INDIAN INSTITUTE OF TECHNOLOGY KHARAGPUR

Date: 23-04-2015 (AN) Spring End-Semester 2015 Time: 3 hours Full Marks: 100

Department: Mechanical Engg Subject: Mechanics of Human Body Subject No: ME 60407

Marks distribution for each question is indicated within brackets.

Assume any suitable data that may be required for solution, stating clear justifications

Answer all questions.

- (1) (a) Briefly describe the method of 'Inverse Dynamics'? State the difference between the methods 'Inverse Dynamics' and 'Forward Dynamics'?
- **(b)** State clearly the steps and governing equations required to find out joint forces and moments in a limb segment using 'Inverse Dynamics Method'?
- (c) A force vector in a Cartesian coordinate system (A) is given as 10i + 20j + 15k. Another new coordinate system (B) is obtained by applying the following sequential rotation and translation with respect to the original Cartesian coordinate system (A):
- (i) Rotations: $+30^{\circ}$ about y-axis, then -20° about z-axis, and then $+20^{\circ}$ about x-axis degrees.
- (ii) Translations: 20 units along x, y and z-axes.

Calculate the <u>transformation matrix</u> and <u>transformed force vector</u> in the new coordinate system (**B**).

$$(6+6+8=20)$$

- (2) (a) What is meant by 'apparent density' of bone? How is bone mechanical properties related to apparent density and its structure?
- (b) What are the techniques for fixation of implant with bone? Draw a labeled sketch of implanted femur.
- (c) State the criteria for selection of implant material for joint replacement. Name the commonly used biomaterials for load bearing implants.

$$(8+6+6=20)$$

- (3) (a) How is implant-bone interfacial failure evaluated? Discuss about Hoffman's failure criterion.
- (b) The state of stress at a point on the implant-bone interface is, $\sigma_x = 40$ MPa, $\sigma_y = 20$ MPa, $\sigma_z = -10$ MPa, $\tau_{xy} = \tau_{yz} = \tau_{zx} = 30$ MPa. Determine the normal and shearing stresses at the implant-bone interface on a plane, which is inclined at 60° with x-axis, 60° with y-axis and 45° with z-axis.
- (c) Using data of Problem 3(b), evaluate Hoffman failure value at implant-bone interface, assuming adjacent bone density $\rho = 0.4 \text{ gm.cm}^{-3}$. Interfacial strengths (MPa): $S_t = 15\rho^{1.71}$, $S_c = 32\rho^{1.85}$, $S_s = 22\rho^{1.65}$

$$(4 + 10 + 6 = 20)$$

- (4) (a) What is meant by 'stress shielding' and 'bone remodelling'?
- **(b)** State the mathematical formulation of the 'internal' bone remodelling process, considering bone remodelling caused by joint replacement.
- (c) Design a computational scheme, using flow diagram, for the iterative simulation of the bone remodelling process.

$$(4 + 8 + 8 = 20)$$

- (5) (a) Discuss briefly the major failure mechanisms of orthopaedic implants.
- (c) Briefly describe the different pathways of tissue differentiation from Mesenchymal Cells.
- (d) What are the salient differences between phenomenological and cell-phenotype specific tissue differentiation algorithm. Explain with the help of governing equations.

$$(5 + 7 + 8 = 20)$$