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Brief Introduction to the paper

Multi-writer Multi-reader Boolean Keyword Searchable Encryption scheme is implemented using the example of a hospital. Following is the brief description of the scheme:

1. MWMRBKSE is based on Key-Policy Attribute Based Encryption (KP-ABE), where each word in the ciphertext (which is an encrypted message from data writer) is considered as an attribute, and a boolean search query from data reader is converted to a boolean key policy. If attributes of some ciphertext are satisfying the key policy of data reader, then data reader can decrypt the corresponding ciphertext.
2. Servers: ETA(Enterprise Trusted Authority) and SS(Storage Server) play the role of servers.
 - ETA sets up (public parameter pp, master public key mpk, master secret key msk) and publishes (pp,mpk). ETA initializes reader list and writer list and stores them on the storage server (SS). Whenever a new reader/writer wants to register, ETA issues them a pair (server key, private key) and adds the corresponding reader/writer to the reader/writer list and updates the reader/writer list in the storage server (SS). Whenever a reader/writer wants to deregister, ETA removes them from the reader/writer list and updates the reader/writer list in the storage server (SS).
 - SS stores the list of currently authorized readers and writers. Whenever a data writers creates a new ciphertext, SS stores that ciphertext. Whenever a data reader wants to search something, he/she creates a boolean Query Q and issues it to SS. SS applies query Q on the currently stored ciphertexts and returns the corresponding result.
3. Clients: Role of clients is played by data readers (DR) and data writers (DW)
 - Data Writers: Role of data writers is played by doctors who want to save patient data in the server. This patient data is encrypted and stored in the storage server. Eg. "Mrs Smith with age 31 was diagnosed with COVID-19 and treated by Dr. Sanchez" is encrypted and stored along with the attributes (Patient name: "Mrs Smith", Patient age: 31, Diagnosed with : "COVID-19", Doctor name: "Dr. Sanchez").
 - Data Reader: Role of data readers is played by doctors who want to read patient history, data analysts who want to analyse hospital data, patients who want to search doctor information, etc. Data reader issues his/her query to SS. SS creates token (which is basically a key-policy) based on the query and searches if currently stored ciphertext attributes satisfy the token key-policy and returns the corresponding result. Eg. if a reader wants to search "COVID patients treated by Dr. Sanchez", which has corresponding query ("COVID" and "Dr. Sanchez"). Since, attributes (Patient name: "Mrs Smith", Patient age: 31, Diagnosed with : "COVID-19", Doctor name: "Dr. Sanchez") satisfy the query "COVID patients treated by Dr. Sanchez", SS will return "Mrs Smith with age 31 was diagnosed with COVID-19 and treated by Dr. Sanchez".

2 Algorithms

MWMRBKSE has nine algorithms as follows :

1. Setup: Setup function takes in input keyword space and outputs public parameter (pp), master public key (mpk) and master secret key (msk).
2. Writer Registration: Writer registration takes in the input of (writer ID,mpk,pp) and issues a pair (writer secret key,writer server key) to the writer and adds writer to the writer list.
3. Reader Registration: Reader registration takes in the input of (reader ID,mpk,msk,pp) and issues a pair (reader secret key,reader server key) to the reader and adds reader to the reader list.
4. Writer deregistration: Writer deregistration takes in the input of writer ID and writer list, and removes the writer with writer ID from the writer list.
5. Reader deregistration: Reader deregistration takes in the input of reader ID and reader list, and removes the reader with reader ID from the reader list.
6. Encryption: Encrypt function takes in the (writer secret key,mpk,message) and creates ciphertext CC,and send (CC,writer ID,message) to the the storage server.
7. C_accept: C_accept function takes in the input (CC,writer ID,message) and check if the writer with writer ID is present in the writer list. If writer is authorized, SS will accept the CC and stores it, else SS will reject the ciphretext.
8. Token_Gen: Token generation function takes in the input of (pp,mpk,reader ID,query Q) and outputs a token $TQ = (D0i,D1i,D2i,D3i,I,reader ID)$ and send it to the server
9. Search: Search algorithm takes in the token $TQ = (D0i,D1i,D2i,D3i,I,reader ID)$ and checks if the reader with reader ID is present in the reader list. If the reader is authorized, then search algorithm will check for all the ciphertext that satisfy query policy from the reader and returns the corresponding ciphertexts, else it rejects the reader.

Out of these 9 algorithms, we have implemented first 7 algorithms along with the LSSS access structure which converts input boolean query to a LSSS matrix.

3 Code Implementation: Setup

3.1 Header Files

Header files, global variable and macros are shown in the Fig. 1.

```

1  #include "pbc.h"
2  #include<gmp.h>
3  #include "pbc_test.h"
4  #include<time.h>
5  using namespace std;
6  #include<bits/stdc++.h>
7  #include<algorithm>
8  #include<iostream>
9  #include<string.h>
10 #include<vector>
11 #define KEYWORD_SIZE 10
12
13 unordered_map<string,mpz_t> keywords;
14

```

Figure 1: Headers

1. Setup(λ, \mathcal{MS})

- 1 From input message space \mathcal{MS} , the algorithm identifies the potential keywords and define a keyword space \mathcal{KS} containing n keyword fields.
 - 2 Runs a generator algorithm \mathbb{G} to obtain $(p_1, p_2, p_3, p_4, G, GT, e)$. Here $G = G_{p_1} \times G_{p_2} \times G_{p_3} \times G_{p_4}$, G and GT are cyclic groups of order $N = p_1 p_2 p_3 p_4$. The algorithm then computes a master public key mpk and a master secret key msk as follows:
 - Selects $\alpha, \beta_1, \beta_2, \dots, \beta_n \in \mathbb{Z}_N, g, u, u_1, u_2, \dots, u_n \in G_{p_1}, X_3 \in G_{p_3}, X_4, h_1, h_2, \dots, h_n \in G_{p_4}$ at random.
 - Computes $H_i = (u_i \cdot h_i), u'_i = u^{\beta_i}$ for $1 \leq i \leq n$.
 - Sets $pp=(G, GT, e, g, n, \mathcal{KS}), mpk=(N, g, g^\alpha, H_i, X_4)$ and $msk=(\alpha, u'_i, X_3)$ for $1 \leq i \leq n$.
 - 3 Sets up two empty lists $RL = \{\perp, \perp\}$ and $WL = \{\perp, \perp\}$ and stores them onto SS.
-

Figure 2: Setup Algorithm

3.2 Initialization of groups and pairings

As shown in Fig. 2, we have to generate 4 primes p_1, p_2, p_3, p_4 and multiply them together to get N which will server as order of the groups G_1, G_2, G_3, G_4, G . Random numbers r_1, r_2, r_3, r_4 are generated by using `mpz_urandomm(mpz_t r, gmp_randstate state, mpz_t size)`, where $size$ is chosen randomly and r gets value from $(0, size - 1)$. Primes p_1, p_2, p_3, p_4 are generated from random numbers r_1, r_2, r_3, r_4 using `mpz_nextprime(mpz_t prime, mpz_t random)`. N is obtained by multiplying p_1, p_2, p_3, p_4 using `mpz_mul(mpz_t N, mpz_t p1, mpz_t p2)`

This paper uses *Type – A1* pairing. So, the p_1, p_2, p_3, p_4 are used to generate pairings G_1, G_2, G_3, G_4, G using `pbk_param_init_a1_gen(pbk_param_t param, mpz_t prime)` and `pairing_init_pbk_param(pbk_pairing pairing, pbk_param_t param)`.

Code for pairing generation is shown in Fig. 3 and Fig. 4.

```
422  int main(int argc, char **argv)
423  //int main()
424  {
425      mpz_t r1,r2,r3,r4,p1,p2,p3,p4;
426      mpz_t size_p;
427
428      mpz_init(p1);
429      mpz_init(p2);
430      mpz_init(p3);
431      mpz_init(p4);
432
433      mpz_init(r1);
434      mpz_init(r2);
435      mpz_init(r3);
436      mpz_init(r4);
437
438      mpz_init(size_p);
439
440      srand(time(0));
441      mpz_set_si(size_p,rand());
442      gmp_randstate_t state;
443      gmp_randinit_mt(state);
444
445      // generate random numbers
446      mpz_urandomm(r1,state,size_p);
447      mpz_urandomm(r2,state,size_p);
448      mpz_urandomm(r3,state,size_p);
449      mpz_urandomm(r4,state,size_p);
450
451      // generate prime numbers
452      mpz_nextprime(p1,r1);
453      mpz_nextprime(p2,r2);
454      mpz_nextprime(p3,r3);
455      mpz_nextprime(p4,r4);
456
457      mpz_t N;
458      mpz_init(N);
459      mpz_mul(N,p1,p2);
460      mpz_mul(N,N,p3);
461      mpz_mul(N,N,p4);
462
```

Figure 3: Prime Generation

```
463 //group G1 of order p1
464 pairing_t pairing1;
465 pbc_param_t param1;
466 pbc_param_init_a1_gen(param1,p1);
467 pairing_init_pbc_param(pairing1,param1);
468 //group G2 of order p2
469 pairing_t pairing2;
470 pbc_param_t param2;
471 pbc_param_init_a1_gen(param2,p2);
472 pairing_init_pbc_param(pairing2,param2);
473 //group G3 of order p3
474 pairing_t pairing3;
475 pbc_param_t param3;
476 pbc_param_init_a1_gen(param3,p3);
477 pairing_init_pbc_param(pairing3,param3);
478 //group G4 of order p4
479 pairing_t pairing4;
480 pbc_param_t param4;
481 pbc_param_init_a1_gen(param4,p4);
482 pairing_init_pbc_param(pairing4,param4);
483 //group GT of order N=p1*p2*p3*p4
484 pairing_t pairing_final;
485 pbc_param_t param_final;
486 pbc_param_init_a1_gen(param_final,N);
487 pairing_init_pbc_param(pairing_final,param_final);
488
```

Figure 4: Pairing Generation

3.3 pp,mpk,msk

All the operations shown in Fig. 2 for generating pp,mpk,msk are done using gmp functions (exponentiation and multiplication). If pairing of some element is unspecified (such as H_i), it is assumed to be belonging to group G of order N . Code for these operations is shown in Fig. 5.¹

Keyword space is also created. Keyword space contains predefined 10 attributes, which are strings. Keyword space is implemented using unordered_map, which maps these string attributes to mpz elements. Keyword space is shown in Fig. 6.

```

513 // find apha and beta[i] values using ZN
514 mpz_t alpha;
515 mpz_init(alpha);
516 mpz_urandomm(alpha,state,N);
517 mpz_t beta[keywords.size()];
518 for (int i=0;i<keywords.size();i++)
519 {
520     mpz_init(beta[i]);
521     mpz_urandomm(beta[i],state,N);
522 }
523 // find g,u and u[i] values
524 mpz_t g;
525 mpz_init(g);
526 mpz_urandomm(g,state,p1);
527 mpz_t single_u;
528 mpz_init(single_u);
529 mpz_urandomm(single_u,state,p1);
530 mpz_t u[keywords.size()];
531 for (int i=0;i<keywords.size();i++)
532 {
533     mpz_init(u[i]);
534     mpz_urandomm(u[i],state,p1);
535 }
536 // find X3
537 mpz_t X3;
538 mpz_init(X3);
539 mpz_urandomm(X3,state,p3);
540 // find X4 and h[i] values
541 mpz_t X4;
542 mpz_init(X4);
543 mpz_urandomm(X4,state,p4);
544 mpz_t h[keywords.size()];
545 for (int i=0;i<keywords.size();i++)
546 {
547     mpz_init(h[i]);
548     mpz_urandomm(h[i],state,p4);
549 }
550 // calculate u_prime[i] and H[i]
551 mpz_t H[keywords.size()],u_prime[keywords.size()];
552 for (int i=0;i<keywords.size();i++)
553 {
554     mpz_init(H[i]);
555     mpz_init(u_prime[i]);
556     mpz_mul(H[i],u[i],h[i]);
557     mpz_mod(H[i],H[i],N);
558     mpz_powm(u_prime[i],single_u,beta[i],N);
559 }

```

Figure 5: Code calculations required for setup

Now for generating pp,mpk,msk. Structures are defined for pp,mpk,msk. Once pp,mpk,msk are created, they are initialized and then assigned the values that are calculated in Fig. 5. G and GT are not used in pp .² Code for pp,mpk,msk is shown in Fig.7, Fig.8, Fig.9.

¹keyword.size() is the size of KS(keyword space) and is defined to be 10

²PBC pairings only have $G1, G2$ and GT in them, but the paper has shown $G1, G2, G3, G4, GT$. To avoid the cross-pairing operation, we implemented all the operation using GMP, and only used PBC for applying pairing.

```

490     vector<string> temp;
491
492     temp.push_back("hospital1");
493     temp.push_back("hospital2");
494     temp.push_back("doctor1");
495     temp.push_back("doctor2");
496     temp.push_back("patient1");
497     temp.push_back("patient2");
498     temp.push_back("disease1");
499     temp.push_back("disease2");
500     temp.push_back("age1");
501     temp.push_back("age2");
502
503     for(int i=0;i<temp.size();i++)
504     {
505         mpz_t t;
506         mpz_init(t);
507         mpz_set_si(t,101+i);
508         mpz_init(keywords[temp[i]]);
509         mpz_set(keywords[temp[i]],t);
510     }
511

```

Figure 6: Keyword space

```

15 // definition of public parameters
16 typedef struct public_parameter_def
17 {
18     mpz_t N;
19     mpz_t g;
20     int n;
21     unordered_map<string,mpz_t> KS;
22 } public_parameter;
23
24 // initialization of public parameters
25 public_parameter initialize_pp(public_parameter pp)
26 {
27     mpz_init(pp.N);
28     mpz_init(pp.g);
29     return pp;
30 }
31
32 // assignment of public parameters
33 public_parameter assign_pp(public_parameter pp,mpz_t N,mpz_t g,unordered_map<string,mpz_t> keywords)
34 {
35     mpz_set(pp.N,N);
36     mpz_set(pp.g,g);
37     pp.n = keywords.size();
38     for (auto i: keywords)
39     {
40         mpz_init(pp.KS[i.first]);
41         mpz_set(pp.KS[i.first],keywords[i.first]);
42     }
43     return pp;
44 }

```

Figure 7: pp structure, initialization and assignment Code

Now, using the structures Fig.7, Fig.8, Fig.9 and setup calculations from Fig.5, we are ready to create pp,mpk,msk as shown in Fig.10.

Setup algorithms also initializes empty reader and writer list. Since every reader and writer has their own secret and server keys, we have used unordered_map that maps reader/writer ID to their corresponding server keys,secret keys. reader/writer list are also implemented using unordered_map that maps reader/writer ID to the tuple (reader/writer ID, server key).

```

46 // definition of master public key
47 typedef struct mpk_def
48 {
49     mpz_t N;
50     mpz_t g;
51     mpz_t g_to_the_alpha;
52     mpz_t H[KEYWORD_SIZE];
53     mpz_t X4;
54 }master_public_key;
55
56 // initialization of master public key
57 master_public_key initialize_mpk(master_public_key mpk)
58 {
59     mpz_init(mpk.N);
60     mpz_init(mpk.g);
61     mpz_init(mpk.g_to_the_alpha);
62     for(int i=0;i<KEYWORD_SIZE;i++)
63         mpz_init(mpk.H[i]);
64     mpz_init(mpk.X4);
65     return mpk;
66 }
67
68 // assignment of master public key
69 master_public_key assign_mpk(master_public_key mpk,mpz_t N,mpz_t g,mpz_t g_to_the_alpha,mpz_t H[],mpz_t X4)
70 {
71     mpz_set(mpk.N,N);
72     mpz_set(mpk.g,g);
73     mpz_set(mpk.g_to_the_alpha,g_to_the_alpha);
74     for(int i=0;i<KEYWORD_SIZE;i++)
75         mpz_set(mpk.H[i],H[i]);
76     mpz_set(mpk.X4,X4);
77     return mpk;
78 }

```

Figure 8: mpk structure, initialization and assignment Code

```

80 // definition of master secret key
81 typedef struct msk_def
82 {
83     mpz_t alpha;
84     mpz_t u_prime[KEYWORD_SIZE];
85     mpz_t u[KEYWORD_SIZE];
86     mpz_t X3;
87 }master_secret_key;
88
89 // initialization of master secret key
90 master_secret_key initialize_msk(master_secret_key msk)
91 {
92     mpz_init(msk.alpha);
93     for(int i=0;i<KEYWORD_SIZE;i++)
94     {
95         mpz_init(msk.u_prime[i]);
96         mpz_init(msk.u[i]);
97     }
98     mpz_init(msk.X3);
99     return msk;
100 }
101
102 // assignment of master secret key
103 master_secret_key assign_msk(master_secret_key msk,mpz_t alpha,mpz_t u_prime[],mpz_t u[],mpz_t X3)
104 {
105     mpz_set(msk.alpha,alpha);
106     for(int i=0;i<KEYWORD_SIZE;i++)
107     {
108         mpz_set(msk.u_prime[i],u_prime[i]);
109         mpz_set(msk.u[i],u[i]);
110     }
111     mpz_set(msk.X3,X3);
112     return msk;
113 }

```

Figure 9: msk structure, initialization and assignment Code

Storage server is also initialized. Storage server stores the ciphertext along with the message for each data writer. Storage server is implemented using unordered_multimap which maps data writer ID, to the ciphertext structure (Fig. 20), which contains the actual message and the corresponding ciphertext from the data writer. Initialization of reader/writer list, server keys, secret keys and storage server is shown in Fig. 10.

```

561     public_parameter pp;
562     pp = initialize_pp(pp);
563     pp = assign_pp(pp,N,g,keywords);
564     gmp_printf("N: %Zd\n",N);
565     gmp_printf("g: %Zd\n",g);
566     cout<<"\nPublic Paramater created successfully\n\n";
567     mpz_t g_to_the_alpha;
568     mpz_init(g_to_the_alpha);
569     mpz_powm(g_to_the_alpha,g,alpha,p1);
570     master_public_key mpk;
571     mpk = initialize_mpk(mpk);
572     mpk = assign_mpk(mpk,N,g,g_to_the_alpha,H,X4);
573     gmp_printf("N: %Zd\n",N);
574     gmp_printf("g: %Zd\n",g);
575     gmp_printf("g^alpha: %Zd\n",g_to_the_alpha);
576     cout<<"H values:\n";
577     for(int i=0;i<10;i++)
578         gmp_printf("%Zd ",H[i]);
579     gmp_printf("\nX4: %Zd \n",X4);
580     cout<<"\nMaster public key created successfully\n\n";
581     master_secret_key msk;
582     msk = initialize_msk(msk);
583     msk = assign_msk(msk,alpha,u_prime,u,X3);
584     gmp_printf("alpha: %Zd \n",alpha);
585     gmp_printf("X3: %Zd \n",X3);
586     cout<<"u_prime values :\n";
587     for(int i=0;i<10;i++)
588         gmp_printf("%Zd ",u_prime[i]);
589     cout<<"\n\nMaster secret key created successfully\n";
590     unordered_map<int,mpz_t> writer_list;
591     unordered_map<int,mpz_t> writer_server_keys;
592     unordered_map<int,mpz_t> writer_private_keys;
593     unordered_map<int,reader_secret_key> reader_private_keys;
594     unordered_map<int,reader_server_key> reader_server_keys,reader_list;
595     //storage servers
596     unordered_multimap<int,ciphertext> SS;
597     int current_wid = 0,current_rid=0;

```

Figure 10: Setup Code

4 Code Implementation: Writer Registration and Deregistration

2. **W_Registration**(pp, mpk, WID)

- 1 Selects $x_{WID} \in Z_N$ at random and sets a secret key $U_{WID} = x_{WID}$.
 - 2 From (mpk, U_{WID}) , it computes $y_{WID} = g^{-x_{WID}}$ and sets server side key $S_{WID} = (WID, y_{WID})$.
 - 3 Updates the local copy of WL as $WL = (WL) \cup \{WID, S_{WID}\}$.
 - 4 Replaces WL stored at SS with the modified WL .
-

Figure 11: Writer registration algorithm

8. **W_Deregistration**(WID, WL)

- 1 It revokes a writer WID by updating local copy of WL as $WL = WL - \{WID, S_{WID}\}$.
 - 2 Replaces WL at server with the modified WL .
-

Figure 12: Writer deregistration algorithm

Writer registration algorithm is shown in Fig.11. Writer ID which is unique to every writer is taken as an input. All the operations are carried out using gmp functions (exponentiation and inverse). Once the writer server keys and writer secret keys are created, they are added to `writer_server_keys` and `writer_private_keys`. Writer is also added to the `writer_list`.

Writer deregistration algorithm is shown in Fig.12. Writer ID which is to be deleted is taken as an input. Writer ID is then used to remove the corresponding writer from `writer_server_keys` and `writer_private_keys` and `writer_list`.

Code for writer registration and deregistration is shown in Fig.13

```

115 // WRITER registration
116 void register_writer(unordered_map<int,mpz_t> &writer_list,unordered_map<int,mpz_t> &writer_server_keys,unordered_map<int,mpz_t> &writer_private_keys,
117 int wid,public_parameter pp, master_public_key mpk, gmp_randstate_t state)
118 {
119     // writer secret key
120     mpz_t x_wid;
121     mpz_init(x_wid);
122     mpz_urandomm(x_wid,state,mpk.N);
123     mpz_init(writer_private_keys[wid]);
124     mpz_set(writer_private_keys[wid],x_wid);
125     // server-writer key
126     mpz_t y_wid;
127     mpz_init(y_wid);
128     mpz_powm(y_wid,mpk.g,x_wid,mpk.N);
129     mpz_invert(y_wid,y_wid,mpk.N);
130     mpz_init(writer_server_keys[wid]);
131     mpz_set(writer_server_keys[wid],y_wid);
132     // update writer list
133     mpz_init(writer_list[wid]);
134     mpz_set(writer_list[wid],y_wid);
135 }
136 }
137
138 // WRITER deregistration
139 void deregister_writer(unordered_map<int,mpz_t> &writer_list,unordered_map<int,mpz_t> &writer_server_keys,unordered_map<int,mpz_t> &writer_private_keys,int wid_to_delete)
140 {
141     writer_list.erase(wid_to_delete);
142     writer_private_keys.erase(wid_to_delete);
143     writer_server_keys.erase(wid_to_delete);
144 }
145 }
146

```

Figure 13: Code for Writer registration and deregistration

5 Code Implementation: Reader Registration

3. **R_Registration**(pp, mpk, msk, RID)

- 1 Selects $x_{RID}, x'_{RID} \in Z_N$ at random.
 - 2 Computes $y_{RID} = \alpha/x_{RID}$ and $u'_{i_RID} = (u'_i)^{1/x'_{RID}}$ for $1 \leq i \leq n$.
 - 3 Sets a read secret key $U_{RID} = (x_{RID}, u_i, u'_{i_RID})$ and a server side key as $S_{RID} = (RID, y_{RID}, x'_{RID})$.
 - 4 Updates the local copy of RL as $RL = (RL) \cup \{RID, S_{RID}\}$.
 - 5 Replaces RL stored at SS with the modified RL .
-

Figure 14: Reader registration algorithm

Reader registration algorithm is shown in Fig.14. Reader ID which is unique to every reader is taken as an input. N^{th} root calculation is done using gmp function `mpz_root`. Division operation was performed using pbc function `pbz_div`.³

As reader server keys and reader private keys have multiple parameters in them, we created structures for them which are shown in Fig. 15

Structures of reader keys are assigned their corresponding values. Once the reader server keys and reader secret keys are created, they are added to `reader_server_keys` and `reader_private_keys`. Reader is also added to the `reader_list`. Code for reader registration is shown in Fig. 16

³In GMP division, we had to choose from remainder division or quotient division. Since, it was not specified in the paper if remainder or quotient is used, we used `pbz_div` division function.

```

147 // definition of READER SECRET KEY
148 typedef struct reader_secret_key_def
149 {
150     mpz_t x_rid;
151     mpz_t u[KEYWORD_SIZE];
152     mpz_t u_prime_rid[KEYWORD_SIZE];
153 }reader_secret_key;
154
155 // initialization of READER SECRET KEY
156 reader_secret_key initialize_reader_secret_key(reader_secret_key u_rid)
157 {
158     mpz_init(u_rid.x_rid);
159     for(int i=0;i<KEYWORD_SIZE;i++)
160     {
161         mpz_init(u_rid.u[i]);
162         mpz_init(u_rid.u_prime_rid[i]);
163     }
164     return u_rid;
165 }
166
167 // definition of READER SERVER KEY
168 typedef struct reader_server_key_def
169 {
170     int rid;
171     mpz_t y_rid;
172     mpz_t x_prime_rid;
173 }reader_server_key;
174
175 // initialization of READER SERVER KEY
176 reader_server_key initialize_reader_server_key(reader_server_key s_rid)
177 {
178     mpz_init(s_rid.y_rid);
179     mpz_init(s_rid.x_prime_rid);
180     return s_rid;
181 }
182

```

Figure 15: Structure for reader server key and reader private key

```

183 // READER registration
184 void register_reader(unordered_map<int,reader_secret_key> &reader_private_keys,unordered_map<int,reader_server_key> &reader_server_keys,unordered_map<int,reader_server_key> &reader_list,
185 int rid,public_parameter pp,master_public_key mpk,master_secret_key msk,gmp_randstate_t state,pairing_t pairing_final)
186 {
187     mpz_t x_rid,x_prime_rid;
188     mpz_init(x_rid);
189     mpz_init(x_prime_rid);
190     mpz_urandomm(x_rid,state,mpk.N);
191     mpz_urandomm(x_prime_rid,state,mpk.N);
192     element_t y,a,b;
193     element_init_Zr(y,pairing_final);
194     element_init_Zr(a,pairing_final);
195     element_init_Zr(b,pairing_final);
196     element_set_mpz(a,msk.alpha);
197     element_set_mpz(b,x_rid);
198     element_div(y,a,b);
199     mpz_t y_rid;
200     mpz_init(y_rid);
201     element_to_mpz(y_rid,y);
202     mpz_t u_prime_rid[KEYWORD_SIZE];
203
204     unsigned long int x_prime_rid_th_root=mpz_get_ui(x_prime_rid);
205     for(int i=0;i<KEYWORD_SIZE;i++)
206     {
207         mpz_init(u_prime_rid[i]);
208         mpz_root(u_prime_rid[i],msk.u_prime[i],x_prime_rid_th_root);
209     }
210     reader_secret_key u_rid = initialize_reader_secret_key(u_rid);
211     mpz_set(u_rid.x_rid,x_rid);
212     for(int i=0;i<KEYWORD_SIZE;i++)
213     {
214         mpz_set(u_rid.u[i],msk.u[i]);
215         mpz_set(u_rid.u_prime_rid[i],u_prime_rid[i]);
216     }
217     reader_private_keys[rid] = u_rid;
218
219     reader_server_key s_rid = initialize_reader_server_key(s_rid);
220     s_rid.rid = rid;
221     mpz_set(s_rid.y_rid,y_rid);
222     mpz_set(s_rid.x_prime_rid,x_prime_rid);
223     reader_server_keys[rid] = s_rid;
224     reader_list[rid] = s_rid;
225 }
226

```

Figure 16: Code for reader registration

6 Code Implementation: Reader Deregistration

9. R_Deregistration(RID , RL)

- 1 It revokes a writer RID by updating local copy of RL as $RL = RL - \{RID, S_{RID}\}$.
 - 2 Replaces RL at server with the modified RL .
-

Figure 17: Reader deregistration algorithm

Reader deregistration algorithm is shown in Fig.12. Reader ID which is to be deleted is taken as an input. Reader ID is then used to remove the corresponding reader from reader_server_keys and reader_private_keys and reader_list.

Code for writer registration and deregistration is shown in Fig. 18

```

228 // READER deregistration
229 void deregister_reader(unordered_map<int,reader_secret_key> &reader_private_keys,unordered_map<int,reader_server_key> &reader_server_keys,
230 unordered_map<int,reader_server_key> &reader_list,int rid_to_delete)
231 {
232
233     reader_list.erase(rid_to_delete);
234     reader_private_keys.erase(rid_to_delete);
235     reader_server_keys.erase(rid_to_delete);
236
237 }

```

Figure 18: Code for Reader deregistration

7 Code Implementation: Encryption

4. Encryption(mpk, W, U_{WID}, M')

- 1 Selects $s \in Z_N, h, Z_0, Z_{1i}, Z'_{1i} \in G_{p_4}$ at random.
 - 2 From input mpk and $W = \{w_1, w_2, \dots, w_n\}$, it computes ciphertext components $CC = (C_0, C'_0, C_i, C'_i)$ as follows

$$C_0 = e(g, g^\alpha)^s, C'_0 = (gh)^s \cdot Z_0, C'_i = (u'_i)^s \cdot Z'_{1i}, C_i = ((H_i)^{w_i})^s \cdot Z_{1i} \cdot g^{U_{WID}} \text{ for } 1 \leq i \leq n.$$
 - 3 Sets a ciphertext $C = (CC, WID, M')$ and sends it to SS.
-

5. C_Accept(C, WL)

- 1 For input $WID \in C$, the algorithm checks WL .
 - 2 If WID is found in WL then the algorithm
 - Replaces $C_i = C_i \cdot y_{WID} = ((H_i)^{w_i})^s \cdot Z_{1i}$
 - Stores C on storage space.
 - 3 Else
 - Rejects input ciphertext C .
-

Figure 19: Encryption and C_accept algorithms

Encryption and C_accept algorithms are shown in Fig.19. Encryption function takes in the input (mpk, M', W, U_{WID}) and outputs the ciphertext $CC = (C_0, C'_0, C_i, C'_i)$. M' is the message from the data writer. mpk is the master public key created as shown in Fig. 8. U_{WID} is the secret key of the data writer with writer id WID , which is allotted to the writer as shown in Fig. 11. $W = (w_1, w_2, \dots, w_n)$ are the mpz numbers corresponding to the attributes extracted from the data writer input message M' . These attribute are extracted using the keyword space maintained as shown in Fig. 6.

Once the ciphertext CC is calculated, encryption function send it to the C_accept function, which checks if the ciphertext is from an authorized data writer. If ciphertext is from an authorized data writer, then some additional calculations are performed and CC is stored in the storage server along with the message M' and the data writer id WID , else CC is rejected.

As ciphertext CC , contains multiple elements in it, we created a structure for the ciphertext, which is shown in Fig. 20. Once ciphertext structure is created, we performed all the operations shown in Fig.19 using GMP and PBC functions, as shown in Fig. 21.

We needed to apply pairing to calculate C_0 , using g and g^α , which are present in the *mpk*. But, g and g^α are mpz numbers and we needed them to be points on the elliptic curve in order to apply pairing. So we converted g and g^α to the points on elliptic curve using `element_from_hash`⁴ by passing the order of group G_{p1} (to which g and g^α belonged) as a size of g and g^α .

```

286 // encrypt
287 typedef struct ciphertext_type
288 {
289     element_t C0;
290     mpz_t C0_prime;
291     mpz_t C[KEYWORD_SIZE], C_prime[KEYWORD_SIZE];
292     string message;
293     int word_size;
294 } ciphertext;
295 ciphertext initialize_cc(ciphertext cc, pairing_t pairing1)
296 {
297     element_init_GT(cc.C0, pairing1);
298     mpz_init(cc.C0_prime);
299     for(int i=0; i<KEYWORD_SIZE; i++)
300     {
301         mpz_init(cc.C[i]);
302         mpz_init(cc.C_prime[i]);
303     }
304     return cc;
305 }
306

```

Figure 20: Ciphertext structure

⁴`element_from_hash(x, size of x)=(x,y)` which is a point on the elliptic curve

```

307 void c_accept(ciphertext cc,unordered_multimap<int,ciphertext> &SS,int wid_writer,unordered_map<int,mpz_t> writer_list,mpz_t N)
308 {
309     int word_size = cc.word_size;
310     for(int i=0;i<word_size;i++)
311     {
312         mpz_mul(cc.C[i],cc.C[i],writer_list[wid_writer]);
313         mpz_mod(cc.C[i],cc.C[i],N);
314     }
315     SS.insert({wid_writer,cc});
316 }
317 void encrypt(const master_public_key mpk,master_secret_key msk,mpz_t W[],string M,int wid_writer,unordered_multimap<int,ciphertext> &SS,
318 int word_size,gmp_randstate_t state,pairing_t pairing1,pairing_t pairing2,pairing_t pairings,pairing_t pairing4,pairing_t pairing_final,
319 mpz_t p1,mpz_t p2,mpz_t p3,mpz_t p4,mpz_t N,unordered_map<int,mpz_t> writer_private_keys,unordered_map<int,mpz_t> writer_list)
320 {
321     mpz_t s;
322     mpz_init(s);
323     mpz_urandomm(s,state,N);
324     mpz_t h,z0,Z1[word_size],Z1_prime[word_size];
325
326     mpz_init(h);
327     mpz_urandomm(h,state,p4);
328
329     mpz_init(z0);
330     mpz_urandomm(z0,state,p4);
331
332     for(int i=0;i<word_size;i++)
333     {
334         mpz_init(Z1[i]);
335         mpz_urandomm(Z1[i],state,p4);
336         mpz_init(Z1_prime[i]);
337         mpz_urandomm(Z1_prime[i],state,p4);
338     }
339     //cout<<"Created required variables\n";
340     element_t g,g_to_the_alpha;
341
342     element_init_G1(g, pairing1);
343     element_init_G2(g_to_the_alpha, pairing1);
344
345     mpz_t temp_g,temp_g_to_the_alpha;
346     mpz_init(temp_g);
347     mpz_init(temp_g_to_the_alpha);
348     mpz_set(temp_g,mpk.g);
349     mpz_set(temp_g_to_the_alpha,mpk.g_to_the_alpha);
350     element_from_hash(g,temp_g,mpz_get_ui(p1));
351     element_from_hash(g_to_the_alpha,temp_g_to_the_alpha,mpz_get_ui(p1));
352     element_t C0;
353     element_init_GT(C0, pairing1);
354
355     pairing_apply(C0, g, g_to_the_alpha, pairing1);
356     element_pow_mpz(C0,C0,s);
357     //cout<<"Created C0\n";
358
359     mpz_t C0_prime;
360     mpz_init(C0_prime);
361     mpz_mul(C0_prime,mpk.g,h);
362     mpz_mod(C0_prime,C0_prime,N);
363     mpz_powm(C0_prime,C0_prime,s,N);
364     mpz_mul(C0_prime,C0_prime,z0);
365     mpz_mod(C0_prime,C0_prime,N);
366     //cout<<"Created C0_prime"<<endl;
367     mpz_t C_prime[word_size];
368     for(int i=0;i<word_size;i++)
369     {
370         mpz_init(C_prime[i]);
371         mpz_powm(C_prime[i],msk.u_prime[i],s,N);
372         mpz_mul(C_prime[i],C_prime[i],Z1_prime[i]);
373         mpz_mod(C_prime[i],C_prime[i],N);
374     }
375     //cout<<"Created C_prime"<<endl;
376     mpz_t C[word_size];
377     for(int i=0;i<word_size;i++)
378     {
379         mpz_init(C[i]);
380         mpz_powm(C[i],mpk.H[i],W[i],N);
381         mpz_powm(C[i],C[i],s,N);
382         mpz_mul(C[i],C[i],Z1[i]);
383         mpz_mod(C[i],C[i],N);
384         mpz_t g_to_the_xwid;
385         mpz_init(g_to_the_xwid);
386         mpz_powm(g_to_the_xwid,mpk.g,writer_private_keys[wid_writer],N);
387         mpz_mul(C[i],C[i],g_to_the_xwid);
388         mpz_mod(C[i],C[i],N);
389     }
390     //cout<<"Created C"<<endl;
391     ciphertext cc = initialize_cc(cc,pairing1);
392     element_set(cc.C0,C0);
393     mpz_set(cc.C0_prime,C0_prime);
394     for(int i=0;i<word_size;i++)
395     {
396         mpz_set(cc.C[i],C[i]);
397         mpz_set(cc.C_prime[i],C_prime[i]);
398     }
399     cc.word_size = word_size;
400     cc.message = M;
401     //cout<<"Created Ciphertext"<<endl;
402     c_accept(cc,SS,wid_writer,writer_list,N);
403 }

```

Figure 21: Code for Encryption and C_accept

8 Demonstration

We have created a demonstration of our code which shows (pp,mpk,msk) generation and allows user to choose from reader/writer registration and deregistration, allows users to print the list of readers/writers (Fig. 22), allows an authorized writer to add message and the corresponding ciphertext (calculation shown in Fig. 21) to the storage server and print all the messages in the storage server (Fig. 23).

To ensure that every reader and writer gets a unique ID, current Rid and current Wid are initialized to 0. Whenever a new reader/writer wants to register, current Rid and current Wid is incremented and allotted as the corresponding reader/writer ID. Code for demo is shown in Fig. 24. Output for the demo code is shown in Fig. 25

```

239 // print READERS
240 void print_readers(unordered_map<int,reader_server_key> reader_list)
241 {
242     if(reader_list.empty()==true)
243         cout<<"No readers found\n";
244     else
245     {
246         for(auto i: reader_list)
247         {
248             cout<<"Reader ID : "<<i.first<<endl;
249             gmp_printf("y_rid : %zd\n",i.second.y_rid);
250             gmp_printf("x_prime_rid : %zd\n",i.second.x_prime_rid);
251             cout<<"-----\n";
252         }
253     }
254 }
255
256 // print WRITERS
257 void print_writers(unordered_map<int,mpz_t> writer_list)
258 {
259     if(writer_list.empty()==true)
260         cout<<"No writers found\n";
261     else
262     {
263         for(auto i: writer_list)
264         {
265             cout<<"Writer ID : "<<i.first<<endl;
266             gmp_printf("y_wid : %zd\n",i.second);
267             cout<<"-----\n";
268         }
269     }
270 }
271

```

Figure 22: Code for printing readers and writers

```
404 //print messages
405 void print_messages(unordered_multimap<int,ciphertext> &SS)
406 {
407     if(SS.empty()==true)
408         cout<<"No messages found\n";
409     else
410     {
411         for(auto i: SS)
412         {
413             cout<<"Writer ID : "<<i.first<<endl;
414             cout<<"Message : "<<i.second.message<<endl;
415             element_printf("C0 : %B\n",i.second.C0);
416             gmp_printf("C0_prime : %Zd\n",i.second.C0_prime);
417             cout<<"C values:\n";
418             for(int j=0;j<i.second.word_size;j++)
419                 gmp_printf("C[%d] : %Zd\n",j,i.second.C[j]);
420             cout<<"C_prime values:\n";
421             for(int j=0;j<i.second.word_size;j++)
422                 gmp_printf("C_prime[%d] : %Zd\n",j,i.second.C_prime[j]);
423             cout<<"-----\n";
424         }
425     }
426 }
```

Figure 23: Code for printing messages and ciphertext stored in the storage server

```

599 while(true)
600 {
601     cout<<"\n\n-----\n";
602     cout<<"1. Register Writer\n";
603     cout<<"2. Register Reader\n";
604     cout<<"3. Deregister Writer\n";
605     cout<<"4. Deregister Reader\n";
606     cout<<"5. Print readers\n";
607     cout<<"6. Print writers\n";
608     cout<<"7. Write a message\n";
609     cout<<"8. Print all the messages\n";
610     cout<<"9. EXIT\n";
611     cout<<"Enter choice:";
612     cin>>choice;
613     cout<<"-----\n";
614     if(choice == 1)
615     {
616         current_wid++;
617         register_writer(writer_list,writer_server_keys,writer_private_keys,current_wid,pp,mpk,state);
618         cout<<"Registration successful. Your WID is = "<<current_wid<<"\n";
619     }
620     if(choice == 2)
621     {
622         current_rid++;
623         register_reader(reader_private_keys,reader_server_keys,reader_list,current_rid,pp,mpk,msk,state,pairing_final);
624         cout<<"Registration successful. Your RID is = "<<current_rid<<"\n";
625     }
626     if(choice == 3)
627     {
628         cout<<"Enter your writer ID:";
629         int wid_to_delete;
630         cin>>wid_to_delete;
631         if(writer_list.find(wid_to_delete) != writer_list.end())
632         {
633             deregister_writer(writer_list,writer_server_keys,writer_private_keys,wid_to_delete);
634             cout<<"Writer "<<wid_to_delete<<" successfully deleted\n";
635         }
636         else
637             cout<<"Error : Writer ID not found\n";
638     }
639     if(choice == 4)
640     {
641         cout<<"Enter your reader ID:";
642         int rid_to_delete;
643         cin>>rid_to_delete;
644         if(reader_list.find(rid_to_delete) != reader_list.end())
645         {
646             deregister_reader(reader_private_keys,reader_server_keys,reader_list,rid_to_delete);
647             cout<<"Reader "<<rid_to_delete<<" successfully deleted\n";
648         }
649         else
650             cout<<"Error : Reader ID not found\n";
651     }
652     if(choice == 5)
653         print_readers(reader_list);
654     if(choice == 6)
655         print_writers(writer_list);
656     if(choice == 7)
657     {
658         int wid_writer;
659         char a[200];
660         cout<<"Enter your WID :";
661         cin>>wid_writer;
662         if(writer_list.find(wid_writer) == writer_list.end())
663             cout<<"Unauthorized Writer!! Please register\n";
664         else
665         {
666             cout<<"Enter message: ";
667             scanf("\n");
668             scanf("%[^\n]s",a);
669             vector<string> words;
670             string M = convert_to_String(a);
671             string M_copy = M;
672             string token;
673             while(token != M_copy)
674             {
675                 token = M_copy.substr(0,M_copy.find_first_of(" "));
676                 M_copy = M_copy.substr(M_copy.find_first_of(" ")+1);
677                 words.push_back(token);
678             }
679             int count_attributes=0;
680             for(auto i: keywords)
681             {
682                 for(int j=0;j<words.size();j++)
683                 {
684                     if(i.first == words[j])
685                         count_attributes++;
686                 }
687             }
688             mp2_t W[count_attributes];
689             for(int i=0;i<count_attributes;i++)
690                 mp2_init(W[i]);
691             int curr=0;
692             for(auto i: keywords)
693             {
694                 for(int j=0;j<words.size();j++)
695                 {
696                     if(i.first == words[j])
697                     {
698                         mp2_set(W[curr],i.second);
699                         curr++;
700                     }
701                 }
702             }
703             //for(int i=0;i<count_attributes;i++)
704             //    _gmp_printf("%zd\n",W[i]);
705             if(count_attributes==0)
706                 encrypt(mpk,msk,W,M,wid_writer,ss,count_attributes,state,pairing1,pairing2,pairing3,pairing4,pairing_final,p1,p2,p3,p4,N,writer_private_keys,writer_list);
707             else
708                 cout<<"Enter valid message\n";
709         }
710     }
711     if(choice == 8)
712         print_messages(ss);
713     if(choice == 9)
714         break;
715 }
716 pairing_clear(pairing1);
717 pairing_clear(pairing2);
718 pairing_clear(pairing3);
719 pairing_clear(pairing4);
720 pairing_clear(pairing_final);
721 return 0;
722 }
723

```

Figure 24: Code for demonstration

```

Starting program: /home/ritu/GmpPbc/MMMBKSE/encryption
N: 15421993861796871567745419258211939
g: 161132099

Public Paramater created successfully

N: 15421993861796871567745419258211939
g: 161132099
g^alpha: 813211510
H values:
191498516977496392 370179345487175168 221975942138405392 177399102934636605 102935439727837475 156400116151532733 17941
7641506459696 617493118170716539 695804611739079403 1966349258834940
X4: 538048332

Master public key created successfully

alpha: 4187453793590279546664818028147925
X3: 222386207
u_prime values :
11676559393761732592787988997325227 14622426950839349139225223933796612 9844958176285383969611153772039045 244908879941
2496590776424405032780 7118885385192555390241663089477317 648257273934661895573815644105563 931280848708632486571090899
2711944 12484171399026149134869189988465836 8956797103094468664869886892224263 13614345779896532760052310617201073

Master secret key created successfully

```

```

-----
1. Register Writer
2. Register Reader
3. Dergister Writer
4. Deregister Reader
5. Print readers
6. Print writers
7. Write a message
8. Print all the messages
9. EXIT
Enter choice:1
-----

```

Registration successful. Your WID is = 1

```

-----
1. Register Writer
2. Register Reader
3. Dergister Writer
4. Deregister Reader
5. Print readers
6. Print writers
7. Write a message
8. Print all the messages
9. EXIT
Enter choice:2
-----

```

Registration successful. Your RID is = 1

```

-----
1. Register Writer
2. Register Reader
3. Dergister Writer
4. Deregister Reader
5. Print readers
6. Print writers
7. Write a message
8. Print all the messages
9. EXIT
Enter choice:5
-----
Reader ID :1
y_rid : 41441488404224768455337497499187
x_prime_rid : 5001145832501452853150770810584659
-----

```

```

-----
1. Register Writer
2. Register Reader
3. Dergister Writer
4. Deregister Reader
5. Print readers
6. Print writers
7. Write a message
8. Print all the messages
9. EXIT
Enter choice:6
-----

```

```

Writer ID :1
y_wid : 13419086734917953913219748946609847
-----

```



```
-----
1. Register Writer
2. Register Reader
3. Dergister Writer
4. Deregister Reader
5. Print readers
6. Print writers
7. Write a message
8. Print all the messages
9. EXIT
Enter choice:3
-----
Enter your writer ID:2
Error : Writer ID not found

-----
1. Register Writer
2. Register Reader
3. Dergister Writer
4. Deregister Reader
5. Print readers
6. Print writers
7. Write a message
8. Print all the messages
9. EXIT
Enter choice:4
-----
Enter your reader ID:1
Reader 1 successfully deleted

-----
1. Register Writer
2. Register Reader
3. Dergister Writer
4. Deregister Reader
5. Print readers
6. Print writers
7. Write a message
8. Print all the messages
9. EXIT
Enter choice:5
-----
No readers found
```

```

-----
1. Register Writer
2. Register Reader
3. Dergister Writer
4. Deregister Reader
5. Print readers
6. Print writers
7. Write a message
8. Print all the messages
9. EXIT
Enter choice:7
-----
Enter your WID :1
Enter message: doctor1 treated patient1 in hospital1

-----
1. Register Writer
2. Register Reader
3. Dergister Writer
4. Deregister Reader
5. Print readers
6. Print writers
7. Write a message
8. Print all the messages
9. EXIT
Enter choice:8
-----
Writer ID :1
Message :doctor1 treated patient1 in hospital1
C0 : [5554114894, 3873481403]
C0_prime : 8448718380160810284639773322016990
C values:
C[0] : 5663008047765256250484760199857600
C[1] : 10199193566408025781738818102489559
C[2] : 5055640196562789449735513194203372
C_prime values:
C_prime[0] : 12670525303695141674258727678109940
C_prime[1] : 3461339956320396827929772777615178
C_prime[2] : 15150028926054044380360672959604083
-----

```

Figure 25: Output of the demo code

9 LSSS Access structure

In MWMRBKSE, each query Q is considered as a policy (Boolean formula). Formally, a Boolean formula is represented as an LSSS access structure which consists of a secret sharing matrix a . A is an $\times m$ share generating matrix where the number of rows, i.e., is equal to the number of keywords in Q . We assume that no keyword is repeated in query Q .

Token Generation algorithm (Fig. 26) takes in the boolean query from the user in an LSSS format, based on the algorithm shown in Fig.27. Input query is in the post-fix form ⁵.

We converted the post-fix input query to a binary tree, with node values as (AND,OR,SET(attributes)). Every node also has a vector which will be assigned values when tree is passed to LSSS algorithm. LSSS matrix will be generated using the vectors of the nodes which have attribute values.

Code for LSSS matrix generation is shown in the Fig. 28. Output for this code with an execution is shown in the Fig. 29.

6. TokGen($pp, mpk, URID, Q$)

- 1 For the input Boolean query $Q = (\mathbb{A}, \rho, \mathbb{T})$, it first selects a random vector v such that $\mathbb{A}_i \cdot v = x_{RID}$ for $1 \leq i \leq \ell$.
 - 2 It selects $r_i \in Z_N, V_{0i}, V_{1i}, V_{2i}, V_{3i} \in G_{p_3}$ at random for $1 \leq i \leq \ell$.
 - 3 Then computes $D_{0i} = g^{\mathbb{A}_i v} \cdot V_{0i}, D_{1i} = (u_{\rho(i)})^{r_i t_{\rho(i)}} \cdot V_{1i}, D_{2i} = (u'_{i_RID})^{r_i} \cdot V_{2i}, D_{3i} = g^{r_i} \cdot V_{3i}$.
 - 4 From (\mathbb{A}, ρ) , DR computes a set of minimum subset I' (that can satisfy a query Q) as $I' = \{(I_1, \sigma_1), (I_2, \sigma_2), \dots\}$ where $I_k \subseteq \{1, 2, \dots, \ell\}$ and $\sigma_k = \{\sigma_{jk} | 1 \leq j \leq |I_k|\}$ satisfying Eq. (1).
 - 5 Finally, DR possessing RID outputs a token for query Q as $T_Q = (D_{0i}, D_{1i}, D_{2i}, D_{3i}, I', RID)$ for $1 \leq i \leq \ell$.
-

Figure 26: Algorithm for Token Generation based on the input query

⁵post-fix(A and B or C)=A B and C or. Basically, post-fix expression is obtained when a binary tree is traversed in a post-order manner

Subroutine vector(T: tree);

Input: tree T, a Boolean formula
in the form of a binary tree
(each node has 0 or 2 children)
with AND and OR as nodes

Output: Returns a vector $v(x)$ for each node
 x of T, with all vectors of same length

Notes: In implementation,
T is a record containing T.node
(possible values are: AND, OR),
T.left, T.right, T.L, T.vector; so $v(x) = T.vector$
{
L=0 /* length of vector
maxL=0 /*maximal length of vector
IF T is a leaf /*T.left=NIL; x=T;
THEN RETURN T.vector= empty
/* $v(x) = T.vector$
ELSE
CHILDV(T, maxL);
Padding(T, maxL)
}

Function Padding(T, maxL) {
IF L < maxL
{ add maxL-L 0's at the end of $v(x)$; L=maxL};
IF x is not a leaf
{
Padding(T.left, maxL);
Padding(T.right, maxL)
}
}

```

Function CHILDV(T, maxL)  {
  IF T.node=OR
  {
    ORCHILD(T.left, T.vector, maxL);
    ORCHILD(T.right, T.vector, maxL)
  }
  IF T.node=AND
  {
    ANDLEFTCHILD(T.left, T.vector, maxL);
    ANDRIGHTCHILD(T.left, T.vector, maxL)
  }
}

Function ORCHILD(X:tree, Y, maxL)  {
  X.vector=Y /* returns same vector before
padding for the root node
  CHILDV(X, maxL)
}

Function ANDCHILDLEFT(X:tree, Y, maxL) {
  X.L= X.L+1 /* length of v(x) increases by 1
  IF X.L> maxL
  {
    maxL=X.L /* increases maxL if needed
    X.vector = Y | 1 /* adds 1 at
the end of vector and returns it
  }
  CHILDV(X, maxL)
}

Function ANDCHILDRIGHT(X;tree, Y, maxL) {
  X.L= X.L+1;
  IF X.L> maxL
  maxL=X.L;
  X.vector=(0^{X.L-1}, -1) /*X.L-1 0's before -1
  CHILDV(X, maxL)
}

```

Figure 27: Algorithm for generating LSSS matrix based on input boolean query tree

```

155 QueryTree* childv(QueryTree* root, int* maxL);
156 QueryTree* orchild(QueryTree* node, vector<int> vector_from_parent, int *maxL);
157 QueryTree* leftandchild(QueryTree* node, vector<int> vector_from_parent, int *maxL);
158 QueryTree* rightandchild(QueryTree* node, vector<int> vector_from_parent, int *maxL);
159
160 //LSSS
161 QueryTree* rightandchild(QueryTree* node, vector<int> vector_from_parent, int *maxL)
162 {
163     int length = vector_from_parent.size()+1;
164     //int length = (node->vec).size()+1;
165     (node->vec).clear();
166     for(int i=0; i<length-1; i++)
167         (node->vec).push_back(0);
168     (node->vec).push_back(-1);
169     if((node->vec).size() > *maxL)
170         *maxL = (node->vec).size();
171     node = childv(node, maxL);
172     return node;
173 }
174
175 QueryTree* leftandchild(QueryTree* node, vector<int> vector_from_parent, int *maxL)
176 {
177     (node->vec).clear();
178     for(int i=0; i<vector_from_parent.size(); i++)
179         (node->vec).push_back(vector_from_parent[i]);
180     (node->vec).push_back(1);
181     if((node->vec).size() > *maxL)
182         *maxL = (node->vec).size();
183     node = childv(node, maxL);
184     return node;
185 }
186 QueryTree* orchild(QueryTree* node, vector<int> vector_from_parent, int *maxL)
187 {
188     (node->vec).clear();
189     for(int i=0; i<vector_from_parent.size(); i++)
190         (node->vec).push_back(vector_from_parent[i]);
191     node = childv(node, maxL);
192     return node;
193 }
194 QueryTree* childv(QueryTree* root, int* maxL)
195 {
196     if(root->value == "OR" || root->value == "or")
197     {
198         root->left = orchild(root->left, root->vec, maxL);
199         root->right = orchild(root->right, root->vec, maxL);
200     }
201     if(root->value == "AND" || root->value == "and")
202     {
203         root->left = leftandchild(root->left, root->vec, maxL);
204         root->right = rightandchild(root->right, root->vec, maxL);
205     }
206     return root;
207 }
208 QueryTree* padding(QueryTree* root, int* maxL)
209 {
210     if((root->vec).size() < *maxL)
211     {
212         int pads = *maxL - (root->vec).size();
213         for(int i=0; i<pads; i++)
214             (root->vec).push_back(0);
215     }
216     if(root->is_leaf == 0)
217     {
218         root->left = padding(root->left, maxL);
219         root->right = padding(root->right, maxL);
220     }
221     return root;
222 }
223 QueryTree* LSSS(QueryTree *root)
224 {
225     if(root != NULL)
226     {
227         int maxL = 0;
228         if(root->is_leaf == 1)
229             return root;
230         else
231         {
232             root = childv(root, &maxL);
233             cout<<maxL;
234             root = padding(root, &maxL);
235         }
236     }
237 }

```

```

238 int main()
239 {
240     char a[200];
241     cout<<"Enter query: ";
242     scanf("\n");
243     scanf("%[^\n]s",a);
244     vector<string> words;
245     char *pch;
246     pch = strtok(a, " ");
247     while(pch != NULL)
248     {
249         words.push_back(convert_to_String(pch));
250         pch = strtok(NULL, " ");
251     }
252     cout<<"Following are the words in the query:\n";
253     for(int i=0;i<words.size();i++)
254         cout<<words[i]<<endl;
255     cout<<"-----\n";
256     QueryTree* r = constructTree(words);
257     r = LSSS(r);
258     map<string,vector<int>> LSSS;
259     cout<<"\nFollowing is the level order traversal of query:\n";
260     printLevelOrder(r);
261     cout<<"-----";
262     cout<<"\nFollowing is the in order traversal of query:\n";
263     inOrder(r,LSSS);
264     cout<<"\n-----\n";
265     cout<<"\nFollowing is the LSSS matrix:\n";
266     for(auto i: LSSS)
267     {
268         cout<<"Attribute: "<<i.first<<"\t";
269         cout<<"Vector: [";
270         for(int j=0;j<i.second.size();j++)
271             cout<<i.second[j]<<" ";
272         cout<<"]"<<endl;
273     }
274     cout<<"\n-----\n";
275     return 0;
276 }
277

```

Figure 28: Code for generating LSSS matrix from input post-fix boolean query

```

ritu@ritu-VirtualBox:~/GmpPbc/MRMWBKSES$ ./a.out
Enter query: doctor1 doctor2 and city1 and
Created tree successfully

Following is the level order traversal of query:
{ and 0 0 }
{ and 1 0 }{ city1 -1 0 }
{ doctor1 1 1 }{ doctor2 0 -1 }
-----
Following is the in order traversal of query:
{ doctor1 1 1 }{ and 1 0 }{ doctor2 0 -1 }{ and 0 0 }{ city1 -1 0 }
-----
Following is the LSSS matrix:
Attribute: city1      Vector: [-1 0 ]
Attribute: doctor1   Vector: [1 1 ]
Attribute: doctor2   Vector: [0 -1 ]
-----

```

Figure 29: Output of LSSS matrix from input post-fix boolean query