



Binary Search

`int[] arr = [1, 3, 7, 10, 11, 14, 20] ↗ Sorted`
target = 14 ↗
search() ↗ S

Brute-force

```
for (int i = 0; i < arr.length; i++)  
{  
    if (arr[i] == target)  
        return i;  
}
```

TC : O(N) ✓
SC : O(1) ✓

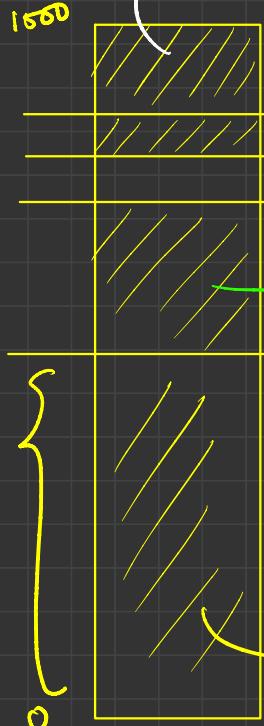
} Linear Search.

Sorted Array \rightsquigarrow searching is possible in TC: $O(\log N)$

3rd Brick, 125 floors Eliminated ($N/8$)
↓
2nd Brick, 875 floors Eliminated ($N/4$)
↓
1st Brick, 500 floors Eliminated ($N/2$)

Binary Search

780

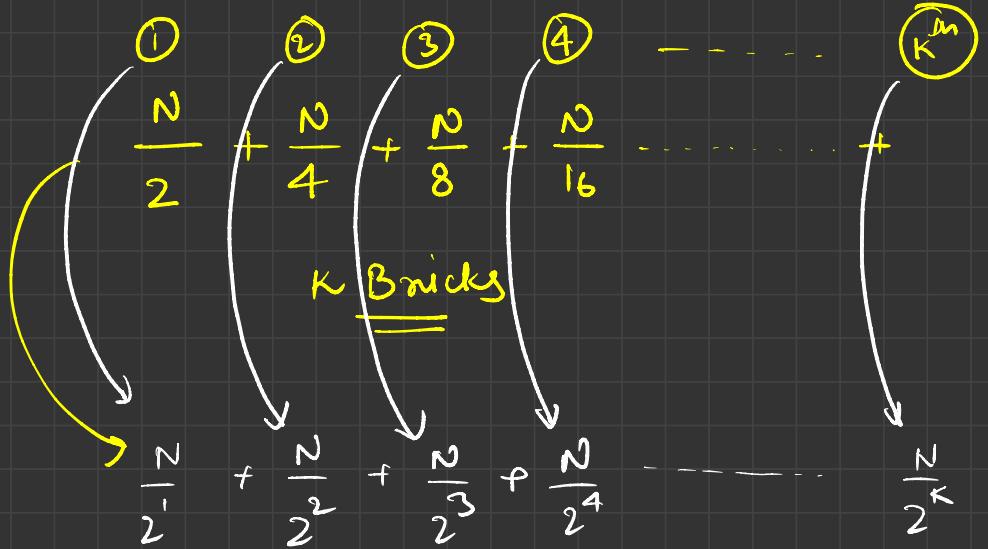


using 2nd Brick, I eliminated 250 ($N/4$) floors

Q) Can you tell from which floor if you through a Brick, it will be break.

you have to min. number of Bricks.

using 1 Brick, I eliminated 500 ($N/2$) floors



$$\frac{N}{2^K} = 1$$

$$N = 2^K$$

$$\boxed{\log_2 N = K}$$

$$\log_{10} N = \log_{10} 2^K$$

$$\log_{10} N = K \log_{10} 2$$

$$\left\{ \frac{\log_{10} N}{\log_{10} 2} = K \right.$$

$$\boxed{\log_2 N = K}$$

So, I can say we need $\log_2 N$ Bricks,

Hence,

$$TC: O(\log_2 N)$$

$$\begin{aligned}\log_2 \underline{1000} &= \log_2 10^3 \\ &= 3 \times \log_2 10 \\ &= 3 \times 3.32 \quad \downarrow \\ &\approx \underline{9.96} \approx \underline{10}\end{aligned}$$

$\text{int arr} = [1, 3, 7, 10, 11, 14, 20]$ $\rightsquigarrow \underline{\text{Sorted}}$



target = 11

$$(0+6)/2 = 3$$

$$\begin{aligned}(4+6)/2 \\ = 5\end{aligned}$$

$$\text{mid} = (\text{low} + \text{high})/2$$

① $\text{arr[mid]} == \text{target}$
return mid;

$$\frac{n}{2} + \frac{n}{4} + \frac{n}{8} + \dots$$

TC: $O(\log_2 N)$

③ $\text{arr[mid]} < \text{target}$

$\text{low} = \text{mid} + 1$; Repeat

④ $\text{arr[mid]} > \text{target}$

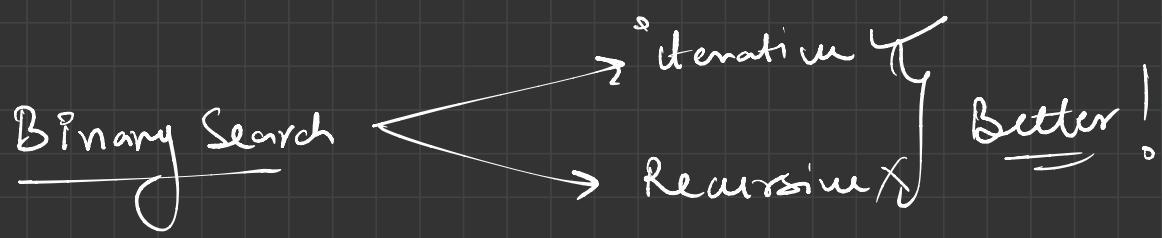
$\text{high} = \text{mid} - 1$; Repeat

Binary Search

- ① the given array will be sorted.

→ If given a sorted Array
→ Expected TC: $O(\log N)$

→ 99% it is Binary Search.



```

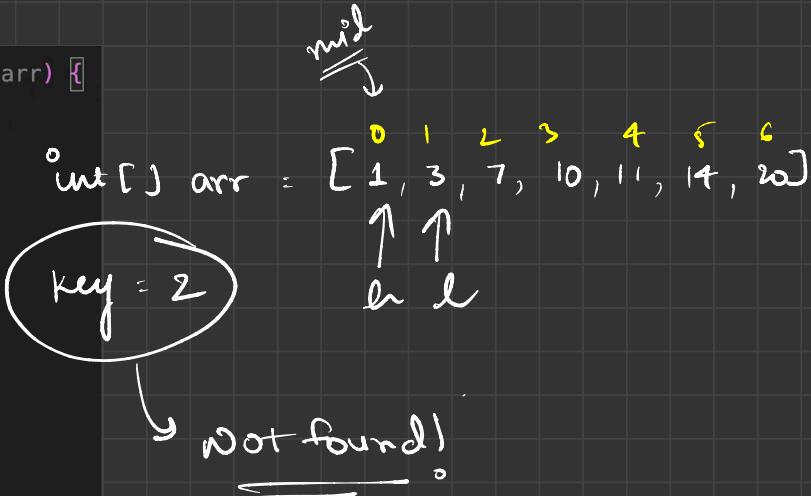
public static int BinarySearchIterative(int key, int[] arr) {
    int low = 0;
    int high = arr.length - 1;

    while (low <= high) {
        int mid = (low + high) / 2;

        if (arr[mid] == key) {
            return mid;
        } else if (arr[mid] > key) {
            high = mid - 1;
        } else {
            low = mid + 1;
        }
    }

    return -1;
}

```



$$TC: O(\log N) \quad SC: O(1)$$

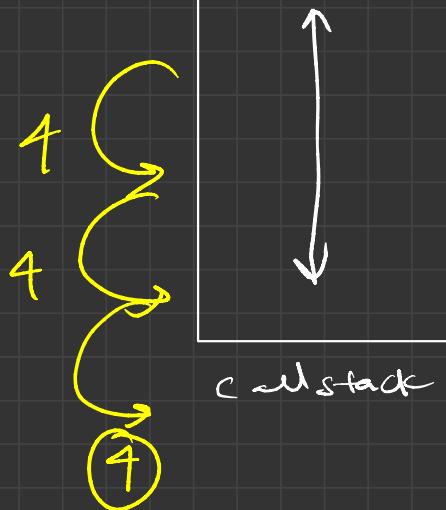
```

public static int BinarySearchRecursive(int key, int[] arr, int low, int high) {
    ① if (low > high) {
        return -1;
    }
    ② int mid = (low + high) / 2;
    if (arr[mid] == key) {
        return mid;
    } else if (arr[mid] > key) {
        return BinarySearchRecursive(key, arr, low, mid - 1);
    } else {
        return BinarySearchRecursive(key, arr, mid + 1, high);
    }
}

```

$$\left\{ \begin{array}{l} T(): O(\log_2 N) \\ S(): O(\log_2 N) \end{array} \right.$$

0 6
 ↓
 int[] arr = [1, 3, 7, 10, 11, 14, 20]
 key = 11



Search Insert Position

$\text{arr}[] = \{ 0, 1, 2, 3, 4, 5, 6 \}$
 $1, 3, 7, 10, 11, 15, 20 \}$

$\text{key} = 2$

$\text{key} = 14$

$\text{key} = 10$

if key is not present
return index of just bigger person!

if key is present in array return its index.

find \rightarrow index of cell value

$\text{arr}[] = \{ 0, 1, 2, 3, 4, 5, 6, 7, 8, 1, 2, 3, 7, 10, 11, 14, 20, 25 \}$

{ person just
greater or equal to

$\text{key} = 13$

lo hi

$\text{potentialAns};$

if ($\text{arr}[\text{mid}] == \text{key}$)

(19) (6)

else if ($\text{arr}[\text{mid}] > \text{key}$)

$\text{potentialAns} = \underline{\text{mid}}$;

$\text{hi} = \text{mid} - 1$;

else

$\text{lo} = \text{mid} + 1$;

$\text{arr}[] = \{ 0, 1, 2, 3, 4, 5, 6, 1, 3, 10, 15, 20, 24, 30 \}$

key = 3)

lo

hi if ($\text{arr}[\text{mid}] == \text{key}$)
return mid

pAns
↓
 $\cancel{\text{if}}(1)$

else if ($\text{arr}[\text{mid}] > \text{key}$)

potentialAns = mid;

hi = mid - 1;

else

lo = mid + 1;

find first and last position of Element

arr[] = { 0 1 2 3 4 5 6 7 8 9 10 11 }
[1, 1, 2, 2, 2, 3, 4, 5, 7, 7, 10, 11]

int fo = -1;

key = 2

{ while (lo <= hi)

{ int mid = (lo + hi) / 2;

if (arr[mid] == key) {

 fo = mid;
 hi = mid - 1;

else if (arr[mid] > key)

 hi = mid - 1;

else

 lo = mid + 1;

}

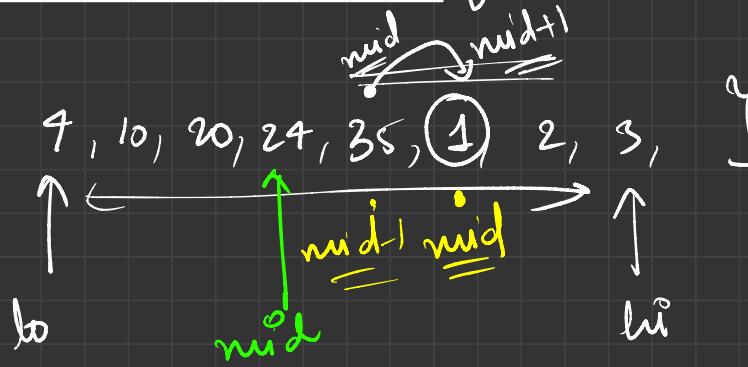
{ TC : O(log N)
SC : O(1)

Find Minimum in a Rotated Sorted Array

int[] = {

$\log_2 N$

TC:



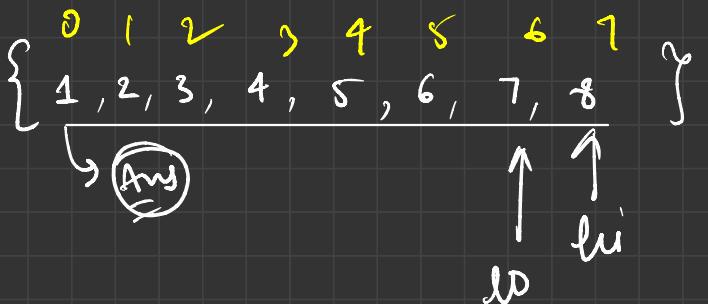
$\text{arr}[\text{mid}+1] < \text{arr}[\text{mid}]$

ans =

$\text{arr}[\text{mid}-1] > \text{arr}[\text{mid}]$

ans =

```
while ( lo <= hi )
{
    int mid = (lo + hi) / 2;
    if ( arr[mid+1] < arr[mid] )
        return mid + 1;
    else if ( arr[mid-1] > arr[mid] )
        return mid;
    else if ( arr[mid] >= arr[low] )
        lo = mid + 1;
    else
        hi = mid - 1;
}
```



```

while ( lo <= hi )
{
    int mid = (lo+hi)/2;
    if ( arr[mid+1] < arr[mid] )
        return mid+1;
    else if ( arr[mid-1] > arr[mid] )
        return mid;
    else if ( arr[mid] >= arr[low] )
        lo = mid+1;
    else
        hi = mid-1;
}

```

```

[ if (arr[0] <= arr[n-1]) {
    return 0;
}
]

```

Square Root of A Number

N

Brute force

$$N = 9$$

$i = \underline{\underline{i-1}}$

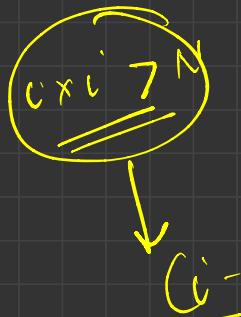
$$i = \sqrt{34}$$

$$1 \times 1 = 1 \leq 9$$

$$2 \times 2 = 4 \leq 9$$

$$3 \times 3 = \underline{\underline{9}} \leq \underline{\underline{9}}$$

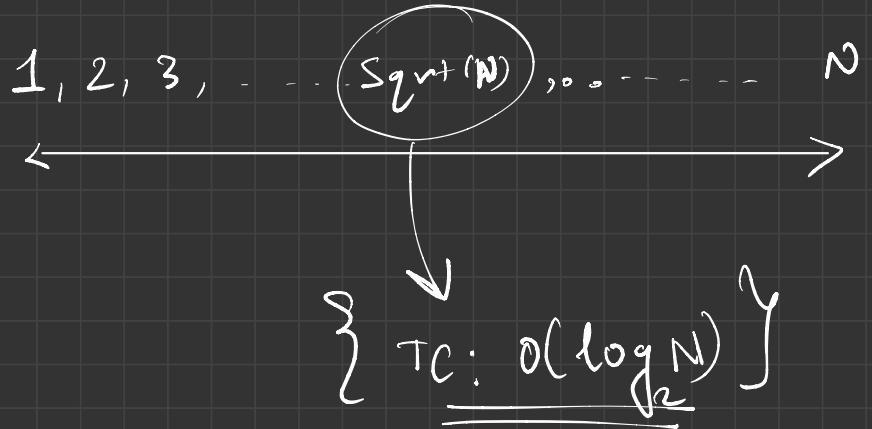
$$4 \times 4 = 16 \leq 9$$



Put $i = 1$
 while ($i \times i \leq N$)
 $i++$
 return $\underline{\underline{i-1}}$

$T C: O(\underline{\underline{\sqrt{N}}})$

1, 2, 3, 4, ..., \sqrt{N}



~~int psqrt = 0;~~

lo = 1, hi = N;

while (lo <= hi)

{ int mid = (lo + hi) / 2;

if (mid * mid == N)
return mid;

else if (mid * mid > N)

hi = mid - 1;

else ~~psqr = mid~~

lo = mid + 1;

}

N = 7

2

No perfect
Square

lo = 3, hi = ~~2~~
mid = 3

just
smaller

Search in 2D Matrix

$\text{mat}[\cdot][\cdot] =$

(0,0)	(0,1)	(0,2)	(0,3)
1	2	3	4
(1,0)	(1,1)	(1,2)	(1,3)
5	6	7	8

$$4 \times 1 \\ 40 \% 4 = 0 \\ (1,0)$$

0, 1, 2, 3, 4 —

$$2 / 4 = 0 \\ 20 \% 4 = 2$$

$$\text{key} = 11 \\ \cancel{\neq}$$

$$6 / 4 = 1 \\ 6 \% 4 = 2$$

$$3 \times 4 \\ \cancel{=} 12$$

$$\boxed{C_r = n/c \\ C_C = n \% c}$$

(1,2)

$$\text{low} = 0 \\ \text{high} = 11$$

$$s19 = 1 \\ s19 = 1$$

1D Array

[1, 2, 3, 4, 5, 7, 8, 9, 10, 11, 12]

0	a	b	c	d	e	9							
1	f	g	h	i	j								
2	k	(l)	m	n	o								

3×6

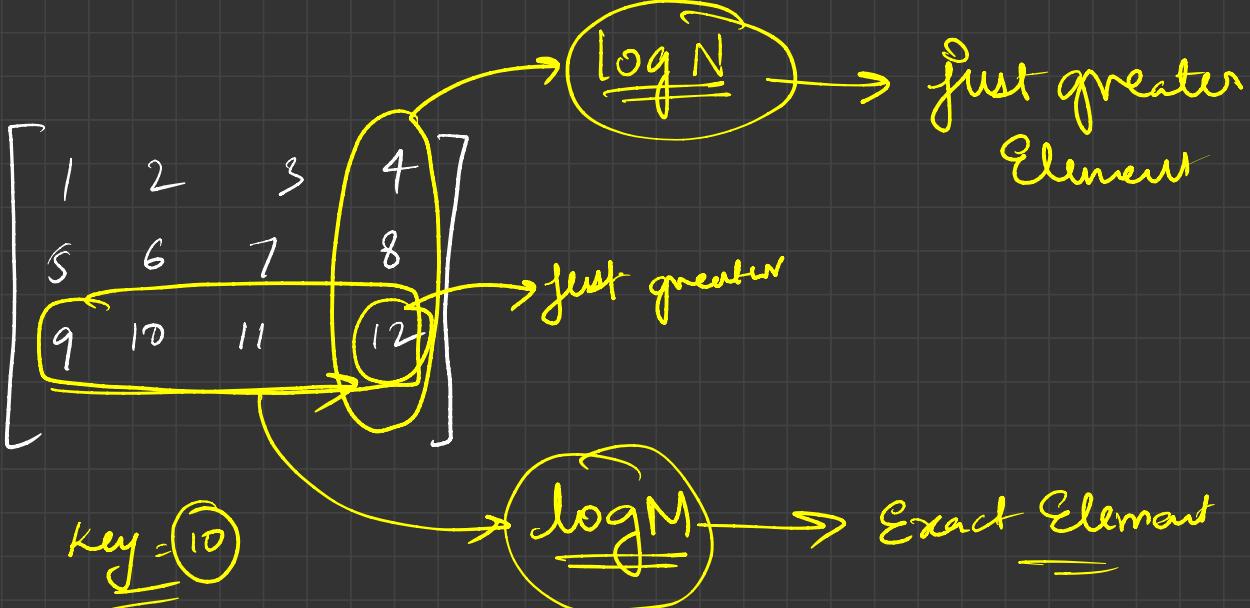
TC: $\log(M \times N)$

key: $\{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15\}$

a, b, c, d, e, f, g, h, i, j, k, l, m, n, o

$lo = 0$ $hi = 15$ $mid = 11$ $11 / 2 = 2$ $11 \% 2 = 1$ (21)

$\frac{8+14}{2} = 11$



1	2	3	4	5	6	7
8	9	10	11	12	13	19
15	16	17	18	19	20	21
22	23	24	25	26	27	28
29	30	31	32	33	34	35
36	37	38	39	40	41	42

exact Element

$\log M$

TC: $O(\log N + \log M)$

$O(\log N \times M)$

just greater

\hookrightarrow potential Row

$\log N$