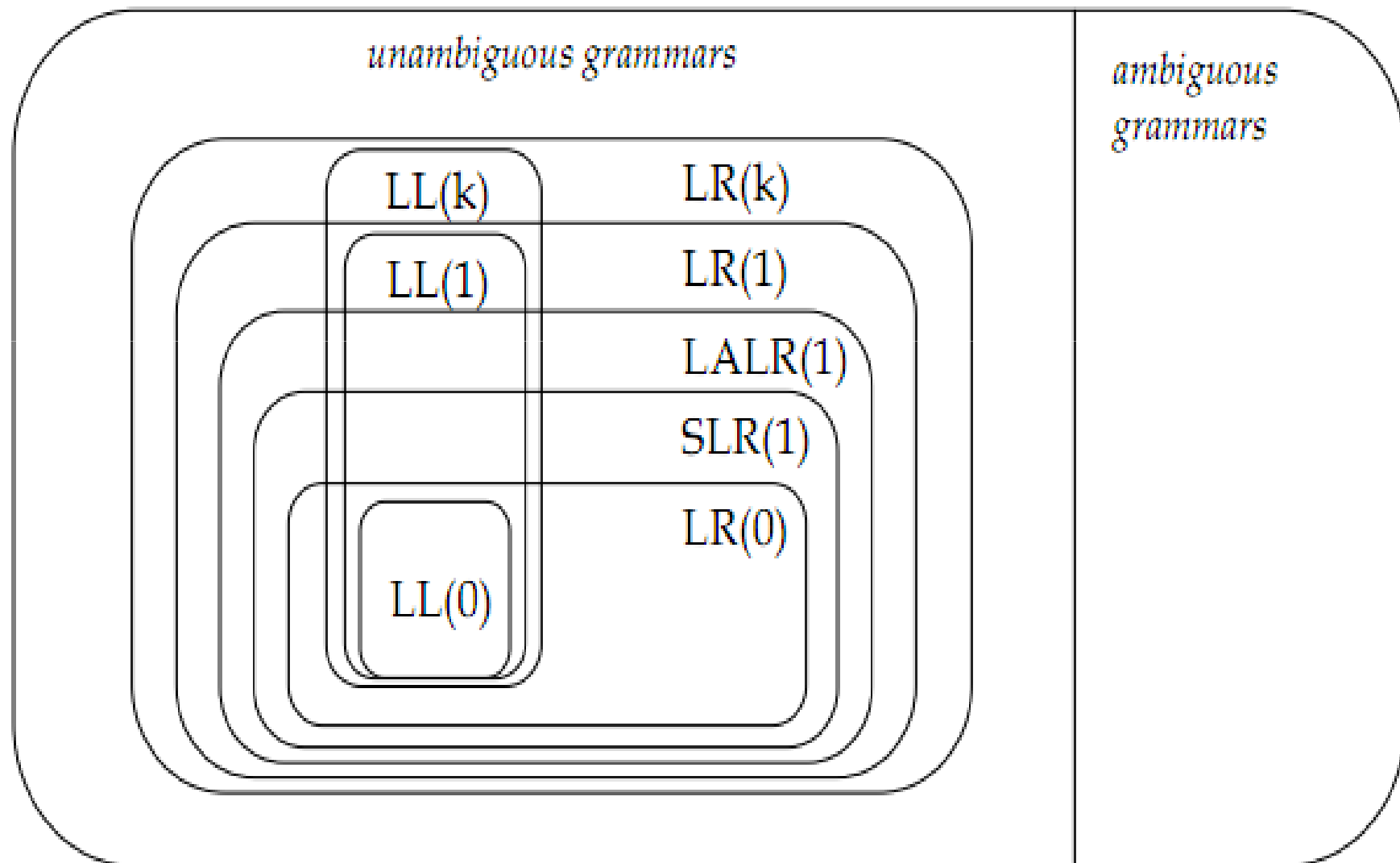


Lecture 10

Syntax Analysis V

Bottom-Up Parsing

Hierarchy of Grammar Class



Viable Prefixes

- α is a viable prefix of a given grammar if:
 - There is a w such that αw is a right sentential form
- $\alpha \mid \omega$ is a state of the shift-reduce parser
- As long as the parser has viable prefixes on the stack no parser error has been seen
- The set of viable prefixes is a regular language (not obvious)
- Construct an automaton that accepts viable prefixes

LR(0) Items

- An LR(0) item of a grammar G is a production of G with a special symbol “.” at some position of the right side
- Thus production $AXYZ$ gives four LR(0) items
$$A \rightarrow .XYZ$$
$$A \rightarrow X.YZ$$
$$A \rightarrow XY.Z$$
$$A \rightarrow XYZ.$$
- An item indicates how much of a production has been seen at a point in the process of parsing
 - Symbols on the left of “.” are already on the stack s
 - Symbols on the right of “.” are expected in the input
- The only item for $X \rightarrow \epsilon$ is $X \rightarrow .$

Viable Prefixes and LR(0) Items

- Consider the input: **(int)**

$$E \rightarrow T + E \mid T$$

$$T \rightarrow int * T \mid int \mid (E)$$

- Then **(E |)** is a state of a shift-reduce parse
- (E** is a prefix of the rhs of **T → (E)**
 - Will be reduced after the next shift
- Item **T → (E.)** says that so far we have seen **(E** of this production and hope to see **)**

Viable Prefixes and LR(0) Items

- The stack may have many prefixes of rhs's
 - $\text{Prefix}_1 \text{Prefix}_2 \dots \text{Prefix}_{n-1} \text{Prefix}_n$
- Let Prefix_i be a prefix of the rhs of $X_i \rightarrow \alpha_i$
 - Prefix_i will eventually reduce to X_i
 - The missing part of α_{i-1} starts with X_i
 - i.e. there is a $X_{i-1} \rightarrow \text{Prefix}_{i-1} X_i \beta$ for some β
- Recursively, $\text{Prefix}_{k+1} \dots \text{Prefix}_n$ eventually reduces to the missing part of α_k

Viable Prefixes and LR(0) Items

- Consider the string $(\text{int} * \text{int})$:
 - $(\text{int} * | \text{int})$ is a state of a shift-reduce parse
 - “(” is a prefix of the rhs of $T \rightarrow (E)$
 - “ε” is a prefix of the rhs of $E \rightarrow T$
 - “int *” is a prefix of the rhs of $T \rightarrow \text{int} * T$
- The “stack of items”
 - $T \rightarrow (.E)$ says, we have seen “(” of $T \rightarrow (E)$
 - $E \rightarrow .T$ says, we have seen of $E \rightarrow T$
 - $T \rightarrow \text{int} * .T$ says, we have seen $\text{int} *$ of $T \rightarrow \text{int} * T$

Recognizing Viable Prefixes

- Therefore, we have to build the finite automata that recognizes this sequence of partial rhs's of productions
- Algorithm:
 1. Add a dummy production $S' \rightarrow S$ to G
 2. The NFA states are the items of G
 - Including the extra production
 3. For item $E \rightarrow \alpha.X\beta$ add transition
 - $E \rightarrow \alpha.X\beta \xrightarrow{X} E \rightarrow \alpha.X.\beta$
 4. For item $E \rightarrow \alpha.X\beta$ and production $X \rightarrow \gamma$ add
 - $E \rightarrow \alpha.X\beta \xrightarrow{\epsilon} X \rightarrow .\gamma$
 5. Every state is an accepting state
 6. Start state is $S' \rightarrow .S$

Recognizing Viable Prefixes

- Given the grammar:

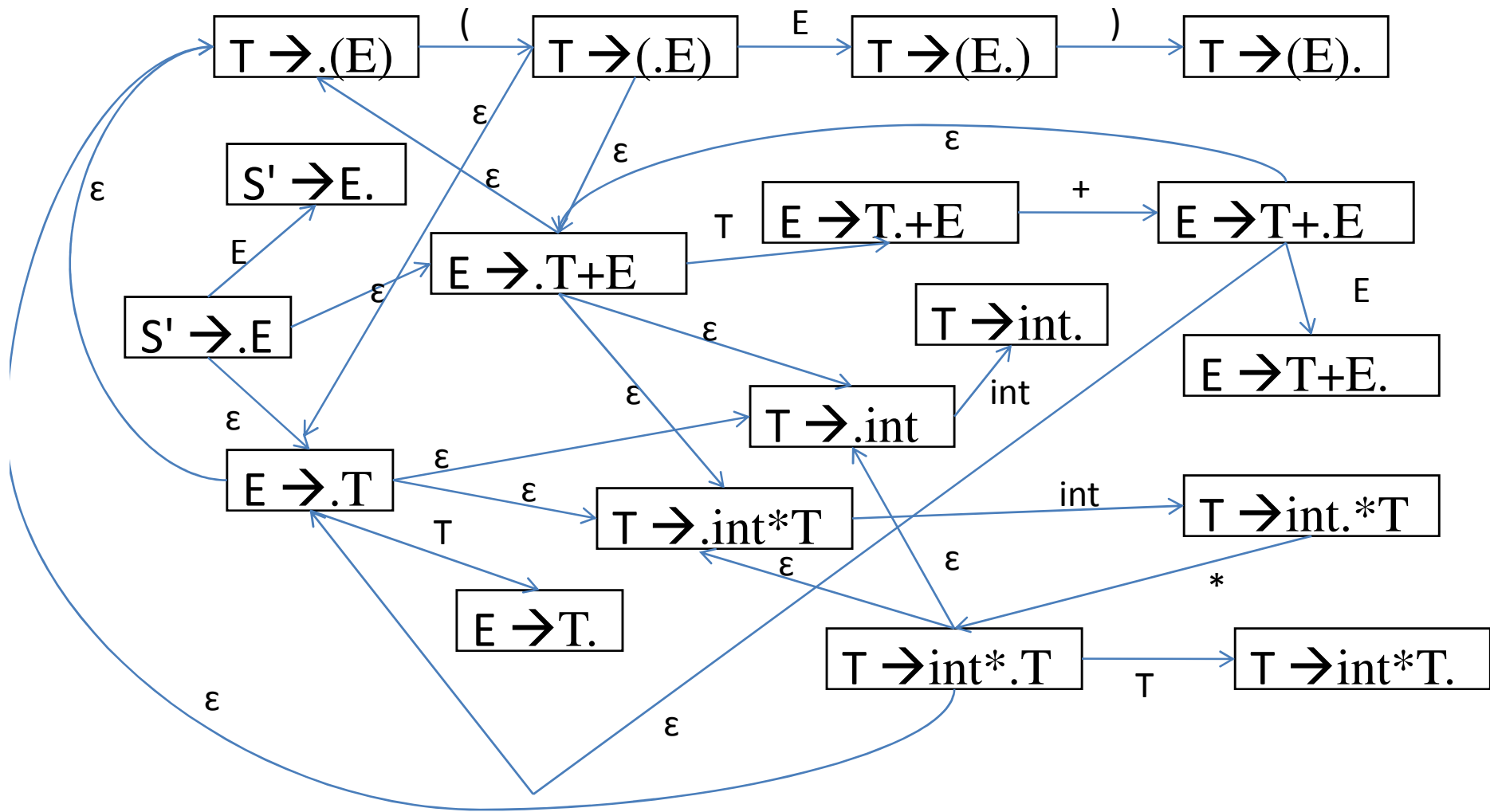
$$S' \rightarrow E$$

$$E \rightarrow T + E \mid T$$

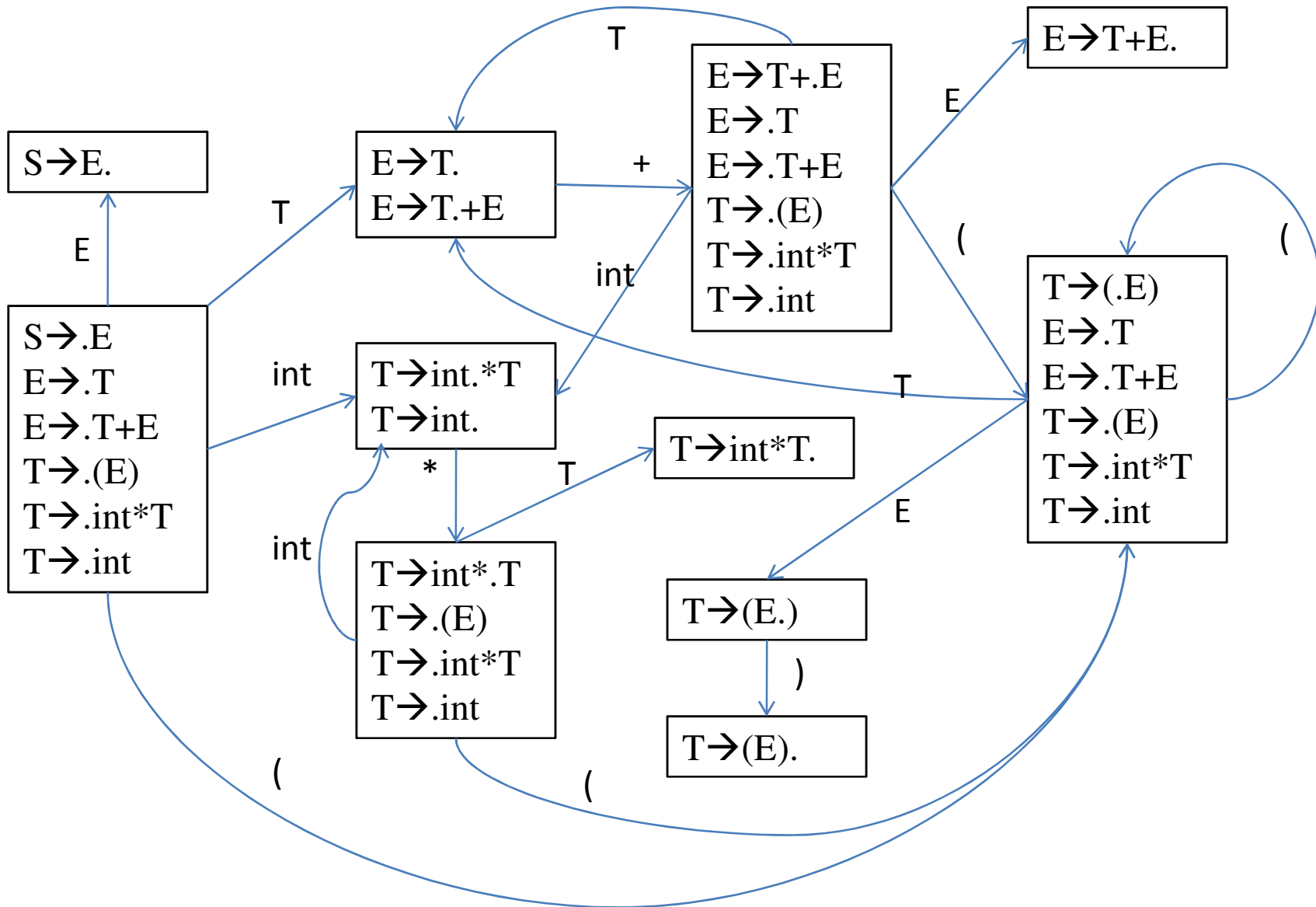
$$T \rightarrow \text{int} * T \mid \text{int} \mid (E)$$

Create an NFA to recognize viable prefixes

Recognizing Viable Prefix



NFA to DFA – Subset Construction



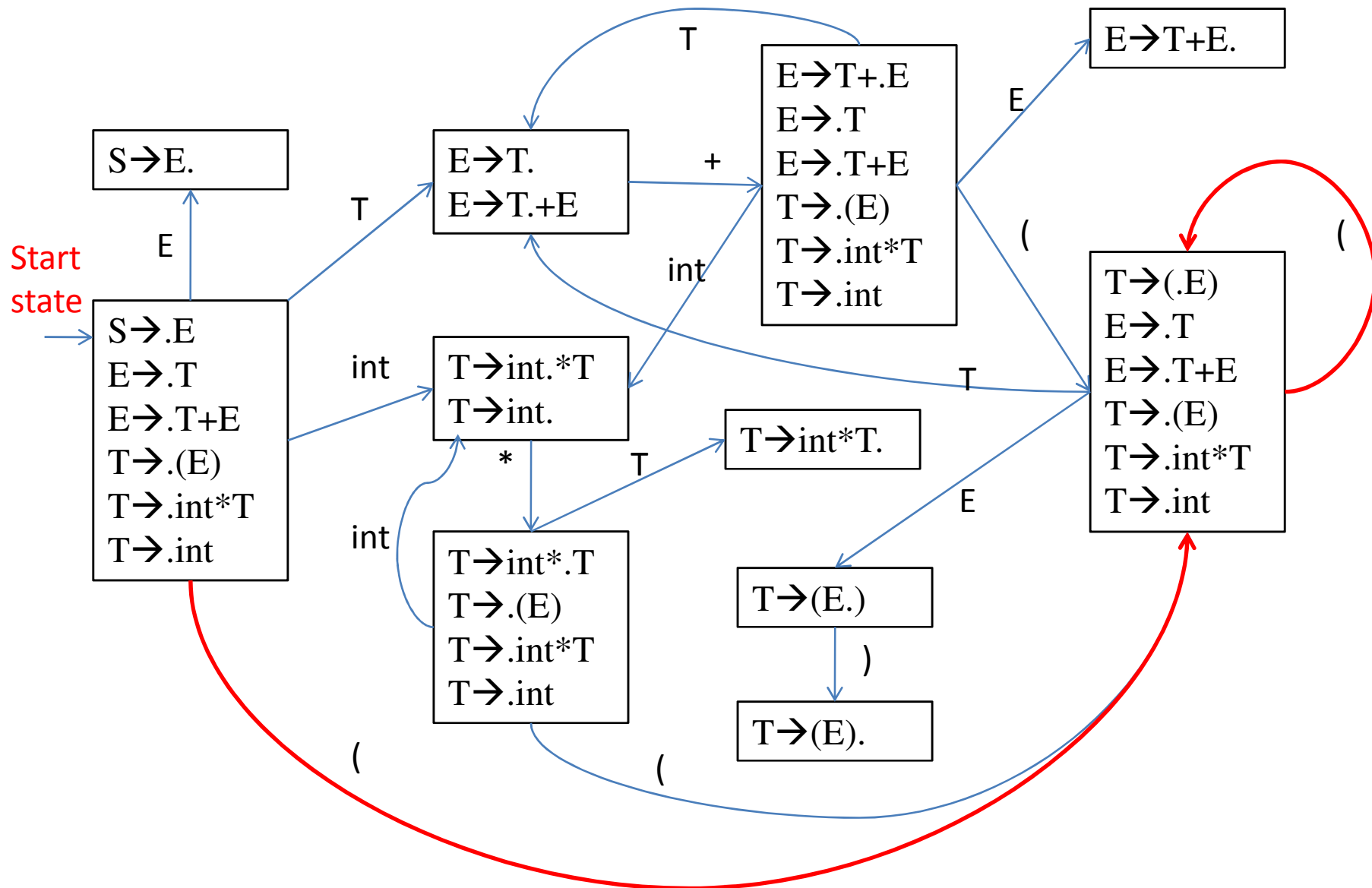
Valid Items

- The states of the DFA are:
 - canonical collections of LR(0) items
- Item $X \rightarrow \beta.\gamma$ is *valid for a viable prefix $\alpha\beta$* if
 - $S' \xrightarrow{*} \alpha X \omega \rightarrow \alpha\beta\gamma\omega$ by a right-most derivation
- After parsing $\alpha\beta$, the valid items are the possible tops of the stack of items
- An item I is valid for a viable prefix α if the DFA recognizing viable prefixes terminates on input α in a state S containing I

Valid Items

- The items in **S** describe what the top of the **item stack** might be after reading input α
- An item is often valid for many prefixes
 - Example: The item **T \rightarrow (.E)** is valid for prefixes
 - (, ((, (((, ((((, ...

NFA to DFA – Subset Construction



LR(0) Parsing

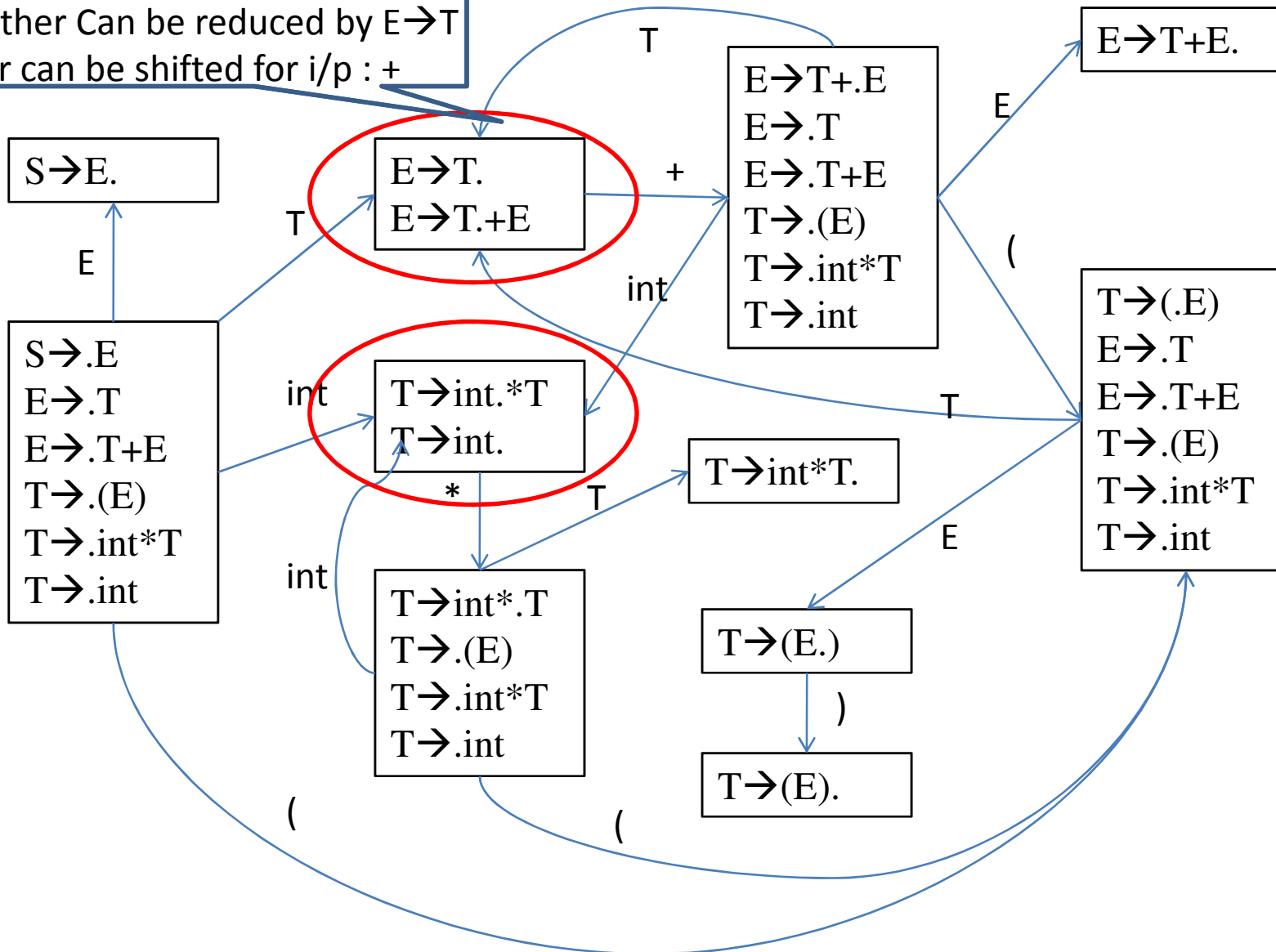
- Assume
 - stack contains α
 - next input token is t
 - DFA on input α terminates in state s
- Reduce by $X \rightarrow \beta$ if
 - s contains item $X \rightarrow \beta$.
- Shift if
 - s contains item $X \rightarrow \beta.t\omega$
 - Equivalent to saying s has a transition labeled t

LR(0) Parsing - Conflicts

- LR(0) has a reduce/reduce conflict if:
 - Any state has two reduce items:
– $X \rightarrow \beta.$ and $Y \rightarrow \omega.$
- LR(0) has a shift/reduce conflict if:
 - Any state has a reduce item and a shift item:
– $X \rightarrow \beta.$ and $Y \rightarrow \omega.t\delta$
- SLR improves on LR(0) shift/reduce heuristics
 - Fewer states have conflicts

Shift Reduce Conflicts

Shift-Reduce conflicts
 Either Can be reduced by $E \rightarrow T$
 Or can be shifted for i/p : +



Countermeasure

- SLR = Simple LR
- Improve on LR(0) shift/reduce heuristics
 - Fewer states have conflicts

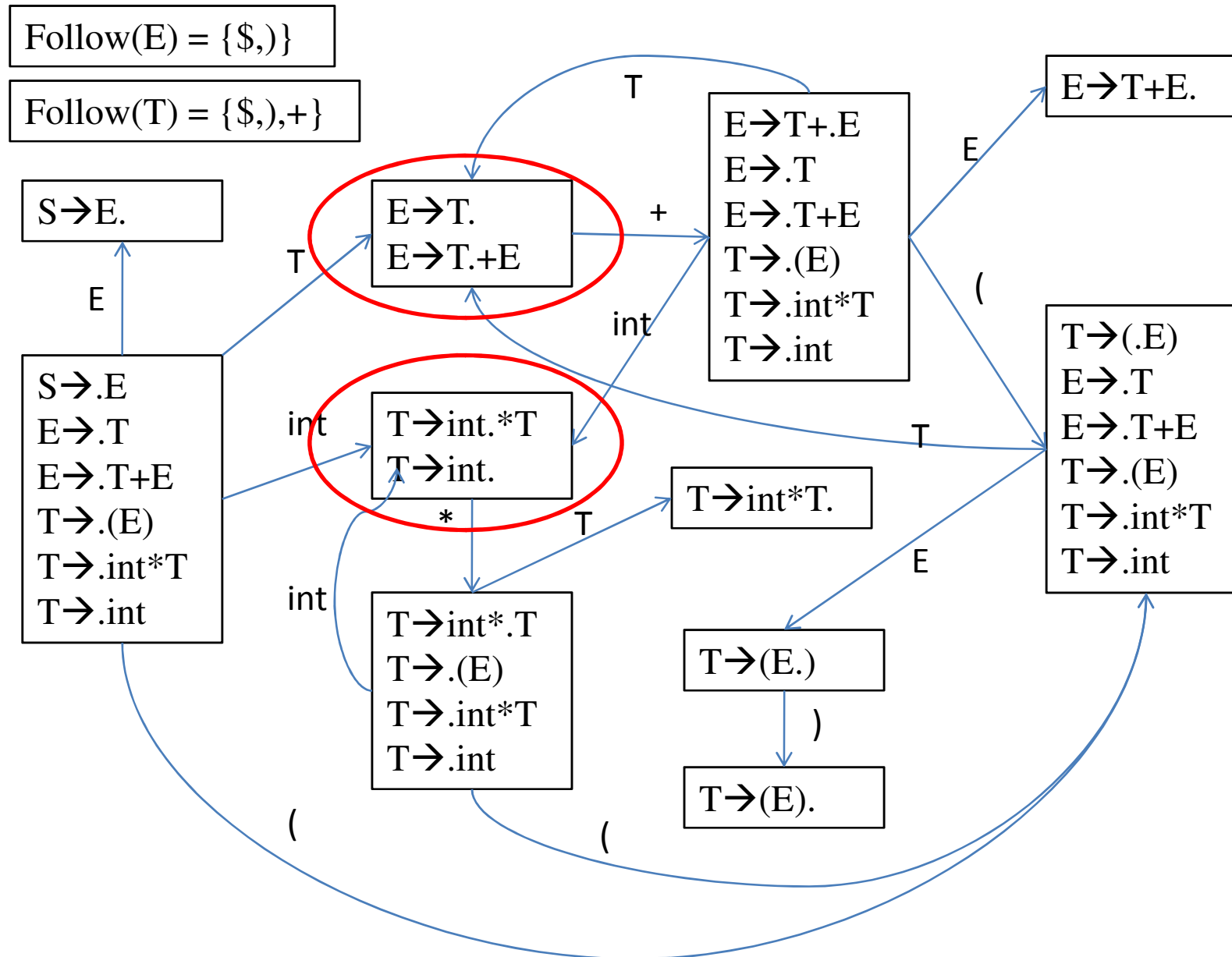
SLR Parsing

- Assume
 - stack contains α
 - next input token is t
 - DFA on input α terminates in state s
- Reduce by $X \rightarrow \beta$ if
 - s contains item $X \rightarrow \beta$.
 - $t \in \text{Follow}(X)$
- Shift if
 - s contains item $X \rightarrow \beta.t\omega$
 - Equivalent to saying s has a transition labeled t

SLR Parsing

- If there are conflicts under these rules, the grammar is not SLR
- The rules amount to a heuristic for detecting handle
 - The SLR grammars are those where the heuristics detect exactly the handle

Shift Reduce Conflicts



SLR Parsing Algorithm

1. Let M be DFA for viable prefixes of G
2. Let $|x_1 \dots x_n \$$ be initial configuration
3. Repeat until configuration is $S| \$$
 1. Let $\alpha|w$ be current configuration
 2. Run M on current stack α
 3. If M rejects α , report parsing error
 1. Stack α is not a viable prefix
 4. If M accepts α with items I , let u be next input
 1. Shift if $X \rightarrow \beta.u\gamma \in I$
 2. Reduce if $X \rightarrow \beta. \in I$ and $u \in \text{Follow}(X)$
 3. Report parsing error if neither applies

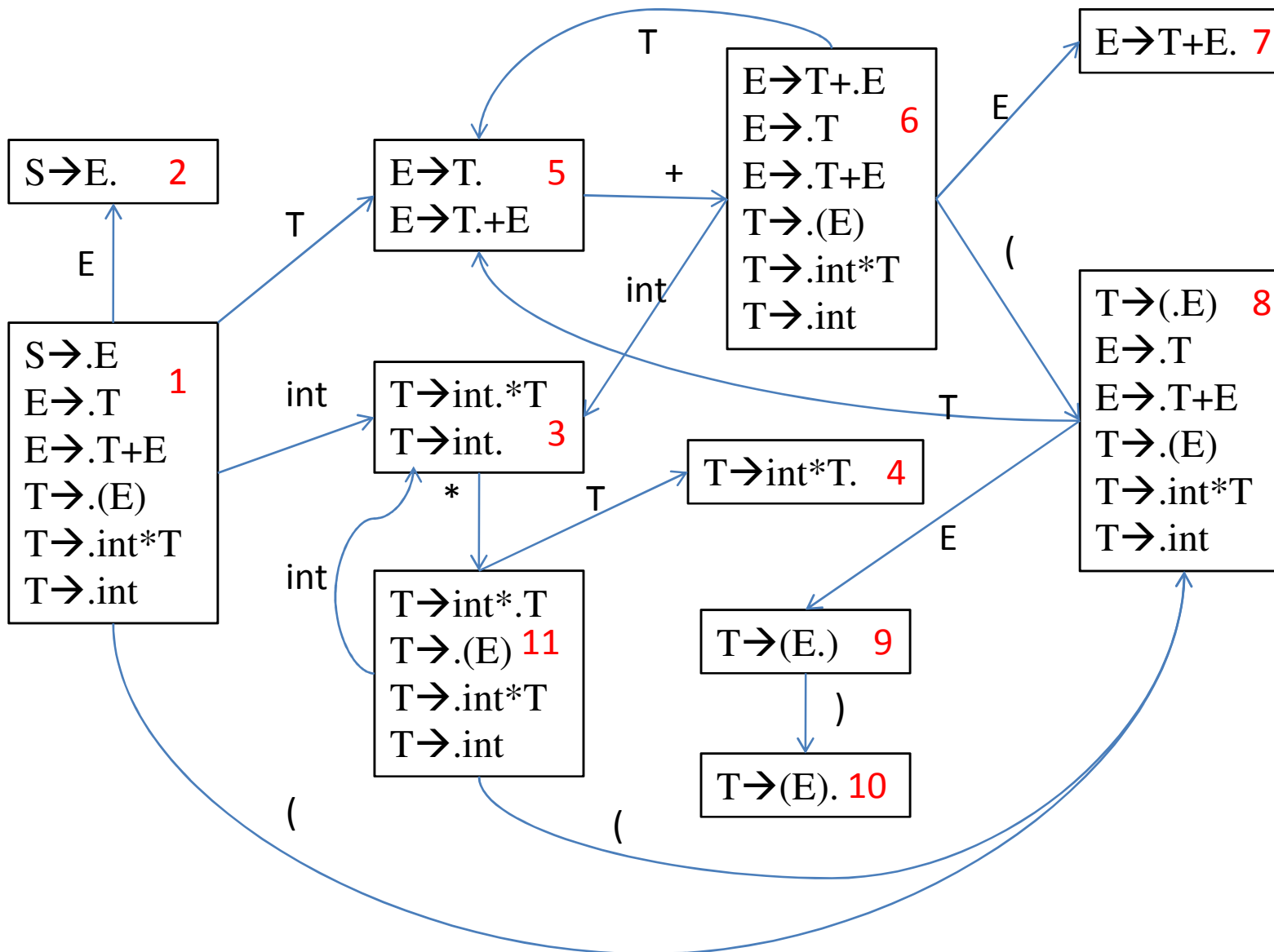
SLR Parsing - Improvements

- Note that Step 3.3 is redundant
- If there is a conflict in the last step, grammar is not SLR(k)
- Lots of grammars are not SLR
 - Including all ambiguous grammars
- We can parse more grammars by using precedence declarations
 - Instructions for resolving conflicts

SLR Parsing

- Consider the ambiguous grammar:
 - $E \rightarrow E + E \mid E * E \mid (E) \mid \text{int}$
- The DFA for this grammar contains a state with the following items:
 - $E \rightarrow E * E.$ and $E \rightarrow E. + E$
 - There is a shift/reduce conflict
- Declaring “ $*$ has higher precedence than $+$ ” resolves this conflict in favor of reducing

SLR Parsing Example



SLR Parsing Example

- Parse the token stream: **int * int\$**

<i>Configuration</i>	<i>DFA Halt State</i>	<i>Action</i>
lint * int\$	1	Shift
int * int\$	3 * \notin Follow(T)	Shift
int * int\$	11	Shift
int * int \$	3 \$ \in Follow(T)	Reduce. $T \rightarrow \text{int}$
int * T \$	4 \$ \in Follow(T)	Reduce. $T \rightarrow \text{int} * T$
T \$	5 \$ \in Follow(T)	Reduce. $E \rightarrow T$
E \$	Accept	

