

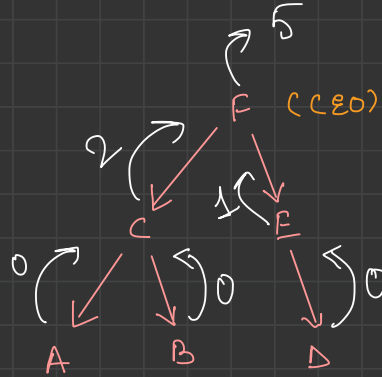


Employee and Managers

o/p

6	A C
	B C
	C F
	D E
	E F
	F F

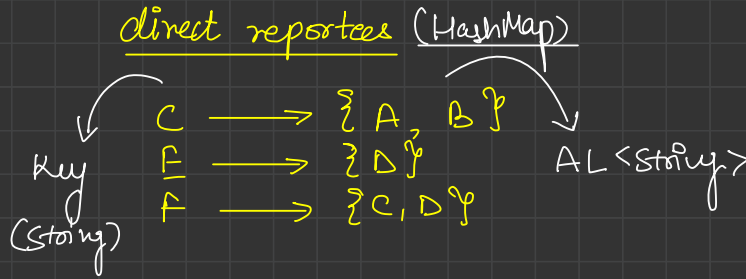
key (Emp) value (Mgs)



o/p

A	→	0
B	→	0
C	→	2
D	→	0
E	→	1
F	→	5

faith : tell me number of emp under you?



callstack

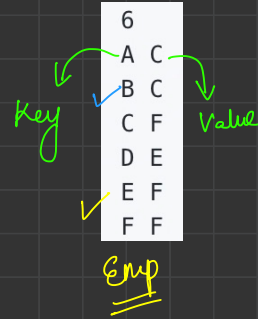
A	→	0
B	→	0
C	→	2
D	→	0
E	→	1
F	→	5

```
✓ HashMap<String, ArrayList<String>> directReportees = new HashMap<>();  
✓ String ceo = "";
```

```
for (String employee : emp.keySet()) {  
    ✓ String manager = emp.get(employee);
```

```
    }  
    if (manager.equals(employee) == true) {  
        ceo = manager;  
        continue;  
    }
```

```
    if (directReportees.containsKey(manager) == true) {  
        ArrayList<String> directRoprting = directReportees.get(manager);  
        directRoprting.add(employee);  
        directReportees.put(manager, directRoprting);  
    } else {  
        ArrayList<String> directRoprting = new ArrayList<>();  
        directRoprting.add(employee);  
        directReportees.put(manager, directRoprting);  
    }  
}
```



employee = F
manager = F

story

C

F

E

AL<String>

{A, B}

{C, E}

{D}

CEO = F

```

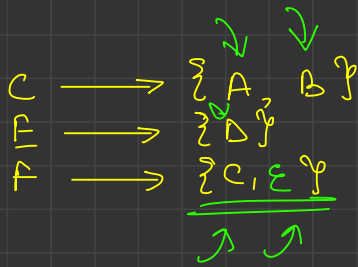
// Faith: number of people directly reporting to emp
public int peopleUnderMe(String emp, HashMap<String, ArrayList<String>> directReportees, HashMap<String, Integer> ans) {
    // base case
    if (directReportees.containsKey(emp) == false) {
        ans.put(emp, 0);
        return 0;
    }

    int numOfPeopleUnderMe = 0;
    for (String directReporting : directReportees.get(emp)) {
        numOfPeopleUnderMe += peopleUnderMe(directReporting, directReportees) + 1;
    }

    ans.put(emp, numOfPeopleUnderMe);

    return numOfPeopleUnderMe;
}

```



A	→	0
B	→	0
C	→	2
D	→	0
E	→	1
F	→	0

Callstack

Problem with given diff o

$arr[] = \{ 5, 10, 3, 2, 50, 20 \}$

$B = 78$

brute force

TC: $O(N^2)$
SC: $O(1)$

```
{ for (int i = 0 → n)
  for (int j = i + 1 → n)
    if (arr[i] - arr[j] == B or arr[j] - arr[i] == B)
      return true;
```

return false

$$\text{arr}[1] = \{ 5, 10, 3, 2, 50, 80 \}$$

$$B = 78$$

$$(x, y)$$

$$\begin{array}{cccc} \swarrow & \swarrow & \swarrow & \uparrow \\ x & x & x & x \end{array}$$

$$x - y = B \rightarrow y = x - B$$

$$\text{OR} \quad y - x = B \rightarrow y = x + B$$

$$\begin{array}{c} 5, 10, 3, 2, \\ 50, 80 \end{array} \checkmark$$

$$\begin{array}{c} x = 2 \\ y = 80 \end{array} \checkmark$$

$$\underline{\underline{x = 5}}$$

$$y = 5 - 78 = -73$$

$$y = 5 + 78 = 83$$

$$\underline{\underline{x = 10}}$$

$$y = 10 - 78 = -68$$

$$y = 10 + 78 = 88$$

$$\underline{\underline{x = 3}}$$

$$y = 3 - 78 = -75$$

$$y = 3 + 78 = 81$$

$$\underline{\underline{x = 2}}$$

$$y = 2 - 78 = -76$$

$$\underline{\underline{y = 2 + 78 = 80}}$$

Array Pair divisible by k

arr[] = { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10 } k = 5



pairs = 5

(1, 9), (2, 8), (3, 7), (4, 6), (10, 5)

arr[] - {^{T T T T T T T T T}
^{0 1 2 3 4 5 6 7 8 9}
1, 2, 3, 4, 5, 6, 7, 8, 9, 10} k = 5

(1, 4) (2, 3) (5, 10) (6, 9) (7, 8)

True

Brute force
{ TC: $O(N^2)$
SC: $O(N)$ } ✓

arr[] = { ^{0 1 2 3 4 5 6 7 8 9} 1, 2, 3, 4, 5, 6, 7, 8, 9, 10 } $k = 5$

(x, y) \rightarrow pair

\Rightarrow (x + y) should be divisible by k

Two num, (x, y)
can pair up together
when sum of them
is divisible by k.

$$x = k \times q_1 + r_1$$

$$y = k \times q_2 + r_2$$

$$x + y = (kq_1 + r_1) + (kq_2 + r_2)$$

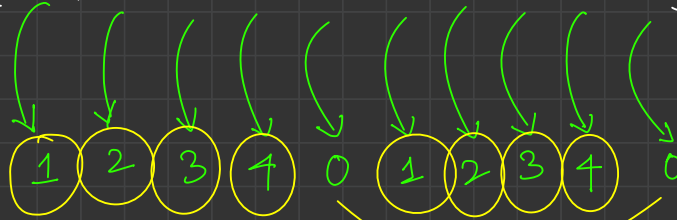
$$x + y = k(\underline{q_1 + q_2}) + \underline{(r_1 + r_2)}$$

\rightarrow divisible by k

should be divisible
by k

arr[] - { 0 1 2 3 4 5 6 7 8 9 } $k = 5$

1, 2, 3, 4, 5, 6, 7, 8, 9, 10



num freq

1 → 2
2 → 2
3 → 2
4 → 2
0 → 2

$$r_1 + r_2 = k$$

$$r_2 = k - r_1$$

Even quantity!

$$r_1 = 1$$

$$r_2 = 4$$

$$r_1 = 2$$

$$r_2 = 3$$

$$r_1 = 3$$

$$r_2 = 2$$

$$r_1 = 4$$

$$r_2 = 1$$

Largest Subarray with zero sum

$$\text{arr}[] = \left\{ \overset{0}{15}, \overset{1}{-2}, \overset{2}{2}, \overset{3}{-8}, \overset{4}{1}, \overset{5}{7}, \overset{6}{10}, \overset{7}{23} \right\}$$

Brute force

Compute all subarray sum, and store maxLen, when sum is zero.

$$\left\{ \begin{array}{l} \text{TC: } O(N^2) \\ \text{SC: } O(1) \end{array} \right.$$

$arr[] = \{ \overset{0}{15}, \overset{1}{-2}, \overset{2}{2}, \overset{3}{-8}, \overset{4}{1}, \overset{5}{7}, \overset{6}{10}, \overset{7}{23} \}$



$\{ \text{if } (x = y)$
Subarray sum is zero

$$\text{arr}[] = \left\{ \begin{array}{c} 0 \quad 1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6 \quad 7 \\ 15, -2, 2, -8, 1, 7, 10, 23 \end{array} \right\}$$

0	15	13	15	7	8	15	25	48
	↘ 0					↘ 5		

$$\text{len} = 2 - 0 = 2$$

$$\text{lim} = 5 - 0 = 5$$

$$\text{max len} = \cancel{2} 5$$

arr[] = {^{0 1 2 3 4 5 6 7}
^{2, 3, 10, -10, -3, 5, -7, 9}}

↗ ↘ ↘ ↘ ↘ ↘ ↗

maxlen = ~~2~~ ~~7~~

Sum = ~~0~~ ~~2~~ ~~5~~ ~~15~~ ~~7~~ ~~2~~ ~~0~~

Map

Sum	firstSeenIndex
2	0
5	1
15	2
7	5
0	-1

len = 3 - 1 = 2

= 4 - 0 = 4

= 6 - (-1) = 7

Subarray Sum Equal to K

int[] arr = {10, 2, -2, -20, 10} K=10

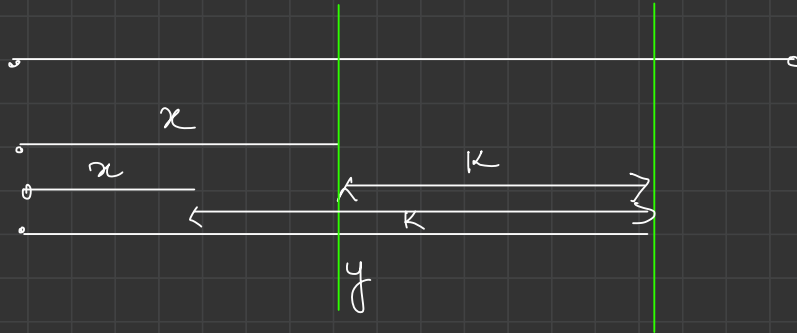
3-Subarrays

brute force

↳ get all subarray sum, and check is equal to K
inc. ans.

{ TC: $O(N^2)$
SC: $O(1)$

int[] arr = {0, 0, 10, 2, -2, -20, 10} K=10



$$x = y - k$$

find

int[] arr = { 0, 0, 10, 2, -2, -20, 10 } K=10

num of subarray = ~~7~~ 7

sum	freq
0	3
10	2
12	1
-10	1

$$x = y - K$$

$$0 - 10 = \underline{\underline{-10}}$$

$$10 - 10 = 0$$

$$12 - 10 = 2$$

$$10 - 10 = \underline{\underline{0}}$$

$$-10 - 10 = -20$$

$$0 - 10 = -10$$