



**MAULANA ABUL KALAM AZAD UNIVERSITY OF  
TECHNOLOGY, WEST BENGAL**

Paper Code : EI-605A

DIGITAL SIGNAL PROCESSING (EC)

Full Marks: 70

*Time Allotted: 3 Hours*

*The figures in the margin indicate full marks.*

*Candidates are required to give their answers in their own words as far as practicable.*

**Group - A**

(Multiple Choice Type Questions)

1×10=10

1. Choose the correct alternatives from *any ten* of the following:

(i) A signal  $x[n]$  is anti symmetric or odd when

- (a)  $x[-n]=x[n] \cdot x[n]$  (b)  $x[n]=-x[n]$   
(c)  $x[n]=[x[n]]^2$  (d)  $x[-n]=-x[n]$

(ii) The region of Convergence of Z-Transform of a unit step function is

- (a)  $|z| > 1$  (b)  $|z| < 1$   
(c) (Real part of Z)>0 (d) (Real part of Z)<0

(iii) A discrete time signal  $x(n) = (-1)^n$  is periodic with fundamental period:

- (a) 4 (b) 6  
(c) 2 (d) 0

(iv) If  $R_1$  is the ROC of  $x(n)$  and  $R_2$  is the ROC of  $y(n)$ , then the ROC of  $x(n)$  convoluted  $y(n)$  is

- (a)  $R_1+R_2$  (b)  $R_1-R_2$   
(c)  $R_1 \cap R_2$  (d)  $R_1 \cup R_2$

(v) The region of Convergence of the Z-Transform of the signal  $2^n u(n) - 3^n u(-n-1)$  is

- (a)  $z > 1$  (b)  $z < 1$   
(c)  $2 < z < 3$  (d) does not exist

**Turn Over**

- (vi) A system described by  $y(n) = nx(n)$ :
- (a) Linear Time varying and stable
  - (c) Non Linear, Time varying and stable
- (vii) The poles of Butterworth low pass filter like on
- (a) an ellipse
  - (c) a parabola
- (viii)  $x(n) = \left(\frac{1}{3}\right)^n u(n)$  is
- (a) Energy signal
  - (c) Both (a) and (b)
- (ix) The value of twiddle factor  $W_8^4$  is given by
- (a) 1
  - (c)  $\frac{1}{\sqrt{2}} - \frac{j}{\sqrt{2}}$
  - (b)  $-j$
  - (d)  $-I$
- (x) The mapping from analog to digital domain in impulse invariant method is
- (a) one to many
  - (c) one to one
  - (b) many to one
  - (d) None of these
- (xi) A signal is a power signal if
- (a)  $E < \infty, P = 0$
  - (c)  $P < \infty, E < \infty$
  - (b)  $P < \infty, E = 0$
  - (d)  $P = \infty, E = 0$
- (xii) Overlap save method is used to find
- (a) Circular Convolution
  - (c) DFT
  - (b) Linear Convolution
  - (d) Z-Transform

### Group - B

#### (Short Answer Type Questions)

Answer *any three* of the following:

2. Define energy signal and power signal. Calculate the power of the signal sequence 5x3=15
- $$x(n) = 2(-1)^n \text{ for } n \geq 0$$
- $$= 0 \quad \text{for } n < 0$$
3. The impulse response of a DTILTI system is  $h(n) = \left(\frac{1}{2}\right)^n u(n)$ . Determine expression for the amplitude response and the phase response of the system. 5

4. A discrete time system is causal if for every choice of  $n_0$  the value of the output sequence  $y(n)$  at  $n=n_0$  depends on only the values of the input sequence  $x(n)$  for  $n \leq n_0$ . From this definition derive the causality condition for a discrete-time LTI system i.e.,  $h(n)=0$  for  $n < 0$ . 5
5. Find the impulse response  $h(n)$  for each of the causal LTI discrete-time systems satisfying the following difference equations and indicate whether each system is an FIR or an IIR system. 5
  - (i)  $y(n) = x(n) - 2x(n-2) + x(n-3)$
  - (ii)  $y(n) + 2y(n-1) = x(n) + x(n-1)$
6. Find the order of Butterworth filter that has a 2dB passband attenuation at a frequency of 20 rad/sec and -10dB stopband attenuation at 30 rad/sec. 5

### Group - C

(Long Answer Type Questions)

Answer any three of the following:

$15 \times 3 = 45$

7. (a) Find out the relation between Fourier transform and Laplace transform with Z-transform.  
 (b) Find the causal signal which is having the Z-transform as  

$$Z(z) \frac{z^2}{(z+1)(z-1)^2}$$
  
 (c) Use one sided Z-transform to find out the solution of difference equation given by  
 $y(n) = \frac{1}{3}y(n-1) + x(n); n > 0$ . Given that,  $y(-1) = 1$  and  $x(n) = (1/3)^n$ .  $5+5+5=15$
8. (a) Obtain a cascade realization of the system characterized by the transfer function  
 $H(z) = 2(z+2)/\{z(z-0.1)(z+0.5)(z+0.4)\}$   
 (b) Determine the direct form-II and transposed direct form-II for the given system  
 $y(n) = 0.5y(n-1) - 0.25y(n-2) + x(n) + x(n-1)$ .
9. (a) Determine the condition for BIBO stability of a causal DTILTI system. Hence prove that an LTI system is BIBO stable if and only if the ROC of the system function includes unit circle.  
 (b) The impulse response of a discrete time system is given by  $h(n) = \{2, -1, 4\}$ . If the input sequence is  $x(n) = \{3, 5, 1, 6\}$ ; find the output sequence  $y(n)$  by using graphical convolution method.
10. (a) Find the 4 point DFT of the sequence  $x(n) = \{1, -2, 3, 4\}$ .  
 (b) Find the circular convolution of the following discrete time sequence:  
 $x_1(n) = \{1, 3, 5, 7\}$  and  $x_2(n) = \{2, 4, 6, 8\}$  using graphical method. Check the result by matrix method of convolution.  $10+5=15$   
 $7+5+3=15$

11. (a) What do you mean by windowing?

(b) What is rectangular window?

(c) Design the symmetric FIR low pass filter using rectangular window for which desired frequency response is expressed as

$$H_d(e^{j\omega}) = \begin{cases} e^{-j\omega\tau}, & \text{for } |\omega| \leq \omega_c \\ 0, & \text{elsewhere.} \end{cases}$$

(d) Determine  $H(z)$  using impulse invariant method at 5Hz sampling frequency from

$$H(s) = \frac{2}{(s+1)(s+2)}.$$

2+2+6+5=15

12. (a) What is meant by order of a filter?

(b) Design a digital Butterworth IIR filter for the given frequency response

$$0.85 \leq |H(e^{j\omega})| \leq 1 \text{ for } 0 \leq \omega \leq 0.2\pi$$

$$|H(e^{j\omega})| \leq 0.2 \text{ for } 0.45\pi \leq \omega \leq \pi$$

Use impulse invariant method.

(c) What are the major factors to be taken into consideration in determining the choice of a specific system realization from amongst many possible representations?

2+10+3=15

**CS/B.TECH/EIE/EVEN/SEM-6/EI-605A/2016-17**



**MAULANA ABUL KALAM AZAD UNIVERSITY OF  
TECHNOLOGY, WEST BENGAL**  
Paper Code : EI-605A

## **DIGITAL SIGNAL PROCESSING**

*Time Allotted : 3 Hours*

*Full Marks : 70*

*The figures in the margin indicate full marks.*

*Candidates are required to give their answers in their own words as far as practicable.*

### **GROUP - A ( Multiple Choice Type Questions )**

1. Choose the correct alternatives for any ten of the following :  $10 \times 1 = 10$
- i) The digital system described by  $y(n) = ax(n) + b$  is a
- a) linear system
  - b) non-linear system
  - c) non-causal system
  - d) dynamic system.

VI-600514

[ Turn over

- ii) The ROC of the Z-transform of a causal sequence is
  - a) the interior of a circle
  - b) the exterior of a circle
  - c) a rectangle
  - d) an annular region.
- iii) For normal DFT calculations number of complex multiplications required is
  - a) N
  - b)  $2N$
  - c)  $2N^2$
  - d)  $N^2$ .
- iv) Poles of a Butterworth filter lie on
  - a) circle
  - b) circle and ellipse
  - c) ellipse
  - d) none of these.
- v) The convolution of  $u(n)$  with  $u(n-4)$  at  $n=5$  is
  - a) 5
  - b) 1
  - c) 2
  - d) 0.
- vi) The sequence of  $x(n) = (-1)^n$  is periodic with a period of
  - a) 6 samples
  - b) 2 samples
  - c) 0 sample
  - d) none of these.
- vii) If a discrete time signal is anti-causal then ROC will include
  - a)  $Z = 0$
  - b)  $Z = \infty$
  - c)  $Z = 0$  and  $Z = \infty$
  - d) none of these.

viii) The Z transform of  $u(-n)$  is

- a)  $\frac{1}{(1-z^{-1})}$
- b)  $\frac{z}{(1-z)}$
- c)  $\frac{1}{(1-z)}$
- d)  $\frac{1}{(z-1)}$

ix)  $y(n) = e^{x(n)}$  is

- a) linear and time invariant system
- b) linear and time variant system
- c) non-linear and time invariant system
- d) non-linear and time variant system.

x) If  $X(z) = Z\{x(n)\}$ , then  $Z\{nx(n)\}$  is equal to

- a)  $X \frac{dX(z)}{dz}$
- b)  $-X \frac{dX(z)}{dz}$
- c)  $X^{-1} \frac{dX(z)}{dz}$
- d)  $-X^{-1} \frac{dX(z)}{dz}$ .

xi) During FFT calculations using DIF algorithm,

- a) outputs are in bit reversal form
- b) inputs are taken in bit reversal form
- c) both input and output are taken in bit reversal form
- d) none of these.

xii) An analog signal is expressed by the equation,  
 $x(t) = 3 \cos 50 \pi t + 10 \sin 300 \pi t - \cos 100 \pi t$ . The Nyquist rate of the signal is

- a) 150 Hz
- b) 300 Hz
- c) 25 Hz
- d) 50 Hz.

**GROUP - B**

**( Short Answer Type Questions )**

Answer any *three* of the following.

$$3 \times 5 = 15$$

2. Find the circular convolution of two sequences  $x(n) = \{1, 1, 2, 2\}$  and  $y(n) = \{1, 2, 3, 4, 5\}$ .
3. Consider a system described by the difference equation,  $y(n) = y(n-1) - y(n-2) + 0.5x(n) + 0.5x(n-1)$ . Find the response of this system to the input  $x(n) = 0.5^n u(n)$  with initial conditions  $y(-1) = 0.75$  and  $y(-2) = 0.25$ .
4. Define energy and power of a signal. Find out the energy of the sequence  $x(n) = \{2, 1, 3, -1, 2, 0, 1, -1\}$ .
5. Sketch the magnitude response of a Butterworth filter and derive an expression of order of such a filter?
6. Consider an LTI system with frequency response

$$H(e^{j\omega}) = e^{-j\left(\omega - \frac{\pi}{4}\right)} \left( \frac{1 + e^{-j2\omega} + 4e^{-j4\omega}}{1 + \frac{1}{2}e^{-j2\omega}} \right)$$

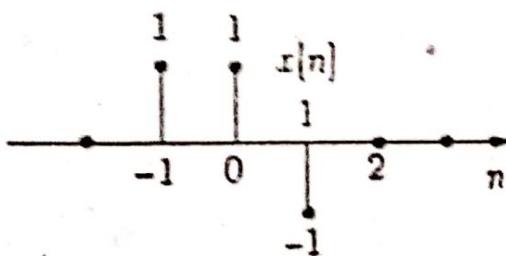
Determine the output  $y(n)$  for all  $n$  if the input is  $x(n) = \cos(\pi n/2)$  for all  $n$ .

7. Prove that the energy of a real valued energy signal is equal to the sum of the energy of its even and odd components.

**GROUP - C**  
**( Long Answer Type Questions )**

Answer any three of the following.  $3 \times 15 = 45$

8. a) Describe how tabulation method can be used to find out the convolution sum.
- b) A DTLTI system with impulse response  $h(n) = \{1, 1, 1\}$  is excited by a sequence,  $x(n) = \{\overset{4}{\underset{1}{\uparrow}}, 3, 2, 1\}$ . Determine the output  $y(n)$  of the system using the tabulation method.
- c) The signal  $x[n]$  shown in the figure below is convolved with itself to get  $y[n]$ . Find out  $y[-1]$ .



$5 + 6 + 4$

9. a) Define ROC. What are the properties of ROC ?
- b) State and prove initial value theorem regarding Z-transform ?
- c) For a causal LTI system, the output  $y(n)$  is related to input  $x(n)$  by the difference equation  $y(n) = \frac{1}{4}y(n-1) + x(n)$ . Calculate  $y(n)$  while  $x(n) = \delta(n-1)$ . ( Hint : use Z transform )

$(2+3)+5+5$

[ Turn over

10. a) Find the DTFT of the sequence,

$$x(n) = \{ \underset{\uparrow}{1}, -1, 1, -1 \}.$$

b) Find the IDTFT of  $X(e^{j\omega}) = e^{-j\omega} \left( \frac{1}{2} + \frac{1}{2} \cos \omega \right)$ .

c) Point out the difference between DTFT and DFT.

d) What is the difference between linear convolution  
and circular convolution ? 4 + 4 + 3½ + 3½

11. a) Draw the following :

i) Direct Form II

ii) Cascade structures for the system described  
by the difference equation :

$$y(n) = \frac{3}{4} y(n-1) - \frac{1}{8} y(n-2) + x(n) + \frac{1}{3} x(n-1)$$

b) Design a digital Butterworth filter to satisfy the  
following constraints :

$$0.8 \leq |H(e^{j\omega})| \leq 1, 0 \leq \omega \leq \frac{\pi}{2}$$

$$|H(e^{j\omega})| \leq 0.1, \frac{3\pi}{4} \leq \omega \leq \pi$$

Use bilinear transformation. Consider a sampling  
period of 1 second. (4 + 4) + 7

12. a) Find the DFT of a sequence  $x(n) = \{ \underset{\uparrow}{1}, 1, 0, 0 \}$  and  
find the IDFT of  $Y(k) = \{ 1, 0, 1, 0 \}$ .

- b) Determine the output response  $y(n)$  if  
 $h(n) = \{1, 1, 1, 1\}$ ;  $x(n) = \{1, 2, 3, 1\}$  by using  
circular convolution (graphical method).
- c) Compute the  $N$ -point DFT of (i)  $x(n) = \delta(n)$ ,  
(ii)  $x(n) = \delta(n - n_0)$ .
- d) Describe decimation in frequency FFT algorithm for  
8 pt. DFT.  $(2\frac{1}{2} + 2\frac{1}{2}) + 4 + 2 + 4$

13. Write short notes on any three of the following :  $3 \times 5$

- a) Radix-2 decimation in frequency algorithm
  - b) Nyquist sampling theorem
  - c) IIR and FIR filters
  - d) Utility of FFT over DFT
  - e) Chebyshev filter
  - f) BIBO stability in  $Z$  domin
  - g) Difference between DTFT and DFT
  - h) Mapping of  $s$ -plane to  $z$ -plane.
-



**MAULANA ABUL KALAM AZAD UNIVERSITY OF  
TECHNOLOGY, WEST BENGAL**  
Paper Code : EI-605A  
**DIGITAL SIGNAL PROCESSING**

Time Allotted : 3 Hours

Full Marks : 70

The figures in the margin indicate full marks.

Candidates are required to give their answers in their own words as far as practicable.

**GROUP - A**

**( Multiple Choice Type Questions )**

Choose the correct alternatives for any ten of the following :

$$10 \times 1 = 10$$

- i) If  $x_1(n)$  and  $x_2(n)$  are finite length sequences of sizes  $L$  and  $M$  respectively, their linear convolution

has the length

- a)  $L + M - 2$
- b)  $L + M - 1$
- c)  $L + M$
- d)  $\text{Max}(L, M)$ .

[ Turn over ]

- ii) In the context of sampling with sampling interval  $T$ , the mapping between  $S$  and  $Z$  plane is
- a)  $Z = \exp(ST)$
  - b)  $S = ZT$
  - c)  $S = \exp(ZT)$
  - d)  $Z = ST$ .
- iii) The inverse  $Z$  transform of  $\frac{Z}{Z-1}$  is
- a)  $u(n)$  as well as  $u(-n)$
  - b)  $u(-n)$  but not  $u(n)$
  - c)  $u(n)$  as well as  $u(-n-1)$
  - d)  $u(n)$  but not  $u(-n-1)$ .
- iv) In FFT, for calculating  $N$ -point DFT total number of complex addition required is
- a)  $N^2$
  - b)  $(N-1) \log_2 N$
  - c)  $\frac{N}{2} \log_2 2N$
  - d)  $N \log_2 N$ .
- v) For a stable system, the impulse response  $h(nT)$
- a) is defined for  $n \geq 0$
  - b) contains impulses
  - c) decays to zero
  - d) is infinite in length.
- vi) A control system has a  $Z$  transform ROC
- a) within a circle
  - b) outside a circle
  - c) on a circle
  - d) through the plane.

- vii) Chebyshev type I filter
- a) is all pole filter
  - b) is all zero filter
  - c) contains both poles and zeros
  - d) contains either poles and zeros.
- viii) FIR filter is of
- a) non-recursive and non-linear type
  - b) non-recursive and linear type
  - c) recursive and non-linear type
  - d) recursive and linear type.
- ix) If Fourier transform of  $x(n)$  is  $X[\omega]$ , the Fourier transform of  $n \times (n)$  is
- a)  $-j \frac{dX[\omega]}{d\omega}$
  - b)  $\frac{dX[\omega]}{d\omega}$
  - c)  $j \frac{dX[\omega]}{d\omega}$
  - d) none of these.
- x) Zero padding is a signal, if it
- a) reduces aliasing
  - b) increases time resolution
  - c) increases frequency resolution
  - d) has no effect.

[ Turn over

- xi) The system having input  $x(n)$  related to output  $y(n) = \log_{10} |x(n)|$  is
- non-linear, causal, BIBO stable
  - linear, non-causal, BIBO stable
  - linear, non-causal, BIBO unstable
  - non-linear, causal, BIBO unstable.
- xii) Impulse invariant method of digital filter design can be used to design
- low-pass filter
  - high-pass filter
  - any type of filter
  - FIR filter.

### GROUP - B

#### ( Short Answer Type Questions )

Answer any *three* of the following.  $3 \times 5 = 15$

2. Determine whether or not  $x(n)$  is periodic.  
If periodic, determine its fundamental period :
- $$x(n) = \cos \frac{\pi}{3} n + \cos \frac{3\pi}{4} n.$$
3. What are the different methods available to find out inverse  $Z$  transform of a sequence ?

Determine the inverse  $Z$  transform of causal signal given

$$\text{by } X(Z) = \frac{1}{(1 - 2z^{-1})(1 - z^{-1})^2}.$$

Find the DFT of  $x(n) = \{1, 1, 2, 2\}$ .

Find out the impulse response of the system described by given differential equation using Z transform.

$$y(n) - 0.7y(n-1) + 0.12y(n-2) = x(n-1) + x(n-2)$$

For the function  $x_1(n)$  and  $x_2(n)$  compute

$$y(n) = x_1(n) * x_2(n) \text{ using graphical method :}$$

$$x_1(n) = \delta(n) + \delta(n-1) - \delta(n-2) - \delta(n-3)$$

$$x_2(n) = \delta(n) - \delta(n-2) + \delta(n-4).$$

### GROUP - C

#### ( Long Answer Type Questions )

Answer any three of the following.  $3 \times 15 = 45$

- a) Prove that an LTI system is BIBO stable if and only if the ROC of the system function includes the unit circle.

- b) Determine the inverse Z transforms of

$$X(z) = \log(1 - 0.5z^{-1}), |z| > 0.5$$

- c) Compute the circular convolution of the following two sequences using concentric circle method :

$$x(n) = \{1, 2, 3, -1, 2\}, h(n) = \{2, 2, 1\}$$

$\uparrow$

$3 + 6 + 6$

[ Turn over

8. a) Find out the 8-point DFT of the following sequence

$$x(n) = \{1, 1, 1, 1, 0, 0, 0, 0\}$$

↑

- b) What do you mean by zero padding ?

- c) Find the output  $y(n)$  of a filter whose impulse response is  $h(n) = \{1, 1, 1\}$  and the input signal

$$x(n) = \{3, -1, 0, 1, 3, 2, 0, 1, 2, 1\}$$

↑

using (i) Overlap-save method, (ii) Overlap-add method.

6 + 2 + 7

9. a) What is the difference between IIR and FIR filter ?

- b) Explain Gibbs phenomenon in digital filter design.  
How can it be eliminated ?

- c) Design a Butterworth filter the bilinear transformation for the specifications :

$$0.8 \leq |H(e^{j\omega})| \leq 1, \quad 0 \leq \omega \leq 0.2\pi$$

$$\leq |H(e^{j\omega})| \leq 0.2, \quad 0.6\pi \leq \omega \leq \pi$$

3 + 4 + 8

10. a) Explain the bit reversal technique.

- b) Find the DFT of a sequence

$$x(n) = \{1, 2, 3, 4, 4, 3, 2, 1\}$$

↑

using DIT-FFT Algorithm.

2 + 10 + 3

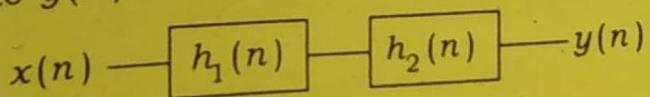
- c) Write down the properties of ROC.

1. a) Determine whether the signal is energy or power signal :  $x(n) = r(n) - r(n-4)$ .

- b) An interconnection of LTI systems is shown below.  
The impulse responses are

$$h_1(n) = \left(\frac{1}{2}\right)^n [u(n) - \delta(n)] \text{ and } h_2(n) = u(n-2).$$

Let the impulse response of the overall system from  $x(n)$  to  $y(n)$  be denoted as  $h(n)$ . Evaluate  $h(n)$ .



- c) Obtain the cascade form realization for the system given by the difference equation

$$y(n) = -0.1y(n-1) + 0.2y(n-2) + 3x(n) \\ + 3.6x(n-1) + 0.6x(n-2).$$

4 + 6 + 5

2. Write short notes on any three of the following : 3 x 5

- a) Mapping of S-plane and Z-plane
- b) Circular Convolution
- c) Warping effect & Prewarping
- d) Radix-2 DIT algorithm
- e) Discrete LTI system
- f) DSP TMS320C 5416 processor.



**CS/B.Tech/Even/EIE/6th Sem/EI-605A/2014**

**2014**

## **Digital Signal Processing**

**Time Alloted : 3 Hours**

**Full Marks : 70**

**The figure in the margin indicate full marks.  
Candidates are required to give their answers in their  
own words as far as practicable**

### **GROUP - A**

#### **( Multiple Choice Type Questions )**

**1. Choose the correct alternatives for any ten of the following:**

**$10 \times 1 = 10$**

**i) If the length of two sequences is given by M and N respectively then the total length of the convoluted sum-**

- a)  $L-M+1$**
- b)  $L+M-1$**
- c)  $L+M+1$**
- d)  $L-M-1$**

**ii) During mapping of many points from s-plane to Z-plane aliasing occurs when the**

- a) Sample of two sinusoidal signals of frequencies which differ by a multiple of the sampling frequency
  - b) Sample of two sinusoidal signals of frequencies which differ by an even multiple of the sampling frequency
  - c) Sample of two sinusoidal signals of frequencies which differ by an odd multiple of the sampling frequency
  - d) None of the above
- iii) For normal DFT calculations number of complex multiplication required
- a) N
  - b) 2N
  - c)  $2N^2$
  - d)  $N^2$
- iv) If the input and output sequence is M and N respectively then the total number of memory location required in direct form-II structure is-
- a)  $\text{MIN}\{M,N\}$
  - b)  $M+N-1$
  - c)  $M+N$
  - d)  $\text{MAX }\{M,N\}$
- v) The Z-transform of  $u(-n)$  is

- a)  $1/(1-Z^{-1})$   
b)  $Z/(1-Z)$   
c)  $1/(1-Z)$   
d)  $1/(Z-1)$
- vi) The inverse Z transform of  $\frac{1}{1-Z^{-1}}$   
a)  $u(n)$  as well as  $u(-n)$   
b)  $u(-n)$  but not  $u(n)$   
c)  $u(n)$  as well as  $u(-n-1)$   
d)  $u(n)$  but not  $u(-n-1)$
- vii) If  $X(z) = Z\{x(n)\}$ , then  $Z\{nx(n)\}$  is equal to  
a)  $z \frac{d}{dz} X(z)$   
b)  $-z \frac{d}{dz} X(z)$   
c)  $z^{-1} \frac{d}{dz} X(z)$   
d)  $-z^{-1} \frac{d}{dz} X(z)$
- viii) DFT  $[x(N-m)]$  is equal to  
a)  $X(N-m)$   
b)  $X(N-k)$   
c)  $X(m-k)$   
d)  $X(m+k)$

- ix) To design a digital filter using Bilinear Transformation we have to substitute

a)  $s = \frac{2z-1}{Tz+1}$

b)  $s = 2T \frac{z-1}{z+1}$

c)  $s = \frac{2z+1}{Tz-1}$

d)  $s = \frac{1-z}{Tz+1}$

- x) During fft calculations using DIF algorithm-

- a) Outputs are in bit reversal form
- b) Inputs are taken in bit reversal form
- c) Both input and outputs are taken in bit reversal form
- d) None of this

- xi) The system having input  $x(n)$  related to output

$$y(n) = \log_{10} |x(n)|$$

- a) non linear, causal, BIBO stable.
- b) linear, non causal, BIBO stable.
- c) linear, non causal, BIBO unstable.
- d) non linear, causal, BIBO unstable.

**GROUP - B**

( Short Answer Type Questions )

Answer any three of the following       $3 \times 5 = 15$

System response is given by:  $y(n) = \sum_{k=0}^n a(k)x(n-k) + \sum_{k=1}^n b(k)y(n-k)$ ,  
check whether the system is LTI or not.

5

Write down some advantages and limitations of DSP.

4+1

Find the inverse Z-Transform of  $X(z) = \frac{z(z^2 - 3z + 4)}{(z-4)(z-2)(z-1)}$

ROC  $2 < |z| < 4$ .

4

Using the bilinear transformation find out the order of a high Butterworth filter having passband with cutoff frequency of 1000 Hz and stopband with cutoff frequency of 500 Hz. The sampling frequency is 5 KHz.

5

Determine the direct form II structure for the given system.

$y(n) = 0.3y(n-1) - 0.5y(n-2) + 0.75y(n-3) + 0.25x(n-1) + 0.55x(n)$ .

5

[ Turn over ]

## GROUP - C

### ( Long Answer Type Questions )

Answer any *three* of the following.

*3x15=*

7. a) Prove that an LTI system is BIBO stable if and only if the R of the system function includes the unit circle.

- b) Find the z-transform and ROC of the signal for  $a > b$  &  $a < b$

$$x(n) = a^n u(n) + b^n u(-n-1)$$

- d) Using the residue method find inverse z transform

$$\frac{1 - 1/(4z)}{1 - 1/(9z)} \text{ ROC: } |Z| > 1/3$$

*2+7*

8. a) Find out the 8-point DFT of the following sequence

$$x(n) = \{1, 1, 1, 1, 1, 1, 0, 0\}$$

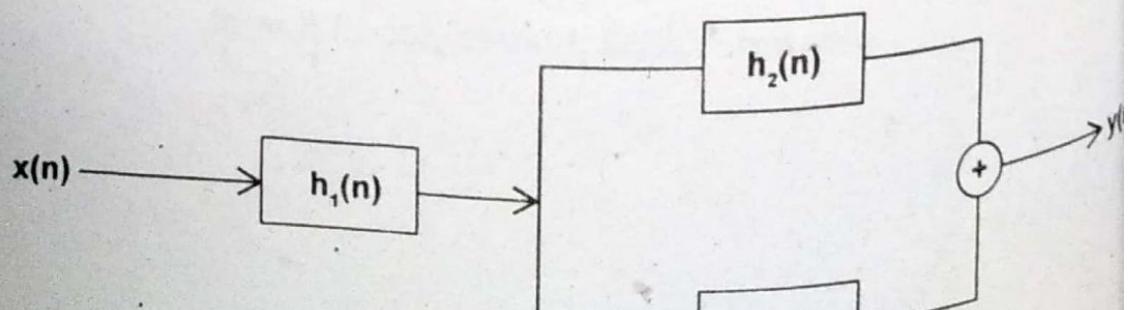
- b) What is twiddle factor?

- c) Compute the N-point DFT for the function  $\delta(n)$ .

- d) Find the output  $y(n)$  of a filter whose impulse response  $h(n) = \{1, 1, 1\}$  and the input signal  $x(n) = \{3, -1, 0, 1, 3, 2, 0, 1, 2, 1\}$  using Overlap-add method.

*5+2+2*

9. a) An interconnection of LTI systems is shown below. The impulse responses are  $h_1(n) = (1/2)^n [u(n) - u(n-4)]$ ;  $h_2(n) = \delta(n)$  and  $h_3(n) = u(n-2)$ . Let the impulse response of the overall system from  $x(n)$  to  $y(n)$  be denoted as  $h(n)$ . Evaluate  $h(n)$ .



# MODEL QUESTION PAPER

CS/B.Tech/Even/EIE/6th Sem/EI-605A/2014

Design a Butterworth filter the bilinear transformation for the specifications

$$0.8 \leq |H(e^{j\omega})| \leq 1, \quad 0 \leq \omega \leq 0.2\pi$$

$$\leq |H(e^{j\omega})| \leq 0.2, \quad 0.6\pi \leq \omega \leq \pi$$

Determine whether or not  $x(n)$  is periodic. If periodic, determine fundamental period:

$$x(n) = \cos \frac{\pi}{3}n + \cos \frac{3\pi}{4}n$$

Find the DFT of a sequence  $x(n) = \{1, 2, 3, 4, 4, 3, 2, 1\}$  using DIT algorithm.

5+10

Write short notes on any three:-

3x5=15

- a) Distinguish FIR and IIR filter.
- b) Circular Convolution.
- c) Warping effect & Prewarping.
- d) Window technique in digital filter design
- e) LTI System.