

Digital Electronics and System

19ECE204

Name : Rithika Sri J

Roll no : CB.EN.U4CSE19D25

Home assignment - 2

$$(1) f(x_1, x_2, x_3, x_4) = \sum m(1, 2, 6, 9, 10, 12, 13, 14, 15)$$

$x_1 x_2$	$x_3 x_4$	00	01	11	10
00		00	1	m_3	1 m_2
01		m_4	m_5	m_7	1 m_6
11		1 m_{12}	1 m_{13}	1 m_8	1 m_{14}
10		m_8	1 m_9	m_{11}	1 m_{10}

$$f(x_1, x_2, x_3, x_4) = \overline{x_2} \overline{x_3} x_4 + x_3 \overline{x_4} + x_1 x_2$$

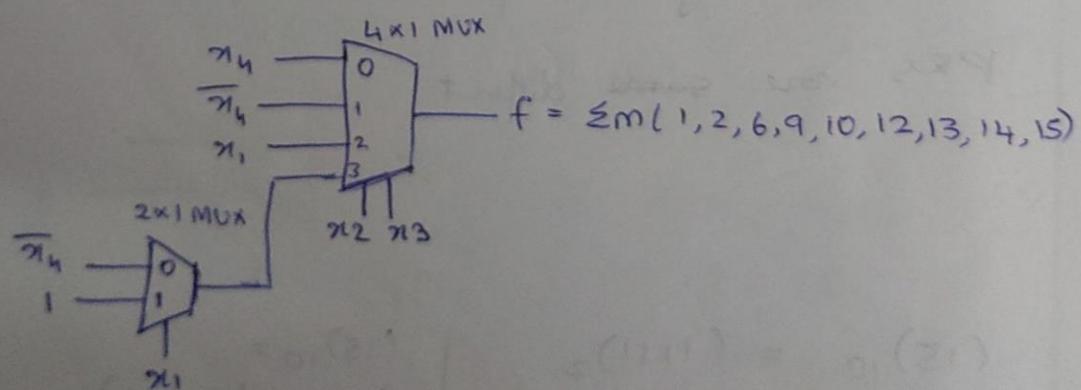
By Shannon expansion Theorem,

$$\begin{aligned} f &= \overline{x_2} \overline{x_3} (1 \cdot 1 \cdot x_4 + 0 \cdot \overline{x_4} + x_1 \cdot 0) + \overline{x_2} x_3 (1 \cdot 0 \cdot x_4 + 1 \cdot \overline{x_4} + x_1 \cdot 0) + x_2 \overline{x_3} (0 \cdot 1 \cdot x_4 + 0 \cdot \overline{x_4} + x_1 \cdot 1) + \\ &\quad x_2 x_3 (0 \cdot 0 \cdot x_4 + 1 \cdot \overline{x_4} + x_1 \cdot 1) \\ &= \overline{x_2} \overline{x_3} (x_4) + \overline{x_2} x_3 (\overline{x_4}) + x_2 \overline{x_3} (x_1) + x_2 x_3 (\overline{x_4} + x_1) \end{aligned}$$

$$\text{Let } g = \overline{x_4} + x_1$$

$$= \overline{x_1} (\overline{x_4} + 0) + x_1 (\overline{x_4} + 1)$$

$$= \overline{x_1} (\overline{x_4}) + x_1 (1)$$

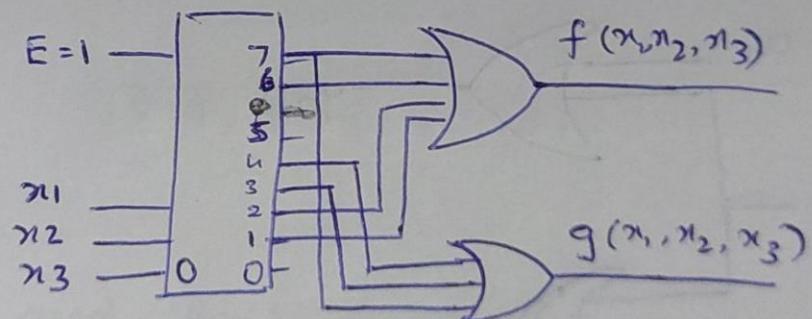


(2)

$$F(x_1, x_2, x_3) = \sum m(1, 2, 6, 7)$$

$$\begin{aligned} G(x_1, x_2, x_3) &= \pi M(0, 1, 2, 5, 6) \\ &= \sum m(3, 4, 7) \end{aligned}$$

In active high decoder,



(3)

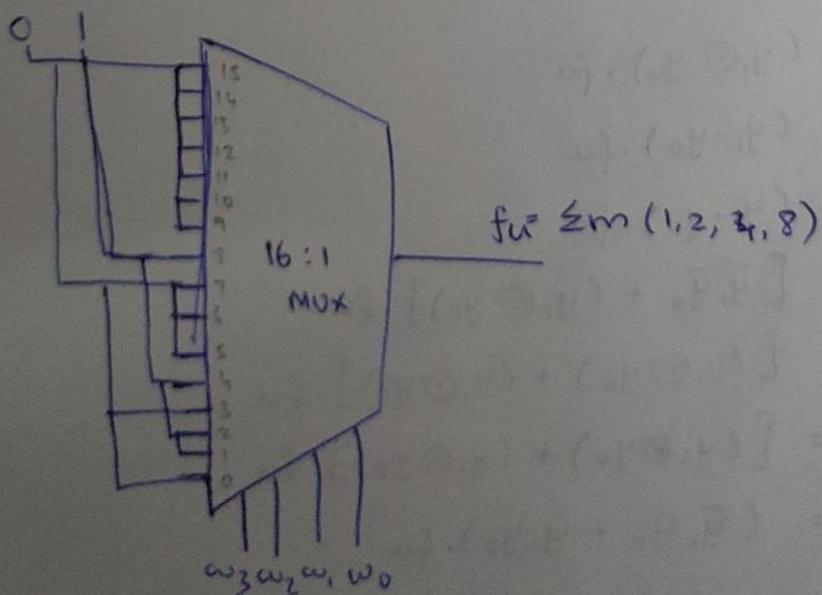
$$\begin{aligned}
 w_0 &\rightarrow \text{coffee} \rightarrow [(a, f, e, d)] \\
 w_1 &\rightarrow \text{tea} \rightarrow [(f, g, e, d)] \\
 w_2 &\rightarrow \text{milk} \rightarrow [(f, e, d)] \\
 w_3 &\rightarrow \text{cocoa} \rightarrow [(e, f, a, b, c, g)]
 \end{aligned}
 \quad
 \begin{array}{c|c}
 a & \\
 \hline
 f & b \\
 \hline
 e & c \\
 \hline
 d &
 \end{array}$$

w_3	w_2	w_1	w_0	y_1	y_0	f_u
0	0	0	0	*	*	0
0	0	0	1	0	0	1
0	0	1	0	0	1	1
0	1	0	0	1	0	1
1	0	0	0	1	1	1

To ensure that exactly only one switch is selected : $f_u = \bar{w}_3\bar{w}_2\bar{w}_1w_0 + \bar{w}_3\bar{w}_2w_1\bar{w}_0 + \bar{w}_3w_2\bar{w}_1\bar{w}_0 + w_3\bar{w}_2\bar{w}_1\bar{w}_0$

$$f_u = \sum m(1, 2, 4, 8)$$

In 16×1 MUX:

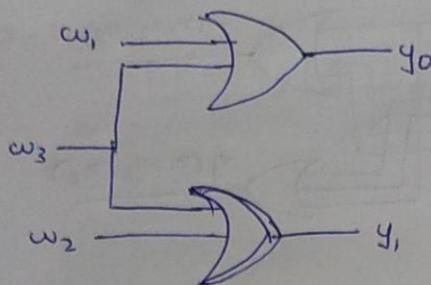


From the table,

$$y_0 = w_1 + w_3$$

$$y_1 = w_2 + w_3$$

Encoder using gates:



To generate seven segment display:

fu	y ₁	y ₀	a	b	c	d	e	f	g
1	0	0	1	0	0	1	1	1	0
1	0	1	0	0	0	1	1	1	1
1	1	0	0	0	0	1	1	1	0
1	1	1	1	1	1	0	1	1	1

From the table,

$$a = y_1'y_0' + y_1y_0 = [y_1 \odot y_0] \cdot fu$$

$$b = c = [y_1 \cdot y_0] \cdot fu$$

$$d = [\bar{y}_1\bar{y}_0 + (\bar{y}_1y_0 + \bar{y}_1y_0)] \cdot fu \\ = [\bar{y}_1\bar{y}_0 + (y_1 \oplus y_0)] \cdot fu$$

$$e = f = (\bar{y}_1\bar{y}_0 + \bar{y}_1y_0 + y_1\bar{y}_0 + y_1y_0) \cdot fu \\ = [(y_1 \oplus y_0) + (y_1 \odot y_0)] \cdot fu$$

$$g = (\bar{y}_1y_0 + y_1y_0) \cdot fu$$

$$a = (y_1 \odot y_0) \cdot fu$$

$$b = (y_1 \cdot y_0) \cdot fu$$

$$c = (y_1 \cdot y_0) \cdot fu$$

$$d = [\bar{y}_1\bar{y}_0 + (y_1 \oplus y_0)] \cdot fu$$

$$e = [(y_1 \oplus y_0) + (y_1 \odot y_0)] \cdot fu$$

$$f = [(y_1 \oplus y_0) + (y_1 \odot y_0)] \cdot fu$$

$$g = (\bar{y}_1y_0 + y_1y_0) \cdot fu$$

$$(4) \quad A = a_3 a_2 a_1 a_0 \quad B = b_3 b_2 b_1 b_0$$

(i) $A = 4$ and $B = 3$

BCD code for 4 : 0100
BCD code for 3 : 0011
 $\underline{+}$
0111

BCD value : 7

(ii)

$A = 7$ and $B = 4$

BCD code for 7 : 0111 (+)
BCD code for 4 : 0100
 $\underline{+}$
1011

Adding 0110 (6),

$$\begin{array}{r} 1011 (+) \\ 0110 \\ \hline 10001 \end{array}$$

BCD value : 11

(iii). $A = 9$ and $B = 8$

BCD code for 9 : 1001 (+)
BCD code for 8 : 1000
 $\underline{+}$
10001

Adding 0110 (6),

$$\begin{array}{r} 10001 (+) \\ 0110 \\ \hline 10111 \end{array}$$

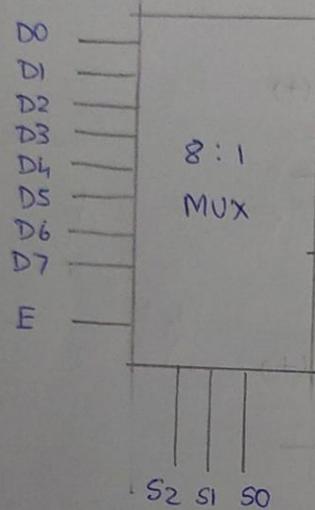
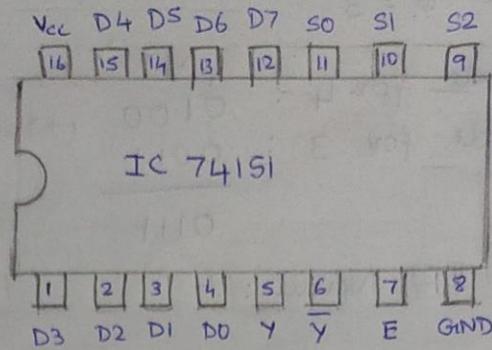
BCD value : 17

(5)

(a)

74151 8:1 MUX

(ii)

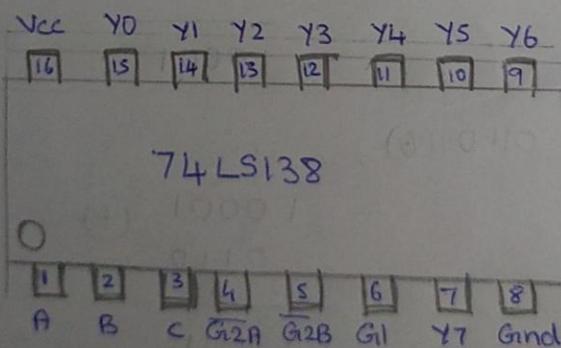


E	S2	S1	S0	Y
0	X	X	X	0
1	0	0	0	D0
1	0	0	1	D1
1	0	1	0	D2
1	0	1	1	D3
1	1	0	0	D4
1	1	0	1	D5
1	1	1	0	D6
1	1	1	1	D7

(b)

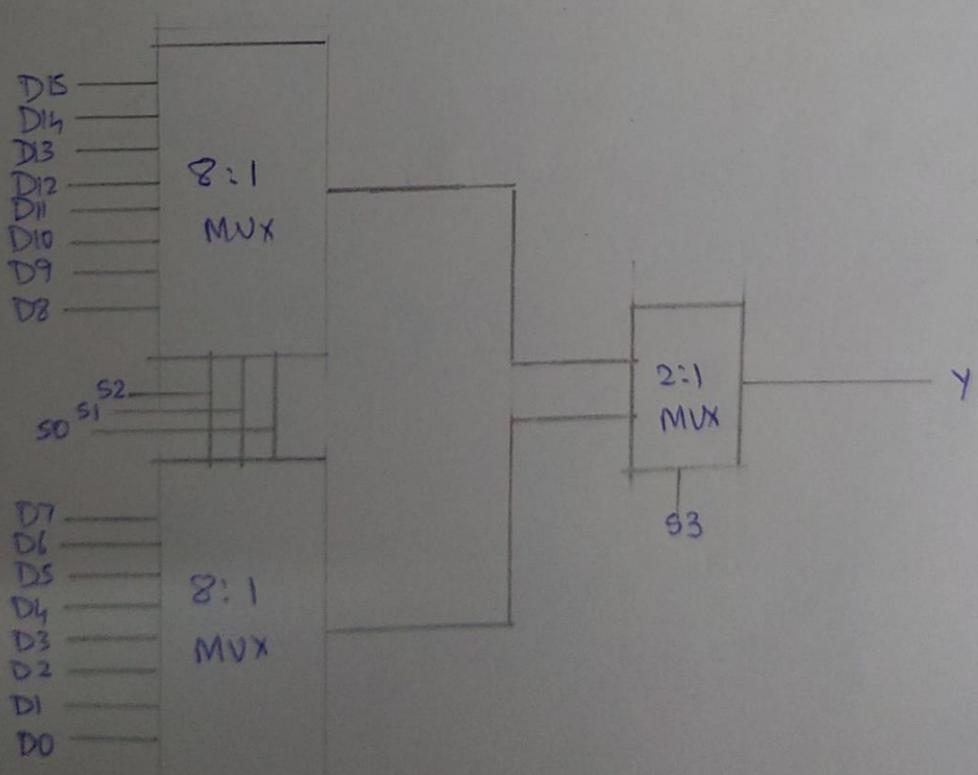
74138 3 to 8 decoder

10



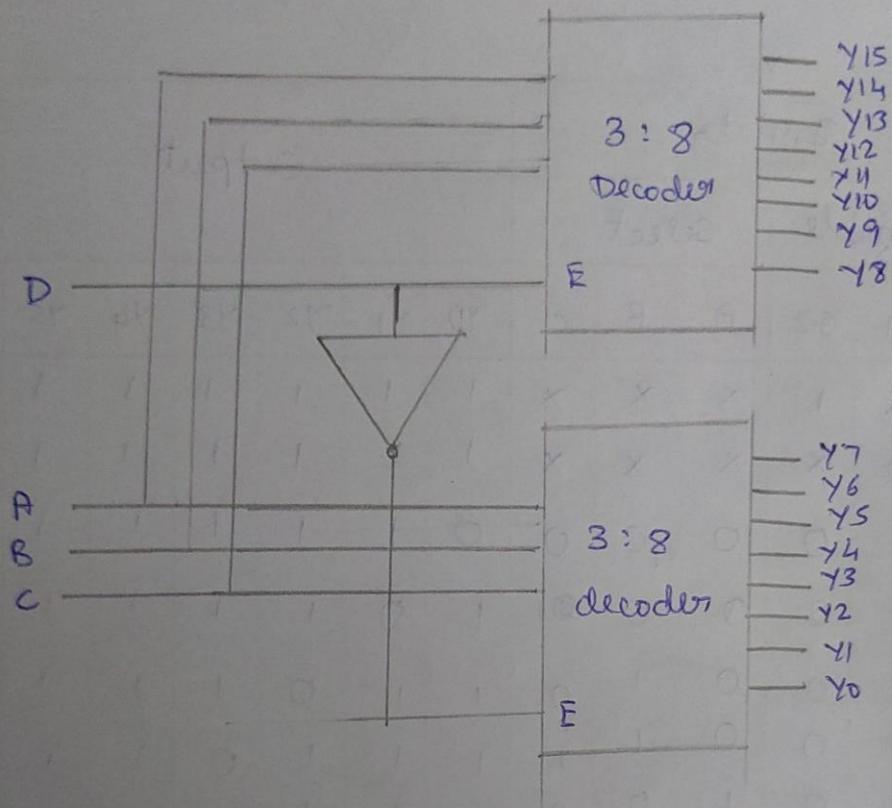
Inputs					Output							
Enable	Select	A	B	C	Y0	Y1	Y2	Y3	Y4	Y5	Y6	Y7
X	1	X	X	X	1	1	1	1	1	1	1	1
0	X	X	X	X	1	1	1	1	1	1	1	1
1	0	0	0	0	0	1	1	1	1	1	1	1
1	0	0	0	0	0	1	0	1	1	1	1	1
1	0	0	1	0	1	1	0	1	1	1	1	1
1	0	0	1	1	1	1	1	0	1	1	1	1
1	0	1	0	0	1	1	1	1	0	1	1	1
1	0	1	0	1	1	1	1	1	1	0	1	1
1	0	1	1	0	1	1	1	1	1	1	0	1
1	0	1	1	1	1	1	1	1	1	1	1	0

(ii) Two 74151 ICs to realize 16:1 MUX:

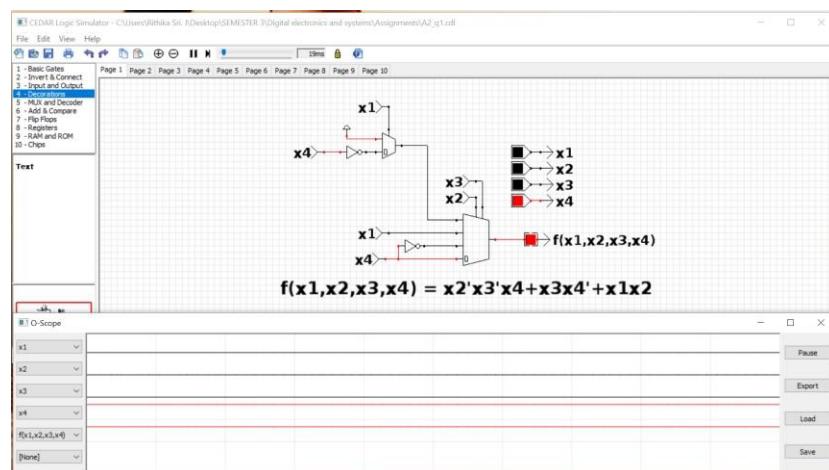
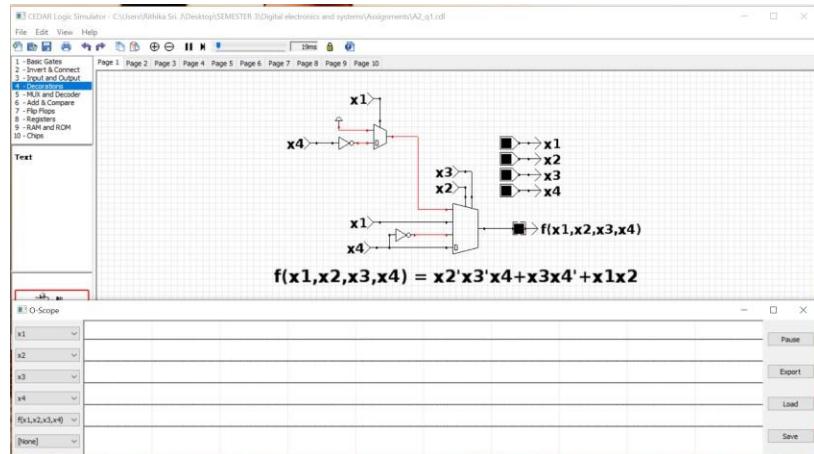
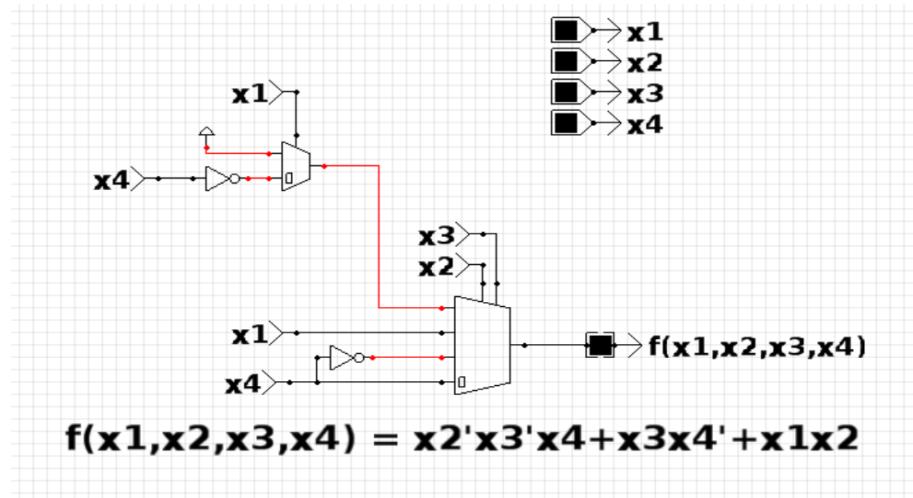


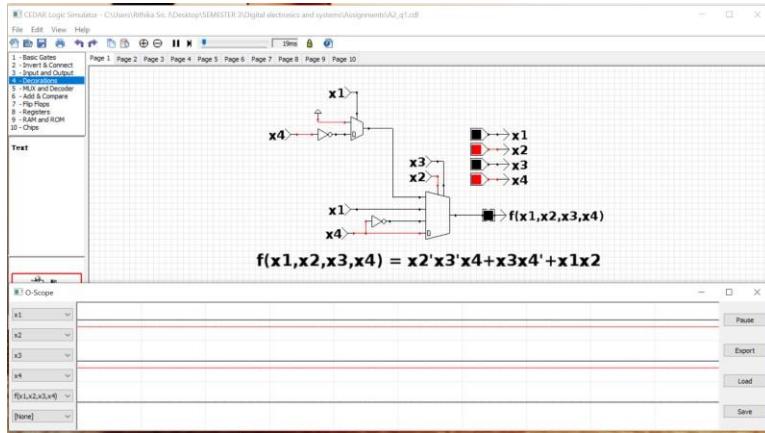
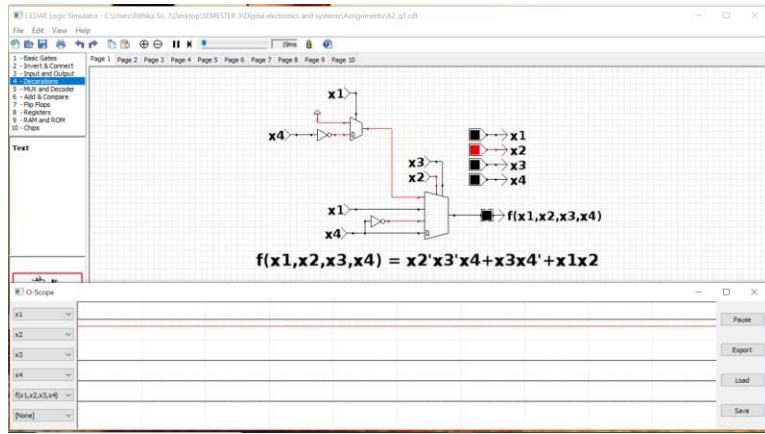
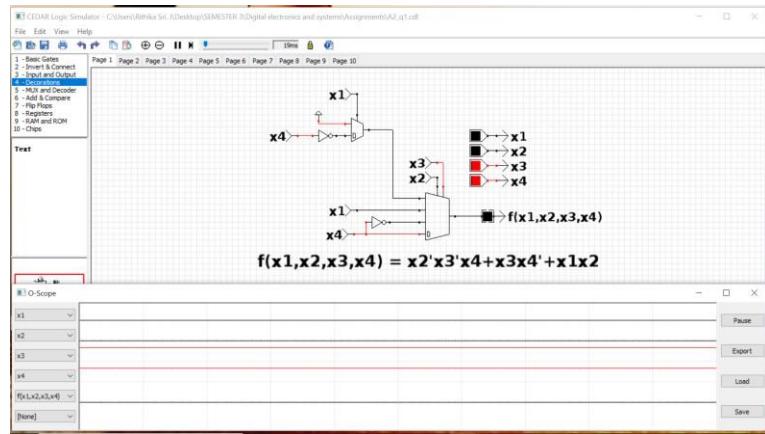
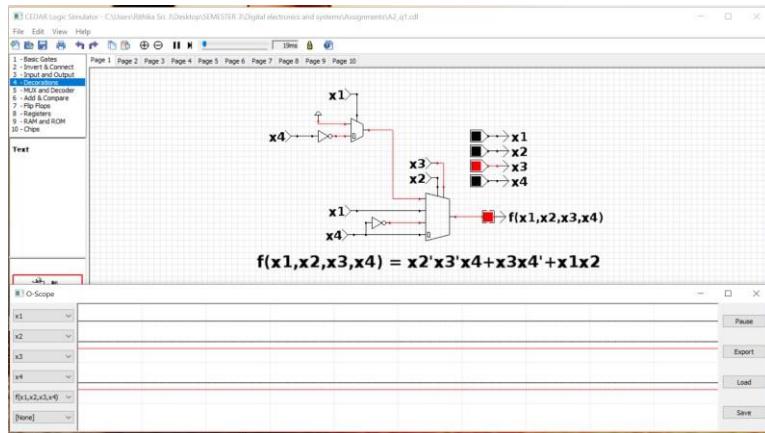
(iii)

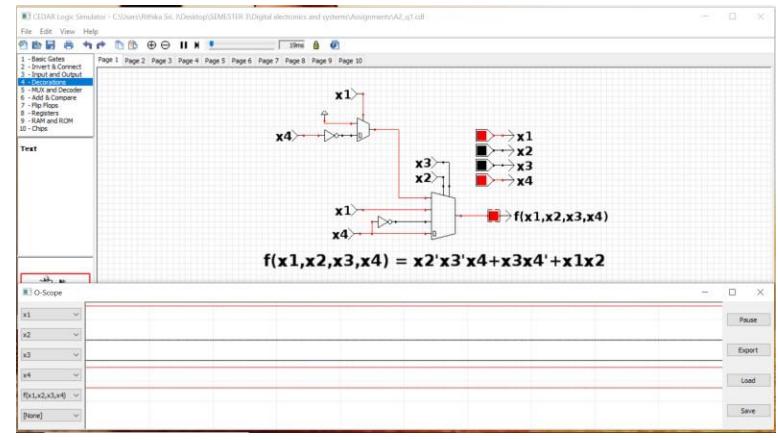
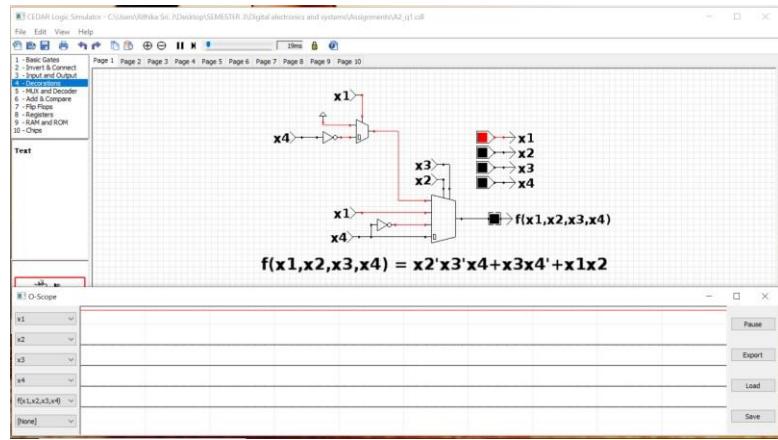
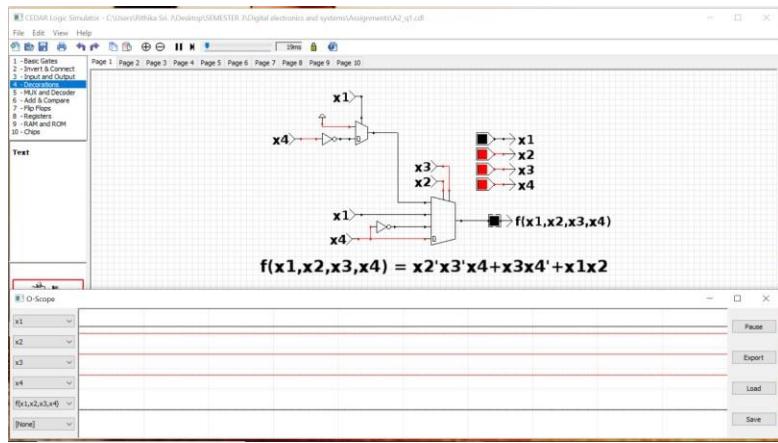
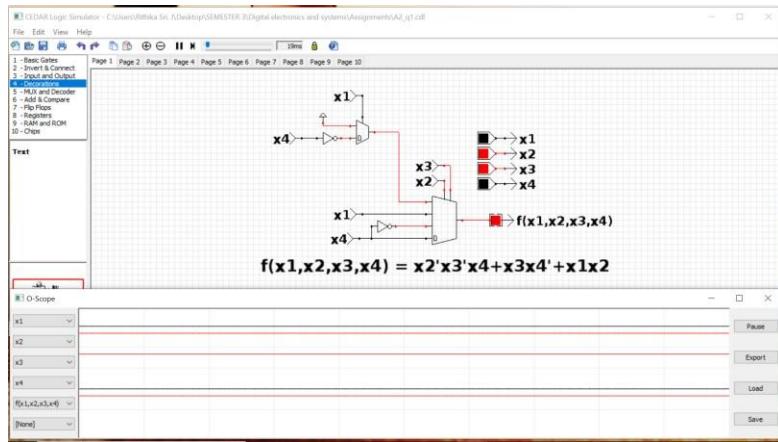
Two 74138 IC to realize 4:16 decoder

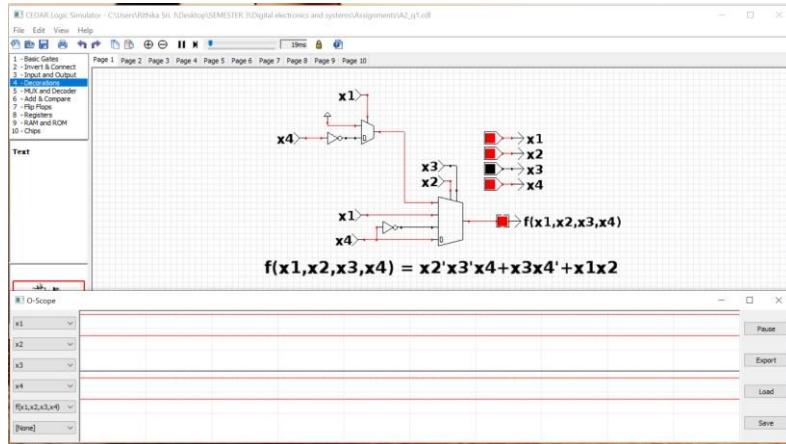
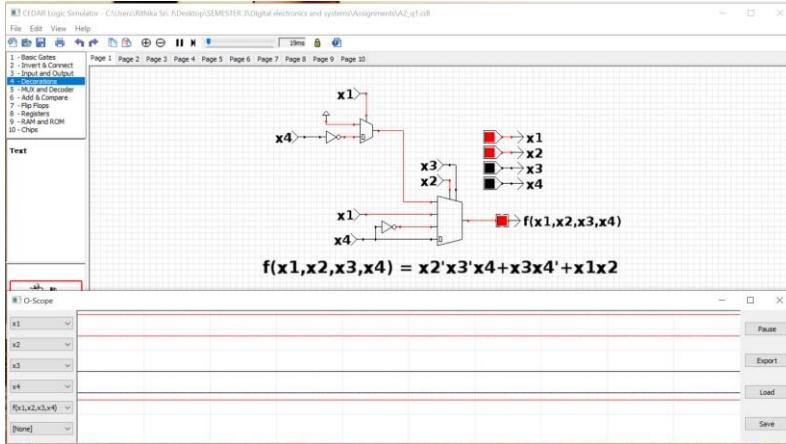
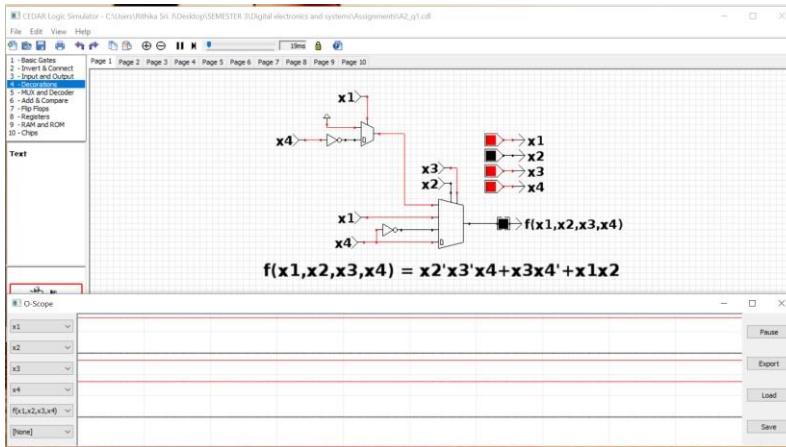
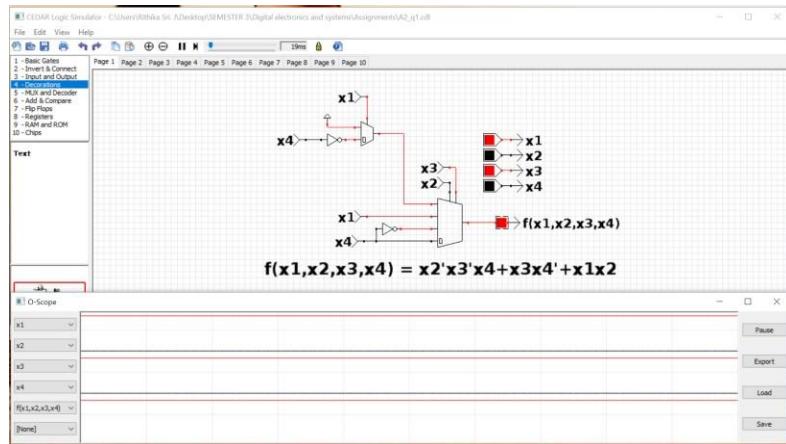


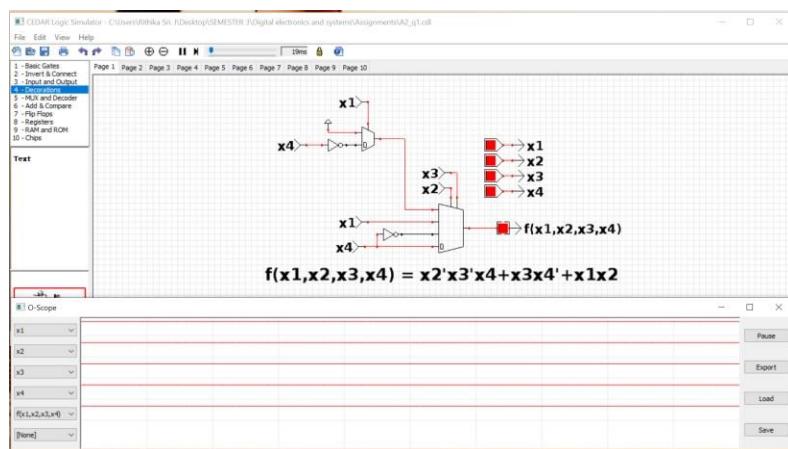
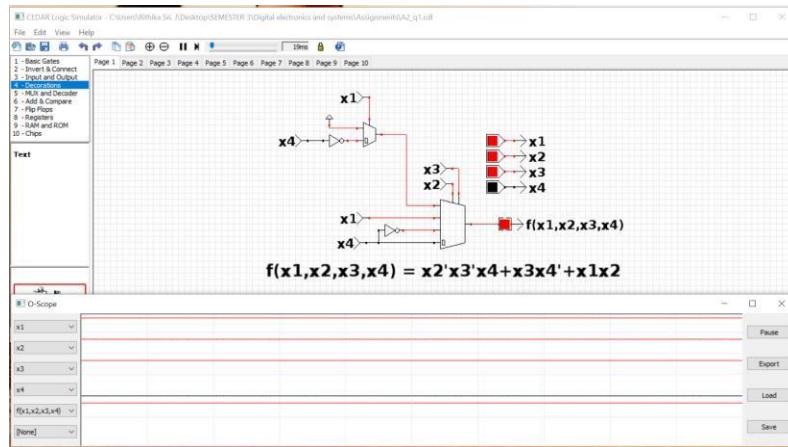
$$(1) F(x_1, x_2, x_3, x_4) = \Sigma m(1, 2, 6, 9, 10, 12, 13, 14, 15)$$





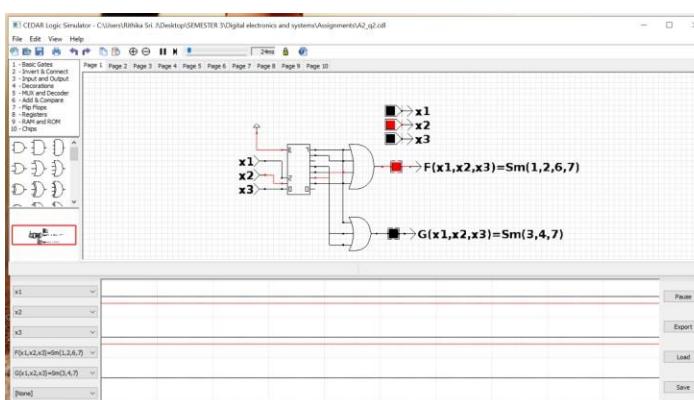
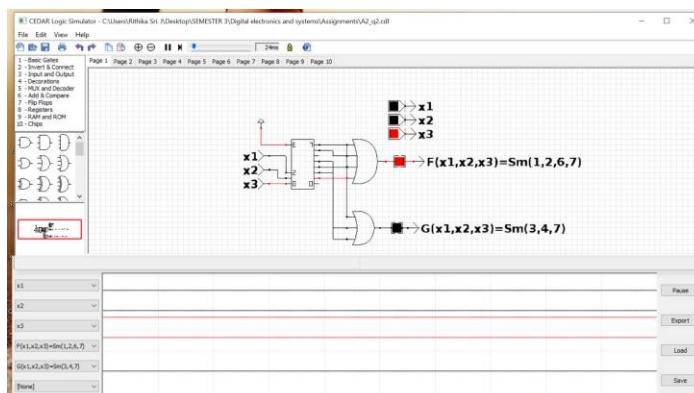
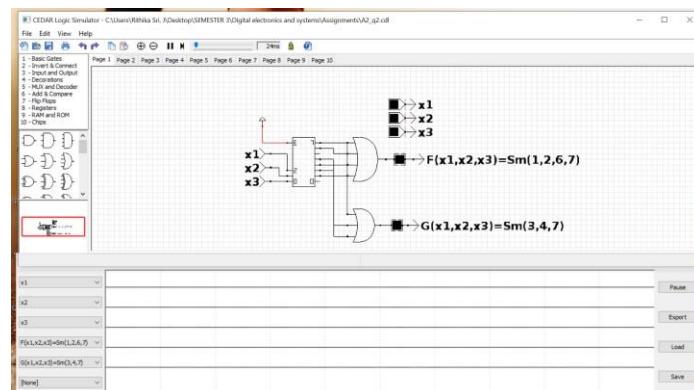
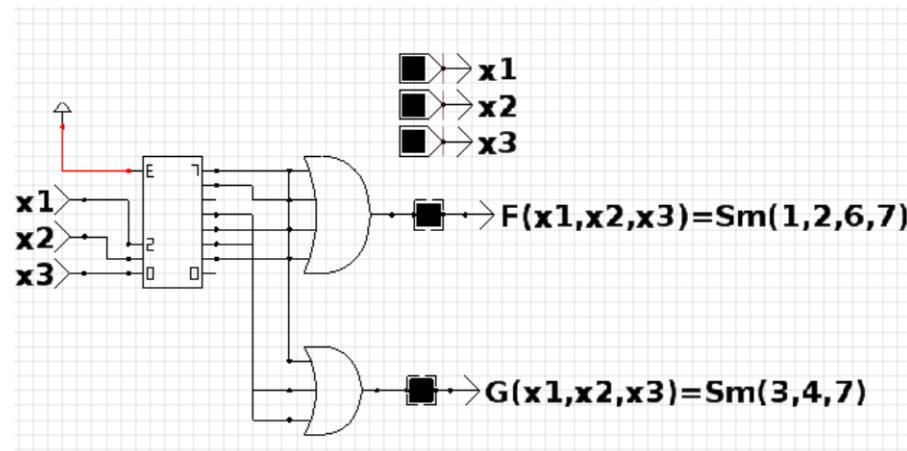


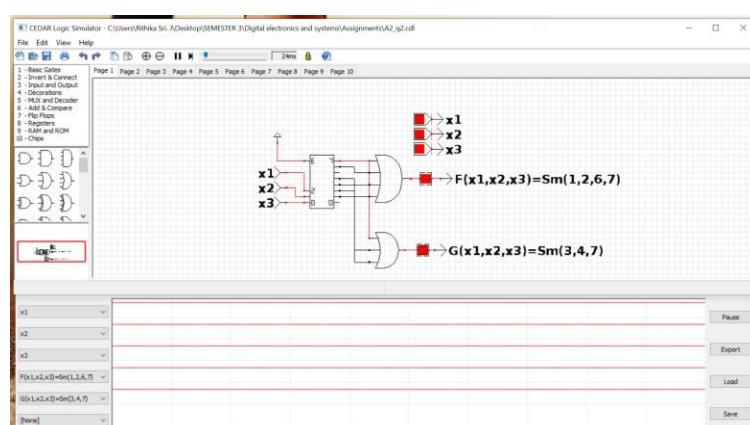
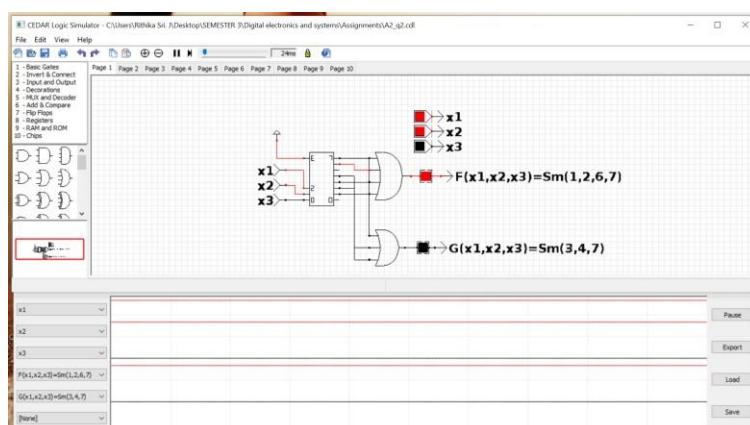
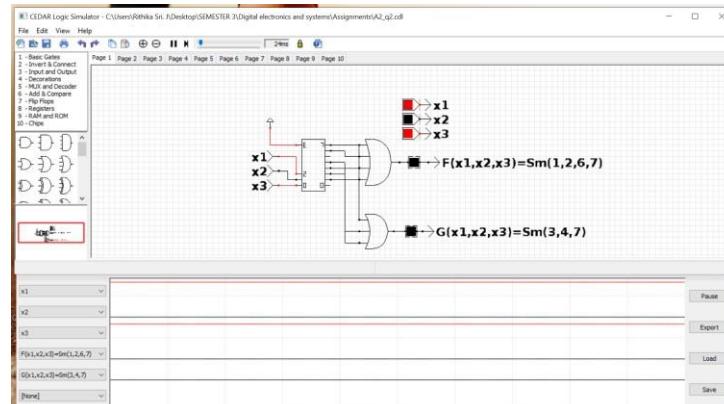
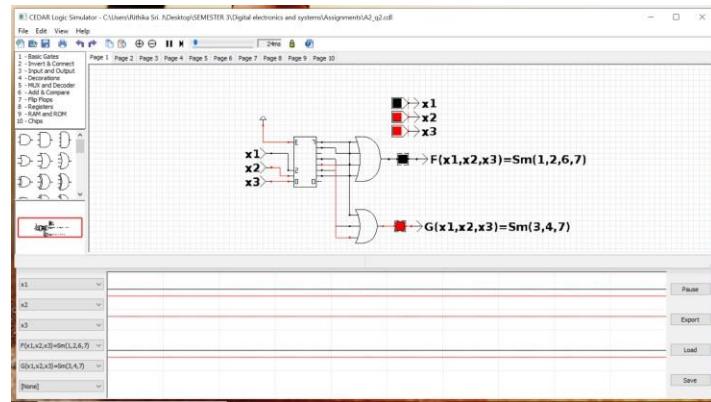




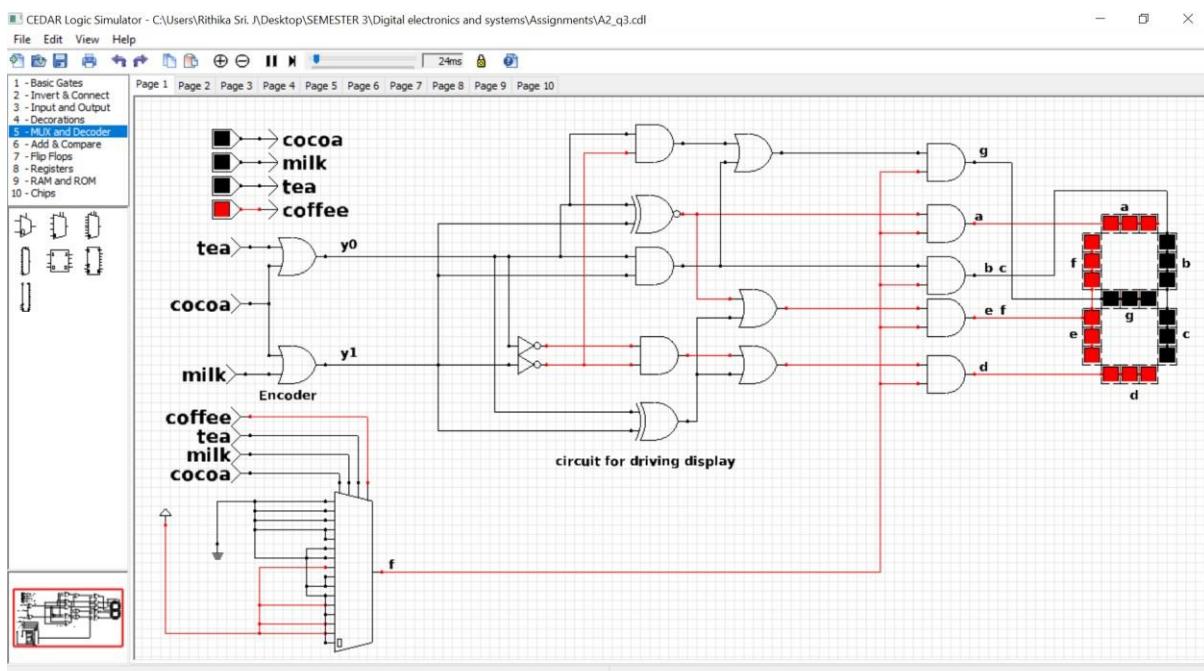
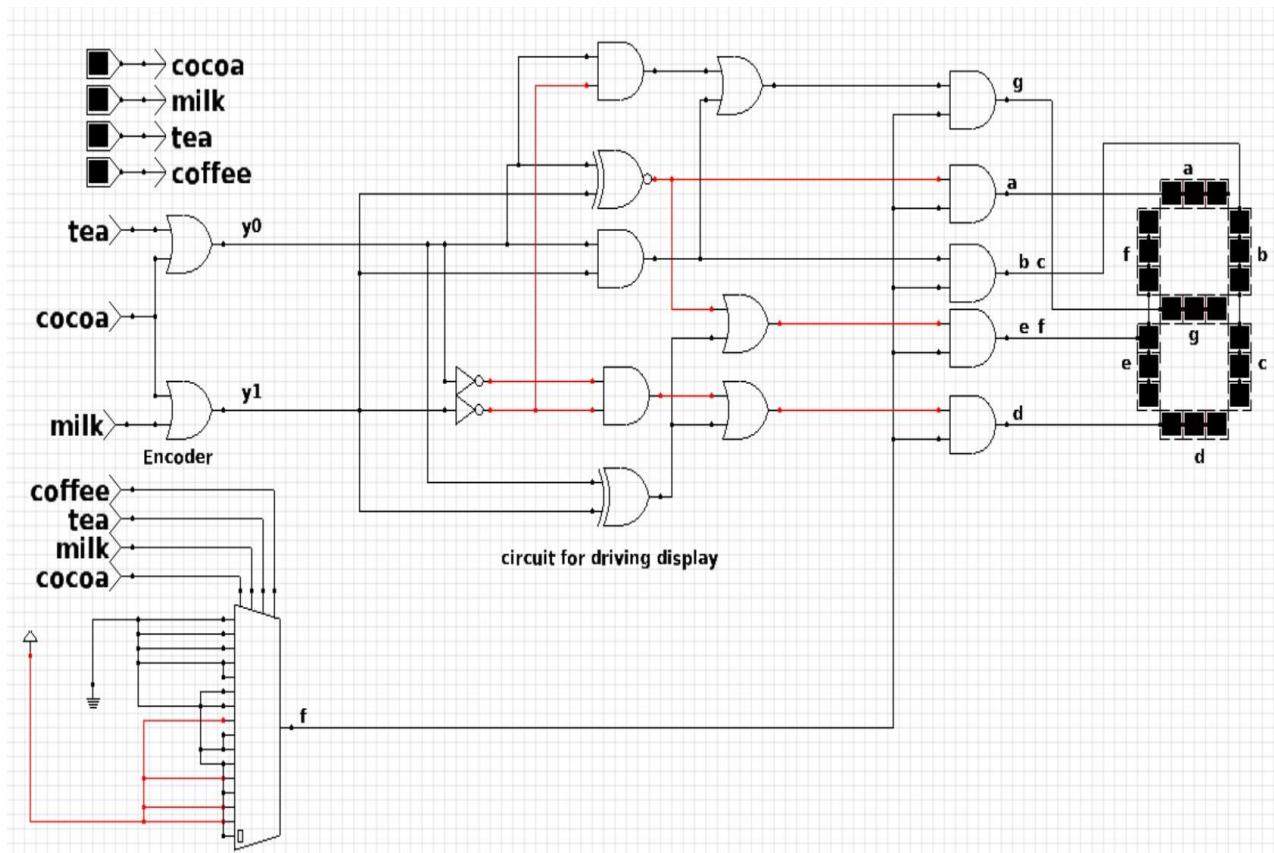
$$(2) F(x_1, x_2, x_3) = \Sigma m(1, 2, 6, 7)$$

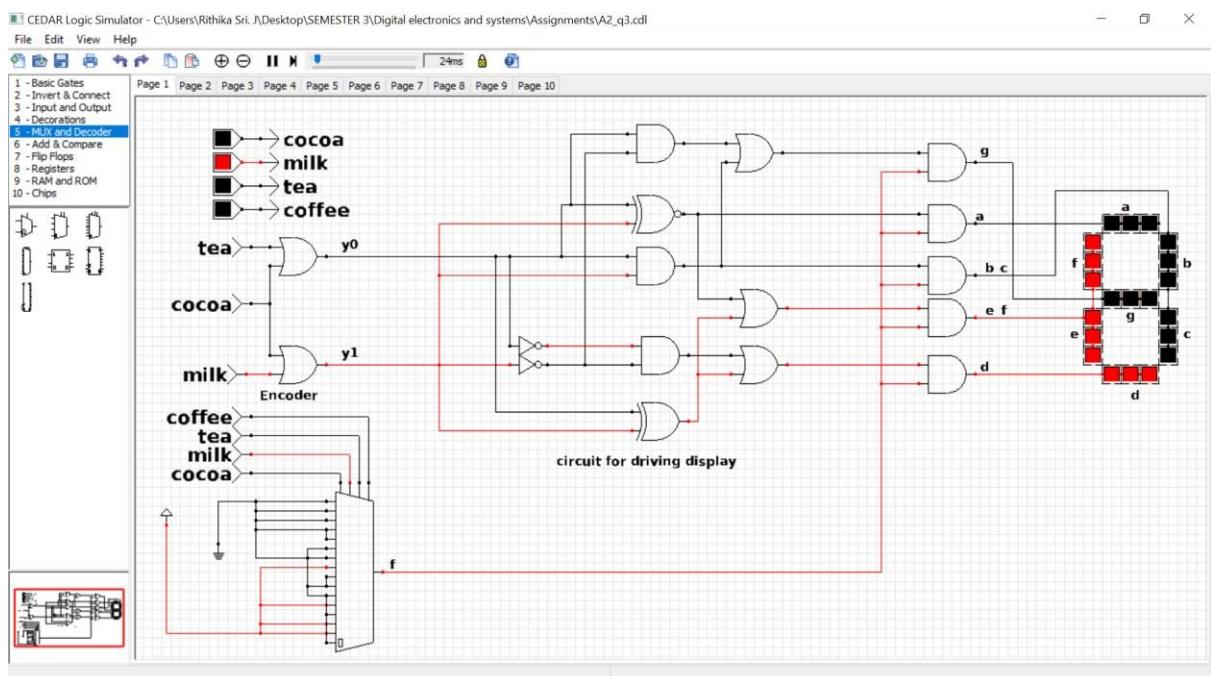
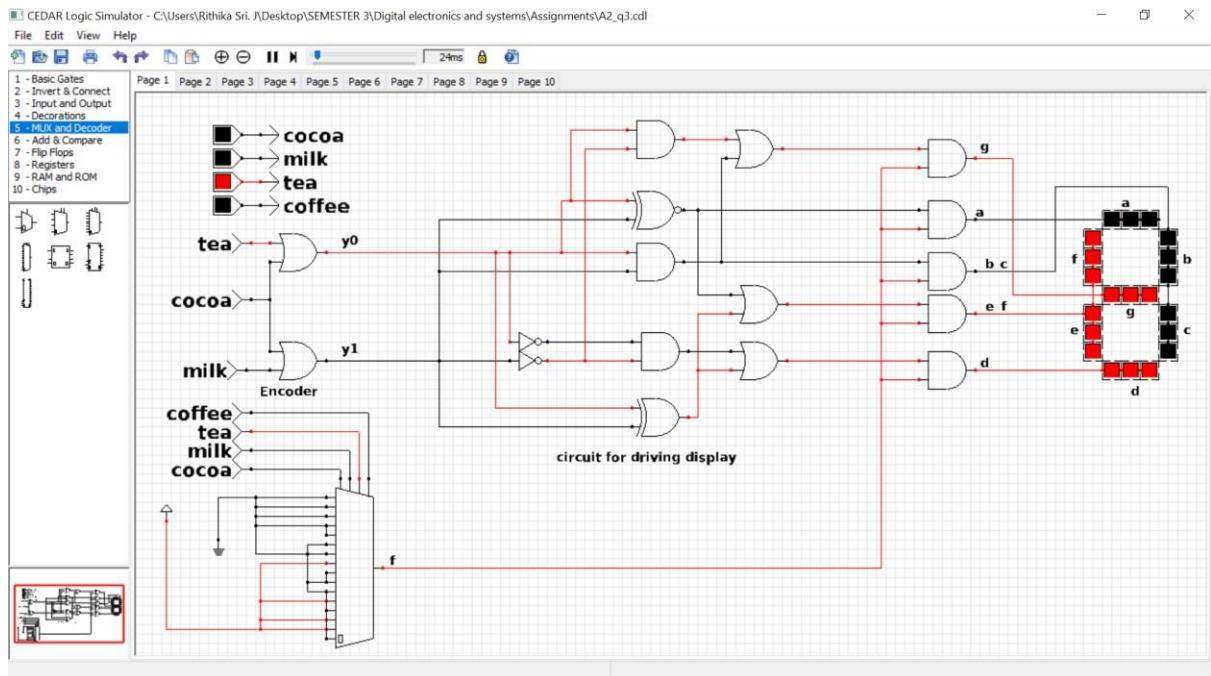
$$G(x_1, x_2, x_3) = \Sigma m(3, 4, 7)$$

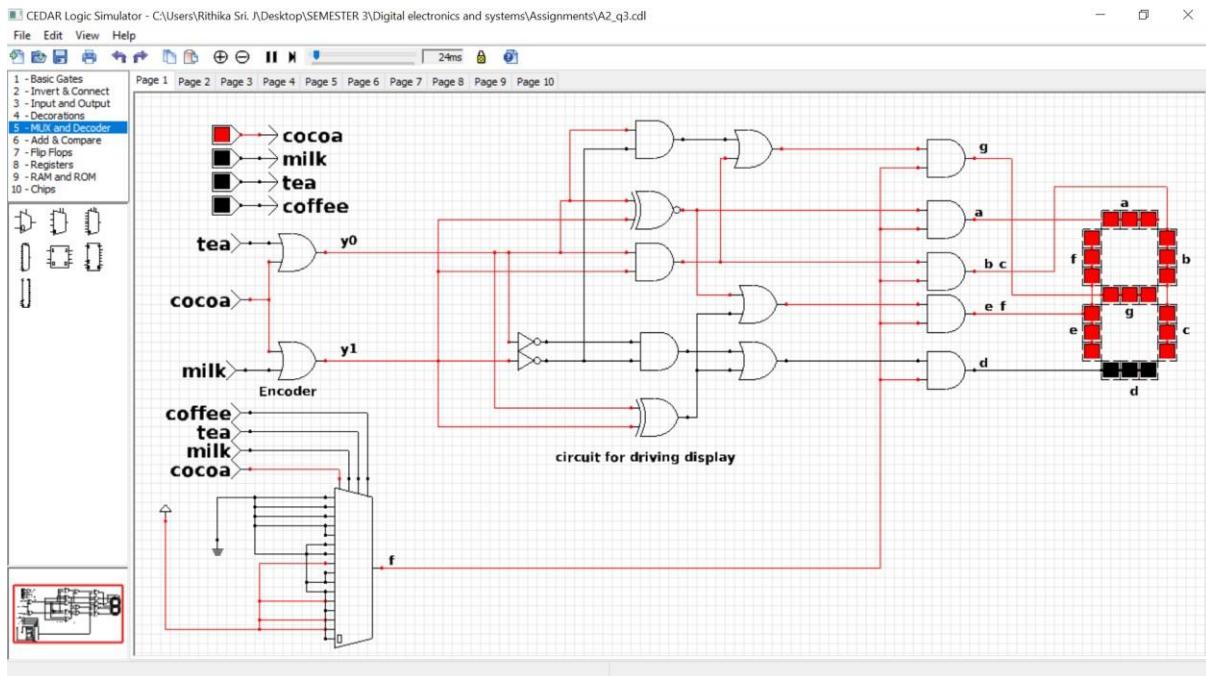




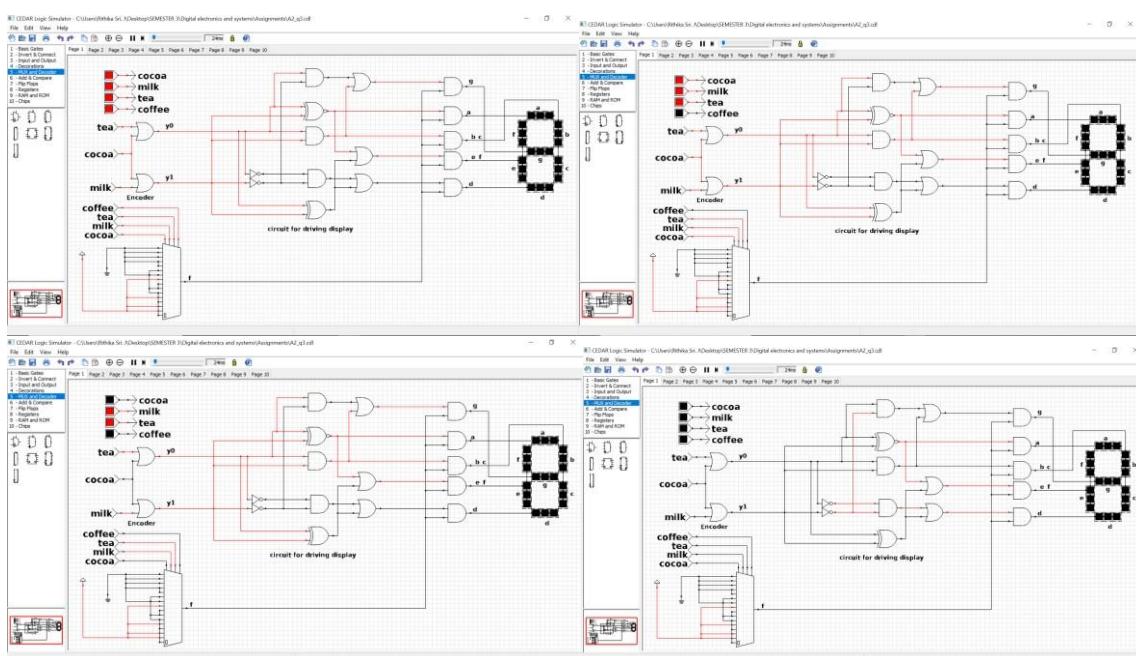
(3)



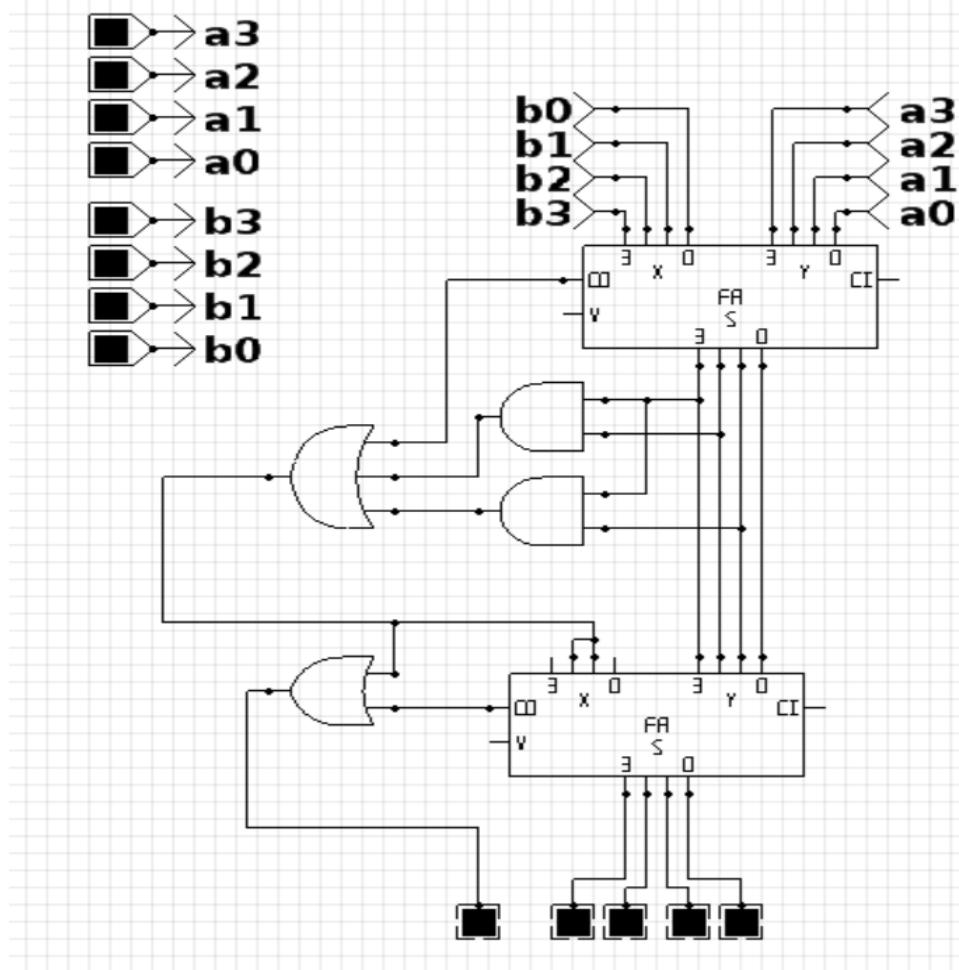




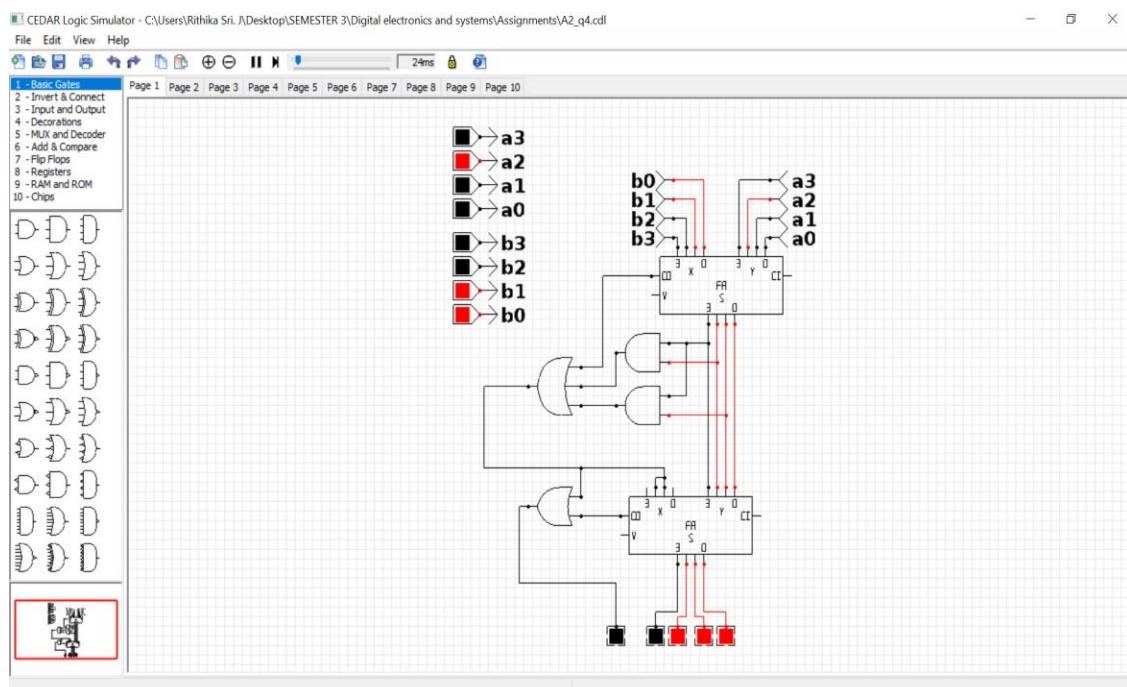
Selecting no switch or more than one switch:



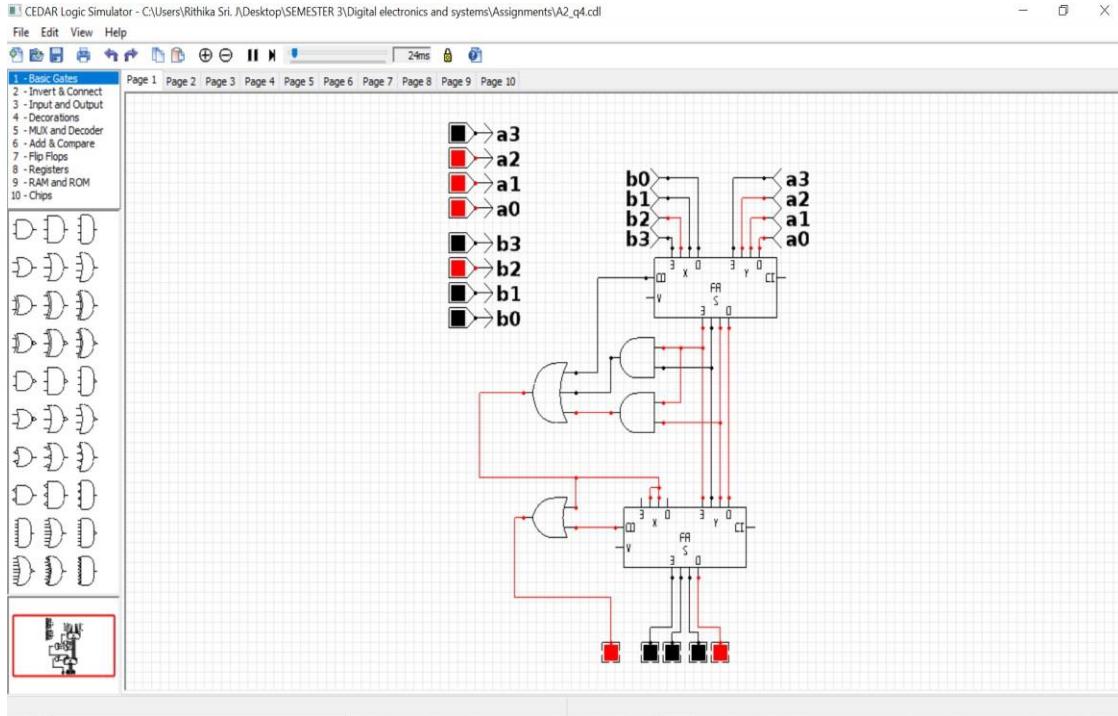
(4) BCD Adder:



a) A=4 and B=3



b) A=7 and B=4



c) A=9 and B=8

