



```
In [9]:
```

```
#Visualizing the Test Results
plt.scatter(X_test, y_test, color= 'red')
plt.plot(X_test, model.predict(X_test), color = 'blue')
plt.title("Visuals for Test DataSet")
plt.xlabel("Space")
plt.ylabel("Price")
plt.show()
```



```
In [ ]:
```

## ALGORITHM:

### LINEAR REGRESSION.

1. Reading and understanding the data
2. Visualizing the data (Exploratory Data Analysis)
3. Data Preparation
4. Splitting the data into training and test sets
5. Building a linear model
6. Residual analysis of the train data
7. Making predictions using the final model and evaluation

$$\hat{Y}_i = b_1 x_i + b_0$$

$$b_0 = \frac{(\sum y)(\sum x^2) - (\sum x)(\sum xy)}{n(\sum x^2) - (\sum x)^2}$$

$$b_1 = \frac{n(\sum xy) - (\sum x)(\sum y)}{n(\sum x^2) - (\sum x)^2}$$

**Program 10:** Implement the non-parametric Locally Weighted Regression algorithm in order to fit data points. Select appropriate data set for your experiment and draw graphs.

```
In [1]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
```

## Functions

```
In [2]: # kernel smoothing function
def kernel(point, xmat, k):
    m,n = np.shape(xmat)
    weights = np.mat(np.eye((m)))

    for j in range(m):
        diff = point - X[j]
        weights[j, j] = np.exp(diff * diff.T / (-2.0 * k**2))

    return weights

# function to return local weight of each training example
def localWeight(point, xmat, ymat, k):
    wt = kernel(point, xmat, k)
    W = (X.T * (wt*X)).I * (X.T * wt * ymat.T)
    return W

# root function that drives the algorithm
def localWeightRegression(xmat, ymat, k):
    m,n = np.shape(xmat)
    ypred = np.zeros(m)

    for i in range(m):
        ypred[i] = xmat[i] * localWeight(xmat[i], xmat, ymat, k)

    return ypred
```

## Data

```
In [3]: #import data
data = pd.read_csv('../input/tipsdata/tips.csv')

# place them in suitable data types
colA = np.array(data.total_bill)
colB = np.array(data.tip)

mcolA = np.mat(colA)
mcolB = np.mat(colB)

m = np.shape(mcolB)[1]
one = np.ones((1, m), dtype = int)

# horizontal stacking
X = np.hstack((one.T, mcolA.T))
print(X.shape)
```

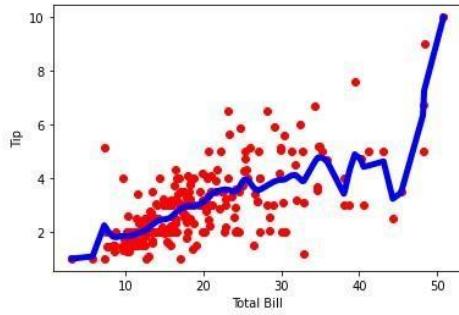
(244, 2)

## Model

```
In [4]: # predicting values using LWLR  
ypred = localWeightRegression(X, mcolB, 0.8)
```

## Analysis

```
In [5]: # plotting the predicted graph  
xsort = X.copy()  
xsort.sort(axis=0)  
plt.scatter(colA, colB, color='red')  
plt.plot(xsort[:, 1], ypred[X[:, 1].argsort(0)], color='blue', linewidth=5)  
plt.xlabel('Total Bill')  
plt.ylabel('Tip')  
plt.show()
```



```
In [ ]:
```

## ALGORITHM:

Date \_\_\_\_\_

Page \_\_\_\_\_

### Locally Weighted Regression Algorithm

1. Read the given data sample to  $x$  and the curvilinear or non linear to  $y$
2. Set the value for Smoothening parameter or Free parameter say  $\tau$
3. Set the bias (Point of interest) set  $x_0$  which is a subset of  $x$ .
4. Determine the weight matrix using:  
$$w(x, x_0) = e^{-\frac{(x-x_0)^2}{2\tau^2}}$$
5. Determine the value of model term parameter  $\beta$  using:  
$$\hat{\beta}(x_0) = (x^T w x)^{-1} x^T w y$$

~~of  $\beta$~~  Predict =  $x_0 \cdot \hat{\beta}$

21/6/23

