




< Previous				 ✓	 ✓		 ✓		Next >
------------	---	---	---	---	---	---	---	---	--------

SVD Exercises

 Bookmark this page

Homework due Nov 13, 2023 10:13 CST Completed

For the following questions use the data loaded with:

```
library(tissuesGeneExpression)
data(tissuesGeneExpression)
```

Important note: When using the SVD in practice it is important to note that the solution to SVD is not unique. This is because $\mathbf{UDV}^T = (-\mathbf{U})\mathbf{D}(-\mathbf{V})^T$. In fact we can flip the sign of each column of \mathbf{U} and as long as we also flip the respective column in \mathbf{V} the decomposition works. Here is R code demonstrating this:

```
s = svd(e)
signflips = sample(c(-1,1),ncol(e),replace=TRUE)
signflips
```

Now we switch the sign of each column and check that we get the same answer. We do this using the function `sweep()`. If x is a matrix and a is a vector, then `sweep(x,1,y,FUN="*")` applies the function `FUN` to each row i `FUN(x[i,],a[i])`, in this case `x[i,]*a[i]`. If instead of 1 we use 2, `sweep()` applies this to columns. To learn about `sweep()`, read `?sweep`.

```
newu= sweep(s$u,2,signflips,FUN="*")
newv= sweep(s$v,2,signflips,FUN="*")
all.equal( s$u %*% diag(s$d) %*% t(s$v), newu %*% diag(s$d) %*% t(newv))
```

This is important to know because different implementations of the SVD algorithm may give different signs, which can lead to the same code resulting in different answers when run in different computer systems.

SVD Exercises #1

1/1 point (graded)

Compute the SVD of `e`:

```
s = svd(e)
```

Now compute the mean of each row:

```
m = rowMeans(e)
```

What is the correlation between the first column of \mathbf{U} and `m`?



Submit

Try again (1 attempt remaining)

SVD Exercises #2

1/1 point (graded)

In the above question, we saw how the first column relates to the mean of the rows of `e`. Note that if we change these means, the distances between columns do not change. Here is some R code showing how changing the means does not change the distances:

```
newmeans = rnorm(nrow(e)) ##random values we will add to create new means
newe = e+newmeans ##we change the means
sqrt(crossprod(e[,3]-e[,45]))
sqrt(crossprod(newe[,3]-newe[,45]))
```

So we might as well make the mean of each row 0 since it does not help us approximate the column distances. We will define `y` as the *detrended* `e` and recompute the SVD:

```
y = e - rowMeans(e)
s = svd(y)
```

We showed that \mathbf{UDV}^T is equal to `y` up to numerical error:

```
resid = y - s$u %%% diag(s$d) %%% t(s$v)
max(abs(resid))
```

The above can be made more efficient in two ways. First, using the `crossprod()` and second not creating a diagonal matrix. Note that in R we can multiply a matrix `x` by vector `a`. The result is a matrix with row `i` equal to `x[i,]*a[i]`. Here is an example to illustrate this.

```
x=matrix(rep(c(1,2),each=5),5,2)
x
x*c(1:5)
```

Note that the above code is actually equivalent to:

```
sweep(x,1,1:5,"*")
```

This means that we don't have to convert `s$d` into a matrix to obtain \mathbf{DV}^T .

Which of the following gives us the same as `diag(s$d)%%t(s$v)` ?

☐ `s$d %%% t(s$v)[,1]`

☒ `s$d * t(s$v)`

☐ `s$d * t(s$v)[,1]`

☐

$L(s_d + s_v)$

☐

$s_v * s_d$

☒

Submit

You have used 2 of 2 attempts

SVD Exercises #3

0/1 point (graded)

If we define $\mathbf{vd} = \mathbf{t}(\mathbf{s} \mathbf{d} * \mathbf{t}(\mathbf{s} \mathbf{v}))$, then which of the following is not the same as $\mathbf{U} \mathbf{D} \mathbf{V}^\top$:

☐ `tcrossprod(s$u,vd)`

☐ `s$u %*% s$d * t(s$v)`

☒ `s$u %*% (s$d * t(s$v))`

☐ `s$u %*% t(vd)`

✖

You have used 2 of 2 attempts

SVD Exercises #4

1/1 point (graded)

Let $\mathbf{z} = \mathbf{s} \mathbf{d} * \mathbf{t}(\mathbf{s} \mathbf{v})$. We showed a derivation demonstrating that because \mathbf{U} is orthogonal, the distance between $\mathbf{e}_{[,3]}$ and $\mathbf{e}_{[,45]}$ is the same as the distance between $\mathbf{y}_{[,3]}$ and $\mathbf{y}_{[,45]}$, which is the same as $\mathbf{z}_{[,3]}$ and $\mathbf{z}_{[,45]}$:

```
z = s$d * t(s$v)
sqrt(crossprod(e[,3]-e[,45]))
sqrt(crossprod(y[,3]-y[,45]))
sqrt(crossprod(z[,3]-z[,45]))
```

Note that the columns `z` have 189 entries, compared to 22,215 for `e`.

What is the difference (in absolute value) between the actual distance

`sqrt(crossprod(e[,3]-e[,45]))` and the approximation using only two dimensions of `z` ?

40.62416

✓

40.62416

Submit

Try again (4 attempts remaining)

SVD Exercises #5

1/1 point (graded)
What is the minimum number of dimensions we need to use for the approximation in SVD Exercises #4 to be within 10% or less?

7



7

Submit

Try again (4 attempts remaining) ⓘ

SVD Exercises #6

1/1 point (graded)
Compute distances between sample 3 and all other samples:

distances = sqrt(apply(e[, -3]-e[, 3], 2, crossprod))

Recompute this distance using the 2 dimensional approximation.
What is the Spearman correlation between this approximate distance and the actual distance?

0.8598592



0.8598592

Submit

Try again (4 attempts remaining) ⓘ



edX

- About
- Affiliates
- edX for Business
- Open edX
- Careers
- News

Legal

- Terms of Service & Honor Code
- Privacy Policy
- Accessibility Policy

[Trademark Policy](#)

[Sitemap](#)

[Cookie Policy](#)

[Your Privacy Choices](#)

Connect

[Idea Hub](#)

[Contact Us](#)

[Help Center](#)

[Security](#)

[Media Kit](#)



© 2023 edX LLC. All rights reserved.
深圳市恒宇博科技有限公司 [粤ICP备17044299号-2](#)