



Problem with given diff.

$$\text{arr[]} = [5, 10, 3, 2, 50, 80] \quad B = 78$$

pair(10, 3)

$$10 - 3 = 7$$

$$3 - 10 = -7$$

TC: O(N²)

SC: O(1)

for (int i = 0 → n)

{

 for (int j = i + 1 → n)

 {

 if (arr[i] - arr[j] == 8 ||

 arr[j] - arr[i] == 8)

 return 1;

Brute force

$$\text{arr[]} = [5, 10, 3, 2, 50, 80]$$

i ↑

← →

j ↑

$$\text{arr[]} = [5, 10, 3, 2, 50, 80] \quad B = 45$$

① sort in array. $\rightarrow TC: O(N \log N)$

$[2, 3, 5, 10, 50, 80]$

i j

NOT WORKING

~~while ($i < j$)
{
 int diff = arr[j] - arr[i];
 if (diff > B)
 j--;
 else if (diff < B)
 i++;
}~~

$\text{arr}[] = [5, 10, 3, 2, 50, 80]$

$$B = 78$$

$$80 - 78$$

$$x - y = 3$$

$$x = 80, y = 2$$

$$x = 50, y = -28$$

$$y = 50, x = 128$$

$$x = 2, y = -76$$

$$y = 2, x = 80$$

$$x = 5, y = -75$$

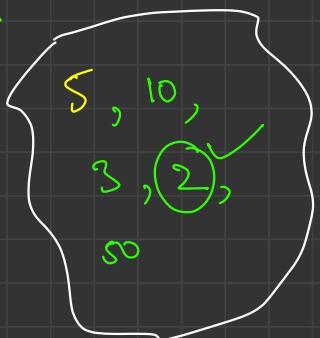
$$y = 5, x = 81$$

$$x = 5$$

$$x = 0, y = -68$$

$$y = 8 - 78 = -70 \quad x = 10, x = 88$$

$$y = 5, x = 78 + 5 = 83$$



set

$$\text{let } x = 5$$

$$5 - y = 3$$

$$\boxed{y = 5 - 3} \rightarrow ①$$

$$\underline{\underline{(80, 2)}}$$

$$\text{let } y = 5$$

$$x - 5 = 3$$

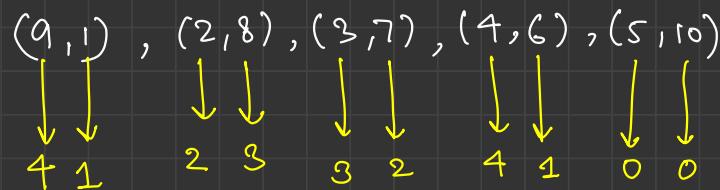
$$\boxed{x = 3 + 5} \rightarrow ②$$

Array pair divisible by K

$$\text{arr}[\Gamma] = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\} \quad \underline{\underline{K=5}}$$

$$N = 10$$

(5)



if $\text{newy} = 1$

$$\text{rem}_2 = 5 - 1 = 4$$

$$\text{rem}_1 = 2$$

$$\text{rem}_2 = 5 - 2 = 3$$

$\text{arr}[\cdot] = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ $k = 5$

rem	freq
1	2
2	2
3	2
4	2
0	2

$O(N)$

```
public boolean arrayPairs(int[] arr, int k) {
    // write code here
    HashMap<Integer, Integer> map = new HashMap<>();
    for (int i = 0; i < arr.length; i++) {
        int rem = arr[i] % k;
        map.put(rem, map.getOrDefault(rem, defaultValue: 0) + 1);
    }
}
```

1 + 1

freq-Map

$$O - (k - 1)$$

$$x \underset{\approx}{=} k$$

$0, 1, 2, \dots, (k - 1)$

rem	freq
1	2
2	2
3	2
4	2
0	2

$O(N)$

```

for (int rem : map.keySet()) {
    int compRem = k - rem;       $\cancel{S - 0} \Rightarrow \cancel{S}$ 
    if (map.containsKey(compRem) == false) {
        // compRem is not present
        return false;
    } else if (map.get(compRem) != map.get(rem)) {
        // compRem freq != rem freq
        return false;
    }
}
return true;

```

$$\text{rem} = 1, \text{ compRem} = 4$$

$$\text{rem} = 2, \text{ compRem} = 3$$

$$\text{rem} = 3, \quad = 2$$

TC: $O(N)$
SC: $O(K)$

$$k=5$$

new	free
1	3
2	5
3	4
4	3

$$\text{rem} = 1 \quad \text{comp} = 4$$

$$\text{rem} = 2 \quad \text{comp} = 3$$

Largest Subarray With Zero Sum

$\text{arr}[] = [15, -2, 2, -8, 1, 7, 10, 28]$

Brute-force

compute all subarray sum, and store maxlen.

TC : $O(N^2)$

SC : $O(1)$

$\text{arr}[] = [0, 1, 2, 3, 4, 5, 6, 7]$
 $[15, -2, 2, -8, 1, 7, 10, 23]$
 ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓
 15 13 15 7 8 15 25 48

15 → 0

13 → 1

7 → 3

8 → 4

len of subarray with

$$\text{sum zero} = 2 - 0 = 2$$

Sum occurred
again

Sum
encountered
first
time

$$5 - 0 = 5$$

$\text{arr} = [\underset{\nearrow}{1}, \underset{\nearrow}{-1}, \underset{\nearrow}{2}, \underset{\nearrow}{-2}]$

$\text{sum} = \cancel{1} \cancel{-1} \cancel{2} \cancel{-2}$

$$1 - (-1) = 2$$

$$2 - (-1) = 4$$

sum	idx
0	-1
1	0
2	2

```
// TC: O(N), SC: O(N)
public int maxLen(int arr[]) {
    // Write your code here
    HashMap<Integer, Integer> map = new HashMap<>();

    int sum = 0;
    int maxlen = 0;
    map.put(key: 0, -1);

    for (int i = 0; i < arr.length; i++) {
        sum += arr[i];

        if (map.containsKey(i - sum)) {
            int len = i - map.get(sum);
            maxlen = Math.max(maxlen, len);
        } else {
            map.put(sum, i);
        }
    }

    return maxlen;
}
```

Equilibrium Index

$a[] \cdot [9, 3, 7, 6, 8, 1, 10]$

Brute-force Approach

$\overbrace{[9, 3, 7, 6, 8, 1, 10]}$

TC: $O(N^2)$

for ($i \rightarrow 0 \rightarrow n$)
 \hat{i}

$\left\{ \begin{array}{l} \text{for } (0 - i) \\ \text{LSum} \end{array} \right.$

for ($i \rightarrow n - 1$)
RSum

$\left. \begin{array}{l} \text{if LSum} = \text{RSum} \\ \text{equil point} \end{array} \right\}$

$\alpha[\Gamma]. [\boxed{0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6} | [9, 8, 7, 6, 8], 1, 10]$

prefix Sum Array

$[\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 \\ 9 & 12 & 19 & 28 & 33 & 34 & 44 \end{matrix}]$

$$pSum[4] = \underbrace{\text{arr}[0] + \text{arr}[1] + \text{arr}[2] + \text{arr}[3]}_{\downarrow} + \text{arr}[4]$$

$$pSum[4] = pSum[3] + \text{arr}[4] \quad pSum[n] = \text{arr}[n] + pSum[n-1]$$

```
→ int [] fsum = new int [n];
```

```
fsum[0] = arr[0];
```

```
for (int i = 1; i < n; i++)
```

```
{
```

```
fsum[i] = arr[i] + fsum[i-1];
```

```
}
```

$\text{arr}[] : [1, 2, 3, 4, 5, 6]$

$$\left\{ \begin{array}{l} pSum[0] = arr[0] \\ pSum[1] = arr[0] + arr[1] = pSum[0] + arr[1] \\ pSum[2] = arr[0] + arr[1] + arr[2] = pSum[1] + arr[2] \\ \vdots \end{array} \right.$$

$$pSum[n] = pSum[n-1] + arr[n]$$

$$a[] = [\begin{smallmatrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 \\ 9, 3, 7, 6, 8, 1, 10 \end{smallmatrix}]$$

$$[LSum[i]] = [\begin{smallmatrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 \\ 9, 12, 19, 25, 33, 34, 44 \end{smallmatrix}] \rightarrow O(N)$$

$$[RSum[i]] = [\begin{smallmatrix} 44, 35, 32, 25, 19, 11, 10 \\ \hline \end{smallmatrix}] \rightarrow O(N)$$

$$RSum[i-1] = a[i-1];$$

for(
int i=n-2 ; i>=0 ; i--)
{
 RSum[i] = a[i] + RSum[i+1];
}

for(
int i=0 → n)

if ([LSum[i]) == RSum[i])

i is equal position.

TC : O(N)
SC : O(N)

$$a[] = [0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10] \quad \text{totalSum} = 44$$

$$lsum[] = [0, 1, 2, 3, 4, 5, 6, 7, 12, 19, 25, 33, 34, 44]$$

$$rsum[] = [44, 38, 32, 25, 19, 12, 7, 0]$$

$$\left\{ \begin{array}{l} lsum = 25 \\ rsum = totalSum - (lsum + a[i]) \end{array} \right.$$

$$44 - 12 + 3 = 35$$

=

$a[] = [9, 3, 7, 8, 8, 1, 10]$

~~X~~ ↑

$$\text{totalSum} = 44$$

$$l\text{sum} = 9 \quad 12 \quad 19 \quad 25$$

$$r\text{sum} = 44 - 25 + 6 = 25$$

```

static int findEquilibriumIndex(int[] a) {
    // Write code here
    int n = a.length;

    int totalSum = 0;
    for (int i = 0; i < n; i++) {
        totalSum += a[i];
    }

    int lSum = 0;
    for (int i = 0; i < n; i++) {
        lSum += a[i];
        int rSum = totalSum - lSum + a[i];

        if (rSum == lSum) {
            return i;
        }
    }

    return -1;
}

```

$\left. \begin{array}{l} T_C: O(N) \\ S_C: O(1) \end{array} \right\}$

Subarray Sum equal k

$$\text{arr}[] = \{10, 2, -2\} - 20, \{10\}, k = 10$$

3

{ Brute force: get all subarrays, and check
sum = Σk }

TC: $O(N^2)$

$$arr[] = \{ 10, 2, -2, -20, 10, 0 \}, \underline{k = 10}$$

Diagram illustrating the array elements:

- Index 0: 10 (boxed)
- Index 1: 12
- Index 2: 10 (boxed)
- Index 3: -10
- Index 4: 10 (boxed)
- Index 5: 0

Variables:

- x (circled)
- y (circled)
- z (circled)

Equation:

$$y - x = k$$

Annotation: $\underline{\underline{\text{prevSum}}}$

$$0 - 10 = -10$$

$$\text{int } \underline{\text{prevSum}} = \underline{\text{Sum}} - \underline{k}$$

$\text{arr}[] = [1, 1, 1, 1, 1]$

$^0 \quad ^1 \quad ^2 \quad ^3 \quad ^4$
 ↓ ↓ ↓ ↓ ↓
 ① ② ③ ④

$$K = 2$$

if ($\underline{\text{currSum}} == K$)
 $\text{ans} += 1$

else
 {

bind ($\underline{\text{prevSum}}$)
 $\underline{\underline{\text{cSum}}} - \underline{\underline{\text{prevSum}}} = K$
 $\text{ans} += 1$;

$$\text{prev} = \cancel{0} - \cancel{2}$$

$$\text{ans} = \cancel{X} \cancel{X}$$

Set

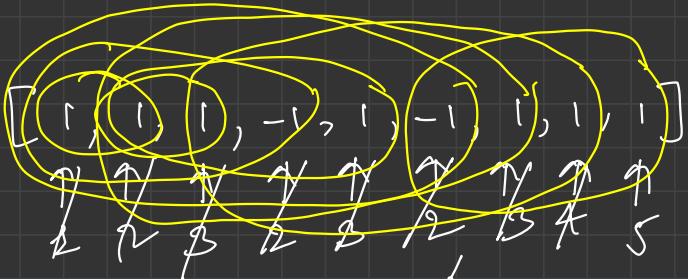
1, 2, 3
4,

$$\underline{\text{currSum}} = 1$$

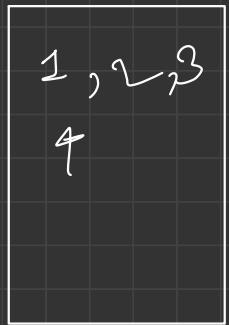
$$\underline{\text{cSum}} - \underline{\text{prevSum}} = K$$

$$\underline{\text{prevSum}} = \underline{\text{currSum}} - K$$

arr[] =



K = 2



ans = 1
2
3

ans = 1 2 3 5 7 8

Set

$\text{arr}[] = [\boxed{1, 1, 1, -1, 1, -1, 1, 1, 1}]$ $k = 2$
 ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓
 2 2 3 2 3 2 3 4 5
 -1 1 0 1 0 1 2 3

Sum	freq
0	2
1	1
2	3
3	3
4	1

ans = $\{4 \neq 9 \neq 8 \neq 9\} \cup \{2\}$

$\text{arr}[] = [1, 1, 1, -1, 1, -1, 1, 1, 1]$ $k=2$

1 2 3 4 5 6 7 8 9 ↑

Sum	freq
0	1
1	1
2	✗ ✗ 3
3	✗ ✗ 3
4	1
5	2

```

public class Main {
    static int solve(int n, int[] arr, int k) {
        // Write your code here
        HashMap<Integer, Integer> mp = new HashMap<>();
        mp.put(key: 0, value: 1);
        int ans = 0;
        int cSum = 0;
        for (int i = 0; i < n; i++) {
            cSum += arr[i];
            int prevSum = cSum - k;
            if (mp.containsKey(prevSum)) {
                ans += mp.get(prevSum);
            }
            mp.put(cSum, mp.getOrDefault(cSum, defaultValue: 0) + 1);
        }
        return ans;
    }
}

```

$\left\{ \begin{array}{l} \text{TC: } O(n) \\ \text{SC: } O(n) \end{array} \right.$