Binary Trees

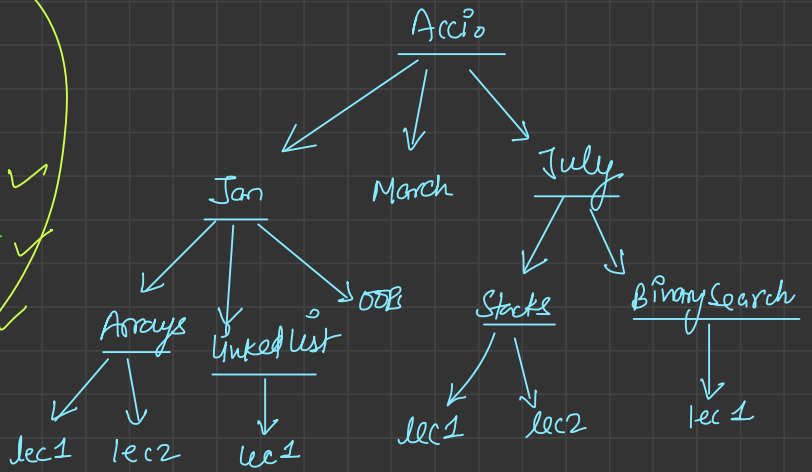
→ Non linear data structure

Data

1. family tree
2. Org. chart
3. file system

→ Trees

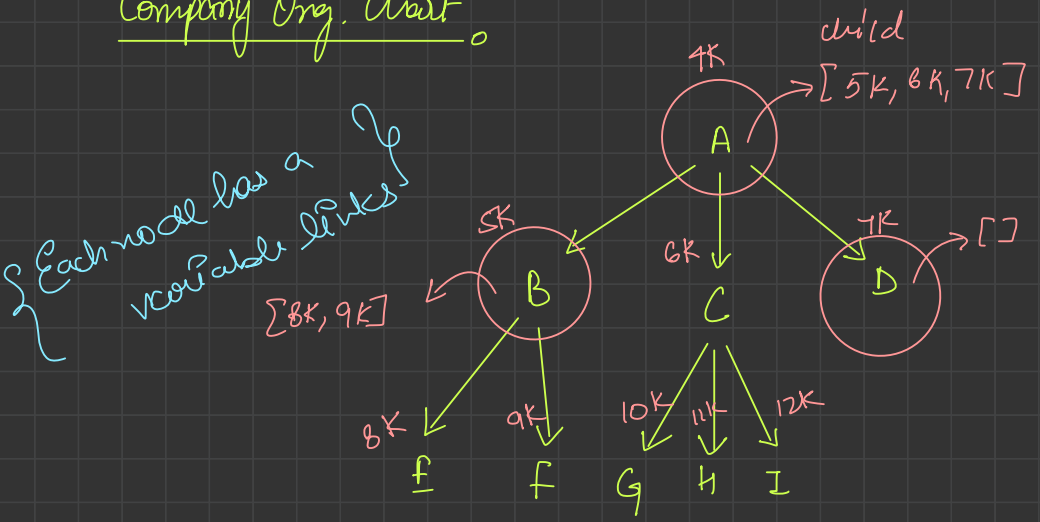
Hierarchy present



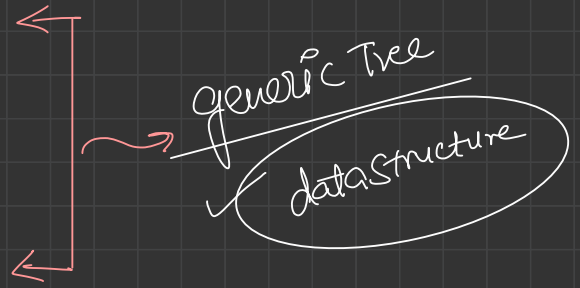
Non - linear

→ Trees!

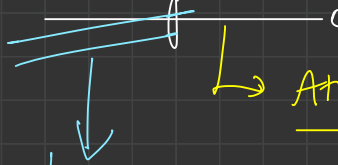
Company Org. Chart




```
class Node
{
    String data;
    ArrayList<Node> child;
}
```



Binary Trees



0, 1 or 2 childs!

↳ Almost two childrens!

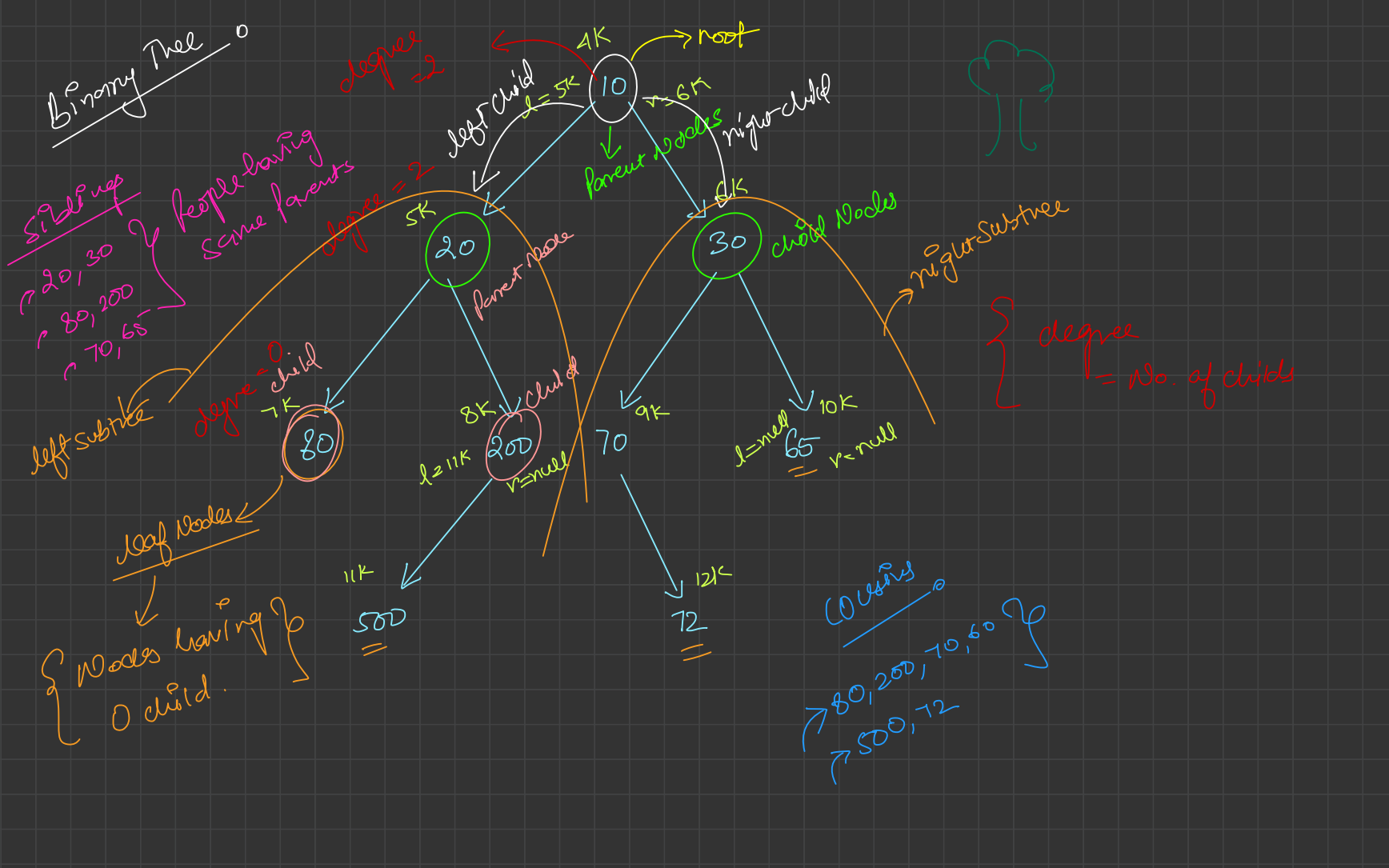
0/1

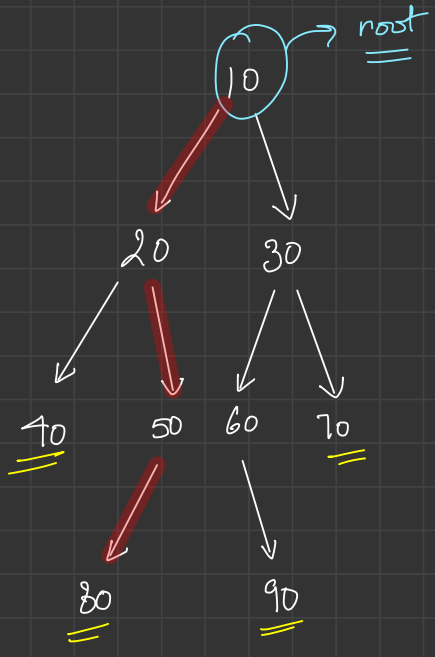
↳ two options

named as

↳ left child
↳ right child

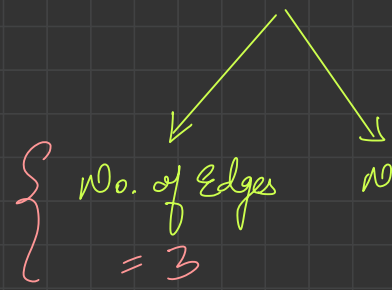
```
class Node
{
    int data;
    Node left;
    Node right;
}
```


Binary Tree
degree = 2
4K
root
10
left child
l = 5K
r = 6K
right child
Parent Nodes
Siblings
20, 30
80, 200
70, 65
People having same parents
degree = 2
5K
20
6K
30
child Nodes
right Subtree
left subtree
degree = 0
child
7K
80
8K
child of
200
l = 11K
r = null
9K
70
l = null
10K
65
r = null
Leaf Nodes
Nodes having 0 child.
11K
500
12K
72
degree = No. of childs
CO Ustins
80, 200, 70, 60
500, 72



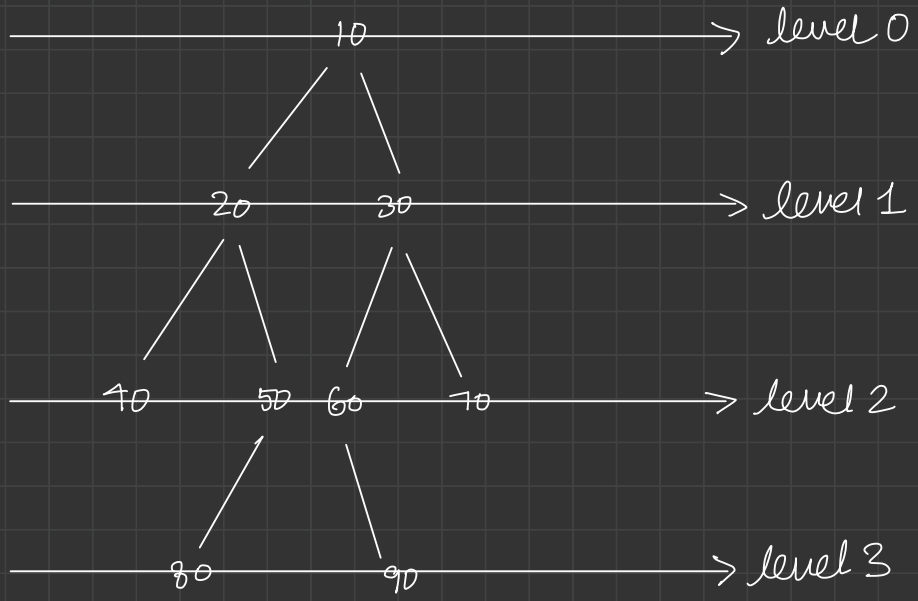
height of the tree

= dist b/w root Node and deepest leaf node



No. of Edges = 3

No. of Nodes = 4

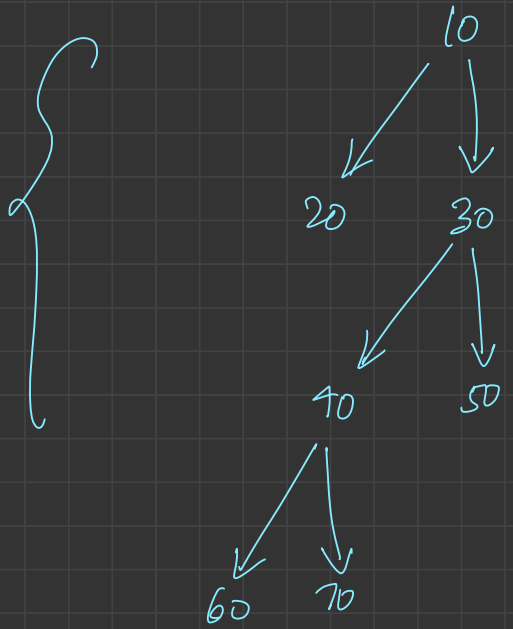

10
level 0
20
30
level 1
40
50
60
70
level 2
80
90
level 3

Perfect Binary Tree

{ No. of people in each level (l) = 2^l }

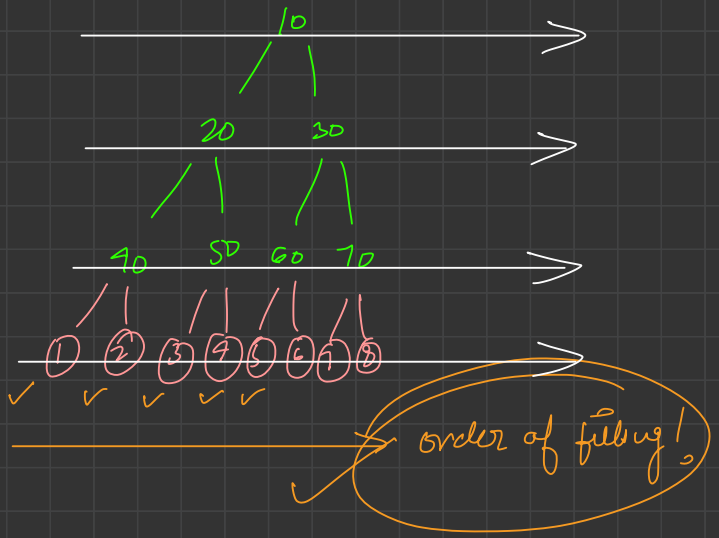
Full Binary Tree

↳ Each Node will Either have 0 or 2 children



Complete Binary Tree

where each level is completely filled except, people in last level are as left positioned as possible



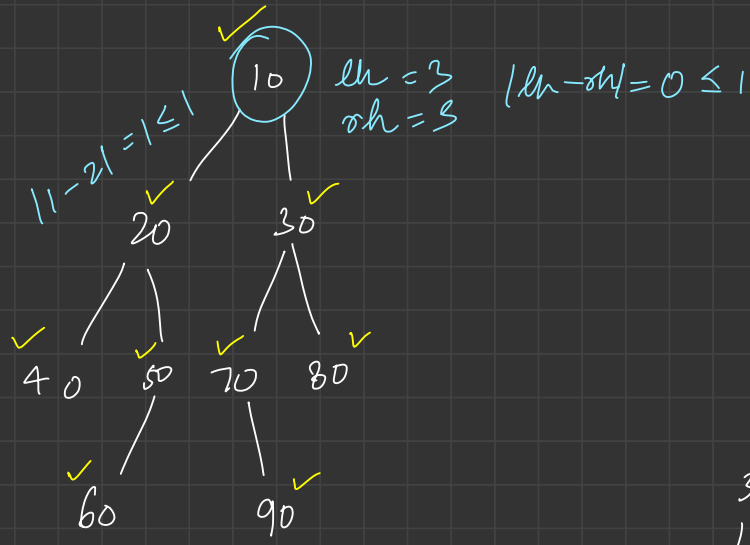
Balanced Binary Tree

↳ When each node of the tree is balanced!

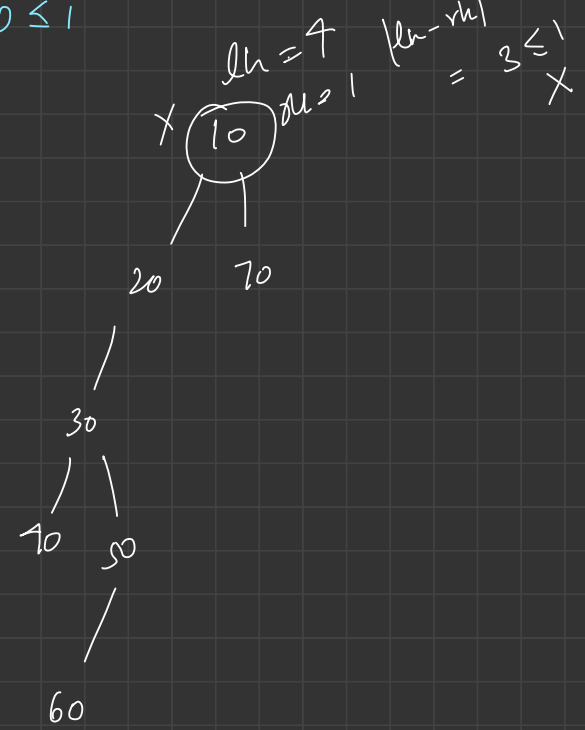
Balanced Node

↳ $|lh - rh| \leq 1$ ✓

- lh → { left subtree height
- rh → right subtree height }



Yes tree is Balanced!



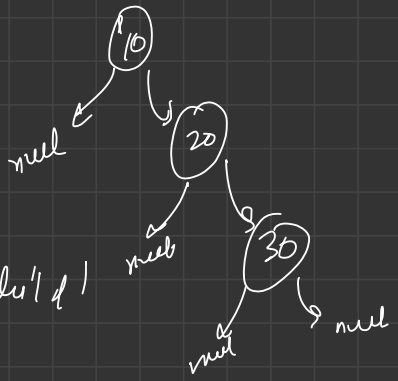
Skew Tree :

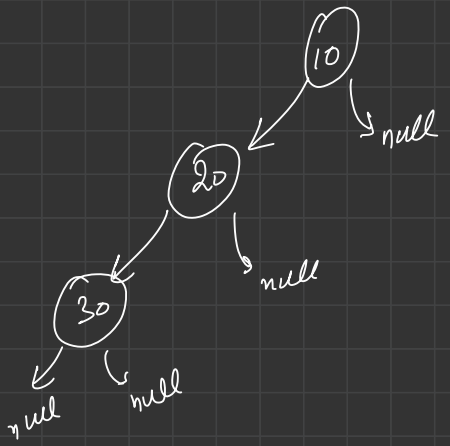
Left Skew Tree :

→ where each node either left child or No child !

Right-skew tree :

either right child or No child !

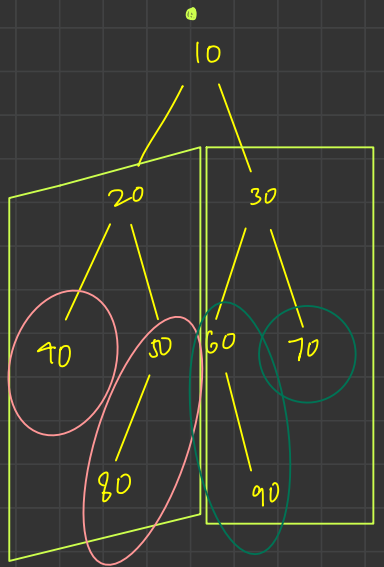


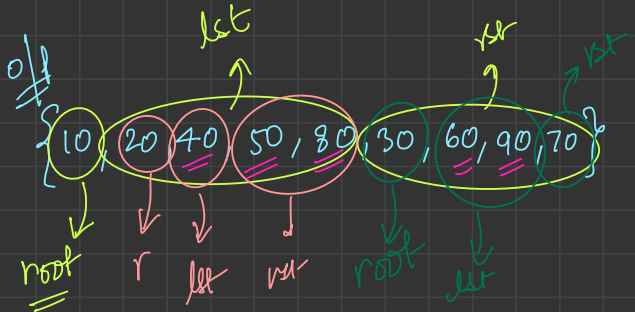


Traversal on trees

(1) Pre Order Traversal

root
lst
rst





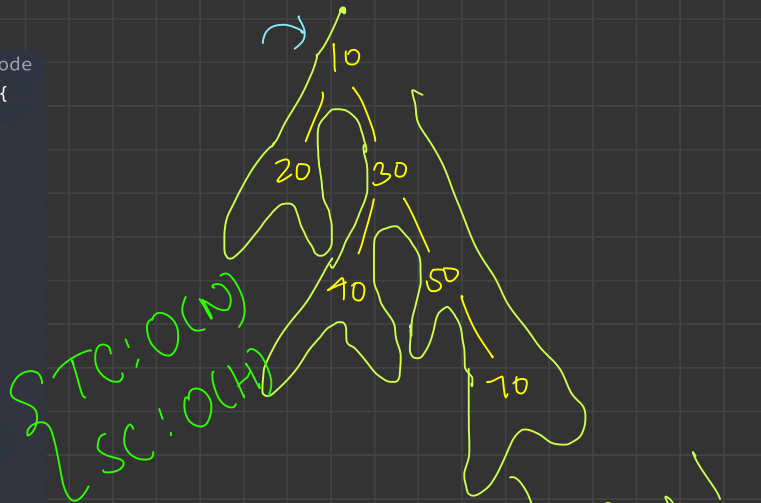
print (root)
preOrder (lst)
preOrder (rst)

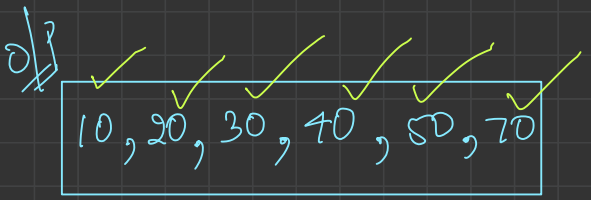
→ preOrder

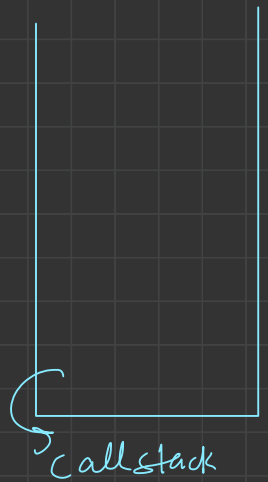
Task: Print preOrder from given root.

```
void preOrder (Node root)
{
    if(root == null)
        return;
    print (root);
    preOrder (root.left);
    preOrder (root.right);
}
```

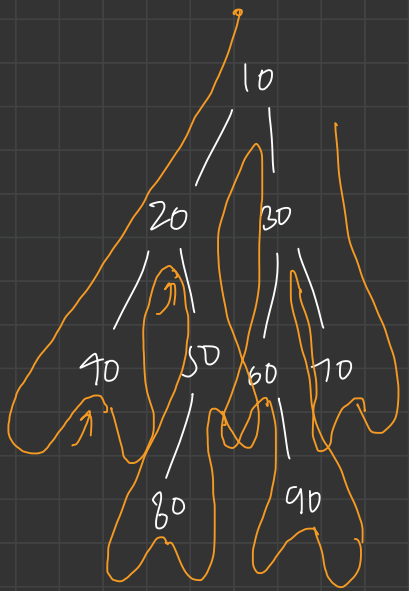
```java
// faith: prints preorder traversal from given node
public static void preorderTraversal(Node root) {
    //Write your code here
    // Base case
    if (root == null) {
        return;
    }

    // print yourself
    System.out.print(root.data + " ");

    // call left subtree to print its preorder
    preorderTraversal(root.left);

    // call right subtree to print ints preorder
    preorderTraversal(root.right);
```

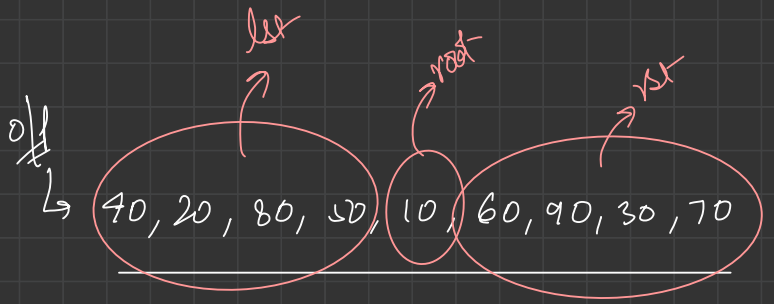






In Order Traversal → lst + root + rst



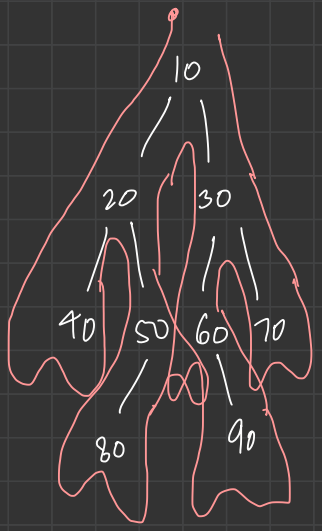


(40, 20, 80, 50, 10, 60, 90, 30, 70)

```
void Inorder (Node root)
{
    Base case!
    inorder (root.left);
    print (root);
    inorder (root.right);
}
```

Post Order Traversal

→ left, right, root



o/p

40, 80, 50, 20, 90, 60, 70, 30, 10

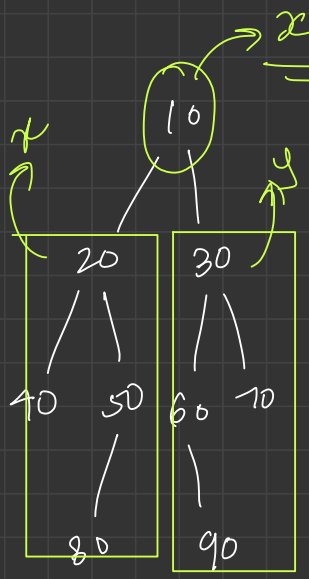
root

left

rst

{40, 80, 50, 20, 90, 60, 70, 30, 10}

Size of Tree. {No. of Nodes}



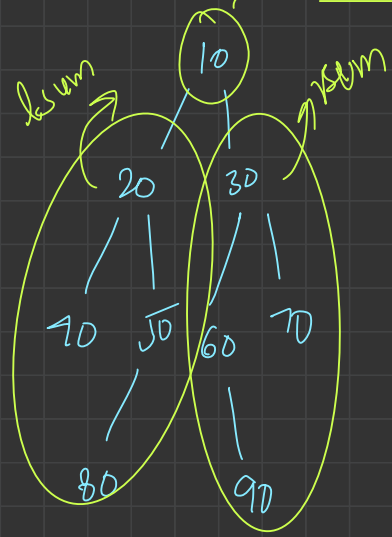
Size = 9

faith: returns size of the tree from root

```
int size(Node root)
{
    if(root == null) return 0;

    int lstSize = size(root.left);
    int rstSize = size(root.right);
    return lstSize + rstSize + 1;
}
```

Sum of tree

↳ Sum of values of Each Node!



lsum + rsum + root.data

overall sum!

=

faith: returns sum of tree starting from root!

```
int Sum(Node root)
{
}
```

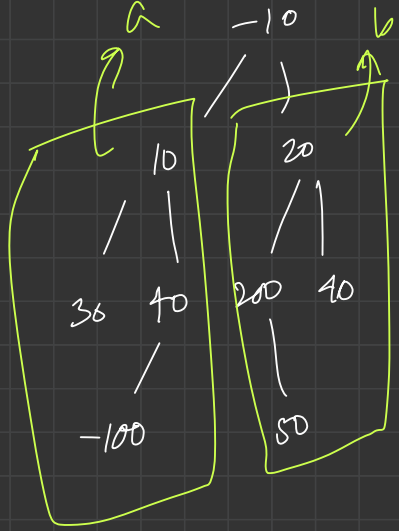
Sum = 450

=

Max^m in a tree

↳ { max^m value present in a tree }

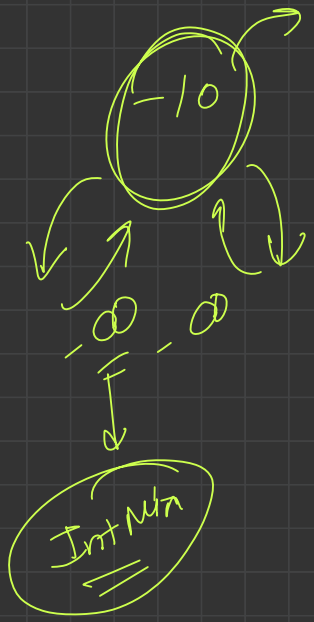
max(a, b, root)



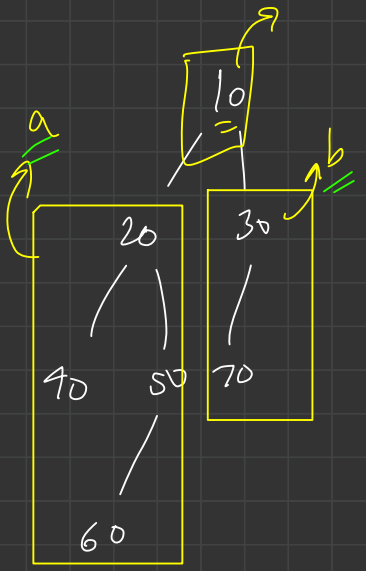
faith: returns max^m value in the tree from root.

```
int maxOfTree(Node root)
{

}
```

Base Case



height of tree



max(a, b) + 1 → yourself

height = 4

faith: returns height of tree starting from root

```
int height(Node root)
{

}
```