



Hashing → technique used for searching purpose

{ Linear Search → TC: $O(N)$
Binary Search → TC: $O(\log_2 N)$

→ $TC: O(1)$ → Searching

ex: 8, 3, 13, 6, 4, 10, 9, 7, 50 (user input)

key = 13

search(int val)

TC: O(1)

boolean arr[]

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
			✓	✓		✓	✓	✓	✓	✓			✓					

50
✓

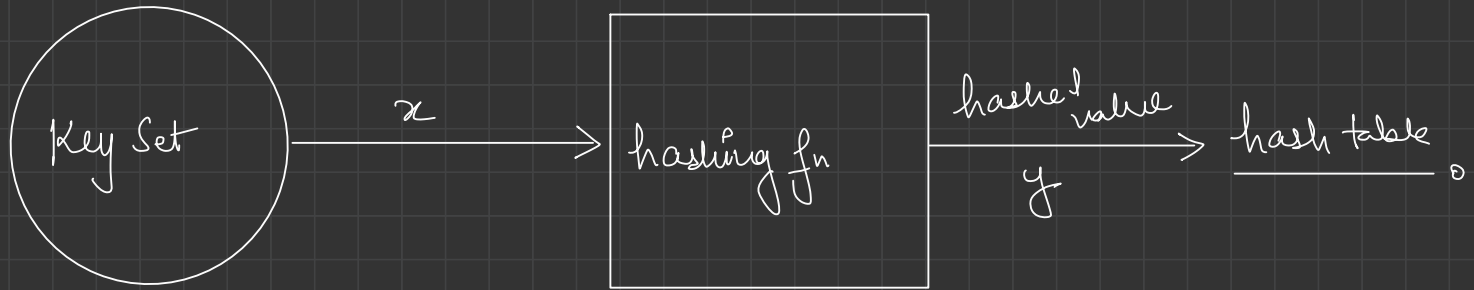
TC: O(1)

search(13)

```
{ if (arr[13] == true)
    return true;
else
    return false;
}
```

a lot of empty space

Memory wastage!
to overcome issue, hashing
was introduced.



hashing fn (2 step process)

step 1

$$g(x) = k$$

integer value

step 2

$$h(k) = y$$

hashed value

Keyset

8

3

66

4

19

207

$$h(x) = x \% 10 \text{ hash fn}$$

size of hash table

$$h(8) = 8 \% 10 = 8$$

$$h(3) = 3 \% 10 = 3$$

$$h(66) = 66 \% 10 = 6$$

$$h(4) = 4 \% 10 = 4$$

$$h(19) = 19 \% 10 = 9$$

$$h(207) = 207 \% 10 = 7$$

Hash Table

0

1

2

3

4

5

6

7

8

9

3

4

66

207

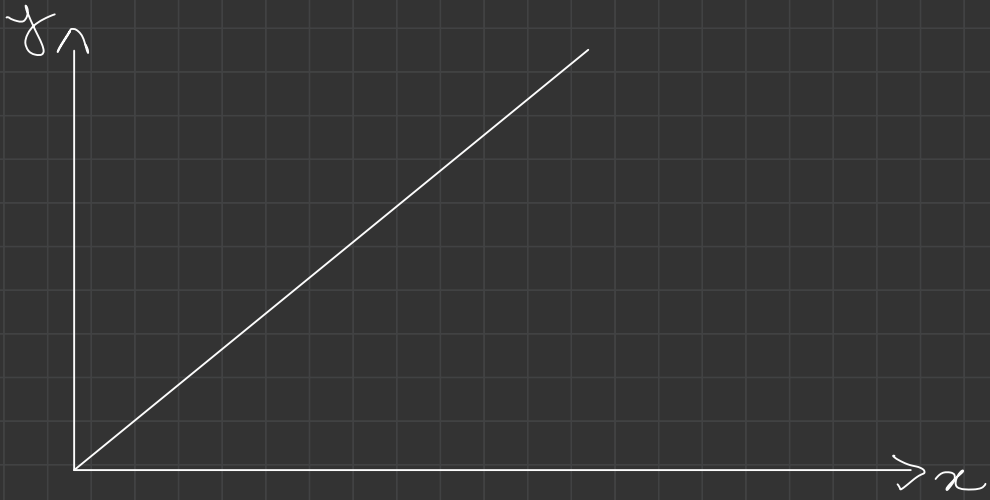
8

19

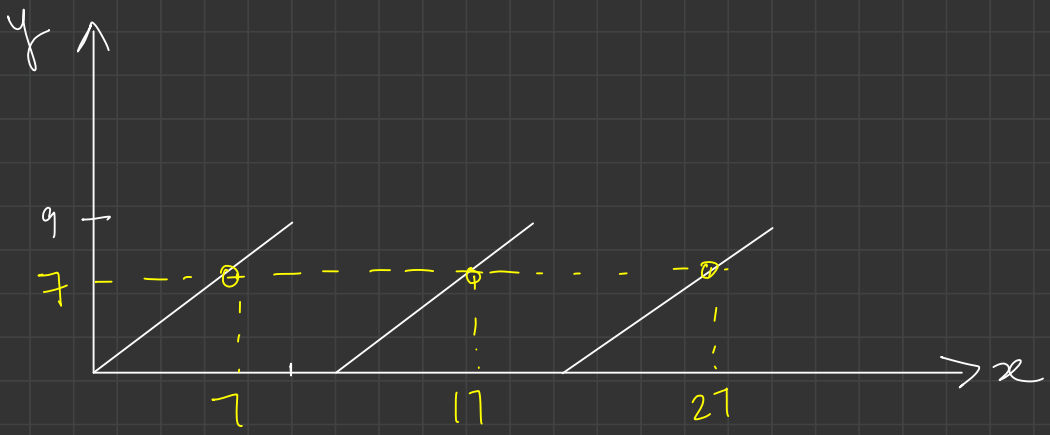
Search (207)

TC: O(1)

One to one mapping



many to one



$$h(x) = x \% 10 \text{ hash fn}$$

Keyset

8

3

66

4

19

207

33

$$h(8) = 8 \% 10 = 8$$

$$h(3) = 3 \% 10 = 3$$

$$h(66) = 66 \% 10 = 6$$

$$h(4) = 4 \% 10 = 4$$

$$h(19) = 19 \% 10 = 9$$

$$h(207) = 207 \% 10 = 7$$

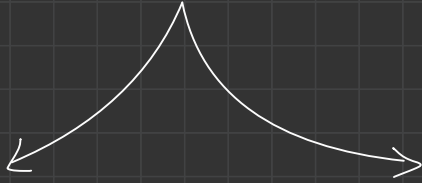
$$h(33) = 33 \% 10 = 3$$

Hash Table

0	
1	
2	
3	3
4	4
5	
6	66
7	207
8	8
9	19

Collision

Methods to Remove Collision



Closed hashing

→ linear probing

→ quadratic probing

Open hashing

→ chaining

Chaining

$$h(x) = x \% 10 \text{ hash fn}$$

Keyset

- 8
- 3
- 66
- 4
- 19
- 207
- 33
- 23

$$h(8) = 8 \% 10 = 8$$

$$h(3) = 3 \% 10 = 3$$

$$h(66) = 66 \% 10 = 6$$

$$h(4) = 4 \% 10 = 4$$

$$h(19) = 19 \% 10 = 9$$

$$h(207) = 207 \% 10 = 7$$

$$h(33) = 33 \% 10 = 3$$

$$h(23) = 3$$

Searching (33)
→ 3

Hash Table
AL LL

0	
1	
2	
3	2 → 33 → 23
4	4
5	
6	66
7	207
8	8
9	19

hash fn

$$h(x) = x \% \underline{\underline{\text{load factor}}}$$



75% of range of values given

0-150

$$\rightarrow lf = \boxed{75} \checkmark$$

Linear Probing

$$h'(x) = [h(x) + f(i)] \% \text{size}$$

\downarrow
 (10)

Keyset

$$h(x) = x \% 10$$

$$f(i) = i, i \in \mathbb{R}[0, \infty)$$

$$\begin{aligned} h'(8) &= [h(8) + f(0)] \% 10 \\ &= (8 + 0) \% 10 = 8 \end{aligned}$$

$$\begin{aligned} h'(3) &= [h(3) + f(1)] \% 10 \\ &= (3 + 1) \% 10 = 4 \end{aligned}$$

$$\begin{aligned} h'(66) &= [h(66) + f(2)] \% 10 \\ &= (6 + 2) \% 10 = 8 \end{aligned}$$

$$h'(33) = [h(33) + f(0)] \% 10 = (3 + 0) \% 10 = 3$$

$$h'(33) = [h(33) + f(1)] \% 10 = (3 + 1) \% 10 = 4$$

$$h'(4) = [h(4) + f(0)] \% 10 = (4 + 0) \% 10 = 4$$

$f(1) \rightarrow 5$

Hash Table

0	
1	
2	
3	3
4	33
5	4
6	66
7	23
8	8
9	

linear hashing

↳ disadv: clustering issue!

quad probing

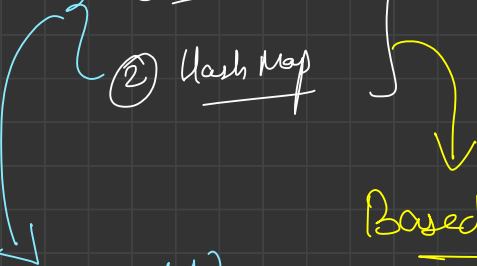
$$h'(n) = [h(n) + f(i)] \% \text{size}$$

$$h(n) = x \% \text{size}$$

$$f(i) = i^2, i \in \mathbb{R}$$

2 - Data Structures

- ① Hash Set
- ② Hash Map



TC: O(1)

Searching

Based On Hash Theory

Hash Set : Stores unique entity

Hash Map
↳ <key, value>

Cart



key

String

value

integer

prd

qty

{
 lays → 2
 coke → 3

$O(1)$

HashMap

TreeMap

TreeSet

here keys are in ordered format

Searching
↳ $O(\log N)$

based

Red Black Tree

↳ Self Balancing Tree