

1. gyakorlat

①

H atom

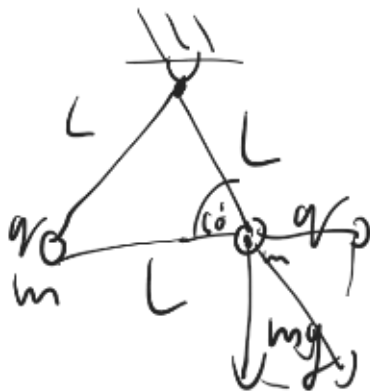


$$F_g = G \frac{m_p \cdot m_e}{r^2}$$

$$F_E = k \cdot \frac{q_1 \cdot q_2}{r^2}$$

$$\frac{F_E}{F_g} = \frac{k \cdot q^2}{G \cdot m_p \cdot m_e} \approx 2,3 \cdot 10^{39}$$

②

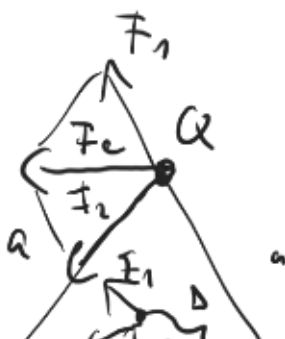


$$\sin \theta = \frac{mg}{F_g}$$

$$\sqrt{3} = \frac{mg}{k \cdot \frac{q^2}{L^2}}$$

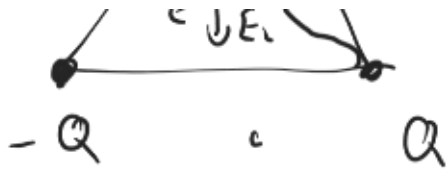
$$m = \sqrt{3} k \cdot \frac{q^2}{L^2 g}$$

③



$$F_1 = k \cdot \frac{Q^2}{a^2}$$

$$F_1 = F_2$$

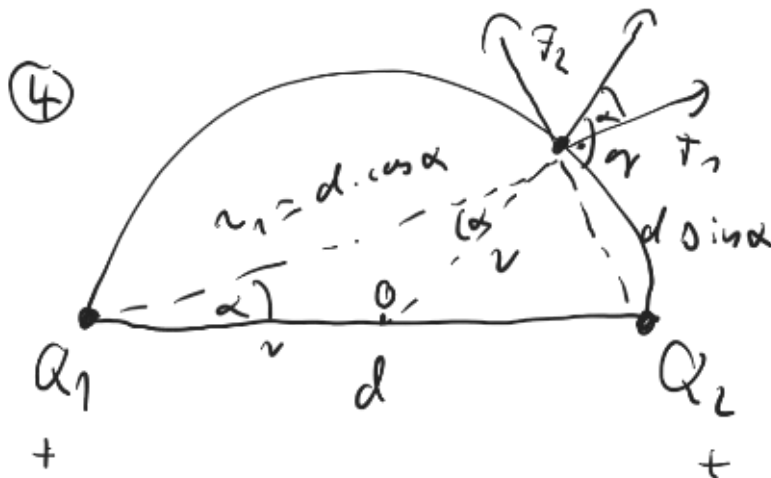


$$F_e = F_1 = F_2 = k \cdot \frac{Q^2}{a^2}$$

$$E_1 = k \cdot \frac{Q}{r^2} = k \cdot \frac{Q}{a^2} \cdot 3 = E_2 = E_1$$

$$\lambda = \frac{a}{\sqrt{3}}$$

$$E = 6 k \frac{Q}{a^2}$$



$$\tan \alpha = \frac{F_2}{F_1}$$

$$F_1 = k \cdot \frac{Q_1 q}{r_1^2} = k \cdot \frac{Q_1 q}{d^2 \cos^2 \alpha}$$

$$F_2 = k \cdot \frac{Q_2 q}{r_2^2} = k \cdot \frac{Q_2 q}{d^2 \sin^2 \alpha}$$

$$\tan \alpha = \frac{Q_2}{Q_1} \cdot \frac{\cos^2 \alpha}{\sin^2 \alpha}$$

$$\tan^3 \alpha = \frac{Q_2}{Q_1}$$

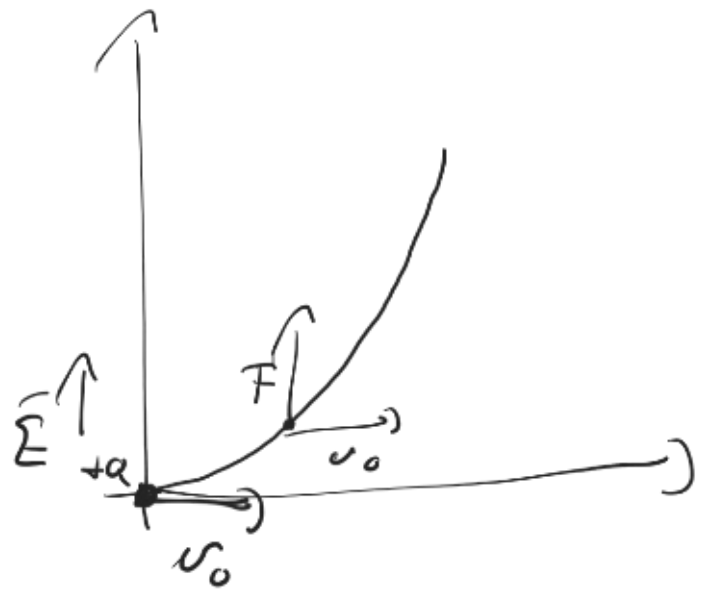
$$\alpha = \arctan\left(\sqrt[3]{\frac{Q_2}{Q_1}}\right)$$

$$(5) \quad \vec{E} = E_0 \vec{j}$$

$$m \rightarrow Q$$

$$\vec{v}_0 = v_0 \cdot \vec{i}$$

$$y(x) = ?$$



$$F = Q \cdot E = m \cdot a_y \rightarrow a_y = \frac{QE}{m}$$

$$y(t) = \frac{1}{2} a_y \cdot t^2$$

$$x(t) = v_0 t \rightarrow t = \frac{x}{v_0}$$

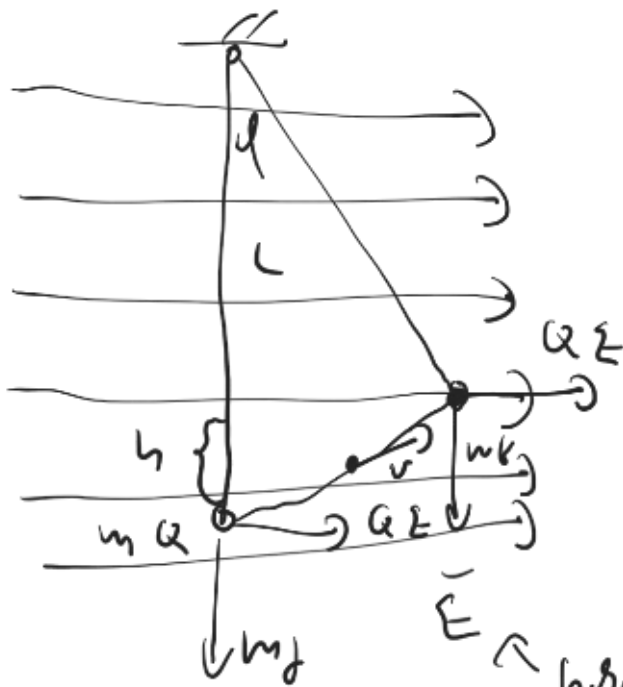
$$y(x) = \frac{1}{2} \frac{QE}{m} \cdot \frac{x^2}{v_0^2}$$

(6)



$$\alpha = \frac{v_c}{\sqrt{2}}$$

①



berapapun $t=0$ $\tan \alpha = \frac{qE}{mg}$

$$(mg')^2 = (mg)^2 + (qE)^2$$

$$h = l(1 - \cos \alpha)$$

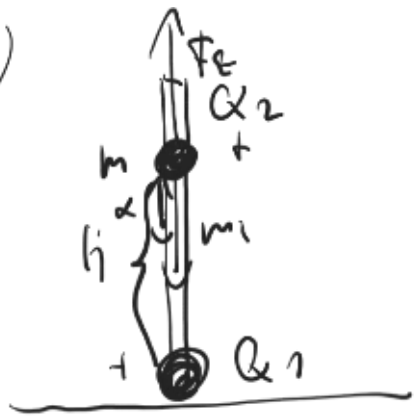
$$v = \sqrt{2gh}$$

$$v = \sqrt{2g l (1 - \cos \alpha)}$$

$$g' = \sqrt{g^2 + \frac{q^2 E^2}{m^2}}$$

$$v =$$

(8)



$$F_E = mg$$

$$k \frac{Q_1 Q_2}{h^2} = mg$$

$$h = \sqrt{\frac{k Q_1 Q_2}{mg}}$$

$$T = ?$$

$$F_E = k \cdot \frac{Q_1 Q_2}{(h-x)^2} - mg$$

$x \ll h$

$$\frac{1}{(h-x)^2} \cdot \frac{(h+x)^2}{(h+x)^2} \cdot \frac{h^2 + 2hx + x^2}{(h^2 - x^2)^2} \approx \frac{1}{h^2} + \frac{2x}{h^3}$$

$$\approx \frac{1}{h^2} + \frac{2x}{h^3}$$

$$F(x) = k Q_1 Q_2 \cdot \left(\frac{1}{h^2} + \frac{2x}{h^3} \right) - mg$$

$$F(x) = k \frac{Q_1 Q_2}{h^2} + \frac{k Q_1 Q_2 2x}{h^3} - mg$$

$$|F(x)| = \frac{k Q_1 Q_2 2x}{h^3}$$

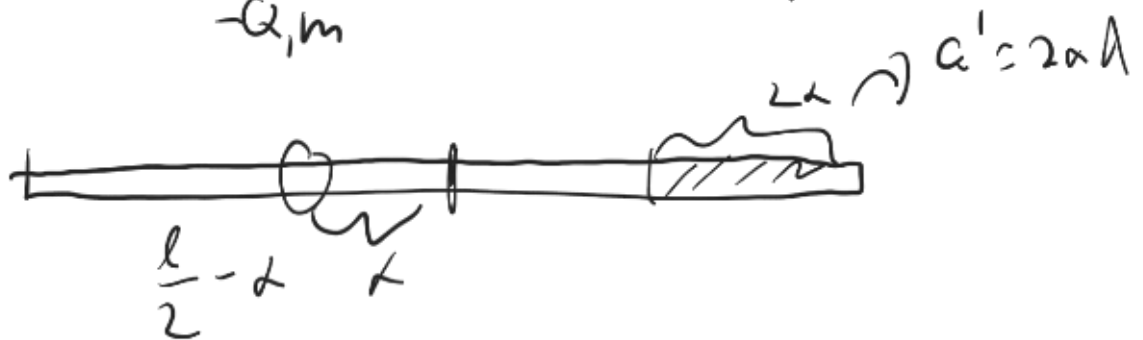
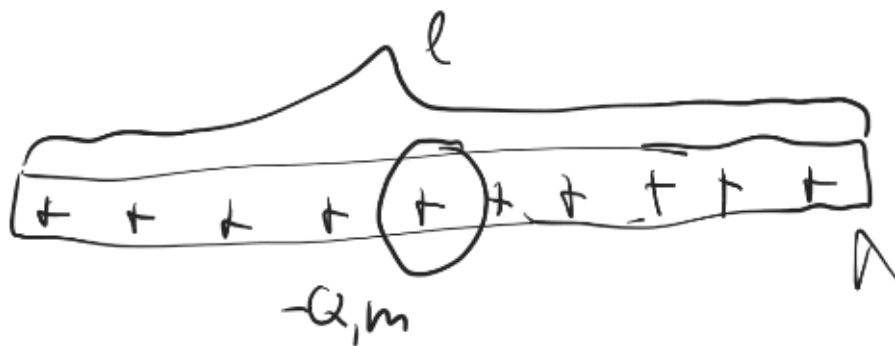
$$m a = - \frac{2 \epsilon Q_1 Q_2}{h^3} x$$

$$\omega = - \frac{2 \epsilon Q_1 Q_2}{m h^3} x$$

$$\omega = \sqrt{\quad} = \frac{2\pi}{T} \Rightarrow$$

$$\Rightarrow T = 2\pi \sqrt{\frac{m h^3}{2 \epsilon Q_1 Q_2}}$$

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$x \ll l$

$$F(x) = \epsilon \frac{Q Q'}{\left(\frac{l}{2} - x\right)^2} \approx$$

$$\approx \frac{\epsilon Q 2 \lambda}{\frac{l^2}{4}} x = \frac{8 \epsilon Q \lambda}{l^2} x$$

$Q \approx Q' \approx \lambda l$

$$F(x) = - \left(\frac{8 \pi \epsilon_0 \hbar^2}{e^2} \right) \psi$$

$$a = \left(\frac{8 \pi \epsilon_0 \hbar^2}{m e^2} \right) \sim \omega$$

$$T = 2 \pi \sqrt{\frac{m e^2}{8 \pi \epsilon_0 \hbar^2}}$$