

Tutorial : 6

A min spanning tree or minimum weight spanning tree is a subset of the edge of connected edge-weight undirected graph that connects all the vertices together without any cycle & with the min possible total edge weight.

Application,

→ Design LAN.

→ Laying pipeline connecting offshore drilling sites refineries and consume markets.

Suppose you want to construct highway or railroad spanning several cities then we can use concept of min span tree.

2. Time Complexity of Prim's algo

$$O(V \log V + E \log V) = O(E \log V)$$

it can be improved $= O(E + \log V)$

$$\text{Space Complexity} \sim O(V)$$

Kruskal's Alg

$$T(C) \rightarrow O(E \log V)$$

$$S(C) \rightarrow O(\log E)$$

Dijkstra's Algo

$$T(C) \rightarrow O(|V| + |E| \log V)$$

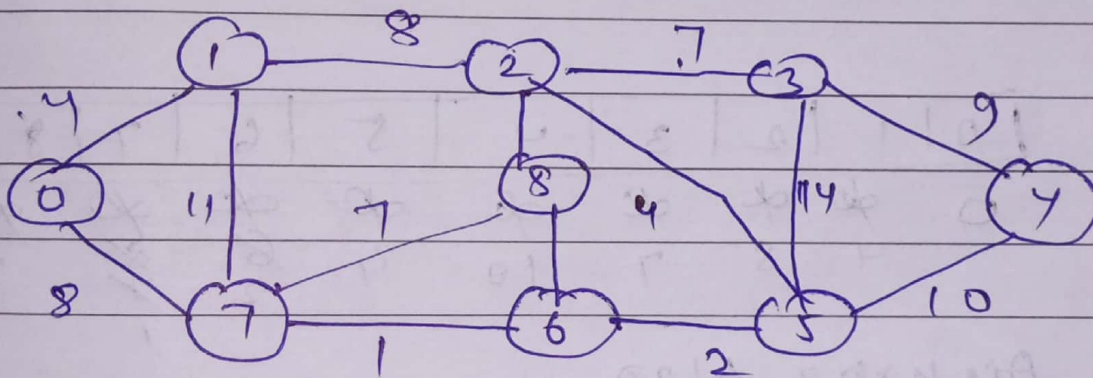
$$S(C) \rightarrow O(|V| + |E|)$$

Bellman Ford

$$T(C) = O(E)$$

$$S(C) = O(V)$$

3. Kruskal's Algo



~~4, 2, 2, 4, 4, 6, 7, 7, 8, 8, 76, 28, 65~~

~~28, 10, 86, 78, 23, 07, 12, 34~~

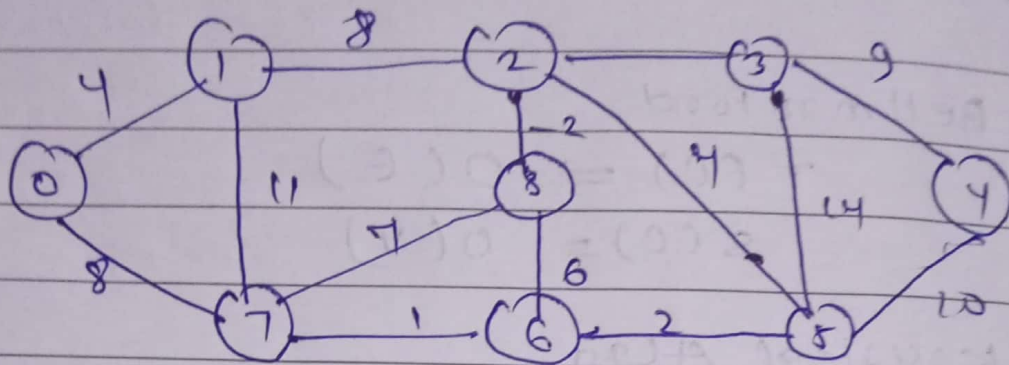
76 28 65 25 10 86 78 23, 07

12, 34, 45, 17, 35

$$\text{weight of MST} = 1 + 2 + 2 + 4 + 4 + 7 + 8 + 9$$

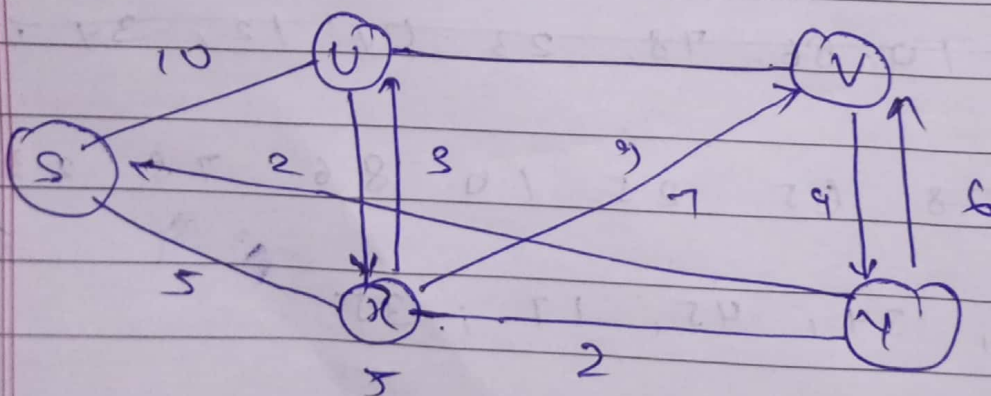
$$= 37$$

Prim's Algo:



0	1	2	3	4	5	6	7	8
0	4	8	7	10	4	8	8	2
	4	8	7	10	4	2	1	2

5 soln: Dijkstra's Algo



node	Shortest distance from source
S	0
X	5
V	9
Y	7

Bellman Ford Algo

1st	$\begin{matrix} 0 \\ \textcircled{S} \end{matrix}$	$\begin{matrix} 10 \\ \textcircled{U} \end{matrix}$	$\begin{matrix} \infty \\ \textcircled{V} \end{matrix}$	$\begin{matrix} 5 \\ \textcircled{X} \end{matrix}$	$\begin{matrix} \infty \\ \textcircled{Y} \end{matrix}$
2nd	$\begin{matrix} 0 \\ \textcircled{S} \end{matrix}$	$\begin{matrix} 10 \\ \textcircled{U} \end{matrix}$	$\begin{matrix} 11 \\ \textcircled{V} \end{matrix}$	$\begin{matrix} 5 \\ \textcircled{X} \end{matrix}$	$\begin{matrix} \infty \\ \textcircled{Y} \end{matrix}$
3rd	$\begin{matrix} 0 \\ \textcircled{S} \end{matrix}$	$\begin{matrix} 4 \\ \textcircled{U} \end{matrix}$	$\begin{matrix} 9 \\ \textcircled{V} \end{matrix}$	$\begin{matrix} 5 \\ \textcircled{X} \end{matrix}$	$\begin{matrix} 7 \\ \textcircled{Y} \end{matrix}$
4th	$\begin{matrix} 0 \\ \textcircled{S} \end{matrix}$	$\begin{matrix} 4 \\ \textcircled{U} \end{matrix}$	$\begin{matrix} 9 \\ \textcircled{V} \end{matrix}$	$\begin{matrix} 5 \\ \textcircled{X} \end{matrix}$	$\begin{matrix} 7 \\ \textcircled{Y} \end{matrix}$

