## 1

## Control Systems

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Abstract—This manual is an introduction to control systems based on GATE problems.Links to sample Python codes are available in the text.					

Download python codes using

svn co https://github.com/gadepall/school/trunk/control/codes

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**Solution:** Given H(s) = 1 and  $G(s) = Ke^{-s}/s$ Phase Margin(PM) is defined as-

Fig. 7.0.1

$$PM = \phi - (-180^{\circ})$$
 (7.0.1.1)

$$\implies \phi + 180^{\circ} \tag{7.0.1.2}$$

where,

9 Compensators

10 OSCILLATOR

$$\phi = \angle G(j\omega_{gc})H(j\omega_{gc}) \qquad (7.0.1.3)$$

9.1 Phase Lead

 $\omega_{gc}$  is the gain-cross over frequency.

7.0.2. Find  $\omega_{gc}$ .

**Solution:** 

$$\left|G\left(j\omega_{gc}\right)H\left(j\omega_{gc}\right)\right| = 1$$

$$\iff \left|\frac{Ke^{-j\omega_{gc}}}{j\omega_{gc}}\right| = 1$$

$$(7.0.2.2)$$

$$\iff \omega_{gc} = K \quad Assuming K > 0 \quad (7.0.2.3)$$

7.0.3. Find  $\phi$ .

**Solution:** 

$$\phi = \angle G(j\omega_{gc})H(j\omega_{gc})$$
(7.0.3.1)
(7.0.3.2)

(7.0.3.3)

7.0.4. By (7.0.1.1)

$$PM = 30^{\circ}$$
 (7.0.4.1)  
by(7.0.3.1)  $K = \pi/3$  (7.0.4.2)

7.0.5. Verify result by plotting the gain and phase plots of  $G(j(\omega))$ 

**Solution:** The following code plots Fig. 7.0.5

codes/ee18btech11038\_plot.py

The Phase plot is as shown-

 $\implies \angle \frac{Ke^{-jK}}{jK}$ 

 $\implies -90^{\circ} - K(180/\pi)$ 

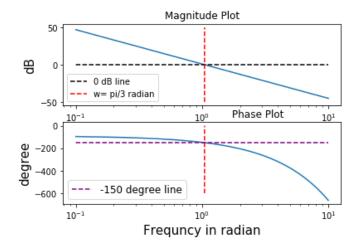


Fig. 7.0.5