

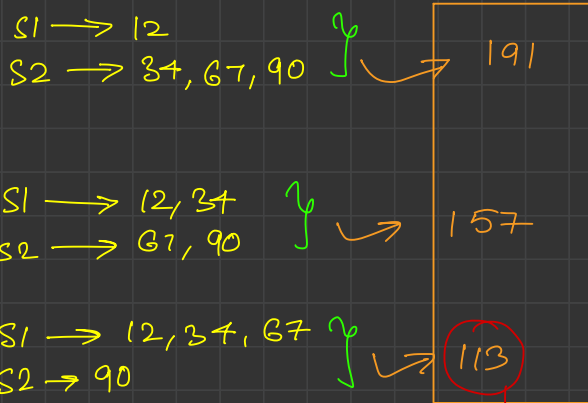


{ Binary Search over Solⁿ }

Allocate Min^m Number of Pages

books[] = { 12, 34, 67, 90 }

students = 2



return

- ① Each student should have min^m one book
- ② Books allocated to a student should be in a contiguous manner.
- ③ All books should be given away

books[] = {⁰12, ¹34, ²67, ³90}

students = 2

Case 1

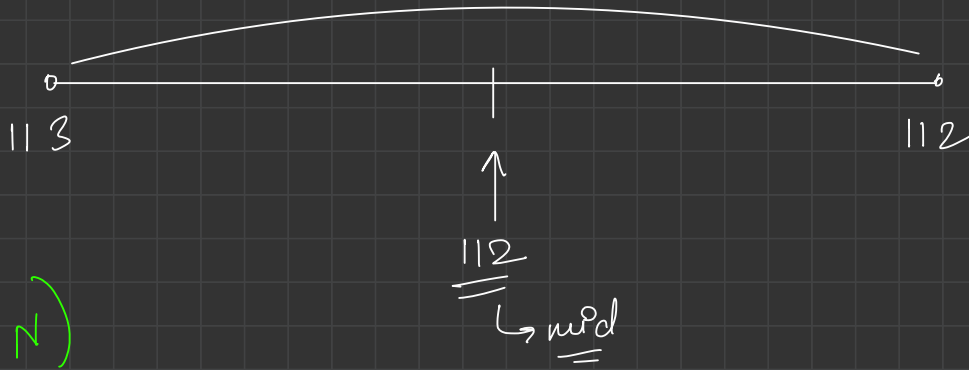
students = 1

S1 → 12, 34, 67, 90 } → 203 pages → ans

Case 2

students = 4

S1 → 12
S2 → 34
S3 → 67
S4 → 90 } → 90 pages → ans



$$\text{TC: } O(N * \log_2 N)$$

✓ parts = ~~1+6~~ ~~1+7~~ 113 ✓

minimize

$$\text{books}[] = \left\{ \begin{array}{cccc} 0 & 1 & 2 & 3 \\ 12, & 34, & 67, & 90 \end{array} \right\}$$

~~↗~~ ~~↗~~ ~~↗~~ ↗

$$\text{limit} = \underline{146}$$

$$S1 \rightarrow 12 + 34 + 67$$

$$S2 \rightarrow 90$$

$$\text{books}[] = \left\{ \begin{array}{cccc} 0 & 1 & 2 & 3 \\ 12, & 34, & 67, & 90 \end{array} \right\}$$

~~↗~~ ~~↗~~ ~~↗~~ ↗

$$\text{limit} = \underline{117}$$

$$S1 \rightarrow 12 + 34 + 67$$

$$S2 \rightarrow 90$$

$$\text{books}[] = \left\{ \begin{array}{cccc} 0 & 1 & 2 & 3 \\ 12, & 34, & 67, & 90 \end{array} \right\}$$

~~↗~~ ~~↗~~ ~~↗~~ ↗

$$\text{limit} = \underline{\underline{103}}$$

$$\left. \begin{array}{l} S1 \rightarrow 12 + 34 \\ S2 \rightarrow 67 \\ S3 \rightarrow 90 \end{array} \right\}$$

books[] = {⁰12, ¹34, ²67, ³90}

limit = 110

S1 → 12 + 34
S2 → 67
S3 → 90

books[] = {⁰12, ¹34, ²67, ³90}

limit = 113

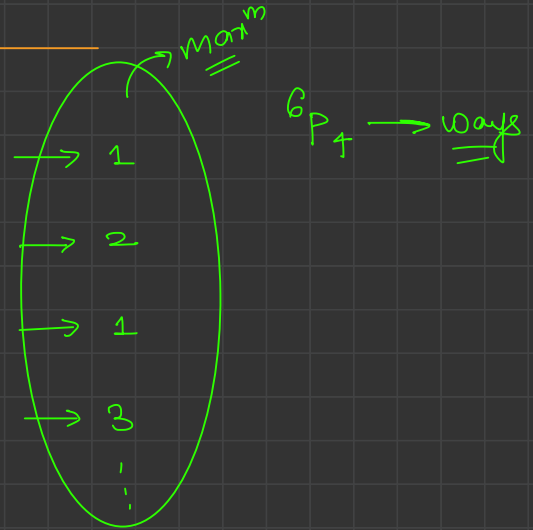
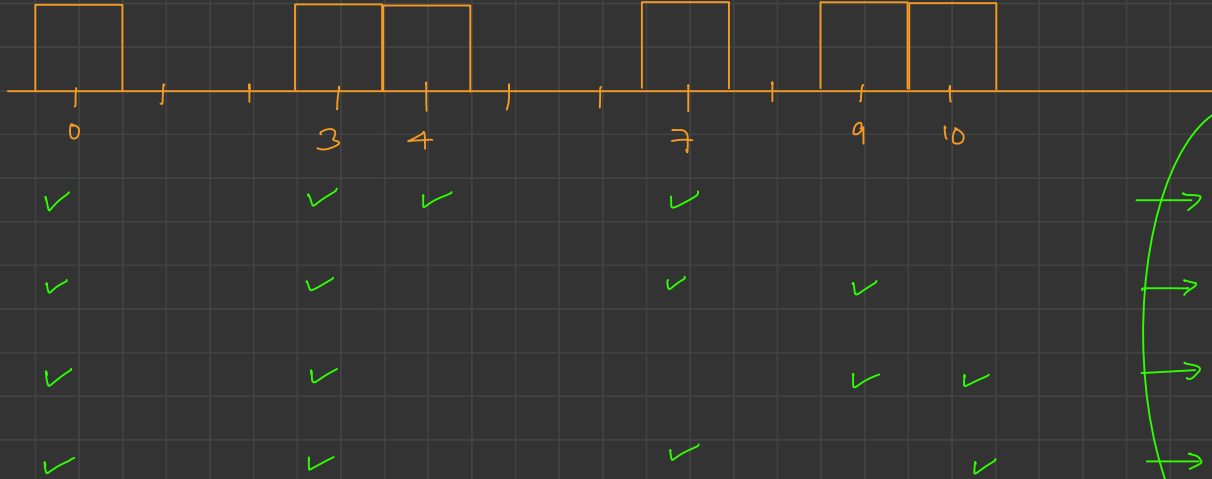
S1 → 12 + 34 + 67

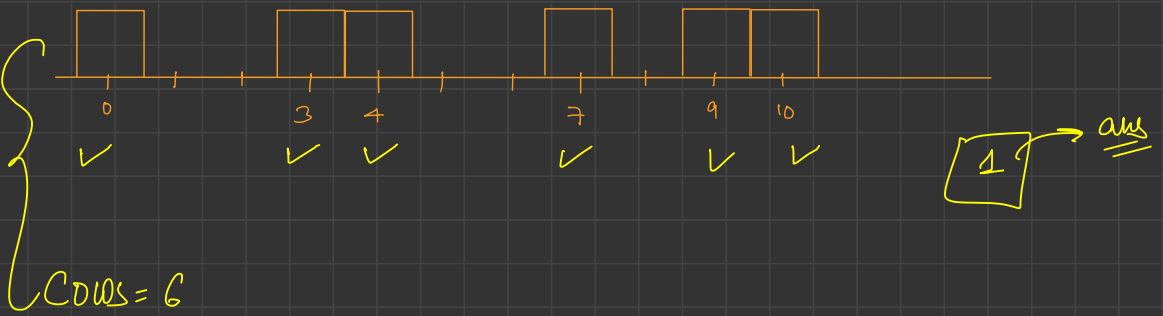
S2 → 90

Aggressive Cows

$$\text{pos}[i] = \{0, 7, 4, 9, 3, 10\}$$

$$\text{cows} = 4$$





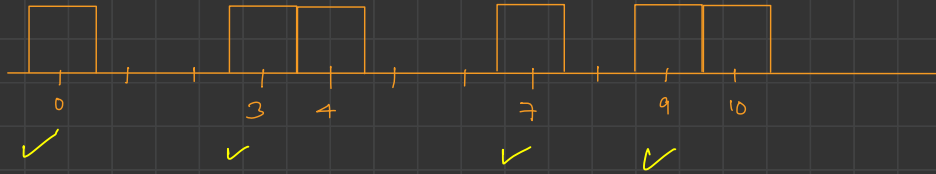
pairs = ~~3~~

$$\min \text{dist} = 5 \checkmark$$



$$\underline{\underline{\text{Cows} = 2}}$$

$$\underline{\underline{\min \text{dist} = 2}}$$



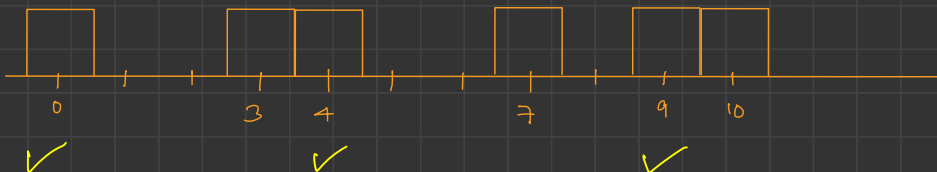
$$\underline{\underline{\text{Cows} = 4}}$$

min dist = 3



cows = 4 ✓

min dist = 4



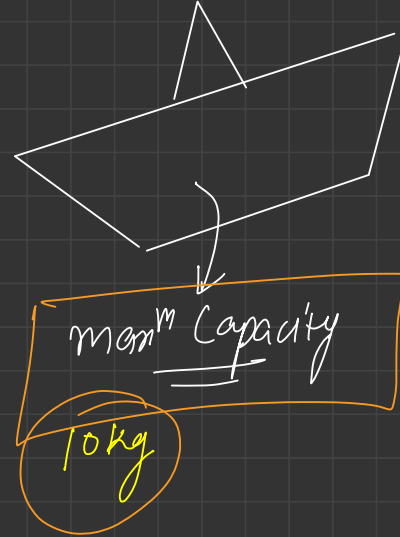
cows = 3

Capacity to ship packages within 5 days

9 8 7 6 5 4 3 2 1

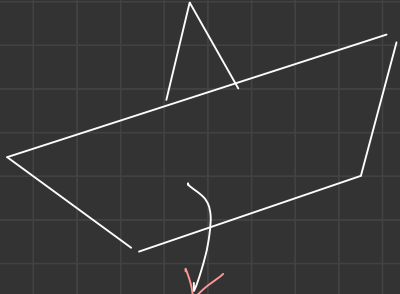
days = 5

minimize



9 8 7 6 5 4 3 2 1


Case 1 days = 1



A hand-drawn diagram of a boat, represented by a parallelogram with a small triangle on top. A red arrow points downwards from the center of the boat.

$$\text{max}^m \text{cap} = \underline{\underline{45 \text{ kg}}}$$

Case 2 days = 0



A hand-drawn diagram of a boat, represented by a parallelogram with a small triangle on top. A red arrow points downwards from the center of the boat.

$$\text{max}^m \text{cap} = \underline{\underline{9 \text{ kg}}}$$

0
~~9kg~~
10kg

|
10kg

0
~~12kg~~
10kg

pans = ~~27~~

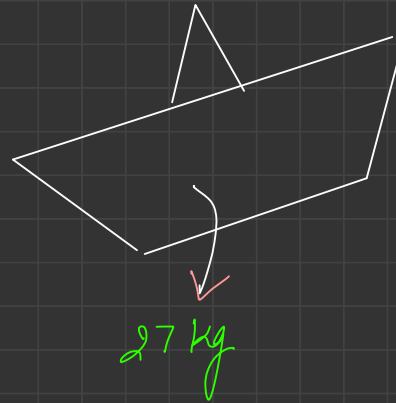
~~17~~
~~12~~

11kg ✓

9	8	7	6	5	4	3	2	1
✓	✓	✓	✓	✓	✓	✓	✓	✓

day 1 $\rightarrow 1 + 2 + 3 + 4 + 5 + 6$

day 2 $\rightarrow 7 + 8 + 9$

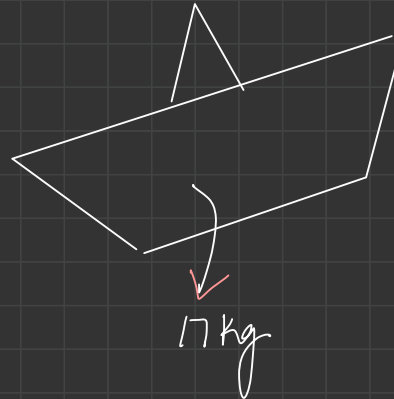


9	8	7	6	5	4	3	2	1
✓	✓	✓	✓	✓	✓	✓	✓	✓

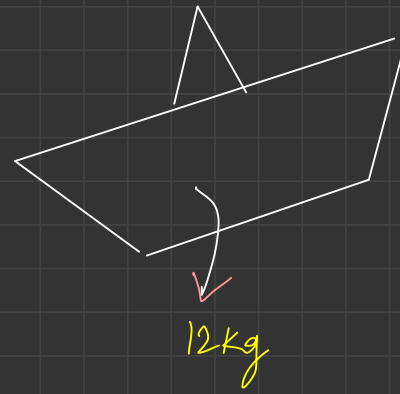
day 1 $\rightarrow 1 + 2 + 3 + 4 + 5$

day 2 $\rightarrow 6 + 7$

day 3 $\rightarrow 8 + 9$



9	8	7	6	5	4	3	2	1
1	2	3	4	5	6	7	8	9



day 1 $\rightarrow 1+2+3+4$

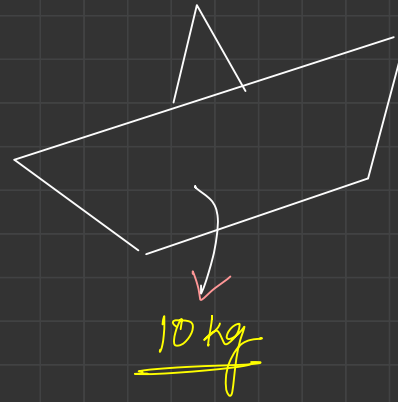
day 2 $\rightarrow 5+6$

day 3 $\rightarrow 7$

day 4 $\rightarrow 8$

day 5 $\rightarrow 5$

9	8	7	6	5	4	3	2	1
→	→	→	→	→	→	→	→	→



day 1 → 1 + 2 + 3 + 4

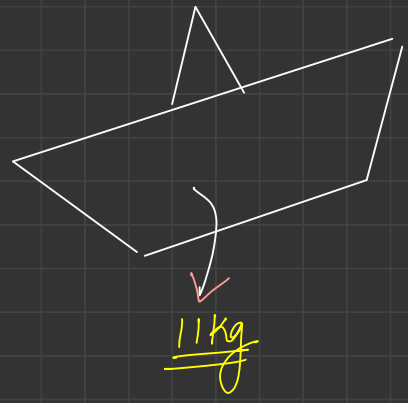
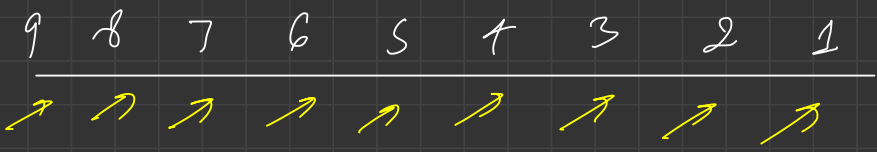
day 2 → 5

day 3 → 6

day 4 → 7

day 5 → 8

day 6 → 9



day 1 → 1 + 2 + 3 + 4

day 2 → 5 + 6

day 3 → 7

day 4 → 8

day 5 → 9



Minimum limit of balls in a bag.

$$\text{arr}[] = \{ 2, 4, 8, 2 \}$$

$$\underline{\underline{\text{maxOpt} = 4}}$$

Case 1 : $\text{maxOpt} = 0$

$$\{ 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 \}$$

$$\hookrightarrow \text{penalty} = 1 \hookrightarrow \underline{\underline{\text{ans}}}$$

Case 2 : $\text{maxOpt} = 0$

$$\{ 2, 4, 8, 2 \}$$

$$\hookrightarrow \text{penalty} = 8$$

$$\text{arr}[1] = \{2, 4, 8, 2\}$$

$\nearrow \nearrow \nearrow \nearrow$
 $(1, 1)$

$$\underline{\underline{\text{penalty} = 4}}$$

$$\underline{\underline{\text{opt} = 1}}$$

$$\text{arr}[1] = \{2, 4, 8, 2\}$$

$\nearrow \uparrow \uparrow \uparrow$
 $(1, 2) \quad (2, 8)$
 \uparrow
 $(2, 4)$
 \uparrow
 $(2, 2)$

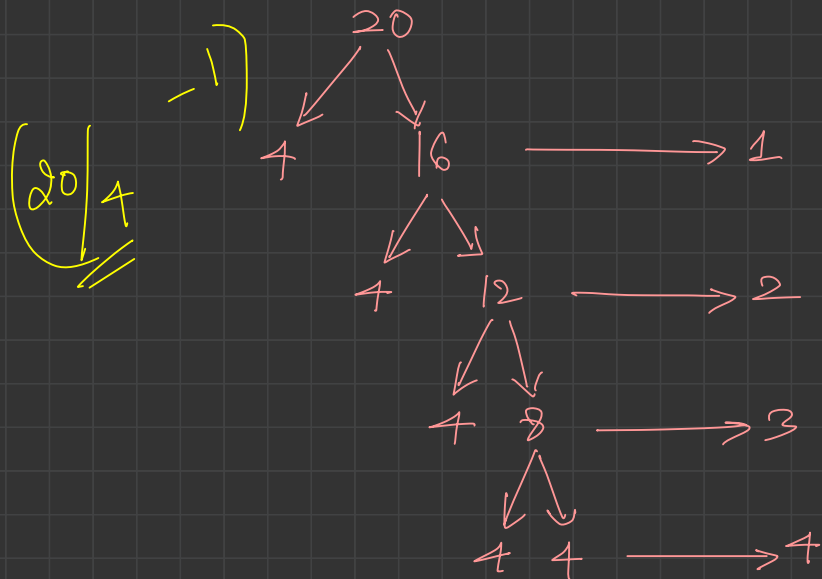
$$\text{penalty} = 2$$

$$\text{opt} = \cancel{X} \cancel{X} \cancel{X}$$

\uparrow

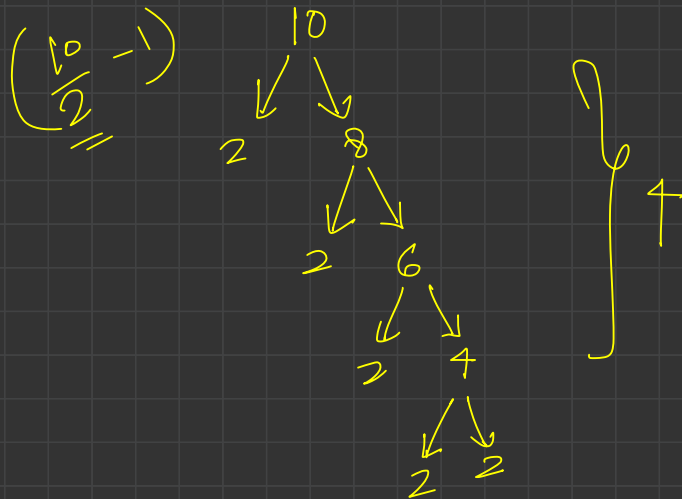
$$\underline{\underline{\text{Balls}}} = \underline{\underline{20}}$$

$$\underline{\underline{\text{penalty}}} = 4$$



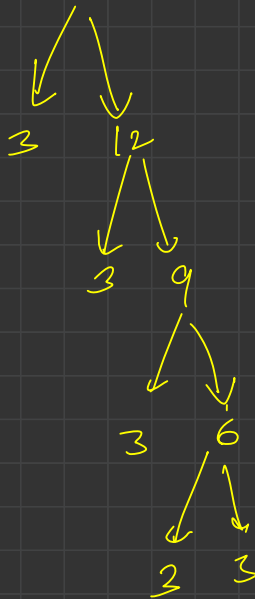
$$\underline{\underline{\text{Balls}}} = 10$$

$$\underline{\underline{\text{penalty}}} = 2$$



Balls = 15

penalty = 3

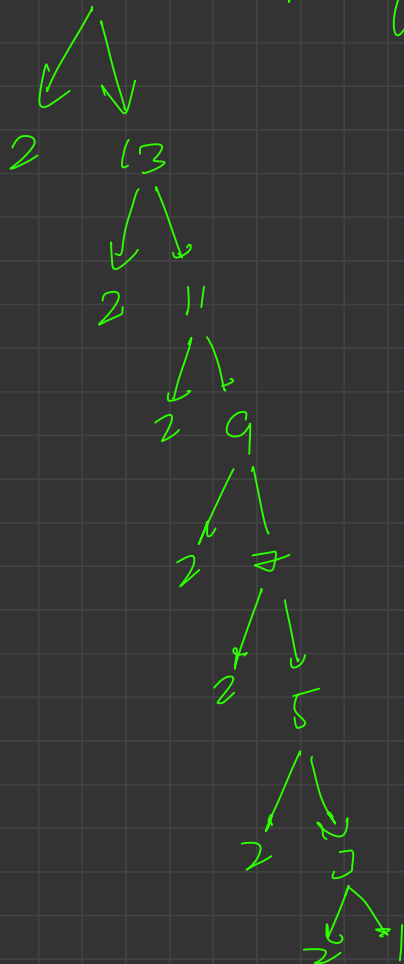


$$\text{Opt} = \frac{\text{Balls}}{\text{penalty}} - 1$$



Balls = 15

penalty = 2



if (Ball % P == 0)

opt = (Ball / P) - 1;

else

opt = (Ball / P);

$$\log_2(10^2) = 2 \times \log_2 10 \xrightarrow{3.1} \approx \underline{\underline{6}}$$

$$\log_2(10^6) = 6 \times \log_2 10 \xrightarrow{3.1} \approx \underline{\underline{18}}$$

