



Stacks → linear data structure

}



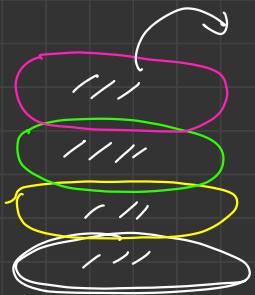
- ① Stack is a linear DS



Stack of plates



## Stack Operations



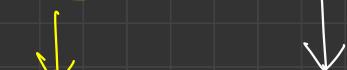
1. addition of new data in a stack  
is done on top

2. deletion of data from a stack  
is done from top

3. data on top is only readable

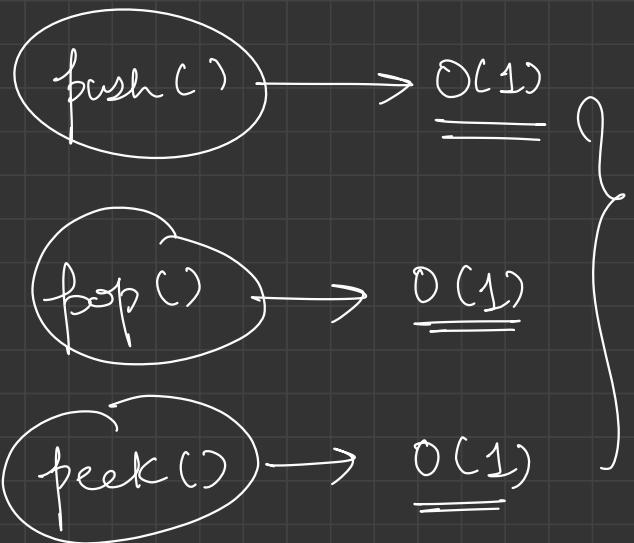
- { ① push() : add data in the stack  
(Top of the Stack)
- { ② pop() : removes topmost element from the  
stack .
- ③ peek() : See data present on the top of the stack

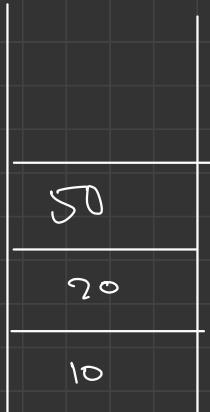
Stack < Integer > st = new Stack <>();



{ Integer, Float, Character, Long }  
↓  
Wrapper classes

OR  
our own  
defined  
classes





St

St. peek()  $\rightarrow$  30

St. pop()

St. peek()  $\rightarrow$  20

St. push(50)

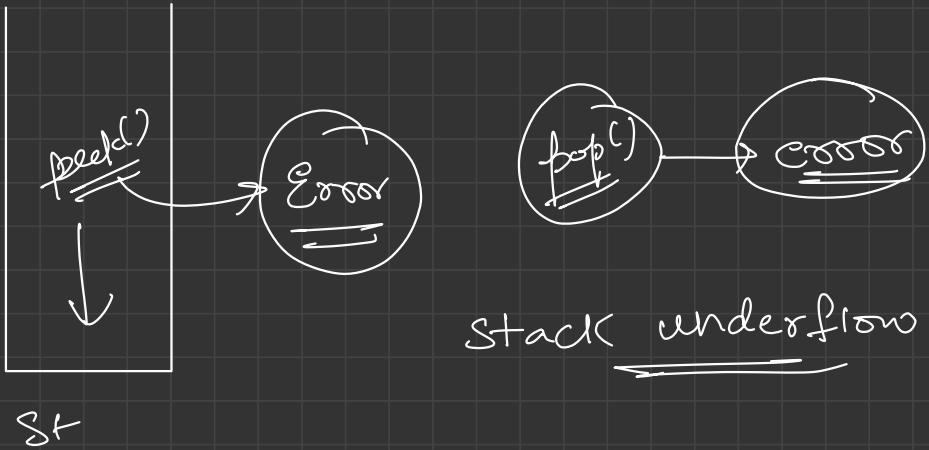
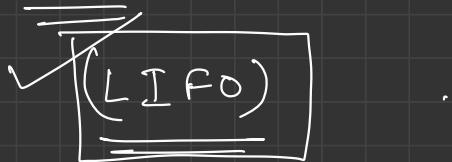
St. peek()  $\rightarrow$  50

St. size()  $\rightarrow$  3

① size()

size of the stack ↴

Stack follows, last in, but first out .



push (20)

push (50)

push (40)

push (30)

pop ()

50

50
40
30
20

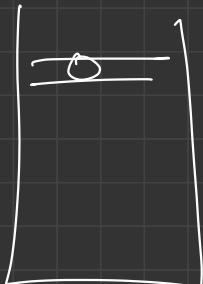
(last person in , first out)

## ArrayList

- ① add at last
- ② get any element
- ③ remove any element
- ④ size
- ⑤ Replace any element

## Stack

- ① push() on top
- ② pop() from top
- ③ peek() See on top()
- ④ size of stack



## linked list



add last()

add first()

remove last()

remove first()

size of linked list()



Q

$$\underline{(a + (b \times c) - (d \times f))} \rightarrow \underline{\text{false}} \quad (\text{No extra brackets})$$

$$(a + ((b + c)) - (d \times f)) \rightarrow \text{true}$$

extra bracket

\* Every bracket is balanced and we don't have  
any extra bracket !

$$( (a+b) \times (c+d) )$$

$(A \times B)$

$((A \times B))$

$$(((a+b) \times (c+d)))$$

$\underline{\underline{((A \times B))}}$

Not Required

~~A A A A A A A A A A A A~~  
( a + ( b \* c ) - ( d \* f ) )

① any operator, or opening bracket,  
possible part of a exp.

(+) → 'c' or operator char.

—  
+  
a  
(

Last person opened has to  
be closed first.

————  
( LIFO)

(-) → ')'   
search for corresponding st  
'( bracket in stack  
if st had some value  
use '( bracket' in stnd.

means, we have an exp.

$$(a+b) + c + (d+c))$$

~~a b + c d + c~~



St

```
if (ch == ')')
{
    st.push(ch);
}
```

```
else
{
    if (st.peek() == '(')
        return true;
}
```

else

```
{
    while(st.peek() != '(')
        st.pop();
    st.pop(); → corresponding opening
```



```

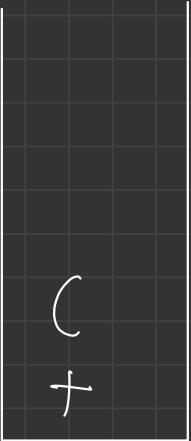
public boolean ExtraBrackets(String exp) {
    // Write your code here
    // true when extra bracket else false
    Stack<Character> st = new Stack<>();
    for (int i = 0; i < exp.length(); i++) {
        char ch = exp.charAt(i);

        // if '(' or ')' or Operator -> push in stack
        if (ch != ')') {
            st.push(ch);
        }

        else {
            // we got a closing bracket
            if (st.peek() == '(') {
                // no expression in between
                return true;
            } else {
                // removal of exp in between
                while (st.peek() != '(') {
                    st.pop();
                }
                // corresponding opening bracket for a closing bracket with exp in between
                st.pop();
            }
        }
    }
    return false;
}

```

ex<sup>2</sup>  $(a+b) + ((c+d))$



st

TC :  $O(N)$  ]  
SC :  $O(N)$  ]

$a+b+c+d$

(5)

for ( $i = 0 \rightarrow n$ )

}

while( )

$\boxed{N \text{ times in its life span}}$

}

O(2N)

$i = 0, 1, 2, 3, 4$

↓    ↓    ↓    ↓    ↓

- - - - -

$N \text{ times}$

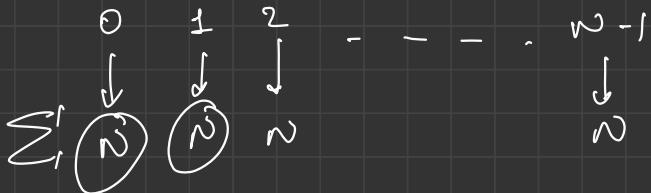
$O(N^2)$

for ( $i \rightarrow 0 \rightarrow n$ )

}

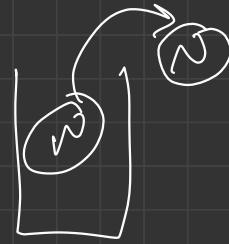
    while ( $\leq N$ )

}



$$= N + N + N + \dots + N \text{ times}$$

$\overbrace{N \times N} = \underline{\underline{N^2}}$



$O(N)$

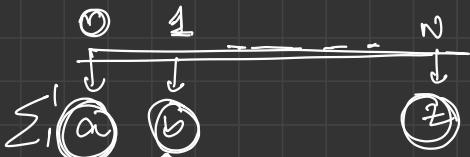
for ( $i = 0 \rightarrow n$ )

}

    while ( $i < n$ )

}

( $N$  time in life)



=  $a + b + \dots + z$   $\text{operator}$

$\Rightarrow \underline{\underline{N}} \text{ times}$

# Next Greater Element on Right

arr[] = [2, 5, 9, 3, 1, 12, 6, 8, 7]

nger[] : [5, 9, 12, 12, 12, -1, 8, -1, -1]

Solve? ① BruteForce

→ int[] nger = new - - -

for (int i=0; i < n)

{ for (int j=i+1; j < n)

if (arr[j] > arr[i])

{ nger[i] = arr[j]  
break;

$$\sum \text{TC} \stackrel{\text{def}}{=} \underline{\underline{O(N^2)}}$$

$$\sum (N-1) + (N-2) + \dots + 1$$

$$= \frac{(N-1)N}{2} = \underline{\underline{O(N^2)}}$$

$\text{Sc: } O(1)$   
 $\text{TC: } O(N^2)$



$\text{arr}[ ] = [2, 5, 9, 3, 1, 12, 6, 8, 7]$

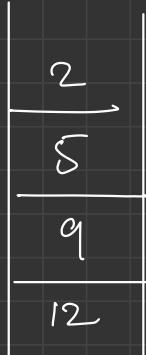
$\text{nger}[ ] = [5, 9, 12, 12, 12, -1, 8, -1, -1]$

## # Approach 1

① traverse array from last to start.

$\begin{array}{ccccccccc} \downarrow & \downarrow & \downarrow & \swarrow & \nwarrow & \searrow & \nearrow & \searrow & \downarrow \\ [2, 5, 9, 3, 1, 12, 6, 8, 7] \\ \rightarrow [5, 9, 12, 12, 12, -1, 8, -1, -1] \end{array}$

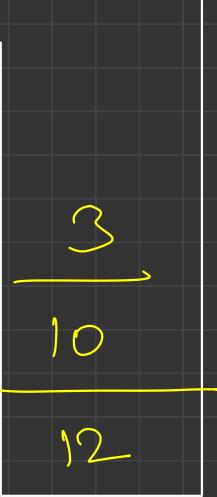
{  
    if ( $\text{st.size}() == 0$ )  
         $\text{nger}[i] = -1$ ;  
    else  
        remove element from the stack  
        if ( $\text{st.size} == 0$ )  $\text{nger}[i] = -1$  till anything bigger  
        else  $\text{nger}[i] = \text{st.pop}();$   
         $\text{st.push}(\text{arr}[i])$ ;



st

10 12 4 5 [ 5 9 12 12 -1 8 -1 -1  
 3 10, 1, 4 [ 2, 5 9, 3, 1, 12, 6, 8, 7 ]

```
class Solution {
    public static long[] nextLargerElement(long[] arr, int n) {
        // Write code here and print output
        long[] nger = new long[n];
        Stack<Long> st = new Stack<>();
        for (int i = n - 1; i >= 0; i--) { → N + 2 loops
            if (st.size() == 0) {
                nger[i] = -1;
            } else {
                while (st.size() > 0 && st.peek() <= arr[i]) {
                    st.pop(); ← N time
                }
                if (st.size() == 0) {
                    nger[i] = -1; ✓
                } else {
                    nger[i] = st.peek(); ← life time
                }
            }
            st.push(arr[i]); ←
        }
        return nger;
    }
}
```

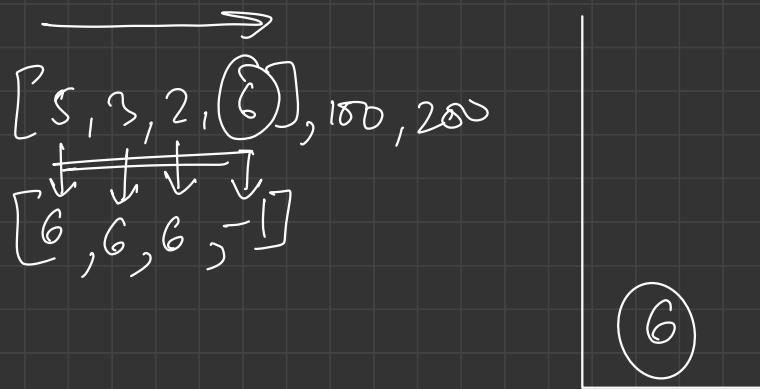


Time Complexity :  $O(N)$

Space Complexity :  $O(N)$  → Stack Space

$\text{arr}[] = [2, 5, 9, 3, 1, 12, 6, 8, 7]$

# Approach 2



push → when topmost element of stack is greater than you

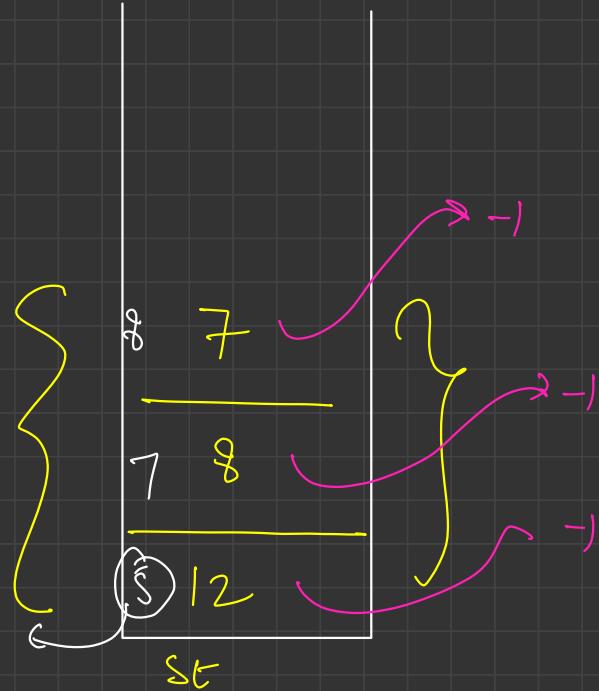
pop() → when some greater than me was encountered,

$\text{arr}[] = [5, 9, 12, 12, 12, -1, 8, -1, -]$

(+) when stack top is greater than me, or empty.

(-) when curr ele, is greater than peek(), and curr is peek's neighbor.

$$\underline{\underline{\text{ngtr}(8)}} = -1$$



```

// Approach 2:
public static long[] nextLargerElement(long[] arr, int n) {
    // Write code here and print output
    long[] nger = new long[n];
    Stack<Integer> st = new Stack<>();

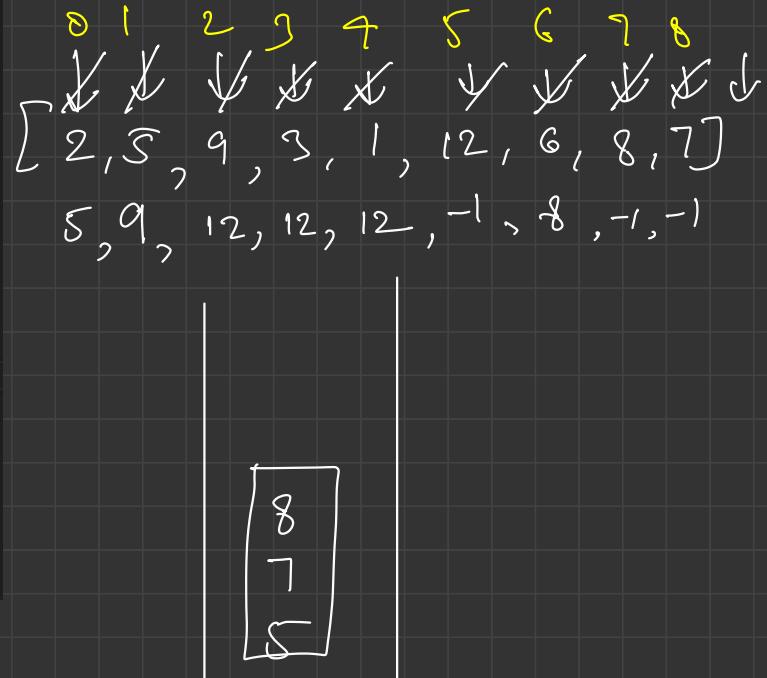
    for (int i = 0; i < n; i++) {
        while (st.size() > 0 && arr[st.peek()] < arr[i]) {
            int idx = st.pop();
            nger[idx] = arr[i];
        }
        st.push(i);
    }

    while (st.size() > 0) {
        int idx = st.pop();
        nger[idx] = -1;
    }

    return nger;
}

```

TC:  $O(N)$   
SC:  $O(N)$

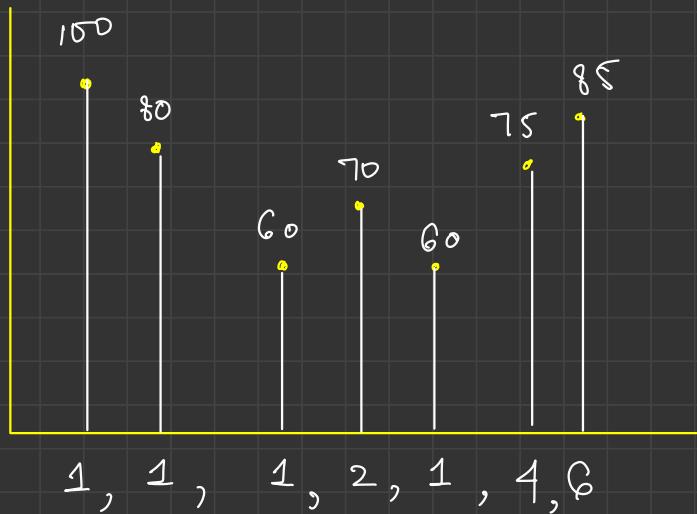


## Stock Span

Stock[] = [100, 80, 60, 70, 60, 75, 85]  
0<sup>th</sup> 1<sup>st</sup> 2<sup>nd</sup> 3<sup>rd</sup> 4<sup>th</sup> 5<sup>th</sup> 6<sup>th</sup>

2 1 4

= 1 - sum

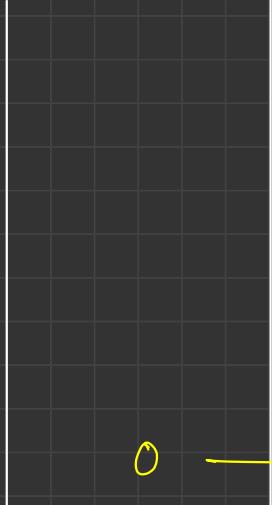


$\downarrow$  [100, 80, 60, 70, 60, 75, 85]

0<sup>th</sup> 1<sup>st</sup> 2<sup>nd</sup> 3<sup>rd</sup> 4<sup>th</sup> 5<sup>th</sup> 6<sup>th</sup>  
0 0 1 2 3 1 0

ngeli [ -1, 0, 1, 1, 3, 1, 0 ]

span[2] [ 1, 1, 1, 2, 1, 4, 6 ]



0 → 100

SC:  $O(N)$

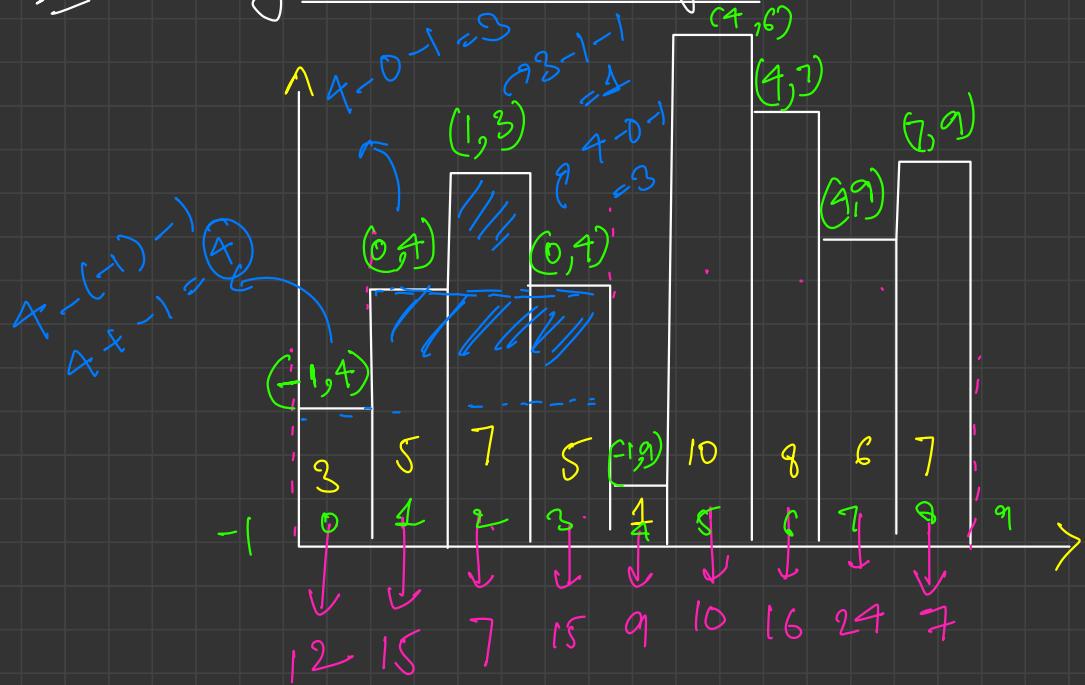
```
class Solution {  
    static int[] nextGreaterEleOnLeftIdx(int[] a, int n) {  
        int[] ngeli = new int[n];  $O(N)$   
        Stack<Integer> st = new Stack<>();  $O(N)$   
        for (int i = n - 1; i >= 0; i--) {  
            if (st.size() == 0) {  
                st.push(i);  
            } else {  
                while (st.size() > 0 && a[st.peek()] < a[i]) {  
                    int idx = st.pop();  
                    ngeli[idx] = i;  
                }  
                st.push(i);  
            }  
        }  
  
        while (st.size() > 0) {  
            int idx = st.pop();  
            ngeli[idx] = -1;  
        }  
  
        return ngeli;  
    }  
  
    static int[] stockSpan(int[] a) {  
        int[] ngeli = nextGreaterEleOnLeftIdx(a, a.length);  
        int[] span = new int[a.length];  
        for (int i = 0; i < a.length; i++) {  
            span[i] = i - ngeli[i];  
        }  
        return span;  
    }  
}
```

TC:  $O(N)$

SC:  $O(N)$

Q

# largest Area Histogram



$$\text{width} = r - l - 1$$

Step 5

① get next smaller element by  ${}^{\circ}\text{idx}$  on left

② get next smaller ele by  $\text{idx}$  on Right

③ width =  $\gamma - l - 1$       area = height  $\times \underline{\text{width}}$



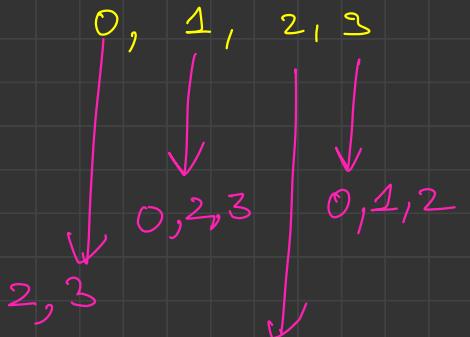
## # Celebrity Problem

	0	1	2	3
0	0 (0,0)	0 (0,1)	1 (0,2)	1 (0,3)
1	1 (1,0)	0 (1,1)	1 (1,2)	1 (1,3)
2	0 (2,0)	0 (2,1)	0 (2,2)	0 (2,3)
3	1 (3,0)	1 (3,1)	1 (3,2)	0 (3,3)

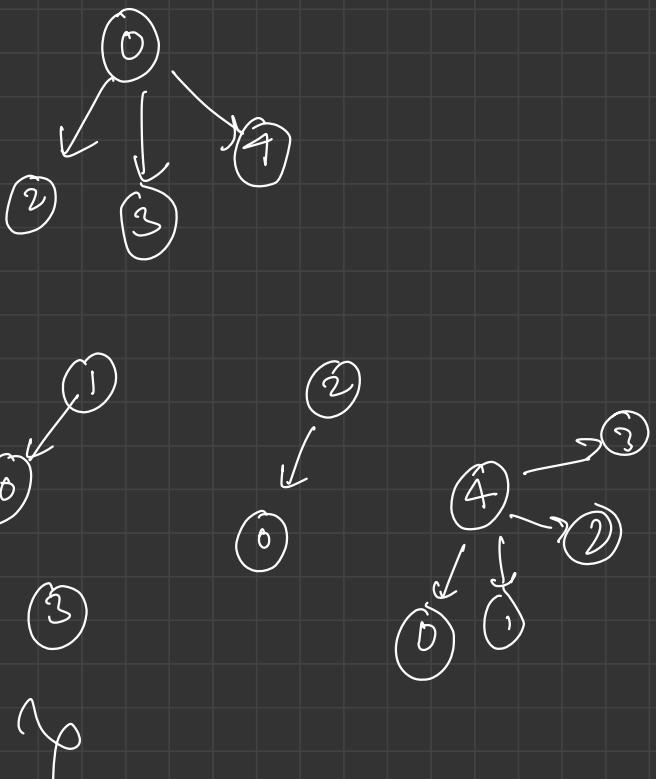
$\left\{ \begin{array}{l} n \times n \\ \downarrow \\ n \text{ different persons} \end{array} \right.$

If  $i$  knows  $j$   $\text{arr}[i][j] = 1$

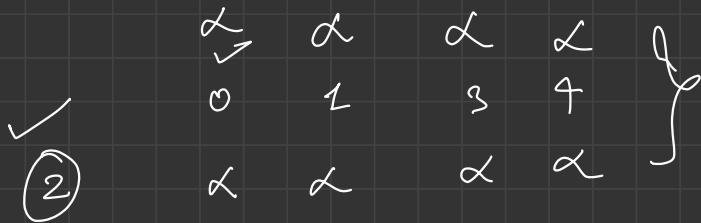
If  $i$  doesn't know  $j$   $\text{arr}[i][j] = 0$



	0	1	2	3	4
0	0	0	1	1	1
1	1	0	0	0	0
2	1	0	0	0	0
3	0	0	0	0	0
4	1	1	1	1	0



- ① He should not know anyone
- ② He should be known by everyone



Only One cell at Max possible!

Brute force  $\underline{\underline{TC: O(N^2)}}$

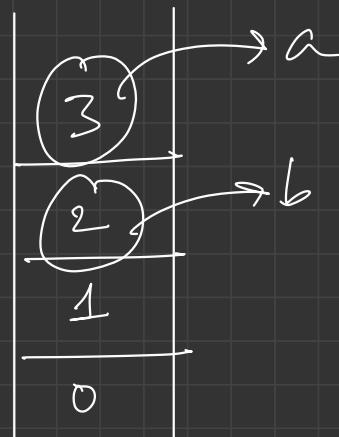
## elimination technique

	0	1	2	3
0	0 (0,0)	0 (0,1)	1 (0,2)	1 (0,3)
1	1 (1,0)	0 (1,1)	1 (1,2)	1 (1,3)
2	0 (2,0)	0 (2,1)	0 (2,2)	0 (2,3)
3	1 (3,0)	1 (3,1)	1 (3,2)	0 (3,3)

~~if~~  $\text{arr}[a][b] = 1$  {a knows b}

b can be my

cell



if  $\text{arr}[a][b] = 0$   
? a doesn't  
know b

Stack

a can be my

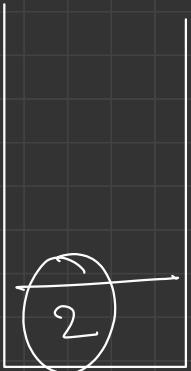
cell

Step 1 get top 2 elements of stack

if  $\text{arr}[a][b] = 1$ , st.push(b) ;

else st.push(a);

	0	1	2	3
0	0 (0,0)	0 (0,1)	1 (0,2)	1 (0,3)
1	1 (1,0)	0 (1,1)	1 (1,2)	1 (1,3)
2	0 (2,0)	0 (2,1)	0 (2,2)	0 (2,3)
3	1 (3,0)	1 (3,1)	1 (3,2)	0 (3,3)



celeb = 2

```

class Solution {
    int findCelebrity(int M[][], int n) {
        // step 1: add everyone to the stack
        Stack<Integer> possibleCelebs = new Stack<Integer>();
        for (int i = 0; i < n; i++) {
            possibleCelebs.push(i);
        }

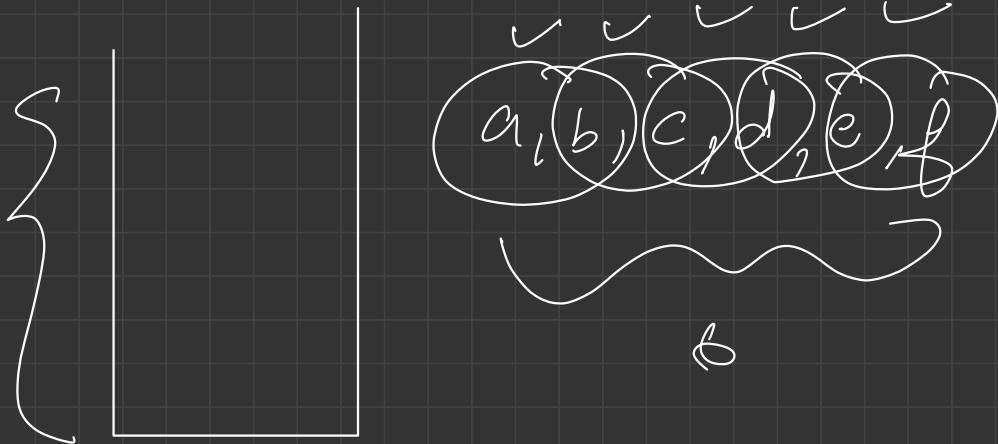
        while(possibleCelebs.size() >= 2) {
            int p1 = possibleCelebs.pop();
            int p2 = possibleCelebs.pop();

            if (M[p1][p2] == 1) {
                // p1 knows p2, hence p2 can be celeb but p1 cann't be
                possibleCelebs.push(p2);
            } else {
                // p1 doesn't know p2, hence p2 can't be a celeb, but p1 can be one
                possibleCelebs.push(p1);
            }
        }

        int celeb = possibleCelebs.pop();
        // check row
        for (int c = 0; c < n; c++) {
            if(M[celeb][c] == 1) {
                return -1;
            }
        }
        if (c != celeb && M[c][celeb] == 0) {
            return -1;
        }
    }
}

```

return celeb;



$$\begin{array}{c}
 \left. \begin{array}{l} TC: O(N) + O(N) + O(N) = O(3N) = O(N) \\ SC: O(N) \end{array} \right\} \\
 \hline
 \end{array}$$

# Evaluate Infix Expressions.

Rule      BODMAS

#

$$2 * 4 / (\underline{4 / 2}) + 6$$

① first Brackets  
are evaluated

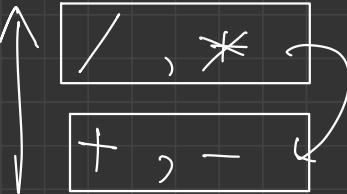
①

$$2 * 4 / 2 + 6$$

② precedence:

③

$$4 + 6$$



④

10

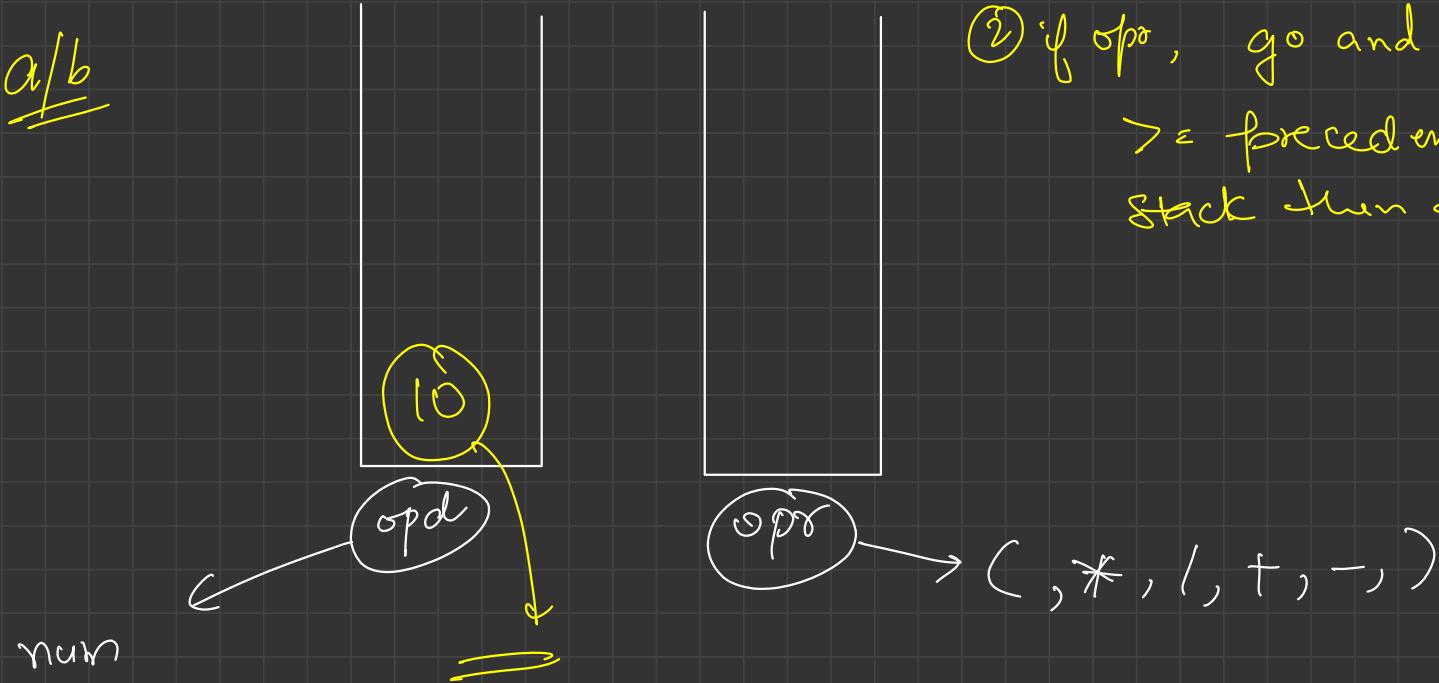
$$\begin{array}{ll} / - 2 & + \rightarrow 1 \\ * - 2 & - \rightarrow 1 \end{array}$$

$$2 * 4 / (4 / 2) + 6$$


① if opd, opd. push (ch)

② if so, go and solve

$> \in$  precede from  
stack then add me.





```

public int precedence(char o) {
    if (o == '+') {
        return 1;
    } else if (o == '-') {
        return 1;
    } else if (o == '/') {
        return 2;
    } else {
        // o -> *
        return 2;
    }
}

```

```

public int eval(int v1, int v2, char o) {
    if (o == '+') {
        return v1 + v2;
    } else if (o == '-') {
        return v1 - v2;
    } else if (o == '/') {
        return v1 / v2;
    } else {
        // o -> *
        return v1 * v2;
    }
}

```

$2 \times 4 / (7 / 2) + 6$

```

public int solve(String exp) {
    // consist of operands
    Stack<Integer> opd = new Stack<>();
    // consist of operators
    Stack<Character> opr = new Stack<>();

    for (int i = 0; i < exp.length(); i++) {
        char ch = exp.charAt(i);

        if (Character.isDigit(ch) == true) {
            opd.push(ch - '0');
        } else if (ch == '(') {
            opr.push(ch);
        } else if (ch == ')') {
            while (opr.peek() != '(') {
                int v2 = opd.pop();
                int v1 = opd.pop();

                char o = opr.pop();

                int ans = eval(v1, v2, o);

                opd.push(ans);
            }
            opr.pop();
        } else {
            // ch -> *, /, +, -
            while (opr.size() > 0 && opr.peek() != '(' && precedence(ch) <= precedence(opr.peek())) {
                int v2 = opd.pop();
                int v1 = opd.pop();

                char o = opr.pop();

                int ans = eval(v1, v2, o);

                opd.push(ans);
            }
            opr.push(ch);
        }
    }
}

```

```

while (opr.size() > 0) {
    int v2 = opd.pop();
    int v1 = opd.pop();

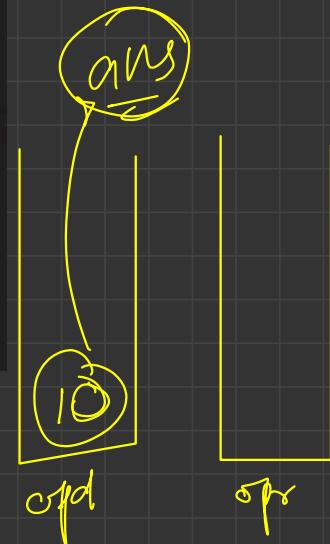
    char o = opr.pop();

    int ans = eval(v1, v2, o);

    opd.push(ans);
}

return opd.peek();
}

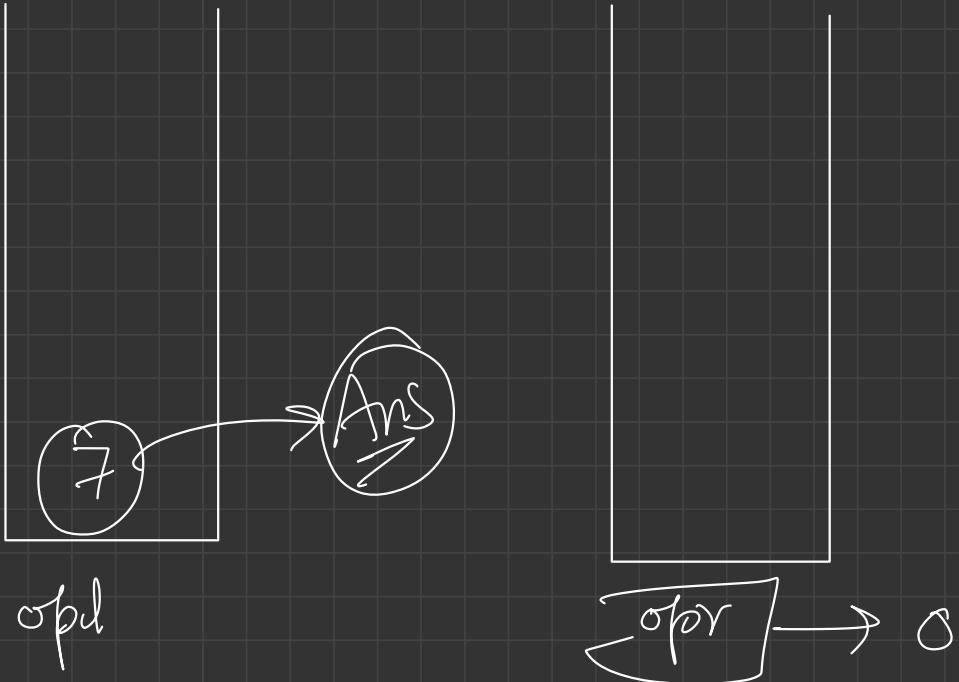
```



$$2 * 4 / ((4 / 2) + (2 * 3)) + 6$$

Diagram illustrating the expression evaluation:

- The expression is  $2 * 4 / ((4 / 2) + (2 * 3)) + 6$ .
- Arrows point from each character to its corresponding memory location:
  - Two locations for  $2$
  - Four locations for  $*$
  - One location for  $4$
  - One location for  $/$
  - Two locations for  $($
  - One location for  $4$  (inside the first parenthesis)
  - One location for  $/$  (inside the first parenthesis)
  - Two locations for  $)$  (inside the first parenthesis)
  - Two locations for  $+$
  - Two locations for  $($  (inside the second parenthesis)
  - One location for  $2$  (inside the second parenthesis)
  - One location for  $*$  (inside the second parenthesis)
  - Three locations for  $3$  (inside the second parenthesis)
  - One location for  $)$  (inside the second parenthesis)
  - One location for  $+$
  - One location for  $6$
- The result is  $V1 * V2 = 8$ .



Convert Infix to postfix and prefix.

$$2 * 4 / (4 / 2) + 6 \rightarrow \underline{\text{Infix}}$$

postfix

prefix

left → right & point.

opd + opr

opr + opd

point → left → right

/ \* 2 4 + / 4 2 6

