# Polkadot Runtime Environment Protocol Specification

March 18, 2019

### 1 Conventions and Definitions

**Definition 1.** Runtime is the state transition function of the decentralized ledger protocol.

**Definition 2.** A path graph or a path of n nodes formally referred to as  $P_n$ , is a tree with two nodes of vertex degree 1 and the other n-2 nodes of vertex degree 2. Therefore,  $P_n$  can be represented by sequences of  $(v_1, ..., v_n)$  where  $e_i = (v_i, v_{i+1})$  for  $1 \le i \le n-1$  is the edge which connect  $v_i$  and  $v_{i+1}$ .

**Definition 3.** radix r tree is a variant of a trie in which:

- Every node has at most r children where  $r = 2^x$  for some x;
- Each node that is the only child of a parent, which does not represent a valid key is merged with its parent.

As a result, in a radix tree, any path whose interior vertices all have only one child and does not represent a valid key in the data set, is compressed into a single edge. This improves space efficiency when the key space is sparse.

**Definition 4.** By a sequences of bytes or a byte array, b, of length n, we refer to

$$b := (b_0, b_1, ..., b_{n-1})$$
 such that  $0 \le b_i \le 255$ 

We define  $\mathbb{B}_n$  to be the **set of all byte arrays of length n**. Furthermore, we define:

$$\mathbb{B} := \bigcup_{i=0}^{\infty} \, \mathbb{B}_i$$

**Notation 5.** We represent the concatenation of byte arrays  $a := (a_0, ..., a_n)$  and  $b := (b_0, ..., b_m)$  by:

$$a || b := (a_0, ..., a_n, b_0, ..., b_m)$$

**Definition 6.** For a given byte b the bitwise representation of b is defined as

$$b := b^7 \dots b^0$$

where

$$b = 2^0 b^0 + 2^1 b^1 + \dots + 2^7 b^7$$

**Definition 7.** By the little-endian representation of a non-negative integer, I, represented as

$$I = (B_n ... B_0)_{256}$$

in base 256, we refer to a byte array  $B = (b_0, b_1, ..., b_n)$  such that

$$b_i := B_i$$

Accordingly, define the function EncLE:

Enc<sub>LE</sub>: 
$$\mathbb{Z}^+$$
  $\rightarrow \mathbb{B}$   $(B_n...B_0)_{256} \mapsto (B_0,B_1,...,B_n)$ 

**Definition 8.** By **UINT32** we refer to a non-negative integer stored in a byte array of length 4 using little-endian encoding format.

**Definition 9.** A blockchain C is a directed path graph. Each node of the graph is called **Block** and indicated by B. The unique sink of C is called **Genesis Block**, and the source is called the **Head** of C. For any vertex  $(B_1, B_2)$  where  $B_1 \rightarrow B_2$  we say  $B_2$  is the **parent** of  $B_1$  and we indicate it by

$$B_2 := P(B_1)$$

### 2 Block

In Polkadot RE, a block is made of two main parts, namely the *block header* and the *list of extrinsics*. The Extrinsics represent the generalization of the concept of transaction, containing any set of data that is external to the system, and which the underlying chain wishes to validate and keep track of.

### 2.1 Block Header

The block header is designed to be minimalistic in order to boost the efficiency of the light clients. It is defined formally as follows:

**Definition 10.** The header of block B, Head(B) is a 5-tuple containing the following elements:

- parent\_hash: is the 32-byte Blake2s hash of the header of the parent of the block indicated henceforth by  $H_p$ .
- number: formally indicated as  $H_i$  is an integer, which represents the index of the current block in the chain. It is equal to the number of the ancestor blocks. The genesis block has number 0.
- $state\_root$ : formally indicated as  $H_r$  is the root of the Merkle trie, whose leaves implement the storage for the system.
- extrinsics\_root: is the field which is reserved for the runtime to validate the integrity of the extrinsics composing the block body. For example, it can hold the root hash of the Merkle trie which stores an ordered list of the extrinsics being validated in this block. This element is formally referred to as H<sub>e</sub>.
- **digest:** this field is used to store any chain-specific auxiliary data, which could help the light clients interact with the block without the need of accessing the full storage. Polkadot RE does not impose any limitation or specification for this field. Essentially, it can be a byte array of any length. This field is indicated as  $H_d$ .

**Definition 11.** The Block Header Hash of Block B,  $H_h(b)$ , is the hash of the header of block B encoded by simple codec:

$$H_b(b) := \text{Blake2} s(\text{Enc}_{SC}(\text{Head}(B)))$$

#### 2.2 Justified Block Header

The Justified Block Header is provided by the consensus engine and presented to the Polkadot RE, for the block to be appended to the blockchain. It contains the following parts:

- block header the complete block header as defined in Section 2.1 and denoted by Head(B).
- **justification**: as defined by the consensus specification indicated by Just(B) [link this to its definition from consensus].
- **authority Ids**: This is the list of the Ids of authorities, which have voted for the block to be stored and is formally referred to as A(B). An authority Id is 32bit.

### 2.3 Extrinsics

Each block contains as well a list of extrinsics. Polkadot RE does not specify or limit the internal of each extrinsics beside the fact that each extrinsics is a byte array encoded using SCALE codec [36].

The extrinsics root is set by the runtime, and its value is opaque to Polkadot RE.

The extrinsics in a block are ordered using pairing each extrinsics by a UINT32 integer sequential number starting at 0 which is encoded using SCALE codec.

### 3 Interactions with the Runtime

Runtime is the code implementing the logic of the chain. This code is decoupled from the Polkadot RE to make the Runtime easily upgradable without the need to upgrade the Polkadot RE itself. In this section, we describe the details upon which the Polkadot RE is interacting with the Runtime.

### 3.1 Loading the Runtime code

Polkadot RE expects to receive the code for the runtime of the chain as a compiled WebAssembly (Wasm) Blob. The current runtime is stored in the state database under the key represented as a byte array:

$$b := 3A.63.6F.64.65$$

which is the byte array of ASCII representation of string ":code" (see Section 9). For any call to the runtime, Polkadot RE makes sure that it has the most updated Runtime as calls to runtime have potentially the ability to change the runtime code.

The initial runtime code of the chain is embedded as an extrinsics into the chain initialization JSON file and is submitted to Polkadot RE (see Section 8).

Subsequent calls to the runtime have the ability to call the storage API (see Section A) to insert a new Wasm blob into runtime storage slot to upgrade the runtime.

### 3.2 Code Executor

Polkadot RE provides a Wasm Virtual Machine (VM) to run the Runtime. The Wasm VM exposes the Polkadot RE API to the Runtime, which, on its turn, executes a call to the Runtime entries stored in the Wasm module. This part of the Runtime environment is referred to as the *Executor*.

In this section, we specify the general setup for an Executor call into the Runtime. In Section 3.3 we specify the parameters and the return values of each Runtime entry separately.

### 3.2.1 ABI Encoding between Runtime and the Runtime Environment

All data exchanged between Polkadot RE and the Runtime is encoded using SCALE codec described in Section 7.1.

#### 3.2.2 Access to Runtime API

When Polkadot RE calls a Runtime entry it should make sure Runtime has access to the all Polkadot Runtime API functions described in Appendix A. This can be done for example by loading another Wasm module alongside the runtime which imports these functions from Polkadot RE as host functions.

#### 3.2.3 Sending Arguments to Runtime

In each invocation of a Runtime entry, the arguments which are supposed to be sent to the entry need to be encoded using SCALE codec into a byte array B. The Executor then needs to retrieve the memory buffer of the Runtime Wasm module and extend it to fit the size of the byte array. Then it needs to copy the byte array value in the correct offset of the extended buffer. Finally, when the Wasm method corresponding to the entry is called, two UINT32 integers are sent to the method as arguments. The first one is the offset of the byte array B in the extended shared memory buffer, and the second one is the size of B.

### 3.2.4 The Return Value from a Runtime Entry

The value which is returned from the invocation represents two consecutive UINT32 integers in which the first one indicates the pointer to the offset of the result returned by the entry encoded in SCALE codec in the memory buffer. The second one provides the size of the blob.

#### 3.3 Entries into Runtime

Polkadot RE assumes that at least the following functions are implemented in the Runtime Wasm blob and has been exported as shown in Snippet 1:

```
(export "version" (func $version))
(export "authorities" (func $authorities))
(export "execute_block" (func $execute_block))
(export "validate_transaction" (func $validate_transaction))
(export "initialise_block" (func $initialise_block))
```

Snippet 1. Snippet to export entries into the Wasm runtime module

The following sections describe the standard based on which Polkadot RE communicates with each runtime entry.

#### 3.3.1 version

This entry receives no argument; it returns the version data encoded in ABI format described in Section 3.2.1 containing the following data:

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Name	Type	Description
spec_name	String	runtime identifier
impl_name	String	the name of the implementation (e.g. C++)
authoring_version	UINT32	the version of the authorship interface
spec_version	UINT32	the version of the runtime specification
impl_version	UINT32	the version of the runtime implementation
apis	ApisVec	List of supported AP

Table 1. Detail of the version data type returns from runtime version function

#### 3.3.2 authorities

This entry is to report the set of authorities at a given block. It receives block\_id as an argument; it returns an array of authority\_id's.

### 3.3.3 execute block

This entry is responsible for executing all extrinsics in the block and reporting back the changes into the state storage. It receives the block header and the block body as its arguments, and it returns a triplet:

Name	Type	Description
results	Boolean	Indicating if the execution was su
storage_changes	[???]	Contains all changes to the state storage
change_updat	[???]	

Table 2. Detail of the data execute block returns after execution

### 3.3.4 validate transaction

[Explain function]

### 4 Network Interactions

### 4.1 Extrinsics Submission

Extrinsic submission is made by sending an extrinsic network message. The structure of this message is specified in Definition 12.

Upon receiving an extrinsics message, Polkadot RE decodes the transaction and calls validate\_trasaction runtime function defined in Section 3.3.4, to check the validity of the extrinsic. If validate\_transaction considers the submitted extrinsics as a valid one, Polkadot RE makes the extrinsics available for the consensus engine for inclusion in future blocks.

### 4.2 Network Messages

Definition 12. Extrinsic submission network message: [Extrinsic submission network message definition]

#### 4.3 Block Submission and Validation

Block validation is the process, by which the client asserts that a block is fit to be added to the blockchain. This means that the block is consistent with the world state and transitions from the state of the system to a new valid state.

Blocks can be handed to the Polkadot RE both from the network stack and from the consensus engine. Both the Runtime and the Polkadot RE need to work together to assure block validity. This can be accomplished by Polkadot RE invoking execute\_block entry into the runtime as a part of the validation process. Polkadot RE implements the following procedure to assure the validity of the block:

```
Algorithm 1. IMPORT-AND-VALIDATE-BLOCK(B, \operatorname{Just}(B))

1: VERIFY-BLOCK-JUSTIFICATION(B, \operatorname{Just}(B))

2: if B is Finalized and P(B) is not Finalized

3: Mark-as-Final(P(B))

4: Verify H_{p(B)} \in \operatorname{Blockchain}

5: State-Changes = Runtime(B)

6: UPDATE-WORLD-STATE(State-Changes)
```

For the definition of the finality and the finalized block see Section 6.3.

# 5 State Storage and the Storage Trie

For storing the state of the system, Polkadot RE implements a hash table storage where the keys are used to access each data entry state. There is no limitation either on the size of the key nor the size of the data stored under them, besides the fact that they are byte arrays.

### 5.1 Accessing The System Storage

Polkadot RE implements various functions to facilitate access to the system storage for the runtime. Section A lists all of those functions. Here we define the essential ones which are also used by the Polkadot RE.

**Definition 13.** The StateRead and StateWrite functions provide basic access to the State Storage:

v = StateRead(k)StateWrite(k, v)

where v and k are byte arrays.

To authenticate the state of the system, the stored data needs to be re-arranged and hashed in a *modified Merkle Patricia Tree*, which hereafter we refer to as the *Trie*, in order to compute the hash of the whole state storage consistently and efficiently at any given time.

As well, a modification has been made in the storing of the nodes' hash in the Merkle Tree structure to save space on entries storing small entries.

Because the Trie is used to compute the *state root*,  $H_r$ , (see Definition 10), which is used to authenticate the validity of the state database, Polkadot RE follows a rigorous encoding algorithm to compute the values stored in the trie nodes to ensure that the computed Merkle hash,  $H_r$ , matches across clients.

### 5.2 The General Tree Structure

Each key value identifies a unique node in the tree. However, a node in a tree might or might not be associated with a key in the storage. Similar to a radix trie, when traversing the Trie subsequences of the key is stored in nodes on the path to the node associated with the key.

To identify the node corresponding to a key value, k, first we need to encode k in a uniform way. Because each node in the trie has at most 16 children, we represents the key as a sequences of 4-bit nibbles:

**Definition 14.** For the purpose of labeling the branches of the Trie, the key k is encoded to  $k_{\rm enc}$  using KeyEncode functions:

$$k_{\text{enc}} := (k_{\text{enc}_1}, \dots, k_{\text{enc}_{2n}}) := \text{KeyEncode}(k)$$

$$\tag{1}$$

such that:

$$\text{KeyEncode}(k) : \begin{cases} \mathbb{B} & \to \text{ Nibbles}_4 \\ k := (b_1, ..., b_n) := & \mapsto & (b_1^1, b_1^2, b_2^1, b_2^1, ..., b_n^1, b_n^2) \\ & := (k_{\text{enc}_1}, ..., k_{\text{enc}_{2n}}) \end{cases}$$

where Nibble<sub>4</sub> is the set of all nibbles of 4-bit arrays and  $b_i^1$  and  $b_i^2$  are 4-bit nibbles, which are the little endian representations of  $b_i$ :

$$(b_i^1, b_i^2) := (b_i \mod 16, b_i / 16)$$

, where mod is the remainder and  $\ /$  is the integer division operators.

By looking at  $k_{\text{enc}}$  as a sequence of nibbles, one can walk the radix tree to reach the node identifying the storage value of k.

### 5.3 Different node types

In this subsection we specifies the structure of the nodes in the Trie:

Notation 15. We refer to the set of the nodes of Polkadot state trie by  $\mathcal{N}$ .

The Trie consists of 2 types of nodes base:

- Leaf: It is a childless stores the remaining subsequence of KeyEncode(k) not accounted for in the path to the node, as well as the value associated to that key.
- **Branch:** It has at least 1 and up to 16 children. It stores the partial key shared by its children. It accounts for one nibble of the key corresponding to to the path passing through each of its children by the position it stores the child. It optionally stores a value of the key corresponding to the path traversed to the node.

Accordingly, we define:

**Definition 16.** We define **NodeType** function to be

NodeType : 
$$\mathcal{N} \to \{\text{Leaf}, \text{Branch}\}\$$
  
 $N \mapsto \text{The type of node } N$ 

**Definition 17.** The **the partial key** of node N of length  $j \leq 380$  to be

$$pk_N := (k_{\text{enc}_i}, ..., k_{\text{enc}_{i+j}})$$

a subsequence of a key k

$$KeyEncode(k) = (k_{enc_1}, ..., k_{enc_{i-1}}, k_{enc_i}, ..., k_{enc_{2n}})$$

corresponding to key-value paired (k, v) in the State storage such that  $pk_N$  is stored in N.

Consequently, for an extension node  $i \ge 2$  and for a branch node i = 0.

### 5.4 The Merkle proof

To prove the consistency of the state storage across the network and its modifications efficiently, the Merkle hash of the storage trie needs to be computed rigorously.

The Merkle hash of the trie is computed recursively. As such, the hash value of each node depends on the hash value of all its children and also on its value. Therefore, it suffices to define how to compute the hash value of a typical node as a function of the hash value of its children and its own value.

**Definition 18.** For a trie node N, Node Prefix function is a value specifying the node type as follows:

$$\operatorname{NodePrefix}(N) := \left\{ \begin{array}{ll} 1 & N \text{ is a leaf node} \\ 128 & N \text{ is a branch node without value} \\ 129 & N \text{ is a branch node with value} \end{array} \right.$$

**Definition 19.** For a given node N, with partial key of  $pk_N$  and Value v, the **encoded representation** of N, formally referred to as  $Enc_{Node}(N)$  is determined as follows, in case which:

• N is a leaf node:

$$\operatorname{Enc}_{\operatorname{Node}}(N) := \operatorname{Enc}_{\operatorname{len}}(N) || \operatorname{Enc}_{\operatorname{HE}}(\operatorname{pk}_N) || \operatorname{Enc}_{\operatorname{SC}}(v)$$

• N is a branch node:

$$Enc_{Node}(N) :=$$
  
 $Enc_{len}(N) || Enc_{HE}(pk_N) || Enc_{LE}(ChildrenBitmap(N)) || Enc_{SC}(v) ||$   
 $Enc_{SC}(H(N_{C_1})) \dots Enc_{SC}(H(N_{C_n}))$ 

Where

- Enc<sub>len</sub>, Enc<sub>HE</sub> and Enc<sub>SC</sub> are encooings defined in Section 7.
- Encle is the little-endian encoding defined in Definition 7.
- C is the unique child of the extension node N.
- ChildrenBitmap $(N) := (b_{15}b_{14}..., b_1, b_0)_2$  where bit  $b_i = 1$  if N has a child with partial key i.
- $N_{C_1} \dots N_{C_n}$  with  $n \leq 16$  are the children nodes of the branch node N.

**Definition 20.** For a given node N, the **Merkle value** of N, denoted by H(N) is defined as follows:

$$H: \mathbb{B} \to \bigcup_{i=0}^{32} \mathbb{B}_{i}$$

$$H(N): \begin{cases} \operatorname{Enc}_{\operatorname{Node}}(N) & \|\operatorname{Enc}_{\operatorname{Node}}(N)\| < 32 \\ \operatorname{Hash}(\operatorname{Enc}_{\operatorname{Node}}(N)) & \|\operatorname{Enc}_{\operatorname{Node}}(N)\| \geqslant 32 \end{cases}$$

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### 6 Consensus Engine

Consensus in Polkadot RE is achieved during the execution of two different procedures. The first procedure is block production and the second is finality. Polkadot RE must run these procedures, if and only if it is running on a validator node.

#### 6.1 Block Tree

In the course of formation of a (distributed) blockchain, it is possible that the chain forks into multiple subchains in various block positions. We refer to this structure as a *block tree*:

**Definition 21.** The **Block Tree** of a blockchain is the union of all different versions of the blockchain observed by all the nodes in the system such as every such block is a node in the graph and  $B_1$  is connected to  $B_2$  if  $B_1$  is a parent of  $B_2$ .

Because every block in the blockchain contains a reference to its parent, it is easy to see that the block tree is actually a tree.

A block tree naturally imposes partial order relationships on the blocks as follows:

**Definition 22.** We say B is descendant of B', formally noted as B > B' if B is a descendant of B' in the block tree.

#### 6.2 Block Production

### 6.3 Finality

Polkadot RE uses GRANDPA Finality protocol [?] to finalize blocks. Finality is obtained by consecutive rounds of voting by validator nodes. Validators execute GRANDPA finality process in parallel to Block Production as an independent service. In this section, we describe the different functions that GRANDPA service is supposed to perform to successfully participate in the block finalization process.

#### 6.3.1 Preliminaries

**Definition 23.** A GRANDPA Voter, v, is represented by a key pair  $(k_v^{pr}, v_{id})$  where  $k_v^{pr}$  represents its private key which is an ED25519 private key, is a node running GRANDPA protocol, and broadcasts votes to finalize blocks in a Polkadot RE - based chain. The set of all GRANDPA voters is indicated by  $\mathbb{V}$ . For a given block B, we have

$$\mathbb{V}_B = \mathtt{authorities}(B)$$

where authorities is the entry into runtime described in Section 3.3.2.

Definition 24. GRANDPA state, GS, is defined as

$$GS := \{ \mathbb{V}, id_{\mathbb{V}}, r \}$$

where:

V: is the set of voters.

 $\mathbb{V}_{id}$ : is an incremental counter tracking membership, which changes in V.

**r**: is the voting round number.

Now we need to define how Polkadot RE counts the number of votes for block B. First a vote is defined as:

**Definition 25.** A GRANDPA vote or simply a vote for block B is an ordered pair defined as

$$V(B) := (H_h(B), H_i(B))$$

where  $H_h(B)$  and  $H_i(B)$  are the block hash and the block number defined in Definitions 10 and 11 respectively.

**Definition 26.** Voters engage in a maximum of two sub-rounds of voting for each round r. The first sub-round is called **pre-vote** and the second sub-round is called **pre-commit**.

By  $V_v^{r,pv}$  and  $V_v^{r,pc}$  we refer to the vote cast by voter v in round r (for block B) during the pre-vote and the pre-commit sub-round respectively.

The GRANDPA protocol dictates how an honest voter should vote in each sub-round, which is described in Algorithm 3. After defining what constitues a vote in GRANDPA, we define how GRANDPA counts votes.

**Definition 27.** Voter v equivocates if they broadcast two or more valid votes to blocks not residing on the same branch of the block tree during one voting sub-round. In such a situation, we say that v is an equivocator and any vote  $V_v^{r,\text{stage}}(B)$  cast by v in that round is an equivocatory vote and

$$\mathcal{E}^{r, \text{stage}}$$

represents the set of all equivocators voters in sub-round "stage" of round r. When we want to refer to the number of equivocators whose equivocation has been observed by voter v we refer to it by:

$$\mathcal{E}_{\mathrm{obs}(v)}^{r,\mathrm{stage}}$$

**Definition 28.** A vote  $V_v^{r,\text{stage}} = V(B)$  is invalid if

- H(B) does not correspond to a valid block;
- B is not an (eventual) descendant of a previously finalized block;
- $M_v^{r,\text{stage}}$  does not bear a valid signature;
- $id_{\mathbb{V}}$  does not match the current  $\mathbb{V}$ ;
- If  $V_v^{r,\text{stage}}$  is an equivocatory vote.

**Definition 29.** For validator v, the set of observed direct votes for Block B in round r, formally denoted by  $\mathrm{VD}^{r,\mathrm{stage}}_{\mathrm{obs}(v)}(B)$  is equal to the union of:

• set of valid votes  $V_{v_i}^{r,\text{stage}}$  cast in round r and received by v such that  $V_{v_i}^{r,\text{stage}} = V(B)$ .

Definition 30. We refer to the set of total votes observed by voter v in sub-round "stage" of round r by  $V_{\text{obs}(v)}^{r,\text{stage}}$ .

The set of all observed votes by v in the sub-round stage of round r for block B,  $V_{\text{obs}(v)}^{r,\text{stage}}(B)$  is equal to all of the observed direct votes casted for block B and all of the B's descendents defined formally as:

$$V^{r,\mathrm{stage}}_{\mathrm{obs}(v)}(B) := \bigcup_{v_i \in \mathbb{V}, B \geqslant B'} \mathrm{VD}^{r,\mathrm{stage}}_{\mathrm{obs}(v)}(B')$$

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The total number of observed votes for Block B in round r is defined to be the size of that set plus the total number of equivocators voters:

$$\#V_{\text{obs}(v)}^{r,\text{stage}}(B) = |V_{\text{obs}(v)}^{r,\text{stage}}(B)| + |\mathcal{E}_{\text{obs}(v)}^{r,\text{stage}}|$$

**Definition 31.** The current **pre-voted** block  $B_v^{r,pv}$  is the block with

$$H_n(B_v^{r,\text{pv}}) = \text{Max}(H_n(B)|\forall B: \#V_{\text{obs}(v)}^{r,\text{pv}}(B) \geqslant 2/3|\mathbb{V}|)$$

Note that for genesis block Genesis we always have  $\#V_{\operatorname{obs}(v)}^{r,\operatorname{pv}}(B) = |\mathbb{V}|$ .

Finally, we define when a voter v see a round as completable, that is when they are confident that  $B_v^{r,pv}$  is an upper bound for what is going to be finalised in this round.

**Definition 32.** We say that round r is completable if  $|V_{\text{obs}(v)}^{r,\text{pc}}| + \mathcal{E}_{\text{obs}(v)}^{r,\text{pc}} > \frac{2}{3} \mathbb{V}$  and for all  $B' > B_v^{r,\text{pv}}$ :

$$|V_{\mathrm{obs}(v)}^{r,\mathrm{pc}}| - \mathcal{E}_{\mathrm{obs}(v)}^{r,\mathrm{pc}} - |V_{\mathrm{obs}(v)}^{r,\mathrm{pc}}(B')| > \frac{2}{3} |\mathbb{V}|$$

Note that in practice we only need to check the inequality for those  $B' > B_v^{r, pv}$  where  $|V_{obs(v)}^{r, pc}(B')| > 0$ .

#### 6.3.2 Voting Messages Specification

Voting is done by means of broadcasting voting messages to the network. Validators inform their peers about the block finalized in round r by broadcasting a finalization message (see Algorithm 3 for more details). These messages are specified in this section.

**Definition 33.** A vote casted by voter v should be broadcasted as a **message**  $M_v^{r, \text{stage}}$  to the network by voter v with the following structure:

$$M_n^{r,\text{stage}} := \text{Enc}_{SC}(r, \text{id}_{\mathbb{V}}, \text{Enc}_{SC}(\text{stage}, V_n^{r,\text{stage}}, \text{Sig}_{\text{ED25519}}(\text{Enc}_{SC}(\text{stage}, V_n^{r,\text{stage}}, r, V_{\text{id}}), v_{\text{id}})$$

Where:

**Definition 34.** The justification for block B in round r of GRANDPA protocol defined  $J^r(B)$  is a vector of pairs of the type:

$$(V(B'), (\operatorname{Sign}_{v_i}^{r, \operatorname{pc}}(B'), v_{\operatorname{id}}))$$

in which either

or  $V_{n_i}^{r,pc}(B')$  is an equivocatory vote.

In all cases,  $\operatorname{Sign}_{v_i}^{r,\operatorname{pc}}(B')$  is the signature of voter  $v_i$  broadcasted during the pre-commit sub-round of round r.

Definition 35. GRANDPA finalizing message for block B in round r represented as  $M_v^{r,Fin}(B)$  is a message broadcasted by voter v to the network indicating that voter v has finalized block B in round r. It has the following structure:

$$M_v^{r, \operatorname{Fin}}(B) := \operatorname{Enc}_{\operatorname{SC}}(r, V(B), J^r(B))$$

in which  $J^r(B)$  in the justification defined in Definition 34.

#### 6.3.3 Initiating the GRANDPA State

A validator needs to initiate its state and sync it with other validators, to be able to participate coherently in the voting process. In particular, considering that voting is happening in different rounds and each round of voting is assigned a unique sequential round number  $r_v$ , it needs to determine and set its round counter r in accordance with the current voting round  $r_n$ , which is currently undergoing in the network.

As instructed in Algorithm 2, whenever the membership of GRANDPA voters changes, r is set to 0 and  $V_{\rm id}$  needs to be incremented.

#### **Algorithm 2.** Join-Leave-Grandpa-Voters $(\mathcal{V})$

- 1:  $r \leftarrow 0$
- 2:  $V_{id} \leftarrow ReadState('AUTHORITY\_SET\_KEY')$
- 3:  $V_{id} \leftarrow V_{id} + 1$
- 4: EXECUTE-ONE-GRANDPA-ROUND(r)

Each voter should run Algorithm? to verify that a round is completable.

#### 6.3.4 Voting Process in Round r

For each round r, an honest voter v must participate in the voting process by following Algorithm 3.

### **Algorithm 3.** PLAY-GRANDPA-ROUND(r)

- 1:  $t_{r,v} \leftarrow \text{Time}$
- 2:  $primary \leftarrow Derive-Primary$
- 3: **if** v = primary
- 4: Broadcast $(M_v^{r-1,\text{Fin}}(\text{Best-Final-Candidate}(r-1)))$
- 5: Receive-Messages(until Time  $\geq t_{r,v} + 2 \times T$  or r is completable)
- 6:  $L \leftarrow \text{Best-Final-Candidate}(r-1)$
- 7: if  $\operatorname{Received}(M^{r,\operatorname{pv}}_{v_{\operatorname{primary}}}(B))$  and  $B^{r,\operatorname{pv}}_v\!\geqslant\! B\!>\! L$
- 8:  $N \leftarrow B$
- 9: **else**
- 10:  $N \leftarrow B': H_n(B') = \max\{H_n(B'): B' > L\}$
- 11: BROADCAST $(M_v^{r,pv}(N))$
- 12: Receive-Messages(until  $B_v^{r,pv} \ge L$  and (Time  $\ge t_{r,v} + 4 \times T$  or r is completable))

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```
13: Broadcast(M_v^{r,pc}(B_v^{r,pv}))
14: Play-Grandpa-round(r+1)
```

### **Algorithm 4.** Best-Final-Candidate(r)

```
1: \mathcal{C} \leftarrow \{B'|B' \leqslant B_v^{r,\mathrm{pv}}: |V_v^{r,\mathrm{pc}}| - \#V_v^{r,\mathrm{pc}}(B') \leqslant 1/3|\mathbb{V}|\}

2: if \mathcal{C} = \phi

3: return \phi

4: else

5: return E \in \mathcal{C}: H_n(E) = \max\{H_n(B'): B' \in \mathcal{C}\}
```

### **Algorithm 5.** Attempt-To-Finalize-Round(r)

```
1: L \leftarrow \text{Last-Finalized-Block}
```

2:  $E \leftarrow \text{Best-Final-Candidate}(r)$ 

3: if 
$$E \geqslant L$$
 and  $V_{\text{obs}(v)}^{r-1,\text{pc}}(E) > 2/3|\mathcal{V}|$ 

4: Last-Finalized-Block $\leftarrow B^{r,pc}$ 

5: **if**  $M_v^{r,\text{Fin}}(E) \notin \text{RECEIVED-MESSAGES}$ 

6: Broadcast $(M_v^{r, \text{Fin}}(E))$ 

7: return

8: schedule-call Attempt-To-Finalize-Round(r) when Receive-Messages

# 7 Auxiliary Encodings

### 7.1 SCALE Codec

Polkadot RE uses Simple Concatenated Aggregate Little-Endian" (SCALE) codec to encode byte arrays that provide canonical encoding and to produce consistent hash values across their implementation, including the Merkle hash proof for the State Storage.

Definition 36. The SCALE codec for Byte array A such that

$$A := b_1 b_2 \dots b_n$$

such that  $n < 2^{536}$  is a byte array referred to  $\text{Enc}_{SC}(A)$  and defined as follows:

$$\operatorname{Enc}_{\operatorname{SC}}(A) := \left\{ \begin{array}{ll} l_1 \, b_1 \, b_2 \dots b_n & 0 \leqslant n < 2^6 \\ i_1 \, i_2 \, b_1 \dots b_n & 2^6 \leqslant n < 2^{14} \\ j_1 \, j_2 \, j_3 \, b_1 \dots b_n & 2^{14} \leqslant n < 2^{30} \\ k_1 \, k_2 \dots k_m \, b_1 \dots b_n & 2^{30} \leqslant n \end{array} \right.$$

in which:

$$\begin{aligned} & l_1^1 l_1^0 = 00 \\ & i_1^1 i_1^0 = 01 \\ & j_1^1 j_1^0 = 10 \\ & k_1^1 k_1^0 = 11 \end{aligned}$$

and n is stored in  $Enc_{SC}(A)$  in little-endian format in base-2 as follows:

$$\begin{vmatrix} l_1^7 \dots l_1^3 \, l_1^2 & n < 2^6 \\ i_2^7 \dots i_2^0 \, i_1^7 \dots i_1^2 & 2^6 \leqslant n < 2^{14} \\ j_4^7 \dots j_4^0 \, j_3^7 \dots j_1^7 \dots j_1^2 & 2^{14} \leqslant n < 2^{30} \\ k_2 + k_3 \, 2^8 + k_4 \, 2^{2 \cdot 8} + \dots + k_m \, 2^{(m-2)8} & 2^{30} \leqslant n \end{vmatrix} \} := n$$

where:

$$k_1^7 \dots k_1^3 k_1^2 = m - 4$$

Definition 37. The SCALE codec for Tuple T such that:

$$T := (A_1, ..., A_n)$$

Where  $A_i$ 's are values of different types, is defined as:

$$\operatorname{Enc}_{\operatorname{SC}}(T) := \operatorname{Enc}_{\operatorname{SC}}(A_1) |\operatorname{Enc}_{\operatorname{SC}}(A_2)| ... |\operatorname{Enc}_{\operatorname{SC}}(A_n)$$

In case of a tuple (or struct) the knowledge of the shape of data is necessary for decoding.

### 7.2 Hex Encoding

Practically, it is more convenient and efficient to store and process data which is stored in a byte array. On the other hand the Trie keys are broken in 4-bits nibbles. Accordingly, we need a method to encode sequences of 4-bits nibbles into byte arrays canonically:

**Definition 38.** Suppose that  $PK = (k_1, ..., k_n)$  is a sequence of nibbles, then  $Enc_{HE}(PK) :=$ 

 $\begin{cases} \text{Nibbles}_4 & \to & \mathbb{B} \\ \text{PK} = (k_1, ..., k_n) & \mapsto & \begin{cases} (0, k_1 + 16 \, k_2, ..., k_{2i-1} + 16 \, k_{2i}) & n = 2 \, i \\ (k_1, k_2 + 16 \, k_3, ..., k_{2i} + 16 \, k_{2i+1}) & n = 2 \, i + 1 \end{cases}$ 

### 7.3 Partial Key Encoding

**Definition 39.** Let N be a leaf or an extension node in the storage state trie with Partial Key  $PK_N$ . We define the **Partial key length encoding** function, formally referred to as  $Enc_{len}(N)$  as follows:

$$\begin{array}{ll} \operatorname{Enc}_{\operatorname{len}}(N) & := \\ \operatorname{NodePrefix}(N) & + \\ \left\{ \begin{array}{ll} (\|\operatorname{PK}_N\|) & \|\operatorname{PK}_N\| < \operatorname{BigKeySize}(\operatorname{NodeType}(N)) \\ (127)\|(\|\operatorname{PK}_N\| - \operatorname{BigKeySize}(\operatorname{NodeType}(N))) & \|\operatorname{PK}_N\| \geqslant \operatorname{BigKeySize}(\operatorname{NodeType}(N)) \end{array} \right. \end{array}$$

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where NodePrefix, NodeType and BigKeySize functions are defined in Definitions 18,16 and 40 respectively.

**Definition 40.** We define BigKeySize function for each node type of the Trie as follows:

# 8 Genesis Block Specification

# 9 Predefined Storage keys

# 10 Runtime upgrade

# Appendix A Runtime API

Runtime API is a set of functions that Polkadot RE exposes to Runtime to access external functions needed for various reasons, such as Storage content access and manipulation, memory allocation and also for efficiency. The function are specified in each subsequent subsection for each category of those functions.

### A.1 Storage

### A.1.1 ext\_set\_storage

Sets the value of a specific key in the state storage.

#### Prototype:

```
(func $ext_storage
  (param $key_data i32) (param $key_len i32) (param $value_data i32)
  (param $value_len i32))
```

#### **Arguments**:

- key: a pointer pointing the buffer containing the key.
- key\_len: the key length in bytes.
- value: a pointer pointing the buffer containing the value to be stored under the key.
- value\_len: the length of the value buffer in bytes.

#### A.1.2 ext\_storage\_root

Retrieves the root of state storage.

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#### Prototype:

```
(func $ext_storage_root
  (param $result_ptr i32))
```

#### **Arguments:**

• result\_ptr: a pointer which points to a byte array which contains the root of state storage after the function concludes.

### A.1.3 ext\_blake2\_256\_enumerated\_trie\_root

Given an array of byte arrays, arranges them in a Merkle trie defined in 5.4 and computes the trie root hash.

### Prototype:

#### **Arguments:**

- values\_data: a pointer pointing to the buffer containing the array where byte arrays are stored consecutively.
- lens\_data: an array of i32 elements each stores the length of each byte array stored in value\_data.
- lens len: the number of i32 elements in lens\_data.
- result: a pointer pointing to the beginning of a 32-byte byte array containing the root of the Merkle trie corresponding to elements of values\_data.

#### A.1.4 To be Specced

- ext\_clear\_child\_storage
- ext\_clear\_prefix
- ext\_clear\_storage
- ext\_exists\_child\_storage
- ext\_get\_allocated\_child\_storage
- ext\_get\_allocated\_storage
- ext\_get\_child\_storage\_into
- ext\_get\_storage\_into
- ext\_kill\_child\_storage
- ext\_set\_child\_storage
- ext\_storage\_changes\_root
- ext\_storage\_root
- ext\_exists\_storage

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### A.2 Memory

#### A.2.1 ext\_malloc

Allocates memory of requested size in the heap.

#### Prototype:

```
(func $ext_malloc
  (param $size i32) (result i32))
```

### **Arguments**:

• size: the size of the buffer to be allocated in number of bytes.

#### Result:

a pointer pointing to the beginning of the allocated buffer.

### A.2.2 ext\_free

Deallocates a previously allocated memory.

### **Arguments:**

• addr: 32bit pointer pointing to the allocated memory.

### A.2.3 Input/Output

- ext\_print\_hex
- ext\_print\_num
- ext\_print\_utf8

### A.3 Cryptograppic auxiliary functions

### A.3.1 ext blake 2256

Computes the Blake2s hash of a given byte array.

#### Prototype:

### **Arguments**:

- data: a pointer pointing the buffer containing the byte array to be hashed.
- len: the length of the byte array in bytes.
- out: a pointer pointing to the beginning of a 32-byte byte array containing the Blake2s hash of the data.

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### A.3.2 To be Specced

- ext\_ed25519\_verify
- ext\_twox\_128
- ext\_twox\_256

# A.4 Sandboxing

### A.4.1 To be Specced

- ext\_sandbox\_instance\_teardown
- ext\_sandbox\_instantiate
- ext\_sandbox\_invoke
- ext\_sandbox\_memory\_get
- ext\_sandbox\_memory\_new
- ext\_sandbox\_memory\_set
- ext\_sandbox\_memory\_teardown

### A.4.2 Misc

### A.4.3 To be Specced

• ext\_chain\_id

# A.5 Not implemented in Polkadot-JS