

TOT-1

(2) $568.23 \rightarrow 5 \times 10^2 + 6 \times 10^1 + 8 \times 10^0 + 2 \times 10^{-1} + 3 \times 10^{-2}$

(3) (a) $37 \rightarrow$

2	37
2	18
2	9 0
2	4 1
2	2 0
	1 0

↓

100101

(b) $0.625 \rightarrow$

0.625	$\times 2 \rightarrow 1.250$
	$0.250 \times 2 \rightarrow 0.500$
0.101	$0.500 \times 2 \rightarrow 1.000$

↓

(c) 25.15625

2	25
2	12 1
2	6 0
2	3 0
	1 1

↑

11001

$0.15625 \times 2 \rightarrow$

$0.31250 \quad 0$

$0.3125 \times 2 \rightarrow$

$0.625 \quad 0$

$\therefore 25.15625 \rightarrow [11001.00101]$

(4) Range $\rightarrow -2^8 \text{ to } 2^8$
 $0 \text{ to } 2^{n+1}-1$
 $0 - 2^8-1$
 $0 \text{ to } 255$

(5) Binary to decimal

$$(a) \quad 11011 \rightarrow 1+2+8+16 \rightarrow 27$$

$$(b) \quad 10110101 \rightarrow 1 + 4 + 8 + 32 + 128 = 128 + 32 + 16 + 4 + 1$$

(128) (181)

(c) $1101101 \rightarrow 1 + 2 + 16 + 32 + 128$

$$(d) \quad 10101.1011 \rightarrow 1 + 4* + 16 + \frac{1}{2} + \frac{1}{8} + \frac{1}{16}$$

\rightarrow 21.6875

$$(e) \quad 0.1101 \rightarrow \frac{1}{2} + \frac{1}{4} + \frac{1}{16} \Rightarrow 0.8125$$

$$(d) \quad 10.101 \rightarrow 2 + \frac{1}{2} + \frac{1}{8} \Rightarrow 2.625$$

(6) Decimal to Octal

(b) $(127)_{10} \rightarrow (111111)_2$

177 octal

(c) 0.5625

$0.5625 \times 2 \rightarrow 1.1250$

$0.1250 \times 2 \rightarrow 0.25$

$0.25 \times 2 \rightarrow 0.5$

$0.5 \times 2 \rightarrow 1$

$(0.\underline{100})_2$

0.44

(d) 89.16257

	89	
$0.16257 \times 2 \rightarrow 0.32514$	0	2
$0.32514 \times 2 \rightarrow 0.65028$	0	2
$0.65028 \times 2 \rightarrow 1.30056$	1	2
$0.30056 \times 2 \rightarrow 0.60112$	0	2
$0.60112 \times 2 \rightarrow 1.20224$	1	2
		1 0

1011001.0010

131.10

(7) Decimal to hexa

(a) $829 \rightarrow (11001110)_2$

33D

(b) $778.7625 \rightarrow (1100001010)_2 \rightarrow 778.$

$$\begin{array}{r} 0.7625 \times 2 \\ \hline 1.525 \\ 1.05 \\ 0.1 \\ \hline 0.2 \\ 0.4 \\ 0.8 \\ \hline \end{array}$$

$$\therefore (1100001010.1100)_2$$

↓
binary

11000.1010.1100

30 A.C

(c) $423 \rightarrow (11010011)_2$

1 A 7.

1 A 7

(d) $2598.675 \rightarrow (101000100110)_2$

$$0.675 \times 2 \rightarrow 1.35$$

$$\begin{array}{r} 1.35 \\ 1.07 \\ 1.04 \\ 0.8 \\ \hline \end{array}$$

$$\begin{array}{r} 101000100110.1010 \\ \hline A \quad 2 \quad 6 \quad A \end{array}$$

A26.A

(8) hexa to decimal

a) $2A5 \rightarrow (001010100101)_2$
 $(677)_{10}$ decimal

b) $0.F1C \rightarrow (0.111100011100)_2$

$$\begin{array}{r} 2 \\ 13 \quad 1 \\ \hline 12 \end{array}$$

$$\frac{1}{2} + \frac{1}{2^2} + \frac{1}{2^3} + \frac{1}{2^4} + \frac{1}{2^8} + \frac{1}{2^9} + \frac{1}{2^{10}}$$
 $\rightarrow 0.9443$

c) $EF.B1 \rightarrow \underbrace{11101111}_{1s}, \underbrace{10110000}_{.0s}$

 $(239)_{10} = \frac{1}{2} + \frac{1}{2^3} + \frac{1}{2^4} + \frac{1}{2^8}$

239.0691
 $_{10}$ decimal

d) $0.9D9 \rightarrow 0.100111011001$

$$= \frac{1}{2} + \frac{1}{2^4} + \frac{1}{2^5} + \frac{1}{2^6} + \frac{1}{2^8} + \frac{1}{2^9} + \frac{1}{2^{12}}$$
 $= 0.615478515$

e) $BB.C10 \rightarrow 101110111100.00010000$

$3004 + 1/2^4$

3004.0625



Octal -> Decimal

(3) (a) 733

$$\rightarrow (111011101)_2$$

$$\rightarrow \text{binary} \rightarrow (477)_{10}$$

decimal

$$(c) (146.21)_8$$

$$\rightarrow (1100110.010001)_2$$

↓

$$(102.265625)_{10}$$

(b) 0.24

$$\rightarrow (0.010100)_2$$

$$\rightarrow \text{binary} \rightarrow \frac{1}{2^2} + \frac{1}{2^4}$$

$$\Rightarrow 0.25 + 0.0625$$

$$(d) (4057.06)_8$$

$$\rightarrow (10000010111.0001)_2$$

$$(0.3125)_{10} \text{ decimal}$$

Binary → Hexa

a) 1011011011 $\rightarrow (2DB)_{16}$

b) 11011101100 $\rightarrow (6E8)_{16}$

c) 1010100.10110100 $\rightarrow (54.B4)_{16}$

d) 00101111011.01111100 $\rightarrow (2FB.7C)_{16}$

Hexa → Binary

a) 4BAC $\rightarrow (01001011.10101100)_2$

b) 29A6 $\rightarrow (00101001.10100110)_2$

c) DC5A.BE4 $\rightarrow (1101110001011010.00111100100)_2$

d) 3A9E.B0D $\rightarrow (0011101010011110.101100011101)_2$

(12) Hexa \rightarrow Octal

(a) $(B9F.AE)_{16} \rightarrow (\underbrace{101110}_{(56)_8}, \underbrace{011111}_{(53)_8}, \underbrace{1010110}_{(54)_8})_2$
 $(5637.534)_8$

(b) $(27A9)_{16} \rightarrow (\underbrace{0010}_{(2)_8}, \underbrace{001111}_{(36)_8}, \underbrace{010100}_{(51)_8})_2$
 $(23651)_8$

(c) $(85C.BD3)_{16} \rightarrow (\underbrace{100001}_{(40)_8}, \underbrace{011100}_{(56)_8}, \underbrace{101110}_{(58)_8}, \underbrace{100011}_{(33)_8})_2$
 $(4134.5723)_8$

(13) Octal \rightarrow Hex

(a) $(3562)_8 \rightarrow (011101110010)_2$
 $(772)_{16}$

(b) $(4567.266)_8 \rightarrow (\underbrace{100101110111}_{(977)_16}, \underbrace{010110110}_{(580)_16})_2$
 $(977.580)_{16}$

(c) $(756.603)_8 \rightarrow (\underbrace{111101110}_{(1EE)_{16}}, \underbrace{110000011}_{(C18)_{16}})_2$
 $\Rightarrow (1EE.C18)_{16}$

(14) Binary \rightarrow Octal



(a) $(\underline{101111})_2 \rightarrow (57)_8$

(b) $(\underline{011} \underline{010} \underline{0111})_2 \rightarrow (327)_8$

(c) $(\underline{1000} \underline{1000} \underline{1001} \underline{0011})_2 \rightarrow (104.463)_8$

(d) $(\underline{101} \underline{010} \underline{101} \underline{101.} \underline{111} \underline{0111} \underline{00}) \rightarrow (1255.734)_8$

(13) Octal \rightarrow Binary

(a) $(46)_8 \rightarrow (100110)_2$

(b) $(407)_8 \rightarrow (100000111)_2$

(c) $(1256)_8 \rightarrow (00101010110)_2$

(d) $(367.52)_8 \rightarrow (011110111.101010)_2$

(i)

BCD

24 21

(ii) 125

0001 0010 0101

(i) 125

1000101011
0001 00100101

(ii) 156

0001 0101 0110

(ii) 156

10111100
0001 01010110

(iii) 98

1001000

(iii) 98

1111110

(iv) 69

01101001

(iv) 69

1100111
0110

X S - 3

(i) 125

010001011000

(ii) 156

010010001001

(iii) 98

11011100

(iv) 69

10011101



(2) BCD → Decimal

(i) $0110 \rightarrow (6)_{10}$

(ii) $0001 \rightarrow (1)_{10}$

(iii) $\underline{0100}, \underline{0101} \rightarrow (45)_{10}$

(iv) $\underline{1001}, \underline{1000} \rightarrow (98)_{10}$

(v) $\underline{1000}, \underline{0111}, \underline{0000} \rightarrow (870)_{10}$

(3) (i) $1000 + 0110$

$$\begin{array}{r} 1000 \\ + 0110 \\ \hline 1110 \end{array}$$

(ii) $\begin{array}{r} 00100101 \\ + 00100111 \\ \hline 01001000 \end{array}$

(iii) $\begin{array}{r} 01010001 \\ + 01011000 \\ \hline 10101001 \end{array}$

(iv) $\begin{array}{r} 10011000 \\ + 10010111 \\ \hline 100101111 \end{array}$



(4)

7 4 2 1

0	0	0	0	0
1	0	0	0	1
2	0	0	1	0
3	0	0	1	0
4	0	1	0	0
5	0	1	0	1
6	0	1	1	0
7	1	0	0	0
8	1	0	0	1
9	1	0	1	0

(5)

2421a) 3864 \rightarrow 0011 1100 1100 0100b) 123 \rightarrow 0001 0010 0011c) 654 \rightarrow 0110 0101 0100d) 468 \rightarrow 0100 0110 1110

(6)

Self complementing are the codes in which, when 9 is represented, if 9's complement of the no. is taken in decimal & represented in the code then this representation is 0s & 1s exchanged of the code of original no.



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Ex → 123

Code → 0001 1000 1001

9's complement of no. in decimal →

999

123

876

876 in binary → 1110 0111 0110

123 → 1000110001001

876 → 11100111.0110

(6) i) 64

→ 10100100

ii) 12

→ 01110110

iii) 65

→ 10101011

iv) 46

→ 01001010

(7) (i) 14 (748210)₈

7 7 7 7 7 7

7 4 3 2 1 0

7's → 0 3 4 5 6 7

(ii) (9876123)₁₀

999999999

9876123

95 → 0123876

(iii) $(12345F)_{16}$

FFFF	FFF	FFF			
1	2	3	4	5	F
E	D	C	B	A	D

(iv) $(543210)_6$

5	5	5	5	5	5
5	4	3	2	1	0
0	1	2	3	4	5

(3) If parity codes will have odd no. of 1's then error.

- (a) 100110010 → (4) → no error
- (b) 011101010 → (5) → Error
- (c) 010101010101010 → (10) → no error

(4) If parity codes will have even no. of 1's then error.

- (a) 11110110 → (2) → Error
- (b) 00110001 → (5) → No error
- (c) 010101010101010 → (7) → No error

(5)

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
P ₁	P ₂	1	P ₃	1	0	0	P ₈	1	0	0	1	0	1	0

$$P_3 = \text{XOR}(1, 1, 0, 1, 0, 0, 0, 0) \\ = 1$$



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$$P_2 = \text{XOR}(1, 0, 0, 0, 0, 1, 0)$$

$$= 0$$

$$P_4 = \text{XOR}(1, 0, 0, 1, 0, 1, 0)$$

$$= 1$$

$$P_8 = \text{XOR}(1, 0, 0, 1, 0, 1, 0)$$

$$= 1$$

(iii)

Manning Code = 101110011001010

(ii)

(i) 000011101010

1	2	3	4	5	6	7	8	9	10	11	12
0	0	0	0	0	0	0	0	0	0	0	0

P₁ P₂ P₄ P₈

$$C_1 = \text{XOR}(0, 0, 1, 1, 1, 1)$$

$$= 0$$

$$C_2 = \text{XOR}(0, 0, 1, 1, 0, 1)$$

$$= 1$$

$$C_4 = \text{XOR}(0, 1, 1, 1, 0)$$

$$= 1$$

$$C_8 = \text{XOR}(0, 1, 0, 1, 0)$$

$$= 0$$

$$C = 0110 = 6$$

We have error in 6th bit so corrected data will be
01011010

(ii) 101110000110

1	<u>2</u>	<u>3</u>	4	5	<u>6</u>	<u>7</u>	8	9	<u>10</u>	<u>11</u>	12
1	0	1	1	1	0	0	0	0	1	1	0
P ₁	P ₂	P ₄			P ₈						

$$C_1 = \text{XOR}(1, 1, 1, 0, 0, 1) = 0$$

$$C_2 = \text{XOR}(0, 1, 0, 0, 1, 1) = 1$$

$$C_4 = \text{XOR}(1, 1, 0, 0, 0) = 0$$

$$C_8 = \text{XOR}(0, 0, 1, 1, 0) = 0$$

$$C = 0010 = 2$$

We have error in 2nd bit corrected data will be

11000110

(iii) 10111110100

1	2	3	4	5	6	7	8	9	10	11	12
1	0	1	1	1	1	1	1	0	1	0	0
P ₁	P ₂	P ₄			P ₈						

$$C_1 = \text{XOR}(1, 1, 1, 1, 0, 0) = 0$$

$$C_2 = \text{XOR}(0, 1, 1, 1, 1, 0) = 0$$

$$C_4 = \text{XOR}(1, 1, 1, 1, 0) = 0$$

$$C_8 = \text{XOR}(1, 0, 1, 0, 0) = 0$$

$$C = 0000 = 0$$

We have errors in no bit.

11110100

(12) (i) 1111
 \rightarrow 1010

(ii) 0011
 \rightarrow 0010

(iii) 0101
 \rightarrow 0110

(iv) 10101010
 \rightarrow 11001100

(13) (i) 0110
 \rightarrow 0101

(ii) 0001
 \rightarrow 0001

(iii) 01000101
 \rightarrow 01100111

(iv) 10011000
 \rightarrow 11010100

(v) 100110010
 \rightarrow 11010101

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Rudraksh Agrawal

2NC6

102015126

$$\textcircled{1} \quad A + \bar{A} \cdot B + A \cdot B = A + B$$

Truth Table :-

\bar{A}	A	B	$A \cdot B$	$\bar{A} \cdot B$	$A + B$	$A + \bar{A} \cdot B + A \cdot B$
1	0	0	0	1	0	0
0	1	0	0	1	1	1
0	1	1	1	0	1	1
1	0	1	0	0	1	1

\textcircled{2}

$$A + B = A + C$$

$$\textcircled{+} \quad \bar{A} + B = \bar{A} + C$$

$$(A + \bar{A}) + B + B = (A + \bar{A}) + C + C$$

$$1 + B = 1 + C$$

$$B = C$$

Hence, proved.

$$\textcircled{3} \quad \text{Given} - A \cdot \bar{B} + \bar{A} \cdot B = C \quad \text{--- } \textcircled{1}$$

$$\text{To prove} - A \cdot \bar{C} + \bar{A} \cdot C = B \quad \text{--- } \textcircled{2}$$

Complementing both sides,

$$\bar{A} \cdot \bar{B} + \bar{\bar{A}} \cdot \bar{B} = \bar{C}$$

$$(\bar{A} + B) \cdot (\bar{A} + B) = \bar{C} \quad \text{--- } \textcircled{3}$$

Putting eqⁿ \textcircled{3} in \textcircled{2}

$$\begin{aligned}
 & \Rightarrow A(\bar{A}+B)(A+\bar{B}) + \bar{A}C = B \\
 & \Rightarrow A(A\cancel{\bar{A}}^0 + \bar{A}\bar{B} + BA + B\cancel{B}^0) + \bar{A}C \\
 & \Rightarrow A(\bar{A}\bar{B} + BA) + \bar{A}C \\
 & \Rightarrow A\cancel{\bar{A}\bar{B}}^0 + ABA + \bar{A}C \\
 & \Rightarrow AAB + \bar{A}C - \textcircled{M}
 \end{aligned}$$

Putting value of C from eqn ① in eqn ④ -

$$\begin{aligned}
 & \Rightarrow AAB + \bar{A}(AB + \bar{A}\bar{B}) \\
 & \Rightarrow AA B + \bar{A}AB + \bar{A}\bar{B} \\
 & \Rightarrow AB + \bar{A}\bar{B} \\
 & \Rightarrow B(A + \bar{A}) = \textcircled{B}
 \end{aligned}$$

④ (i) $F(A, B, C) = AB + A\bar{B}C + \bar{A}B\bar{C} + B\bar{C}$

SOP

		BC		A					
		00	01	11	10				
A	B	0	0	1	1				
		1	0	1	1				

$= B + AC$

POS

$$(A+B), (B+C)$$

(ii) $F(A, B, C, D) = \Sigma(5, 6, 9, 10, 11, 13, 14, 15)$

AB CD

		CD		AB						
		00	01	11	10					
A	B	00	0	0	0	0				
		01	0	1	0	1				
A	B	11	0	1	1	1				
		10	0	1	0	1				

(SOP) $\rightarrow AC + AD + BC\bar{D} + B\bar{C}\bar{D}$

(POS) $\rightarrow (C\bar{D}) \cdot (\bar{A}+B) \cdot (A+\bar{C}+\bar{D})$

(iii) $F(A, B, C, D, E) = \Sigma(0, 1, 2, 3, 4, 5, 8, 9, 10, 11)$

$$\begin{matrix} A=0 \\ A=1 \end{matrix}$$

BC \ DE	00	01	11	10
00	1	1	1	0
01	1	0	0	1
11	0	0	0	0
10	1	1	1	0

BC \ DE	00	01	11	10
00	0	0	0	0
01	0	0	0	0
11	0	0	0	0
10	0	0	0	0

$$A=0$$

$$A=1$$

SOP $\rightarrow A \cdot (\bar{C} + \bar{B}\bar{E}) = \bar{A}\bar{C} + \bar{A}\bar{B}\bar{E}$

POS $\rightarrow A \cdot (\bar{B} + \bar{C}) \cdot (\bar{C} + \bar{E})$

(iv) $F(A, B, C, D, E) = \prod(0, 1, 2, 4, 5, 6, 9, 11, 12, 13, 14, 15)$

BC \ DE	00	01	11	10
00	0	0	1	0
01	0	0	1	0
11	0	0	0	0
10	1	0	0	1

BC \ DE	00	01	11	10
00	1	1	1	1
01	1	1	1	1
11	1	1	1	1
10	1	1	1	1

$$A=0$$

$$A=1$$



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$$SOP \Rightarrow A + (\bar{C}DE + B\bar{C}\bar{E}) \cdot \bar{A} = (\bar{A}B\bar{E} + \bar{A}BC + \bar{A}BD + \bar{A}BE)$$

$$POS \Rightarrow (B+D+A), (\bar{B}+\bar{E}+A), (\bar{B}+\bar{C}+A), (A+B+E)$$

⑤

$$(i) F(A, B, C, D, E, F) = \sum m(0, 1, 2, 4, 5, 7, 8, 9, 10, 14, 15, 17, 19, 20, 28, 29, 34, 36, 40, 41, 42, 43)$$

	<u>List I</u>	<u>List II</u>	<u>List III</u>
	A B C D E F	A B C D E F	A B C D E F
0	0 0 0 0 0 0 ✓	(0,1) 0 0 0 0 0 ✓	(0,1,4,5) 0 0 0 0 -
1	0 0 0 0 0 1 ✓	(0,2) 0 0 0 0 - 0 ✓	(0,1,8,9) 0 0 - 0 0 -
2	0 0 0 0 1 0 ✓	(0,4) 0 0 0 - 0 0 ✓	(0,2,8,10) 0 0 - 0 - 0
4	0 0 0 1 0 0 ✓	(0,8) 0 0 - 0 0 0 ✓	(2,10,34,42) - 0 - 0 1 0
8	0 0 1 0 0 0 ✓	(1,5) 0 0 0 - 0 1 ✓	(8,9,40,41) - 0 1 0 0 -
5	0 0 0 1 0 1 ✓	(1,9) 0 0 - 0 0 1 ✓	(8,10,40,43) - 0 1 0 - 0
9	0 0 1 0 0 1 ✓	(1,17) 0 - 0 0 0 1	(40,41,42,43) 1 0 1 0 -
10	0 0 1 0 1 0 ✓	(2,10) 0 0 - 0 1 0 ✓	
17	0 1 0 0 0 1 ✓	(2,34) - 0 0 0 1 0 ✓	
20	0 1 0 1 0 0 ✓	(4,5) 0 0 0 1 0 - ✓	
34	1 0 0 0 1 0 ✓	(4,20) 0 - 0 1 0 0	
36	1 0 0 1 0 0 ✓	(4,36) - 0 0 1 0 0	
40	1 0 1 0 0 0 ✓	(8,9) 0 0 1 0 0 -	
7	0 0 0 1 1 1 ✓	(8,10) 0 0 1 0 - 0 ✓	
14	0 0 1 1 1 0 ✓	(8,40) - 0 1 0 0 0 ✓	
19	0 1 0 0 1 1 ✓	(5,7) 0 0 0 1 - 1	
28	0 1 1 1 0 0 ✓	(9,41) 0 1 0 0 - 1 ✓	
41	1 0 1 0 0 1 ✓	(10,19) 0 1 - 1 0 0	
42	1 0 1 0 1 0 ✓	(17,19) 1 0 - 0 1 0	
15	0 0 1 1 1 1 ✓	(20,28) 1 0 1 0 0 - ✓	
29	0 1 1 1 0 1 ✓	(34,42) 1 0 1 0 - 0 ✓	
43	1 0 1 0 1 1 ✓	(40,41) 1 0 1 0 0 - ✓	
		(40,42) 1 0 1 0 - 0	

(7, 15)	00-111
(14, 15)	00111-
(28, 29)	01110-
(41, 43)	1010-1
(42, 43)	10101-

PJ Table

Minterms	0	1	2	4	5	7	8	9	10	14	15	17	19	20	28	29	34	36	40	41	42	43
(1, 17)	x											x										
(4, 20)		x													x							
(4, 36)		x																		x		
(5, 7)			x	x																		
(10, 14)							x	x														
(17, 19)												x	x									
(20, 28)													x	x								
(14, 15)									x	x												
(28, 29)														x	x							
(0, 1, 4, 5)	x	x	x	x																		
(0, 1, 8, 9)	x	x			*	x	x															
(0, 2, 8, 10)	x		*	x	*	x	x															
(2, 10, 34, 42)	x				*	x	x									x				x		
(8, 9, 40, 41)			*	x	x													x	x			
(8, 10, 40, 42)		*	x	*	x													x	x	x	x	
(40, 41, 42, 43)																*	x	x	x	x	x	

$$\begin{aligned}
 F = & \bar{A}B\bar{C}\bar{D}F + \bar{A}BCD\bar{E} + \bar{B}\bar{B}EF\bar{F} + A\bar{B}CD \\
 & + \bar{A}\bar{B}\bar{D}\bar{E} + \bar{A}\bar{B}CDE + \bar{A}\bar{C}DEF
 \end{aligned}$$



$$(ii) F(A, B, C, D, E, F) = 2m(6, 7, 8, 9) + d(10, 11, 12, 13, 14, 15)$$

	<u>List I</u> ABCDEF	<u>List II</u> ABCDEF	<u>List III</u> ABCDEF	<u>List IV</u> ABCDEF
8	001000✓	(8,9)	00100_	(8,9,10,11) 0010__
6	000110✓	(8,10)	0010_0	(8,9,12,13) 001_0_
9	001001✓	(8,12)	001_00	(8,10,12,14) 00L_0
10	001010✓	(6,7)	00011_	(6,7,14,15) 0D_11_
12	001100✓	(6,14)	00_110	(9,11,13,15) 001_-1
7	000111✓	(9,11)	0010_1	(10,11,14,15) 001_1-
11	001011✓	(9,13)	001_01	(12,13,14,15) 0011_-
13	001101✓	(10,11)	00101_-	
14	001110✓	(10,14)	001_-10	
15	001111✓	(12,13)	00110_-	
		(12,14)	0011_0	
		(7,15)	00_111	
		(11,15)	001_-11	
		(13,15)	0011_-1	
		(14,15)	00111_-	

PI Table

Minterms.	6	7	8	9	10	11	12	13	14	15
(6, 7, 14, 15)	x	x							x	x
(8, 9, 10, 11, 12, 13, 14, 15)			x	x	x	x	x	x	x	x

Essential terms → 00_11_ , 001_ __

$$F = (\bar{A}\bar{B}DF + \bar{A}\bar{B}C)$$

(iii) $F(A, B, C, D, E, F) = \sum m(0, 12, 8, 9, 15, 17, 21, 24, 25, 27, 31)$

	<u>list I</u> ABCDEF	<u>list II</u> ABCDEF	<u>list III</u> ABCDEF
0	000000	(0, 1) 00000-	(0, 8, 1, 9) 00-00-
1	000001	(0, 2) 0000-0	(1, 9, 17, 25) 0--001
2	000010	(0, 8) 00-000	(1, 17, 9, 25) 0--001
8	001000	(8, 24) 0-1000	(8, 9, 24, 25) 0-100-
9	001001	(1, 9) 00-001	
17	010001	(1, 17) 0-0001	
24	011000	(8, 9) 00100-	
21	010101	(9, 25) 0-1001	
25	011001	(17, 21) 010-01	
25	001111	(17, 25) 01-001	
27	011011	(24, 25) 01100-	
31	011111	(25, 27) 0110-1 (15, 31) 0-1111 (27, 31) 011-11	

Prime Implicant Table

	0	1	2	8	9	15	17	21	24	25	27	31
(0, 2)	x	x				*						
(17, 21)						x	x					
(25, 27)										x	x	
(15, 31)						x						x
(27, 31)										x	x	
(0, 1, 8, 9)	x	x	x	x								
(1, 9, 17, 25)	x		x		x							
(8, 9, 24, 25)			x	x				x				

$$F = \bar{A}\bar{B}\bar{C}\bar{E} + \bar{A}\bar{B}D + \bar{A}\bar{B}\bar{D}\bar{E} + \bar{B}\bar{C}DE + \bar{A}BCD$$



$$F = 0000_0 + 010_01 + 0110_1 + 0_1111 + 00_00 \\ + 0_100_0$$

$$= \bar{A}\bar{B}\bar{C}\bar{D}\bar{F} + \bar{A}\bar{B}\bar{C}\bar{E}F + \bar{A}\bar{B}\bar{C}\bar{D}\bar{F} + \bar{A}\bar{C}\bar{D}\bar{E}F + \bar{A}\bar{B}\bar{D}\bar{E} \\ + \bar{A}\bar{C}\bar{D}\bar{E}$$

(iv) $F(A, B, C, D, E, F) = \sum m(0, 4, 12, 16, 19, 24, 27, 28, 29, 31)$

	<u>List I</u>	<u>List II</u>
0	ABCDEF	ABCDEF
4	000000	(0, 4) 000_00
16	000100	(0, 16) 0_0000
12	010000	(4, 12) 00_100
24	001100	(16, 24) 01_000
19	010001	(24, 28) 011_00
28	011000	(19, 27) 01_011
27	011001	(28, 29) 01110_
29	011101	(27, 29) 011_11
31	011111	(29, 31) 0111_1

<u>Pairs</u>	0	4	12	16	19	24	27	28	29	31
(0, 4)	x	x								
(0, 16)	x			x						
(4, 12)		x	x							
(16, 24)			x		x					
(12, 28)		x					x			
(24, 28)				x		x		x		
(19, 27)				x	x					
(28, 29)					x		x		x	
(27, 31)						x			x	
(29, 31)							x	x		

Since no pairs are grouped,
we skip this step and
directly make the prime
implicant table

$$F = \bar{A}\bar{B}\bar{C}\bar{E}\bar{F} + \\ \bar{A}\bar{B}\bar{D}\bar{F} + \\ \bar{A}\bar{B}\bar{D}\bar{C}\bar{F} + \\ \bar{A}\bar{C}\bar{D}\bar{E}\bar{F} \\ + \bar{A}\bar{B}\bar{C}\bar{D}\bar{F}$$

6 (i) $\Pi M(1, 4, 5, 11, 12, 14) \cdot d(6, 7, 15)$

		CD	00	01	11	10
		AB	00	01	11	10
	00	D	0		1 (1)	
	01	0	0		X X	
	11	0	1	X	0	
	10	D	1	0	1	

POS

$$F = (A\bar{C}D + \bar{B}\bar{D} + \bar{A}\bar{C})$$

(ii) $\Pi M(3, 6, 8, 11, 13, 14) \cdot d(1, 5, 7, 10)$

		CD	00	01	11	10
		AB	00	01	11	10
	00	1	X	0	1	
	01	1	X	X	0	
	11	1	0	1	0	
	10	0	1	0	X	

POS

$$F = [(A+B) \cdot (\bar{B}+\bar{C}+D) \cdot (\bar{B}+C+\bar{D}) \cdot \\ (\bar{A}+\bar{B}+\bar{C}) \cdot (\bar{A}+B+C+D)]$$