

Filter (Digital Filter)

➤ Comparison between Analog and digital filter.

(2)

Digital filter

Infinite impulse response filter.

$$h(n) = \{1, 2, -2, 3, \dots\}$$

Finite impulse response filter.

(FIR)

$$h(n) = \{1, 2, 3, 4\}.$$

➤ Comparison between FIR & FIR? (From book).
(FIR \rightarrow linear phase)

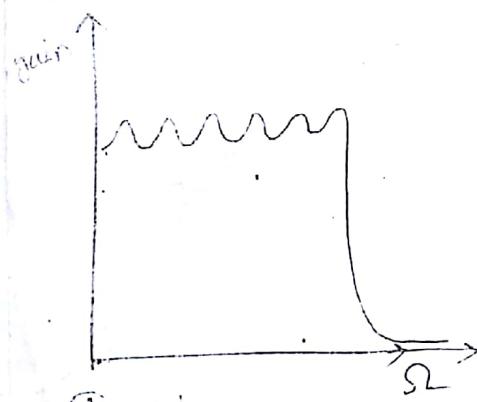
Digital filter

Butterworth filter

(Here transfer characteristics are smooth for both passbands and stopbands)

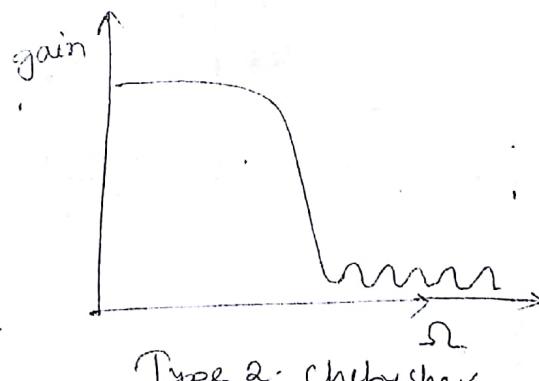
Chebyshev filter

(Equinepples are present either in the stop band or in the pass band.)



Type 1

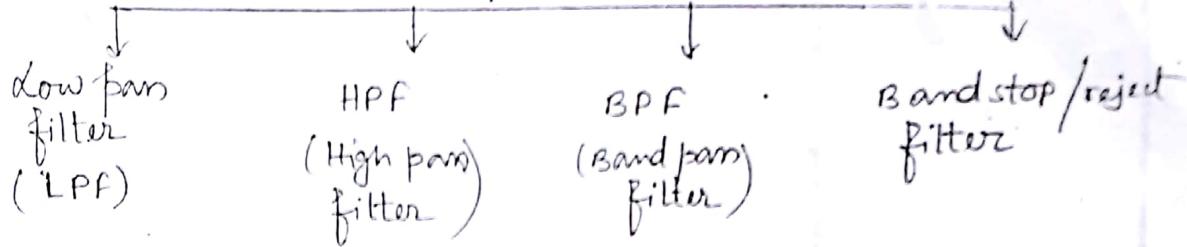
Chebyshev



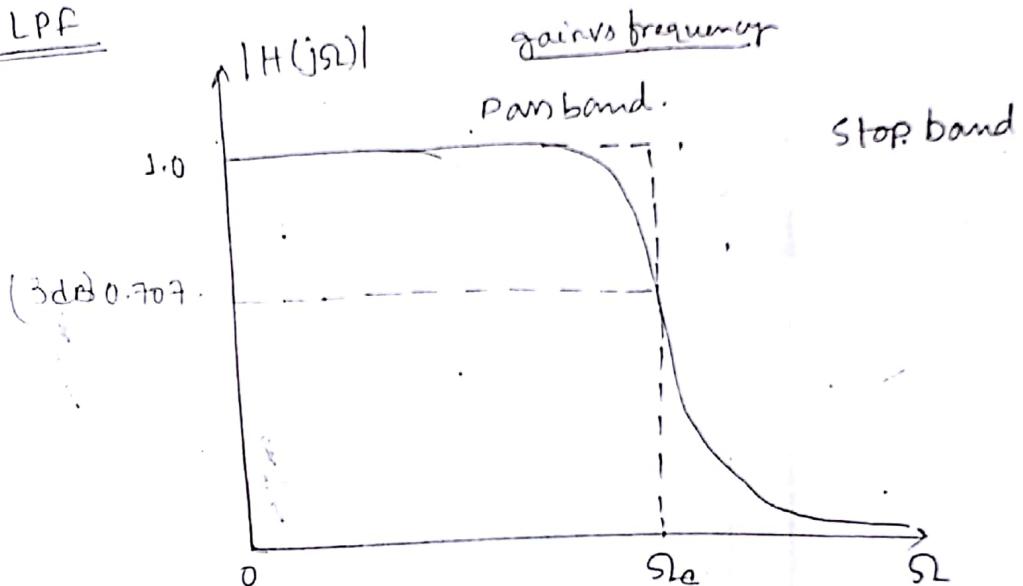
Type 2. Chebyshev

➤ Comparison between these two.

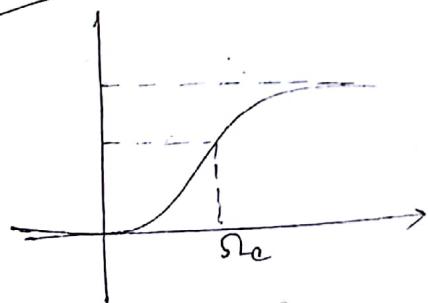
④ Filter classification based on characteristics:-



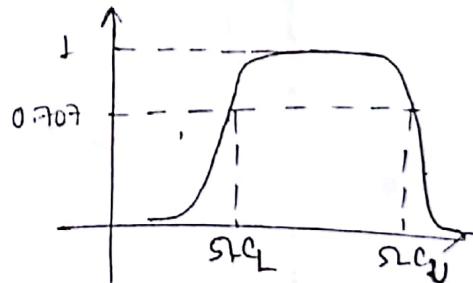
LPF



HPF



BPF

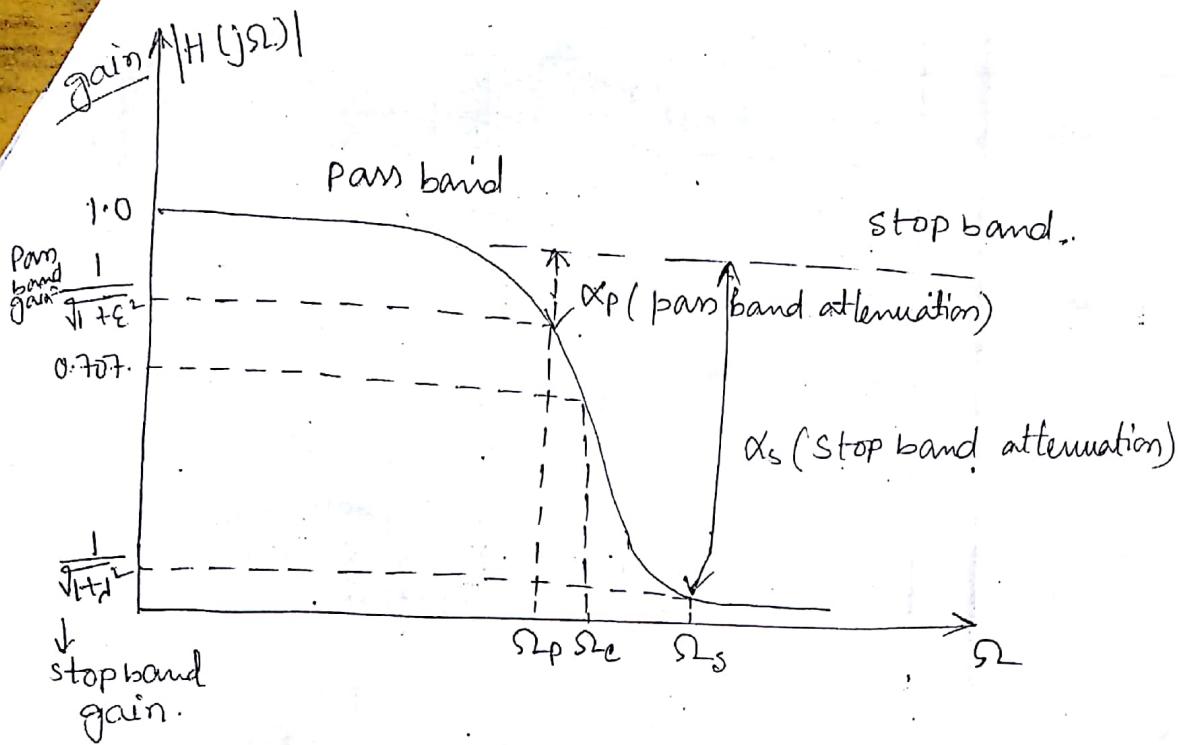


⑤ IIR filter design:-

Butterward low pass filter design:-

Digital (Digital from analog):-

Step 1:-



Difference bet'n IIR and FIR:-

IIR

1) IIR stands for infinite impulse response system.

2) less powerful than FIR filters, requires less processing power and less work to set up the filters.

3) They are more easy to change "On-the-fly"

4) These are less flexible.

5) Cannot implement linear-phase filtering.

6) More efficient

7) Used as notch (band stop), band pass function.

8) Higher sensitivity.

9) Delay is less.

FIR

1) finite impulse response system.

2) FIR filters are more powerful than IIR, but also require more processing power and more work to set up the filters.

3) They are less easy to change "On-the-fly" as you can by

4) Their greater power means more flexibility and ability to finely adjust.

5) Can implement linear-phase filtering.

6) less efficient

7) used as anti-aliasing, low pass baseband filters.

8) lower sensitivity.

9) Delay is more than IIR filter.

Analog filter transfer funⁿ

Step 1 :- From the given specifications find order of the filter.

$\Omega_s, \Omega_p \rightarrow$ Given.

as $\frac{1}{\sqrt{1+\epsilon^2}} \neq \frac{1}{\sqrt{1+r^2}} \rightarrow$ Given.

$$N = \frac{\log \sqrt{\frac{10^{0.1\alpha_s} - 1}{10^{0.1\alpha_p} - 1}}}{\log \left(\frac{\Omega_s}{\Omega_p}\right)} \text{ or, } N = \frac{\log \left(\frac{d}{\epsilon}\right)}{\log \left(\frac{\Omega_s}{\Omega_p}\right)}$$

$$\text{Where, } d = \sqrt{10^{0.1\alpha_s} - 1}, \epsilon = \sqrt{10^{0.1\alpha_p} - 1}$$

Step 2 :- From the value of N equate it to the next higher integer.

Step 3 :- From the value of N , find the transfer function of filter ~~H(s)~~ $H(z)$ from table no - S.1 (E.G) when ~~$\Omega_c = 1$~~ $\Omega_c = 1$ rad/sec.

$$\text{Step 4 :- } \Omega_c = \Omega_p / (10^{0.1\alpha_p} - 1)^{\frac{1}{2N}}$$

$$= \frac{\Omega_s}{(10^{0.1\alpha_s} - 1)^{\frac{1}{2N}}}$$

$$\Omega_c = \frac{\Omega_p}{(\epsilon)^{1/N}} = \frac{\Omega_s}{(d)^{1/N}}$$

Step 5 :- From the calculated value of Ω_c we obtained analog filter transfer function -

- $H_a(s)$ by replacing $s \rightarrow \frac{s}{\Omega_c}$

(For HPF it will be $\frac{\Omega_c}{s}$)

From $H_a(s)$ find $H(z)$ by using anyone of the following method. \rightarrow

- a) Approximation of Derivative.
- b) Impulse invariance method. (II)
- c) Bilinear transformation method. (BT)
- d) Matched Z-transform.

short note.

Step - 7 :-

From $H(z)$ realize the filter

H.W :- 5.2, 5.4,

Ex :- S.5.

$0 \rightarrow$ Low-pass filter

II method :-

Here relation between analog angular frequency, (Ω) and digital angular frequency (ω)

$$(\text{Eq}) \quad \omega = \Omega T$$

Where T is the sampling period. If not mentioned consider $T=1$.

Now, In II method 1st find $H_a(s)$ in terms of sum of single pole.

$$H_a(s) = \sum_{k=1}^N \frac{c_k}{s-p_k}$$

Then $H(z)$ can be obtained by

$$H(z) = \sum_{k=1}^N \frac{c_k}{1 - e^{p_k T} z^{-1}}$$

Ex :- S.11, S.13, S.15(VRI), PP-S.17, S.8

* Bilinear transformation

Here s is replaced by $s = \frac{2(1-z^{-1})}{T(1+z^{-1})}$

Ex - $S \cdot 16$ (imp), $S \cdot 18$ (imp),

Ex - S.S.

$$0.9 \leq |H(j\omega)| \leq 1 \rightarrow 0 \leq \omega \leq 0.2\pi.$$

$$|H(j\omega)| \leq 0.2 \rightarrow 0.4\pi \leq \omega \leq \pi.$$

$$\frac{1}{\sqrt{1+\epsilon^2}} = 0.9 \rightarrow \epsilon =$$

$$\frac{1}{\sqrt{1+\epsilon^2}} = 0.2 \leftrightarrow \epsilon =$$

$$\omega_p = 0.2\pi, \omega_s = 0.4\pi$$

$$N^2 \frac{\log(\epsilon)}{\log(\frac{\omega_s}{\omega_p})} = 4$$

$$\omega_c = \omega_p \cdot (\epsilon)^{1/N}$$

Ex' - 5.1 Given, $\alpha_p = 1\text{dB}$, $\alpha_s = 30\text{dB}$, $\omega_p = 200\text{ rad/sec}$

$$\omega_s = 600\text{ rad/sec.}$$

$$\Rightarrow N^2 \frac{\log \sqrt{\frac{10^{0.1\alpha_s}-1}{10^{0.1\alpha_p}-1}}}{\log \left(\frac{\omega_s}{\omega_p} \right)} = \frac{\log \sqrt{\frac{10^{0.1 \times 600}-1}{10^{0.1 \times 200}-1}}}{\log \left(\frac{600}{200} \right)}$$

$$= \frac{\log \sqrt{\frac{10^6-1}{10^3-1}}}{\log(3)}$$

$$= \text{Ans. } 3.758$$

$$N = 4$$

$$\begin{aligned} &= \frac{\log \sqrt{\frac{10^6-1}{10^3-1}}}{\log \left(\frac{6}{2} \right)} \\ &= \frac{\log \sqrt{10^3}}{\log \left(10^4 \right)} \\ &= \frac{\log(10^{\frac{3}{2}})}{\log(10^4)} \\ &= \frac{2.0}{0.477} = 41.9 \approx 12. \end{aligned}$$

S.2

$$\alpha_p = 3 \text{ dB}, \Omega_p = 2\pi \times 500 = 1000\pi \text{ rad/sec}$$

$$\alpha_s = 40 \text{ dB}, \Omega_s = 2\pi \times 1000 = 2000\pi \text{ rad/sec.}$$

$$N_2 = \frac{\log \sqrt{\frac{10^{0.1\alpha_s} - 1}{10^{0.1\alpha_p} - 1}}}{\log \left(\frac{\Omega_s}{\Omega_p} \right)}$$

$$= \frac{\log \left(\sqrt{\frac{10^{0.1 \times 40} - 1}{10^{0.1 \times 3} - 1}} \right)}{\log \left(\frac{2000}{1000} \right)}$$

$$= \frac{\log (100.23)}{\log (2)}$$

$$= 6.64 = 7.$$

~~Butterworth filter pole~~

S.4

$$\alpha_p = -2 \text{ dB}, \Omega_p = 20 \text{ rad/sec}$$

$$\alpha_s = -10 \text{ dB}, \Omega_s = 30 \text{ rad/sec.}$$

$$N = \frac{\log \sqrt{\frac{10^{0.1 \times 20} - 1}{10^{0.1 \times 20} - 1}}}{\log \left(\frac{10}{2} \right)} = \frac{\log \sqrt{\frac{10^3 - 1}{10^3 - 1}}}{\log (s)} = \frac{\log (3.176)}{\log (s)}$$

$$N_2 = \frac{\log \sqrt{\frac{10^{0.1 \times 10} - 1}{10^{0.1 \times 2} - 1}}}{\log \left(\frac{30}{20} \right)} > \frac{\log \sqrt{\frac{10^1 - 1}{10^0 \cdot 3} - 1}}{\log (3/2)}$$

$$= 3.36$$

$$= 4.$$

from table 5.1,

$$H(s) = \frac{1}{(s^2 + 0.76537s + 1)(s^2 + 1.8477s + 1)}$$

$$\omega_c = \frac{\cancel{\omega_p}}{(10^{0.1\alpha_p} - 1)^{\frac{1}{2N}}}$$

$$= \frac{20}{(10^{0.1 \times 2} - 1)^{\frac{1}{2 \times 4}}}$$

$$= \frac{20}{(10^{0.2} - 1)^{\frac{1}{8}}} = 21.3867$$

$$s \rightarrow \frac{s}{21.3867} \text{ in } H(s)$$

i.e., $H(s) = \frac{1}{\left[\left(\frac{s}{21.3867} \right)^2 + 0.76537 \times \frac{s}{21.3867} + 1 \right]}$

$$\times \frac{1}{\left(\frac{s}{21.3867} \right)^2 + 1.8477 \times \frac{s}{21.3867} + 1}$$

$$= \frac{1}{\left(\frac{s}{21.3867} \right)^2}$$

Q Using BT design a high pass filter with cut-off frequency 100Hz and down ~~3dB~~ 10 dB. at 350Hz.
 Sampling frequency is 5000 Hz.

\Rightarrow

$$T = \frac{1}{F_s} = \frac{1}{5000} = 0.0002 \text{ sec}$$

$$\alpha_s = 10 \text{ dB} \quad f_c = 1000 \text{ Hz}$$

$$\alpha_p = 3 \text{ dB} \quad \omega_{lp} = \omega_c$$

$$\omega_s = 350 \text{ Hz} \quad \omega_p = 2\pi \times 1000$$

$$\omega_s = 2\pi \times 350$$

$$= 2000\pi$$

$$= 6283.1$$

$$= 2199.11 \pi$$

$$N = \frac{\log \left(\sqrt{\frac{10^{0.1\alpha_s}}{1 - 1}} \right)}{\log \left(\frac{\omega_s}{\omega_p} \right)} = \frac{\log \left(\sqrt{\frac{9}{0.995}} \right)}{\log \left(\frac{2199.11}{6283.1} \right)}$$

$$= \frac{\log \left(\sqrt{\frac{10^{0.1 \times 10}}{1 - 1}} \right)}{\log \left(\frac{2199.11}{6283.1} \right)} = \frac{\log \left(\sqrt{\frac{9}{0.995}} \right)}{\log \left(\frac{3}{0.35} \right)}$$

$$= \frac{\log \left(\sqrt{\frac{9}{0.995}} \right)}{\log \left(0.35 \right)} = \frac{\log(3)}{\log(0.35)}$$

$$\omega_s = 2\pi \times 350 = 700\pi, \quad \omega_p = 2000\pi$$

Using BT method

$$\Omega_s = \frac{2}{T} \tan \frac{\omega_s}{2}$$

$$= \frac{2}{2 \times 10^{-4}} \tan(350\pi)$$

$$= 3552.46$$

$$\omega_p = \frac{2}{2 \times 10^{-4}} \cdot \tan(1000\pi)$$

$$= 67659.8$$

$$N = \frac{\log \left(\sqrt{\frac{10^{0.1 \times 10} - 1}{10^{0.1 \times 3} - 1}} \right)}{\log \left(\frac{3552.46}{67659.83} \right)}$$

$$\Rightarrow \frac{\log(3.007)}{\log(0.525)} = -0.373 \approx 1.$$

~~± 1.708~~ $\approx 1.708 \approx 2$.

$$s \rightarrow \frac{\Omega_c}{s}$$

$$H(s) = \frac{1}{s + \sqrt{2}s + 1} = \frac{1}{\left(\frac{67659.8}{s}\right)^2 + \sqrt{2} \times \frac{67659.8}{s} + 1}$$

$$= \frac{1}{\left(\frac{\Omega_c}{s}\right)^2 + \sqrt{2} \frac{\Omega_c}{s} + 1}$$

Now as the filter is high pass filter s is replaced

by $\frac{\Omega_c}{s}$.

$$\text{i.e. } s \rightarrow \frac{\Omega_c}{s} = \frac{67660}{s}$$

$$H_a(s) = \frac{1}{\left(\frac{67660}{s}\right)^2 + \sqrt{2} \left(\frac{67660}{s}\right) + 1} = \frac{s}{67660 + 8}$$

$$\text{Now, in BT method } s = \frac{2}{T} \frac{(1-z^{-1})}{(1+z^{-1})}$$

$$H(z) = \frac{\frac{2}{T} \frac{(1-z^{-1})}{(1+z^{-1})}}{67660 + \frac{2}{T} \frac{(1-z^{-1})}{(1+z^{-1})}}$$

$$H(z) = \frac{\frac{2}{T} \left(\frac{z-1}{z+1} \right)}{67660 + \frac{2}{T} \left(\frac{z-1}{z+1} \right)}$$

$$\underline{Q} \quad H(s) = \frac{2}{(s+1)(s+2)} \text{ Find } H(z) \text{ using BT method}$$

where $T = 1 \text{ sec.}$

\Rightarrow

$$H(\underline{z}) = \frac{2}{T} \frac{(1-z^{-1})}{(1+z^{-1})}$$

$$H(z) = \frac{2}{\left[\frac{2(1-z^{-1})}{(1+z^{-1})} + 1 \right] \left[\frac{2}{T} \times \frac{(1-z^{-1})}{(1+z^{-1})} + 2 \right]}$$

$$= \frac{2}{\left(2 \cdot \frac{(z-1)}{(z+1)} + 1 \right) \left(2 \cdot \frac{(z-1)}{(z+1)} + 2 \right)}$$

$$= \frac{2}{\left[2 \cdot \frac{(z-1)}{(z+1)} + 1 \right] \cdot 2 \cdot \left[\frac{z-1}{z+1} + 1 \right]}$$

$$= \frac{1}{2z-2+z+1} \times \frac{z-1+z+1}{z+1}$$

$$= \frac{1}{z-1} \times \frac{2z}{z+1}$$

$$= \frac{(z+1)}{2z(z-1)}$$

$$= \boxed{\frac{1+z^{-1}}{2z}}$$

$$= \frac{2(1-z^{-1}) + (1+z^{-1})}{(1+z^{-1})} \times \frac{2(1-z^{-1}) + 2(1+z^{-1})}{(1+z^{-1})}$$

$$= \frac{2}{2-2z^{-1}+1+z^{-1}} \times \frac{1}{2-2z^{-1}+2+2z^{-1}} \quad (1+z^{-1})$$

$$= \frac{2}{(1+z^{-1})} \times \frac{4}{(1+z^{-1})} = \frac{2(1+z^{-1})^2}{4(1+z^{-1})}$$

Bilinear transformation method

Here s is replaced by $\frac{2}{T} \frac{(1-z^{-1})}{(1+z^{-1})}$

relation between ω and Ω .

$$\begin{aligned}
 s &= \frac{2}{T} \frac{(1-z^{-1})}{(1+z^{-1})} = \frac{2}{T} \frac{(re^{j\omega}-1)}{(re^{j\omega}+1)} = \frac{2}{T} \left[\frac{r\cos\omega + j r \sin\omega - 1}{r\cos\omega + j r \sin\omega + 1} \right] \\
 &= \frac{2}{T} \left[\frac{r\cos\omega - 1 + j r \sin\omega}{r\cos\omega + 1 + j r \sin\omega} \right] \\
 &\Rightarrow \frac{2}{T} \times \frac{\{(r\cos\omega - 1) + j r \sin\omega\} \{r(\cos\omega + 1) - j r \sin\omega\}}{(r\cos\omega)^2 + (r\sin\omega)^2} \\
 &\Rightarrow \frac{2}{T} \times \frac{(r\cos\omega - 1)(r\cos\omega + 1) - j r \sin\omega(r\cos\omega - 1) + j r \sin\omega(r\cos\omega + 1)}{r^2(\cos^2\omega + \sin^2\omega) + 2r\cos\omega + 1} \\
 &= \frac{2}{T} \times \frac{(r\cos\omega)^2 - 1 - j r \sin\omega(r\cos\omega + 1) + j r \sin\omega(r\cos\omega + 1)}{r^2(\cos^2\omega + \sin^2\omega) + 2r\cos\omega + 1} \\
 &= \frac{2}{T} \times \frac{r^2(\cos^2\omega + \sin^2\omega) - 1 + j r \sin\omega(r\cos\omega + 1) + j r \sin\omega(r\cos\omega + 1)}{r^2 + 2r\cos\omega + 1} \\
 &= \frac{2}{T} \times \frac{r^2(\cos^2\omega + \sin^2\omega) - 1 + 2jr\sin\omega}{r^2 + 2r\cos\omega + 1} \\
 &\text{For } j\Omega = \frac{2}{T} \times \frac{r^2 - 1 + 2jr\sin\omega}{r^2 + 1 + 2r\cos\omega} \Rightarrow \frac{2}{T} \left[\frac{r^2 - 1}{r^2 + 1 + 2r\cos\omega} + j \frac{2r\sin\omega}{r^2 + 1 + 2r\cos\omega} \right]
 \end{aligned}$$

Equate Imaginary

$$\begin{aligned}
 \Omega &= \frac{2}{T} \left[\frac{2r\sin\omega}{r^2 + 1 + 2r\cos\omega} \right] = \frac{2}{T} \left[\frac{2\sin\omega}{2 + 2\cos\omega} \right] \text{ when } r = 1 \\
 &= \frac{2}{T} \left[\frac{\sin\omega}{1 + \cos\omega} \right] = \frac{2}{T} \frac{2\sin\omega \cos\omega}{2 + 2\cos\omega} \\
 \Omega &= \frac{2}{T} \tan \frac{\omega}{2} \quad | \quad \omega = 2 \tan^{-1} \frac{\sqrt{2}\Omega}{2}
 \end{aligned}$$

④ In case of TI method the relation of ω and Ω is linear. But for BT method it is non-linear.

Due to this non-linear effect the distortion and error is known as Warping effect. (S. 6105.48).

To minimize the distortion pre-warping is used.

H.W - S.18,

PP - S.9

Ex - S.30, S.32,

PP \rightarrow S.17.

— O —

Step-7

Realization of filter :-

- 1) Direct form 1 (DF1)
- 2) Direct form 2 (DF2)
- 3) Cascade form
- 4) parallel form.

DF1 :-

Delay $\Rightarrow x(n) \rightarrow [z^{-1}] \rightarrow x(n-1)$

Adder \Rightarrow

Multiplexer \Rightarrow

DFI :-

We know,

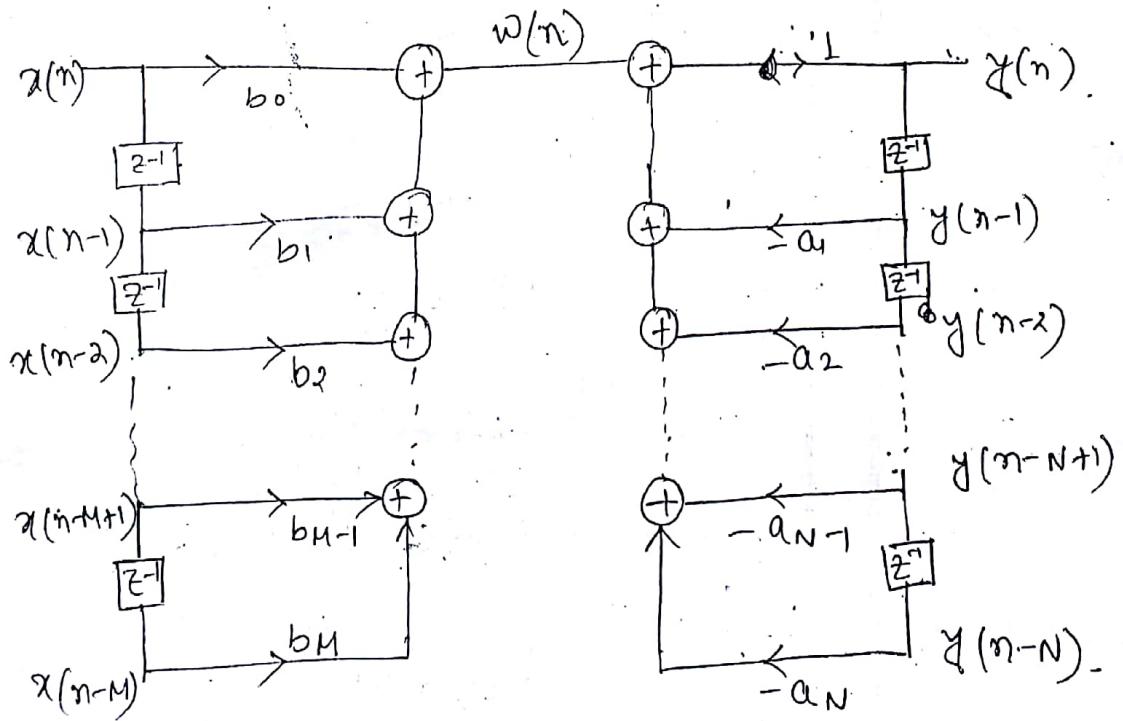
$$y(n) = - \sum_{k=1}^N a_k y(n-k) + \sum_{k=0}^M b_k x(n-k)$$

$$\Rightarrow -a_1 y(n-1) - a_2 y(n-2) \dots \neq a_N y(n-N)$$

$$+ \underbrace{b_0 x(n) + b_1 x(n-1) \dots + b_M x(n-M)}_{w(n)}$$

$$w(n) = b_0 x(n) + b_1 x(n-1) + b_2 x(n-2) \dots + b_M x(n-M) \quad \xrightarrow{\textcircled{1}}$$

$$y(n) = -a_1 y(n-1) - a_2 y(n-2) \dots - a_N y(n-N) + w(n) \quad \xrightarrow{\textcircled{2}}$$



DF2

We know,

$$y(n) = -\sum_{k=1}^N a_k y(n-k) + \sum_{k=0}^M b_k x(n-k)$$

$$Y(z) = -\sum_{k=1}^N a_k z^{-k} Y(z) + \sum_{k=0}^M b_k z^{-k} X(z),$$

$$\Rightarrow Y(z) \left[1 + \sum_{k=1}^N a_k z^{-k} \right] = \sum_{k=0}^M b_k z^{-k} X(z)$$

$$\Rightarrow H(z) = \frac{Y(z)}{X(z)}$$

$$= \frac{\sum_{k=0}^M b_k z^{-k}}{\left[1 + \sum_{k=1}^N a_k z^{-k} \right]} = \frac{Y(z)}{W(z)} \cdot \frac{W(z)}{X(z)}$$

$$\frac{Y(z)}{W(z)} = \sum_{k=0}^M b_k z^{-k} \Rightarrow Y(z) = \sum_{k=0}^M b_k z^{-k} W(z)$$

$$\text{So, } y(n) = \sum_{k=0}^M b_k w(n-k).$$

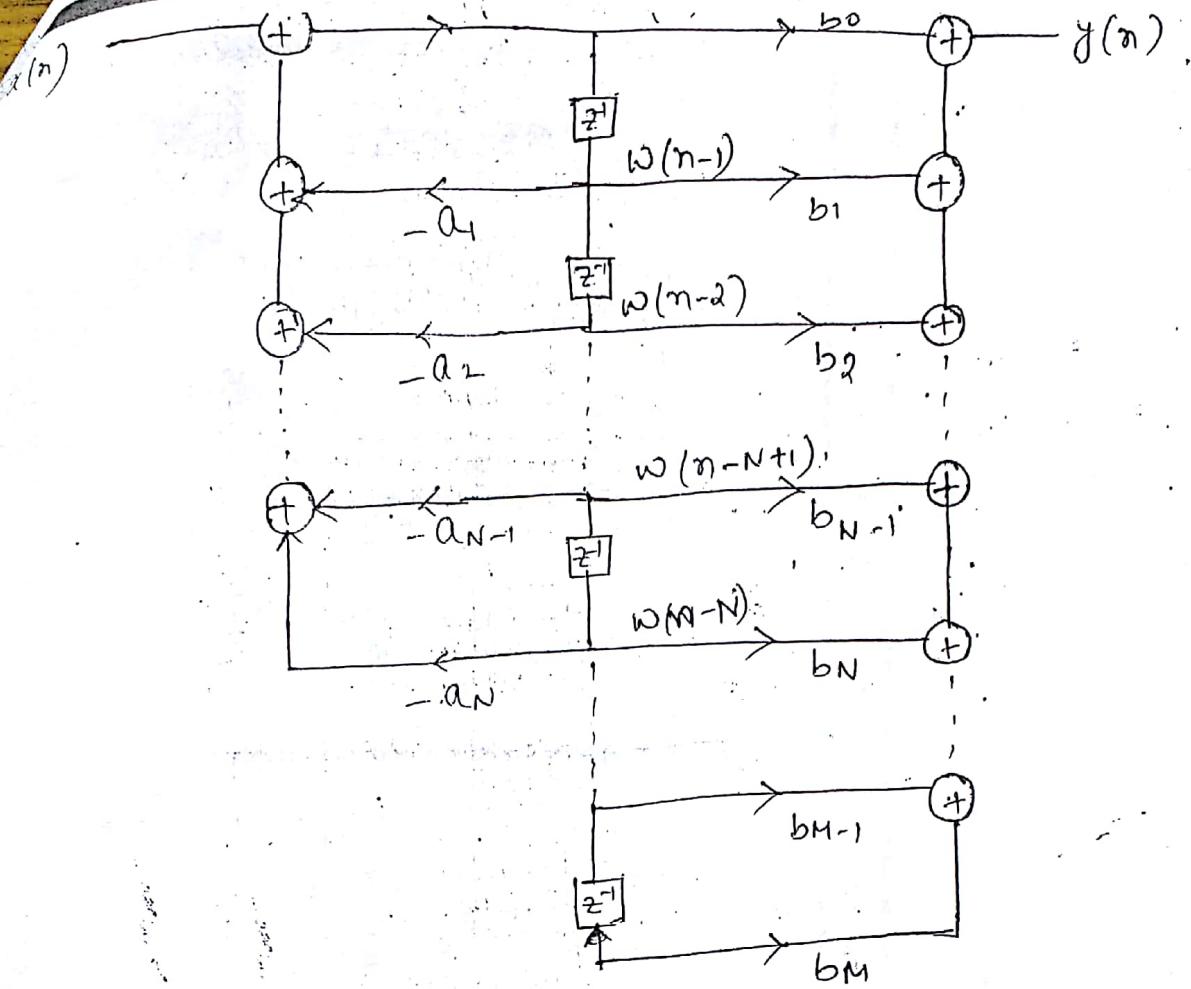
$$y(n) = b_0 w(n) + b_1 w(n-1) + \dots + b_M w(n-M) \quad \text{---(2)}$$

Now,

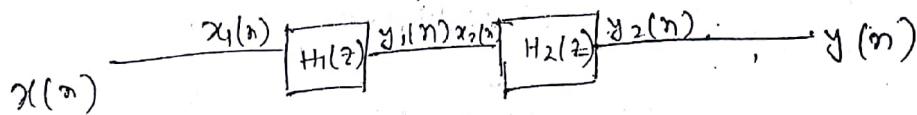
$$\frac{W(z)}{X(z)} = \frac{1}{1 + \sum_{k=1}^N a_k z^{-k}} \Rightarrow X(z) = \cancel{W(z) + \cancel{W(z)}} \\ = W(z) + \sum_{k=1}^N a_k z^{-k} W(z).$$

$$x(n) = w(n) + \sum_{k=1}^N a_k w(n-k)$$

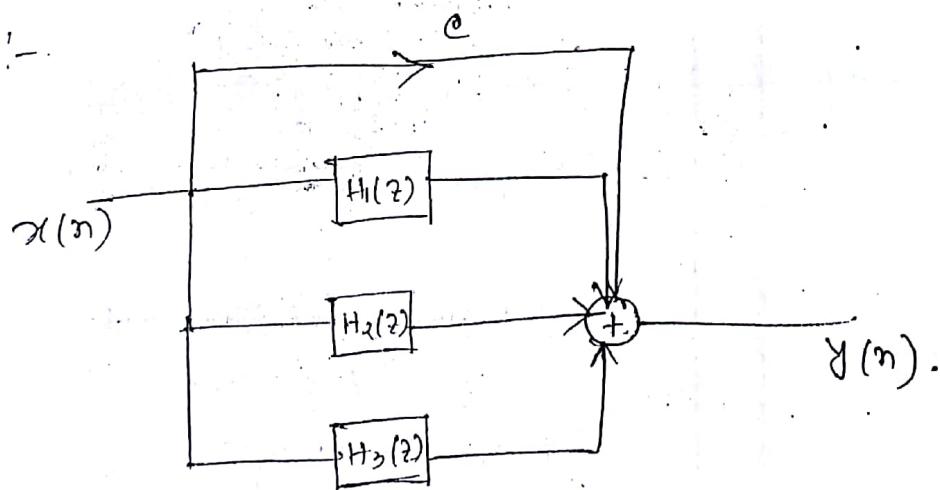
$$\Rightarrow w(n) = x(n) - a_1 w(n-1) - a_2 w(n-2) - \dots - a_N w(n-N) \quad \text{---(1)}$$



Cascade :-



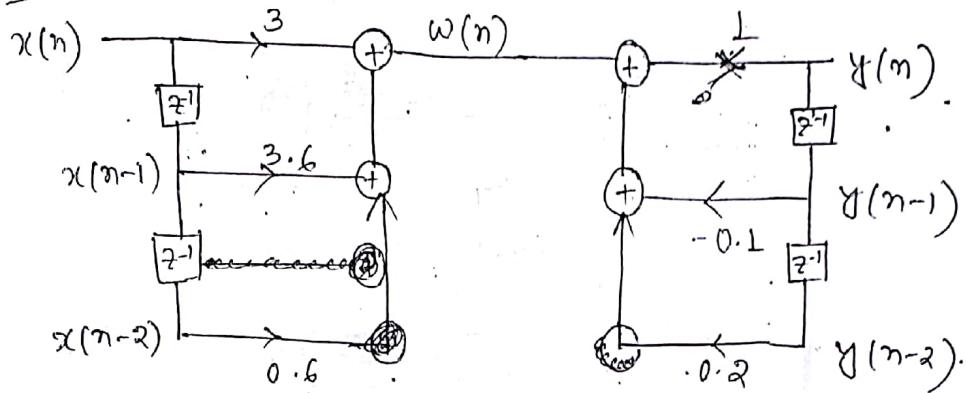
Parallel :-



$$y(n) = -0.1y(n-1) + 0.2y(n-2) + 3x(n) + 3.6x(n-1) + 0.6x(n-2)$$

Realize using DFI, DFQ, Cascade, parallel.

\Rightarrow DFI :-

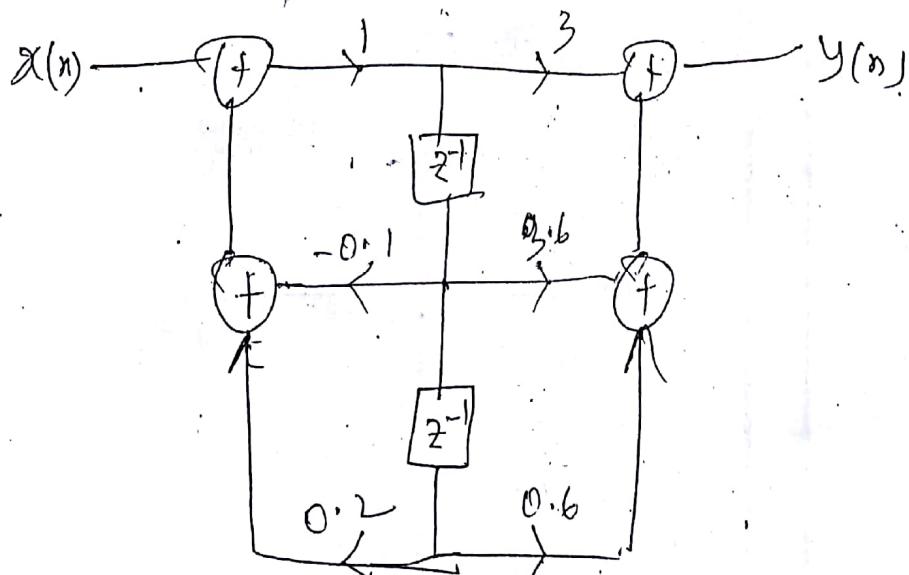


DFQ :-

$$Y(z) = -0.1z^{-1}Y(z) + 0.2z^{-2}Y(z) + 3X(z) + 3.6z^{-1}X(z) + 0.6z^{-2}X(z)$$

$$\Rightarrow Y(z) \left[1 + 0.1z^{-1} - 0.2z^{-2} \right] = 3X(z) + 3.6z^{-1}X(z) + 0.6z^{-2}X(z)$$

$$\Rightarrow H(z) = \frac{Y(z)}{X(z)} = \frac{3 + 3.6z^{-1} + 0.6z^{-2}}{1 + 0.1z^{-1} - 0.2z^{-2}}$$



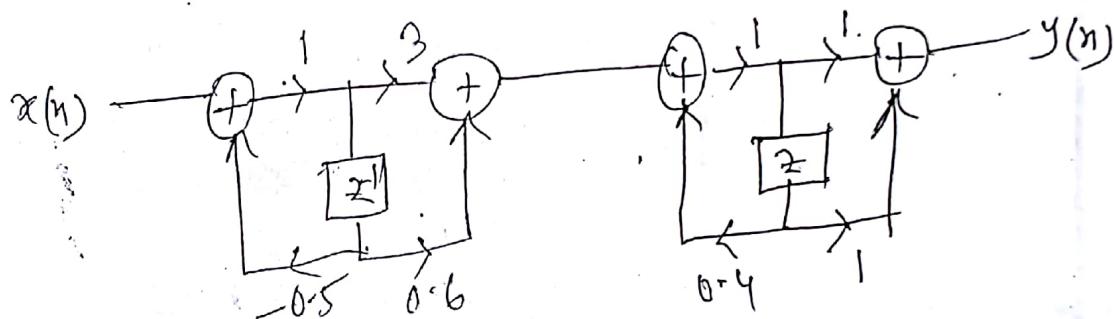
Cascade

$$H(z) = \frac{3 + 3 \cdot 6 z^{-1} + 0.6 z^{-2}}{1 + 0.1 z^{-1} - 0.2 z^{-2}}$$

$$= \frac{(3 + 0.6 z^{-1})(z^{-1} + 1)}{(1 + 0.5 z^{-1})(1 - 0.4 z^{-1})}$$

$$= H_1(z) H_2(z)$$

$$H_1(z) = \frac{3 + 0.6 z^{-1}}{1 + 0.5 z^{-1}}, \quad H_2(z) = \frac{1 + z^{-1}}{1 - 0.4 z^{-1}}$$



Parallel

$$H(z) = \frac{3 + 3 \cdot 6 z^{-1} + 0.6 z^{-2}}{1 + 0.1 z^{-1} - 0.2 z^{-2}}$$

$$= 0.2 z^{-2} + 0.1 z^{-1} + 1 \left[\begin{array}{c} -3 \\ \hline 0.6 z^{-2} + 3 \cdot 6 z^{-1} + 3 \\ \hline 0.6 z^{-2} - 0.3 z^{-1} - 3 \\ \hline 3.9 z^{-1} + 6 \end{array} \right]$$

$$H(z) = -3 + \frac{3.9 z^{-1} + 6}{1 + 0.1 z^{-1} - 0.2 z^{-2}}$$

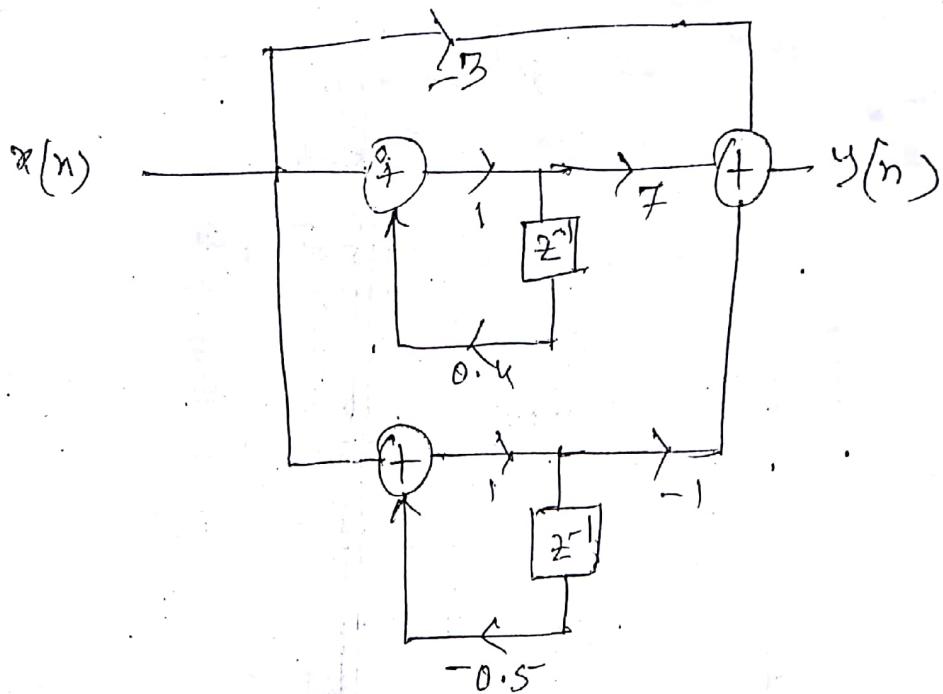
$$= -3 + \frac{A}{1 - 0.4 z^{-1}} + \frac{B}{1 + 0.5 z^{-1}}$$

$$= -3 + \frac{7}{1 - 0.4 z^{-1}} - \frac{1}{1 + 0.5 z^{-1}}$$

↓
C

↓
 $H_1(z)$

↓
 $H_2(z)$



H.W:- Ex - S.21, S.23, S.26, S.25, S.28,
 w3 vvt i)

Filter design - Organizer.

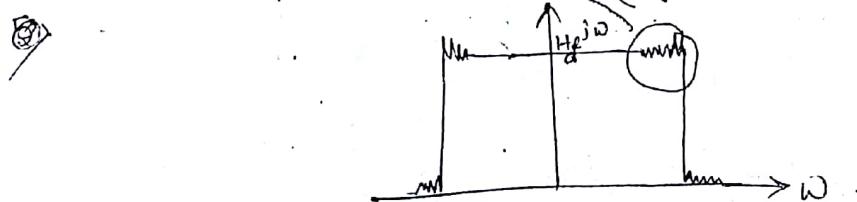
① FIR filter

1) Explain the linear phase of FIR filter. (Pg - 6.2, 6.3)

2) Short note of fourier series designing FIR method
 (Pg - 6.16, 6.17)

3) Window technique / Windowing :- (Pg - 6.29)
 6.31

4) Gibbs phenomenon :- (Pg - 6.29)



5) Rectangular Window :- Pg (6.33)

6) Triangular

② Dsp processors (Pg no - 11.17)