



Binary Trees

- Linear ds
 - ↳ arrays
 - ↳ array list
 - ↳ queues
 - ↳ stacks
 - ↳ linked list
 - ↳ doubly linked list

↳ linear data

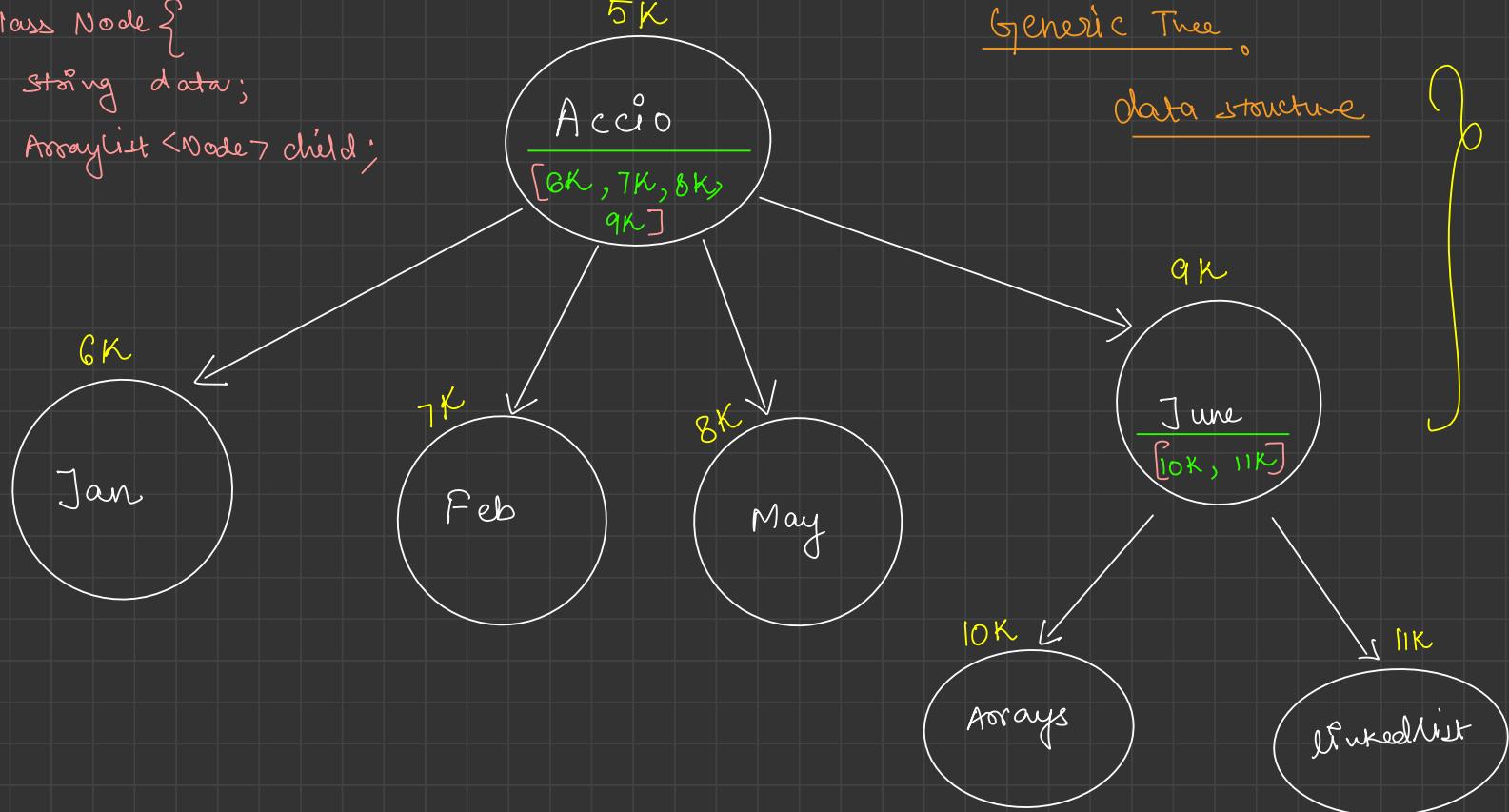


data \rightarrow family tree
 \rightarrow organisation chart
 \rightarrow file system

work on this kind of data



```
class Node {  
    String data;  
    ArrayList<Node> child;  
}
```



Binary Trees

$0|1 \rightarrow 2 \text{ options}$

(Atmost 2 options)

* In trees we have
parent child relationship

Siblings
 $D, E \quad \emptyset$
 B, C

leaf Node

degree = 2

Node left child

A

Node

right child

①

Node

Root Node degree = no. of children

} all leaf Nodes will have degree = 0

Subtree

②

B

①

C

Subtree

③

F

leaf Node

class Node

{
 int data;
 Node left;
 Node right;
}

④

D

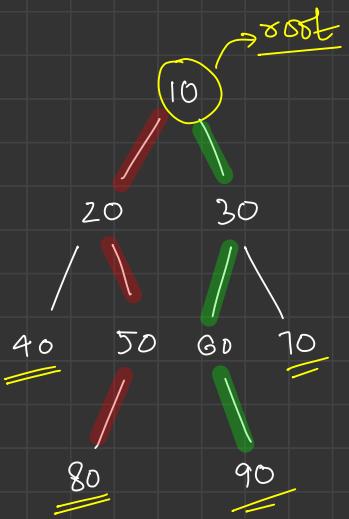
⑤

E

⑥

G

leaf Node

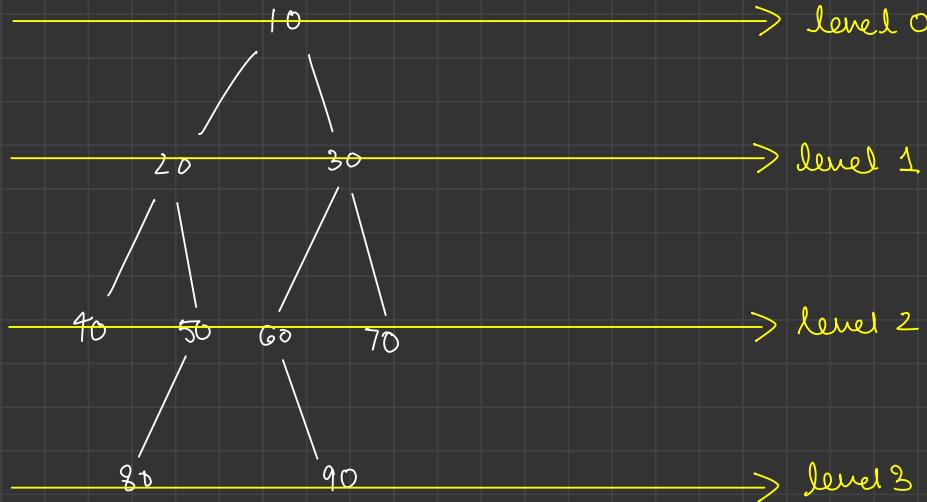


height of a Binary Tree

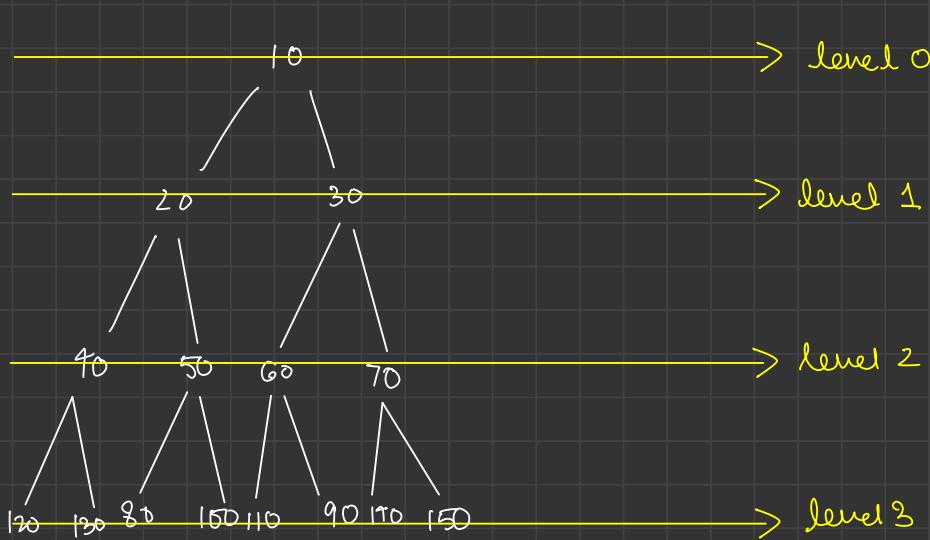
{ dist. b/w root Node and the deepest leaf Node }

in term of Edges = 3

in term of Nodes = 4



Perfect Binary Trees } No. of Nodes in each level $h = 2^h$



$$\{1 \text{ Node}\} \curvearrowright 2^0$$

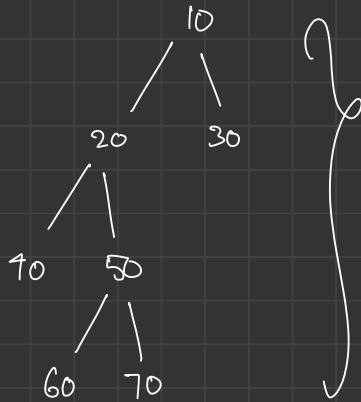
$$\{2 \text{ Nodes}\} \curvearrowright 2^1$$

$$\{4 \text{ Nodes}\} \curvearrowright 2^2$$

$$\{8 \text{ Nodes}\} \curvearrowright 2^3$$

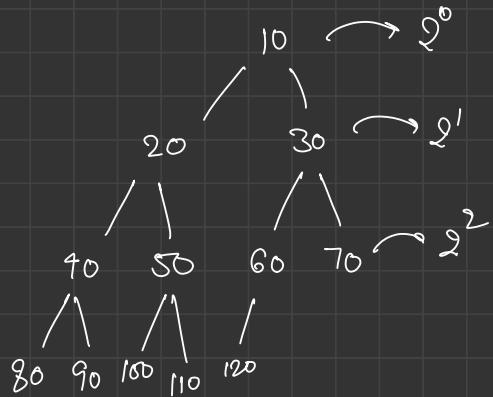
full Binary Tree .

each nodes has either zero or two children



Complete Binary Tree

where each level is completely filled, except the last level,
where nodes in last level are as left positioned as possible.

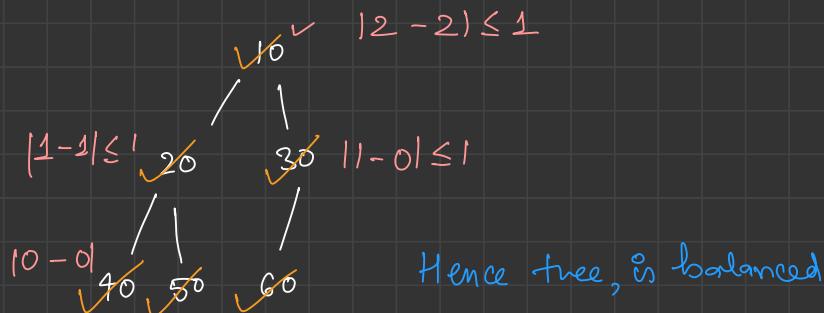


Balanced Binary Tree

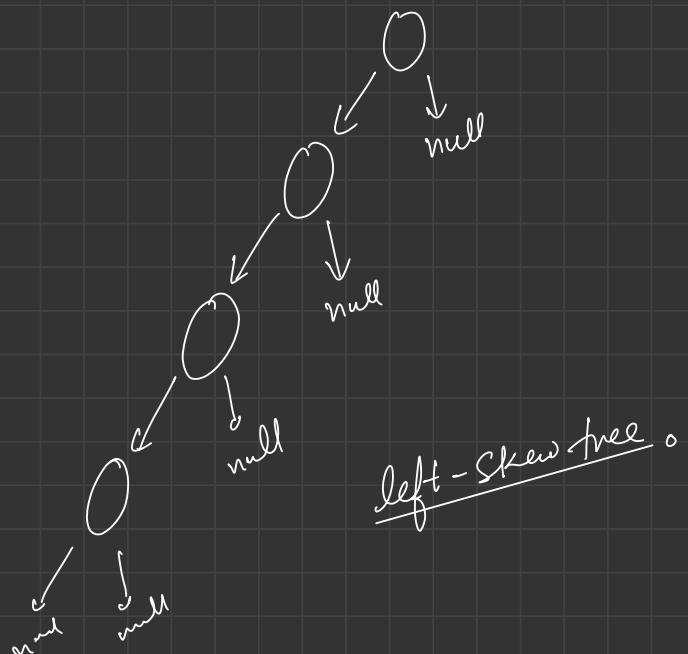
when each node of a tree is balanced

Balanced Node

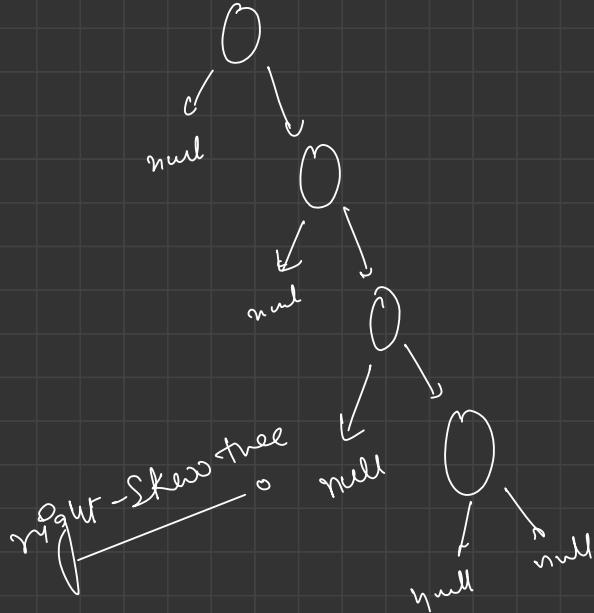
$$|\text{height of left subtree} - \text{height of right subtree}| \leq 1$$



Skew Tree



left-Skew tree

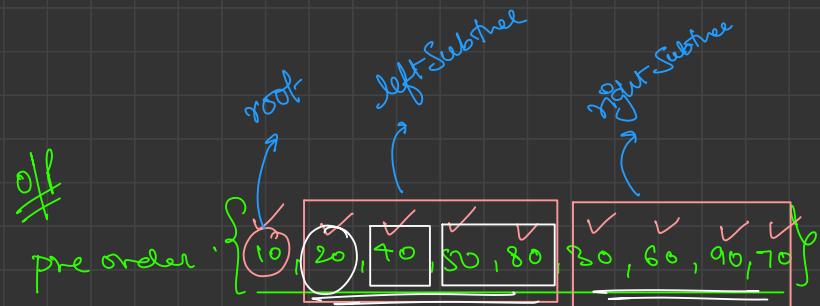
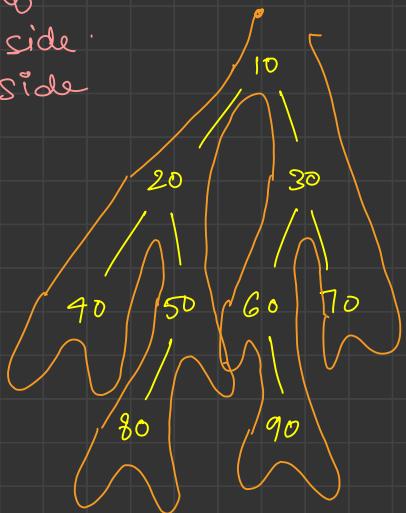


right-Skew tree

Traversal over Tree

① pre - order traversal

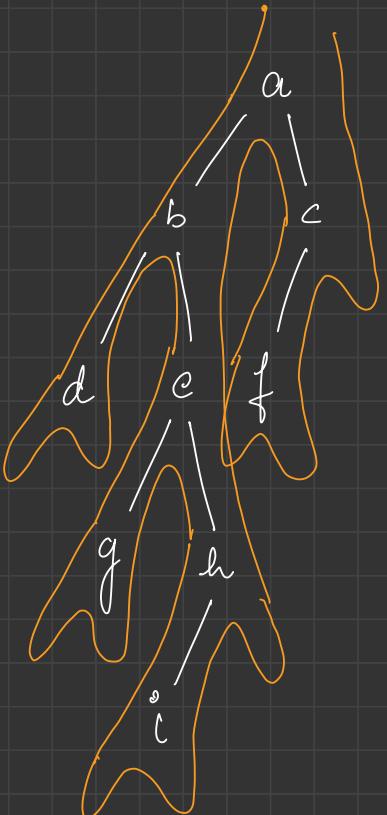
{
put yourself
explore left side.
explore right side

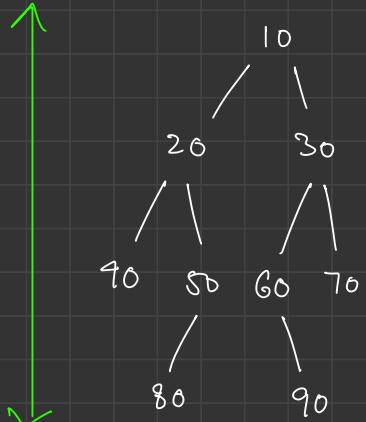


pre - order

Euler path

{ 10, 20, 40, 50, 80, 30, 60, 90, 70 }





TC: $O(N)$
SC: $O(h)$

→ finish if point the order from root

```
void printPreOrder( Node root )
{
    ① if (root == null) return;
```

② print (root.data);

③ printPreOrder (root.left);

④ printPreOrder (root.right);

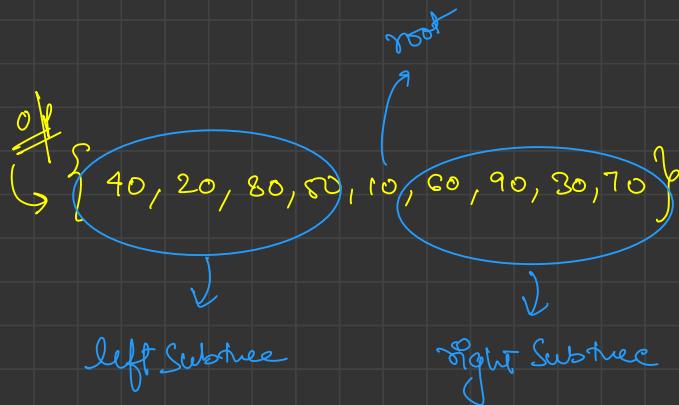
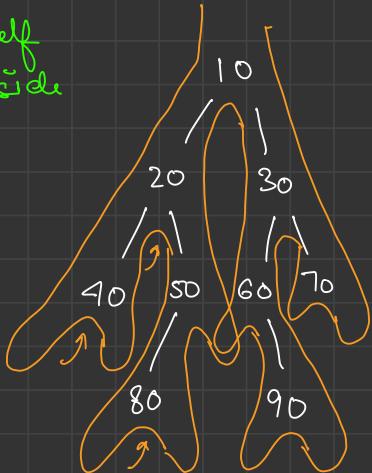


10, 20, 40, 50, 80

(2)

In - order traversal

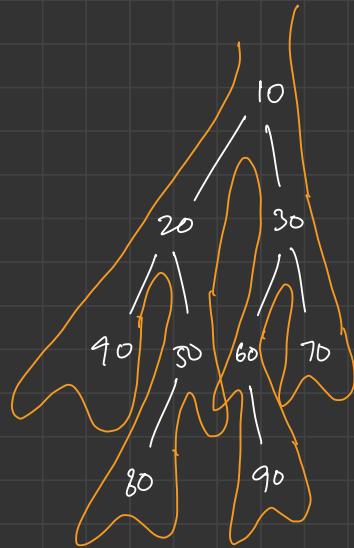
{ explore left side
print yourself
explore right side



Euler path : { 40, 20, 80, 50, 10, 60, 90, 30, 70 }

Post Order Traversal

{ explore left side
explore right side
print yourself



off

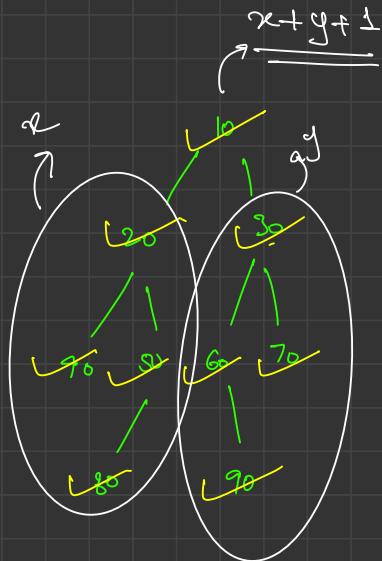
40, 80, 50, 20, 90, 60, 70, 30, 10

~~Euler paths~~

{ 40, 80, 50, 20, 90, 60, 70, 30, 10 }

Size of binary Tree

↳ { No. of nodes in a binary Tree }

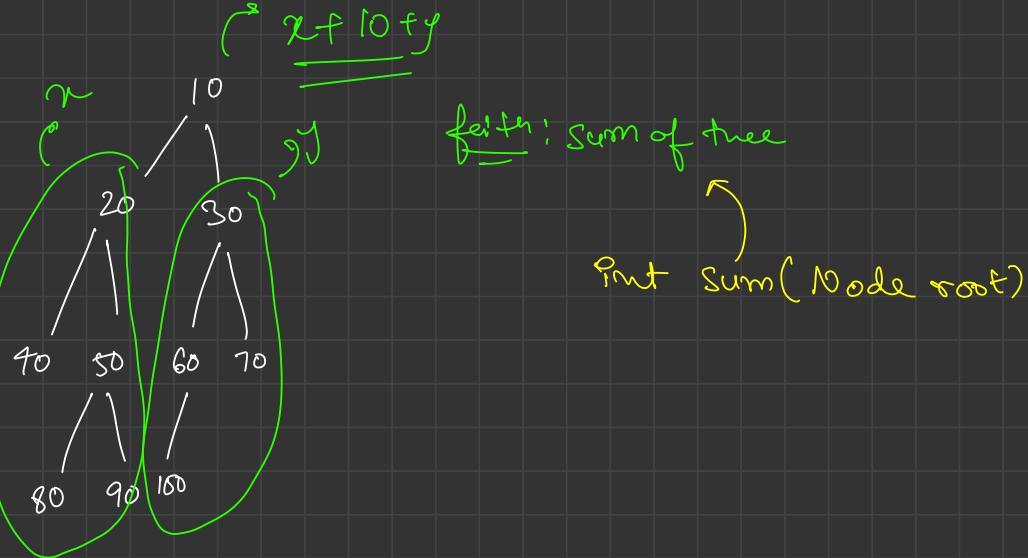


$$\boxed{\text{Size} = 9}$$

~~feihi~~: returns size of the tree
Put size (Node \Rightarrow root)

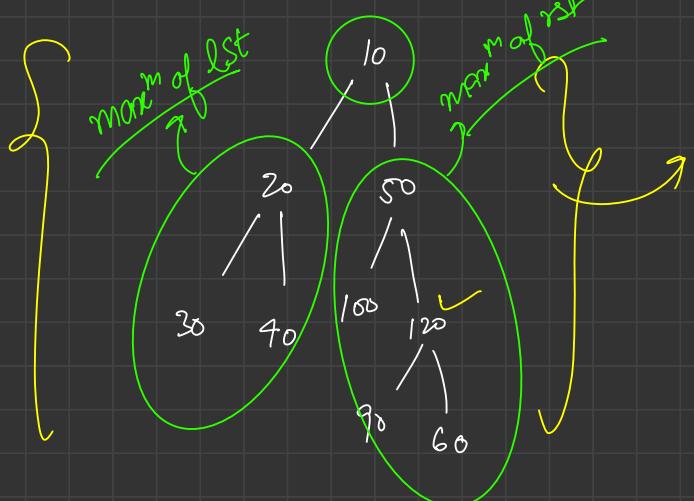
Sum of tree

{ Sum of all the values of Nodes }



Max of tree

↳ Max^m value present in a tree



max^m(max^m(lst, max^m(rst, root.val)))

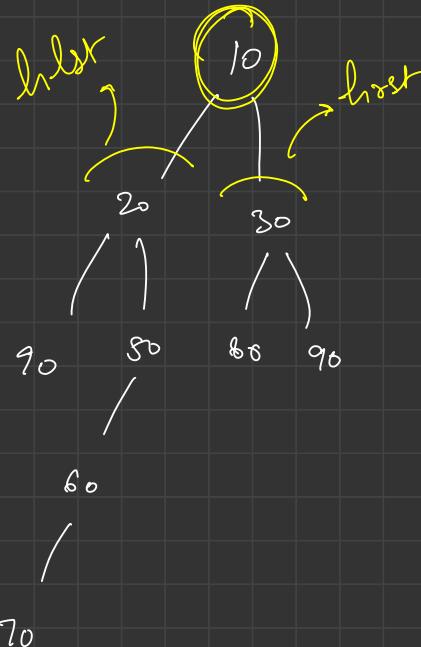
120
faile: max^m of a tree.

int maxtree (Node root)

height of tree

(Nodes)

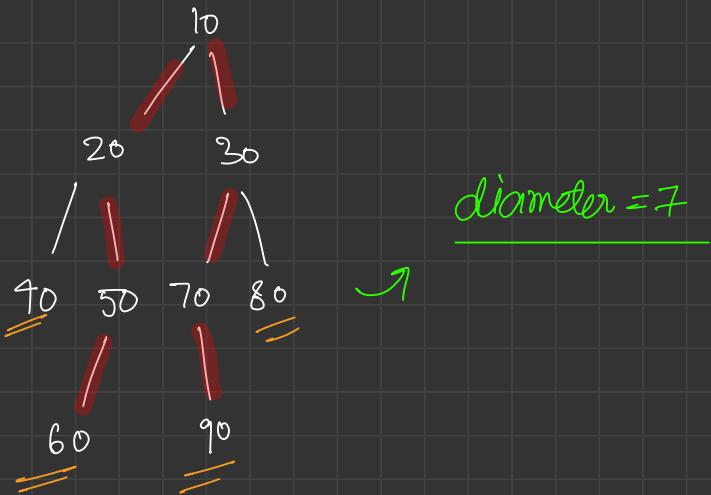
$\max^m(\text{left}, \text{right}) + 1 \rightarrow \underline{\text{root Node}}$

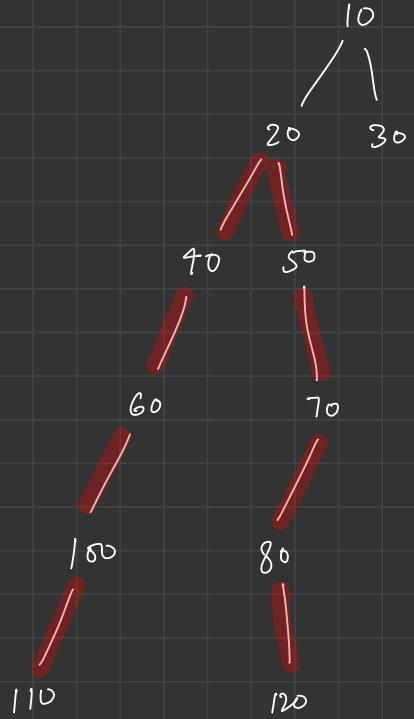


faiss height of tree

int height (Node node)

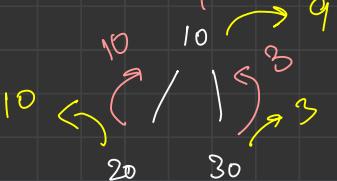
diameter of tree. } max^m dist b/w any two leaf Nodes }





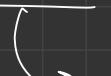
Diameter = 9

$\max^m(\text{lst}, \text{rst}, \text{root's dia}) \rightarrow \underline{\text{dia}}$



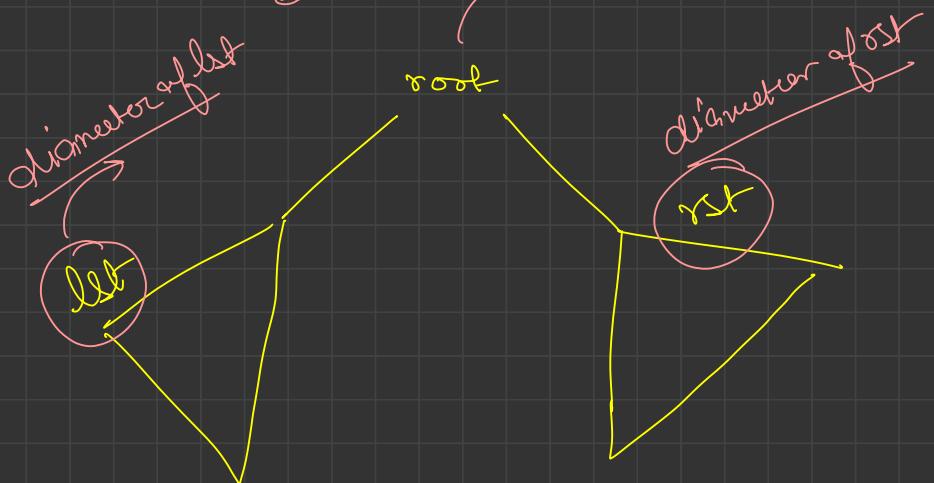
Diameter of tree
max^m of dia of each node

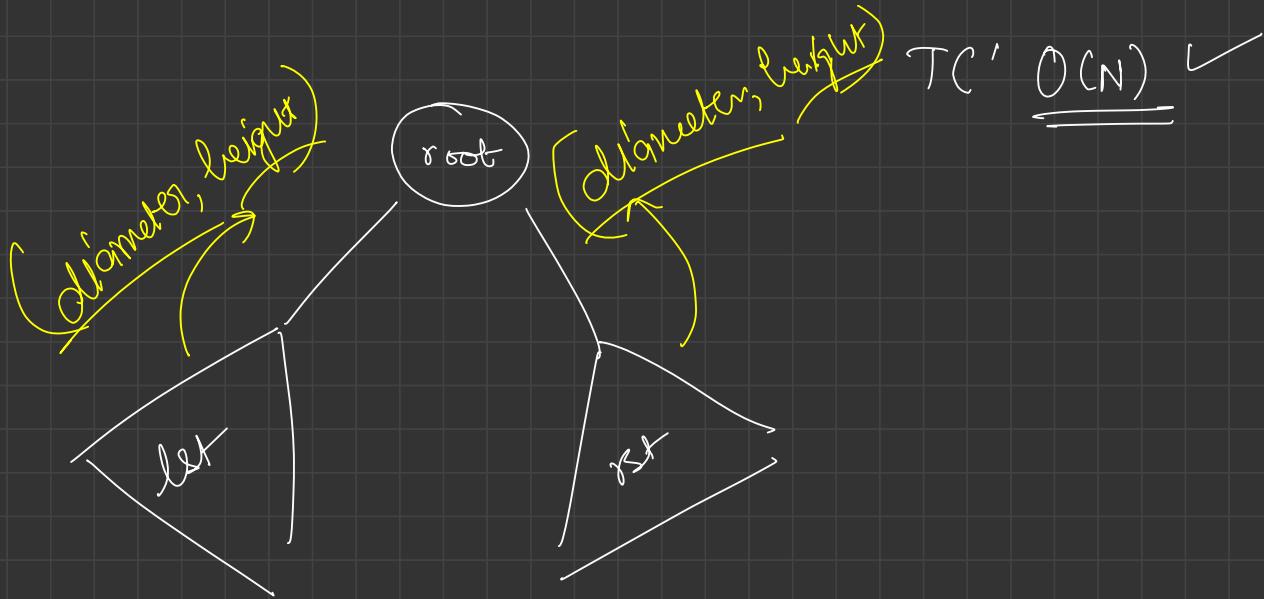
int diameter (Node root)



faith: returns diameter of tree !

max(left, right, root's diam) !





} faith \longrightarrow diameter + height }

TC' $O(N)$ ✓